

# 1 Introduction



## 2 OLAP and Graph Databases

This chapter introduces the main concepts that forms the theoretical foundation necessary to better understand the work presented in this dissertation. Initially, we will explore the definition of Data Warehouse, Multidimensional Model and OLAP tools. Then, we will dive into concepts related to Graph and Graph Databases.

### 2.1 Data Warehouse

According to (INMON, 2005), a data warehouse (DW) is “a subject-oriented, integrated, nonvolatile, and time-variant collection of data in support of management’s decisions”. The first important aspect of a data warehouse is that it is subject-oriented, which means that the information stored in the DW is related to the company’s subject. Consider a retail company for example: the main subjects can be product, sale, vendor and customer, therefore the data in the warehouse will be related to these entities.

The second characteristic of a data warehouse is that it is integrated, which means it contains data coming from multiple different sources. During the process of loading the warehouse, the data is converted, formatted, normalised and go through any other process to make the final information stored in the warehouse consistent. Another important aspect of a data warehouse is that it is nonvolatile, which means that the data in the warehouse does not get updated as operational environment. The warehouse is loaded in batches and it stores a snapshot, creating a history of the data. The final important aspect of a DW is that every record of data contains some sort of a time attribute to mark the moment in which the record is accurate.

Figure 2.1 shows the basic elements of a data warehouse (KIMBALL; ROSS, 2011). The Operational Source Systems capture and store the transactions of the business and they are considered elements outside of the data warehouse, since there is no control on the content or the format of the data that they store. The Data Staging Area is where the process of Extract-Transformation-Load (ETL) is made: the data is extracted from the operations source system, then they are transformed in order to integrate all the information in a consistent format, and finally the data is loaded into the presentation area.

The Data Presentation Area is where the data is organised, stored and accessed by analytical applications. According to (KIMBALL; ROSS, 2011), this area should be composed by a series of integrated data marts, which are repositories that present the data for a single process of the organisational business. A data mart stores atomic data and

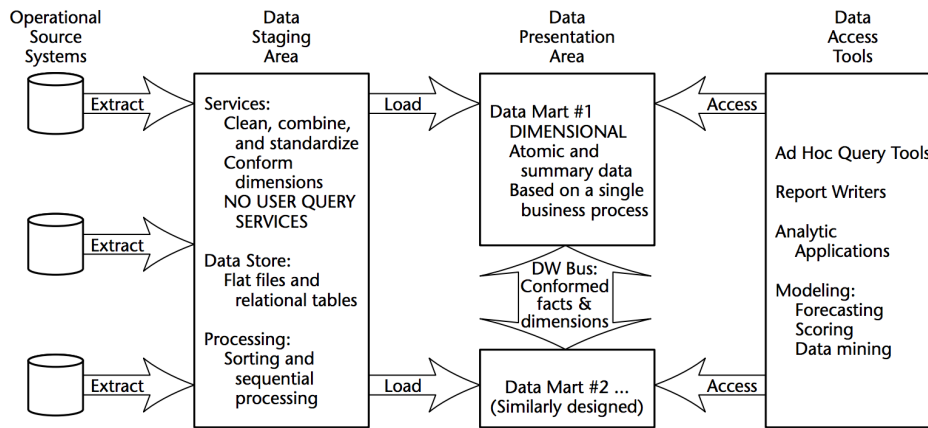


Figure 2.1 – Elements of a Data Warehouse (KIMBALL; ROSS, 2011)

organizes them in a model that is more legible to humans. The most popular technology used to implement data marts adopted by the industry is On-Line Analytical Processing (OLAP), that will be covered in more detail along this chapter.

Finally, the Data Access Tools query the data in the presentation area. This element is formed by a set of different applications, since simple ad hoc queries until complex data mining application.

## 2.2 Multidimensional Model

The main functionality of a data warehouse is to facilitate multidimensional analysis (OLAP COUNCIL, 1997). This type of analysis reduces the number of misinterpretations by aligning the data with the analyst's mental model of the business. The multidimensional analysis provides an easy navigation through the database, showing specific subsets of data in different orientations and performing analytical calculations.

