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## Breakpoint Selection

1. You are driving on a straight road from Madison to Nosidam. Your car has a fuel capacity of  $C$ , which means that you can drive  $C$  miles after refueling. There are refueling stations along the way at  $d_1, d_2, \dots, d_n$ . You drive from Madison with a full fuel tank. Your goal is to reach Nosidam with the fewest amount of times to refuel.

**Solution:**

## Interval Stabbing

2. There are  $n$  intervals  $[[a_1, b_1], [a_2, b_2], \dots, [a_n, b_n]]$ . We say that a set of point  $S$  **stabs** all the intervals if every interval in the set contains at least one point in  $S$ . Find a minimal set of point  $S$ .

**Solution:**

## Preemptible Job Scheduling

3. There are  $n$  jobs. Job  $i$  is available at time  $s_i$ , and it require  $p_i$  processing time. Jobs are preemptible. Design an algorithm to minimize  $\sum_i c_i$ , where  $c_i$  is the time when job  $i$  is completed. Prove its correctness.

**Solution:**