In order to perform multidimensional analysis, the data must be organised in a multidimensional model, where information is stored in a multidimensional array called *hypercube* or *cube* (VASSILIADIS, 1998). A cube is composed by cells that store *measures* aggregated by the data *dimensions*. A *dimension* is a cube's structural attribute formed by a list of properties that are similar to each other according to the user's perception of the data. Measures are the values being analysed by the user. Figure 2.2 shows an example of the dimensions and measures extracted from a sales application.

As shown in Figure 2.2 , each dimension (Geography, Time and Item) can be associated with an hierarchy of data aggregation levels. This feature allows user to view the data from different levels of details, for example: the measure *Sales* aggregated by *Region* can be detailed by *Country* or even further detailed by *City*.

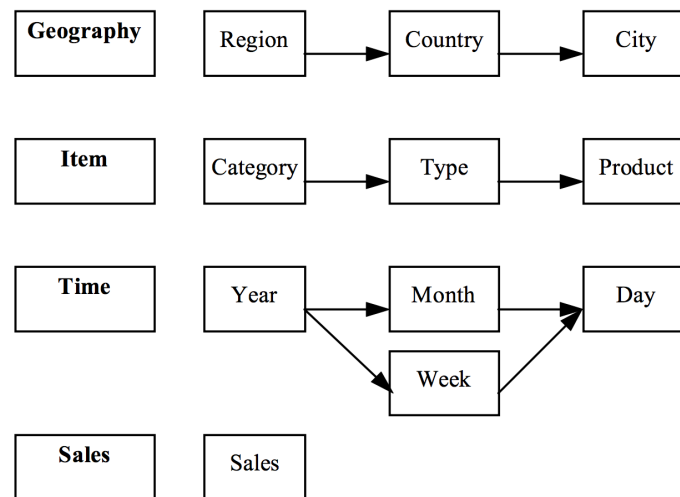


Figure 2.2 – Example of dimensions and measure for a sales application (VASSILIADIS, 1998)

## 2.3 OLAP

On-Line Analytical Processing (OLAP) is a category of technological tools used by analysts and managers to extract new knowledge from consolidated enterprise data (OLAP COUNCIL, 1997). In order to achieve this goal, data are organised in cubes and stored following multidimensional models. The access to this data should be fast, consistent and interactive and it should provide various views of information, reflecting the different dimensions of an enterprise as perceived by the user.

Usually, the data loaded into an OLAP system comes from a data warehouse. According to (INMON, 2005), the relationship between OLAP systems and data warehouse is complimentary: while OLAP offers control and flexible ways to explore data in different dimensions and hierarchy levels, data warehouse provides a robust data source for the OLAP system, where up-to-date data is available already extracted and properly integrated.

### 2.3.1 Types of OLAP Systems

There are two approaches for the physical model of an OLAP system (VASSILIADIS; SELLIS, 1999): Multidimensional On-Line Analytical Processing (MOLAP) and Relational On-Line Analytical Processing (ROLAP) Architectures. The MOLAP architecture provides a direct multidimensional view of the data. This approach stores the data in a Multidimensional Database Management System (MDBMS), which use n-dimensional arrays that contains the measures of the cube. This type of DBMS has a better performance than traditional Relational Databases, but it is more difficult to manage updates.

The ROLAP architecture is a multidimensional interface to relational data. This approach uses a traditional Relational Database Management System (RDBMS) to store

the data organised in a star or snowflake schema. A star schema is formed by one or more dimension tables and one centralised fact table, which stores the measures of interest for the OLAP system. Figure 2.3 shows an example of a star schema, where the tables TIME, GEOGRAPHY, ACCOUNT and PRODUCT are dimension tables and SALES is the fact table.

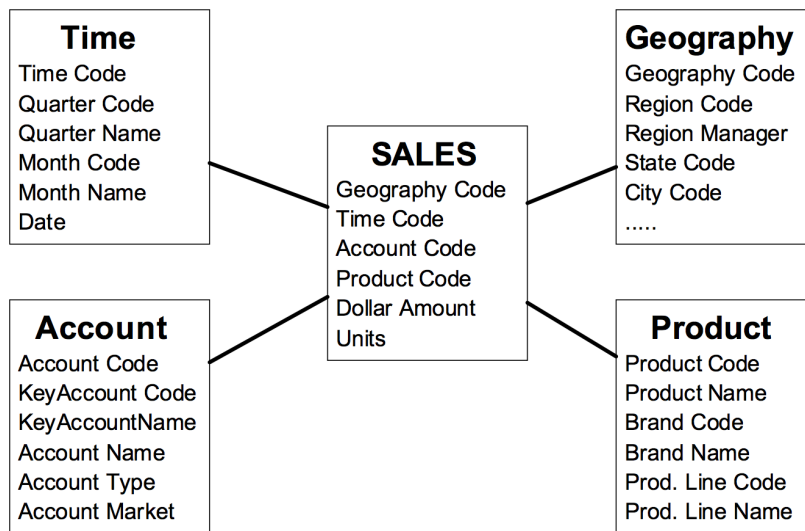


Figure 2.3 – Example of a Star Schema (VASSILIADIS; SELLIS, 1999)

Despite MOLAP architecture has the advantage of relying on a multidimensional native storage mechanism, the ROLAP approach allows easy integration with existing relational information systems and has the advantage of relational data being more efficiently stored than multidimensional data.

### 2.3.2 OLAP Operators

As mentioned earlier in this chapter, an OLAP system should provide a fast and interactive way for the user to explore the data stored in the cube. These are the main OLAP operations that can be used to navigate and manipulate different dimensions of the data (VASSILIADIS, 1998):

**Roll-up** Aggregates information along one dimension, summarising data on a higher level in its hierarchy. Consider the dimensions shown in Figure 2.2 and the measure of total dollar amount of sales per city, we can perform a roll-up operation to obtain the total dollar amount of sale per state.

**Drill-down** Detail information along one dimension, navigating the data from a higher to a lower hierarchy. Consider the measure of total dollar amount of sales per year, we can drill-down this query to obtain the total dollar amount of sales per month.

**Slice** Selects a slice of the cube according to user-specified dimension values. For instance, the user can select to view the total dollar amount of sales for the year of 2016.

**Dice** Selects a subcube from the original data according to user-specified conditions referred to more than one dimension. For instance, the user can select to view to total dollar amount of sales for the year of 2016 in the city of Recife.

**Pivot** Changes the orientation of dimensions in the cube, i.e. swap a row dimension to a column dimension.

There are other operations that can be performed in a OLAP system, but the ones shown above are considered the basic set of operations to support dynamic multidimensional analysis (INMON, 2005).

## 2.4 Graph

Graph is a data structure formed by a set of vertices (or nodes)  $V = \{v_1, \dots, v_n\}$  and a set of pair of vertices called edges (or relationships)  $E = \{v_1v_2, \dots, v_nv_m\}$ . It can be represented graphically (where the vertices are shown as circles and edges are shown as lines, as shown in Figure 2.4) or mathematically in the form  $G = (V, E)$  (TOBERGTE; CURTIS, 2013).

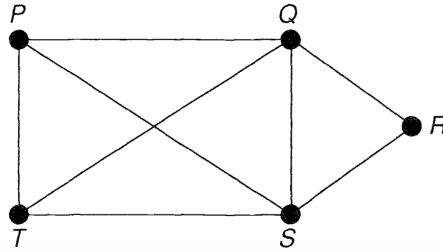


Figure 2.4 – Example of graph (TOBERGTE; CURTIS, 2013)

There are several real world applications that can take advantage of a graph model, specially the ones where the relationship between entities is an important information to be represented (MILLER, 2013). Consider, for example, a social network application similar to Twitter, where a user can follow another user. In this scenario, we can represent a user as a vertex and the relationship between users as an edge, as shown in Figure 2.5

### 2.4.1 Graph Theory

Graph Theory is a branch of Mathematics dedicated to the study of graph structures (TOBERGTE; CURTIS, 2013). Given the definition of a general graph explained above, there are several classifications and concepts associated with graph structures.

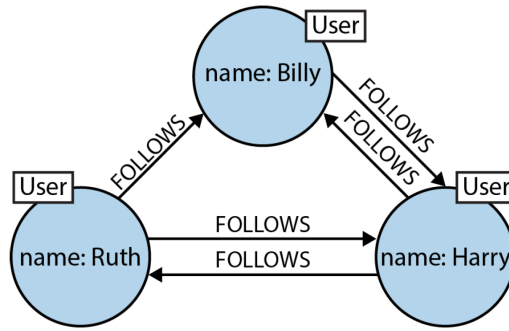


Figure 2.5 – Example of graph representation of a social network (MILLER, 2013)

**Loop** When an edge starts and finishes in the same vertex, as the one shown in Figure 2.6 starting at vertex  $T$  and finishing at vertex  $T$ .

**Multigraph** When a graph allows multiple edges connecting the same pair of vertices, as illustrated in Figure 2.6 with two edges connecting vertices  $Q$  and  $R$ .

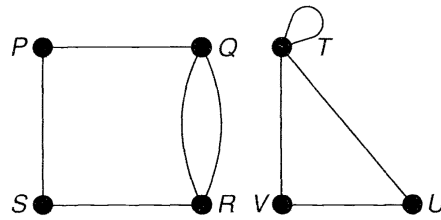


Figure 2.6 – Example of a multigraph with a loop (TOBERGTE; CURTIS, 2013)

**Simple Graph** When a graph does not have loops or multiple edges, as the one depicted in Figure 2.4.

**Complete Graph** When each pair of distinct vertices are connected to each other, as shown in Figure 2.7.

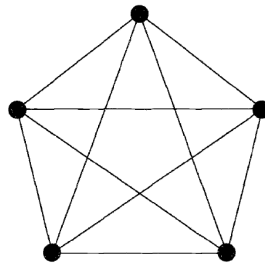


Figure 2.7 – Example of a complete graph (TOBERGTE; CURTIS, 2013)

**Directed Graph** When the edges have directions expliciting the start and end of the connection, as illustrated in Figure 2.8.



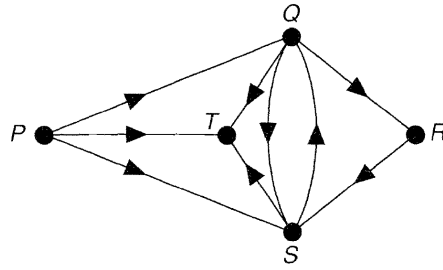
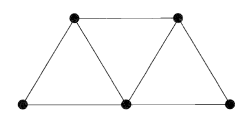


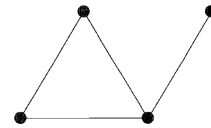
Figure 2.8 – Example of a directed graph (TOBERGTE; CURTIS, 2013)

**Subgraph** It is a graph obtained from another graph  $G$ , where its vertices are a subset of the vertices of  $G$  and its edges are a subset of the edges of  $G$ . Figure 2.9 shows in 2.9b a subgraph of the graph in 2.9a.

**Path** It is a subgraph obtained by a sequence of adjacent and distinct vertices.



(a) Original graph



(b) Subgraph

Figure 2.9 – Example of a subgraph (TOBERGTE; CURTIS, 2013)

There are other types of classifications of a graph and other concepts associated to it (TOBERGTE; CURTIS, 2013). These are the main definitions for the purposes of understanding the work presented here.

### 2.4.2 Network Analysis

There are different kind of analysis that can be done depending on the nature of the graph data. Due to the work presented here, we will explore the aspects of social network analysis, which focus on the structure of relationships (edges) between entities (vertices) in the graph. Several types of analysis can be performed in a graph, but the measure of a node's centrality is historically one of the most studied cases of analysis (FREEMAN, 1978). A common application for a centrality measure is to find out what are the focal points in a social network, i.e. who are the people that are the most connected to other people? There are three types of centrality measures (FREEMAN, 1978):

**Degree Centrality** This measure is given by the number of adjacent vertices. Considering a social network, a person (vertex) that has the greatest number of connections can be considered one of the focal points of the network, since it can directly read the

most nodes in the graph. Given a graph with  $n$  vertices, the maximum value the degree centrality of a vertex in the graph can be is  $n - 1$ . The degree centrality of a vertex is related to its potential communication activity.

**Betweenness Centrality** This measure is given by the frequency in which a vertex is present in the shortest path between other vertices. Considering a social network, a person with high betweenness centrality is capable of influencing others by intercepting connections between several vertices in the graph. The betweenness centrality of a vertex is related to its potential control of communication.

**Closeness Centrality** This measure is given by the inverse of the average distance of the shortest path of a vertex between other vertices in the graph. Considering a social network, a person with high closeness centrality do not depend as much on others to communicate with other people in the network. The closeness centrality of a vertex is related to its potential independency and efficiency to control communication.

## 2.5 Graph Databases

Graph Databases are an alternative to Relational Database Management Systems (RDBMS), which are commonly used in the industry since the early 1980's. Despite the popularity of RDBMSs, GDBs allow the storage of data in graph model, which is a more natural way to represent information for some applications, such as social networks, semantic web pages and recommendation systems (MILLER, 2013).

The most popular form of graph model is the labeled property graph model (ROBINSON; WEBBER; EIFREM, 2015). The main characteristics of a labeled property graph are:

- Nodes (vertices) and Relationships (edges) can contain properties, i.e. key-value pairs
- Nodes can be labeled with one or more labels
- Relationships are named and directed, i.e. always have start and end nodes

An example of a labeled property graph was shown in Figure 2.5, where the nodes have the label “User” and the property “name” and the relationships are named “Follows” and have arrows indicating the direction of the edge.

### 2.5.1 Historical Overview

Scientific research related to graph data models were continuously published between 1980's and the first half of 1990's. Then, the database community attention turned to

semistructured data model, due to the emergence of XML and the growth of hypertext document applications (ANGLES; GUTIERREZ, 2008). From this period, the main focus of the graph databases proposed was to establish a better way to represent data and methods to retrieve and manipulate data modeled as graph.

Recently this area has gained again attention from the community, due to the emergence of trendy projects (chemistry, biology, social network, semantic web, among others) where the importance of information relies not only in the entities but also in the relationship between them (ANGLES, 2012). Most recent implementations of graph databases are concerned with handling increasing amount of data and improving performance in retrieving and manipulating data.

The most popular graph database according to DBEngines<sup>1</sup> website is Neo4J<sup>2</sup>. It is an open source native graph storage database implemented in Java. Neo4J has its own query language called Cypher, which can be used to create, update and retrieve nodes and relationships. This graph database also provides high availability and scalability for big volume of graph data.

Besides Neo4J, there are other popular graph databases according to DB Engine site. OrientDB<sup>3</sup> is a NoSQL Multi-Model database, which means it stores data in the form of documents, key-value stores, objects, graph and others. Like Neo4J, OrientDB is also implemented in Java, but it uses an extended version of SQL that includes special operators to manipulate graph. This database allows the creation of a pre-defined data schema and the definition of complex data type, like dates, decimals and binary objects (BLOB).

TitanDB<sup>4</sup> is a native graph database implemented in Java. In order to establish connection with the hard disk, Titan needs to be linked to a data storage system - Cassandra<sup>5</sup>, HBase<sup>6</sup> or BerkeleyDB<sup>7</sup> - that is suitable for the application. The creation of nodes, edges and the submission of queries can be done through a Java API or through a Gremlin server.

## 2.5.2 Comparing Graph Databases Performance

One of the basic tasks when manipulating a database is to retrieve an object given its id. The experiment described in (JOUILI; VANSTEENBERGHE, 2013) records the average time to retrieve a node by its id, given an 500000 nodes graph and 4 clients

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<sup>1</sup> <https://db-engines.com/en/system/Neo4j>

<sup>2</sup> <https://neo4j.com/>

<sup>3</sup> <http://orientdb.com/orientdb/>

<sup>4</sup> <http://titan.thinkaurelius.com/>

<sup>5</sup> <http://cassandra.apache.org/>

<sup>6</sup> <https://hbase.apache.org/>

<sup>7</sup> <http://www.oracle.com/technetwork/database/database-technologies/berkeleydb/overview/index.html>

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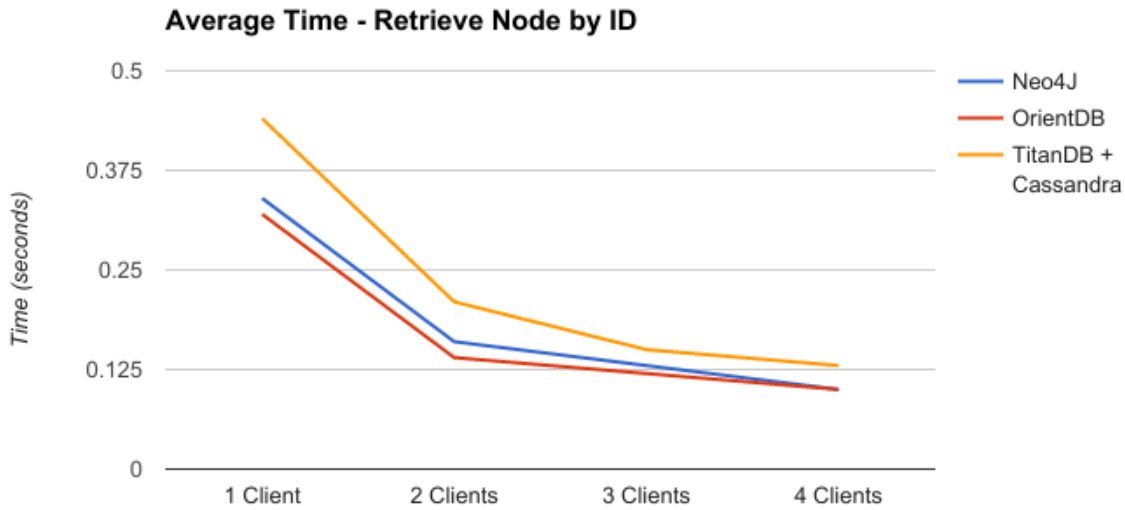


Figure 2.10 – Chart with mean time that each DB took to retrieve a node by its id

executing this action 200 times. This process was executed using Neo4J, OrientDB and TitanDB using Cassandra as backend.

According to Figure 2.10, Neo4J and OrientDB have similar performance, being OrientDB slightly faster to retrieve a node given its id. On the other hand, TitanDB using Cassandra as backend has a bad performance compared with the other DBs. However, TitanDB can be connected with other backend services, which can improve its performance for this task.

Another common concern among developers is the amount of memory taken by the database. In the experiment shown in (MCCOLL et al., 2014), a graph containing 32,000 nodes and 256,000 edges was stored in Neo4J, OrientDB and TitanDB and the amount of memory required by each database was measured.

From the Figure 2.11, we can notice that OrientDB is the one that consumes the most, reaching up to 10.156 MB of memory. On the other hand, TitanDB requires less memory, only needing 388 MB to store the graph.

## 2.6 Final Considerations

In this chapter, we discussed the main concepts related to the work presented in this dissertation. Initially, the definition of Data Warehouse and Multidimensional Model were introduced, followed by a detailed view on different types and operators an OLAP system can have. Then, we covered the main components of a graph and how it can be

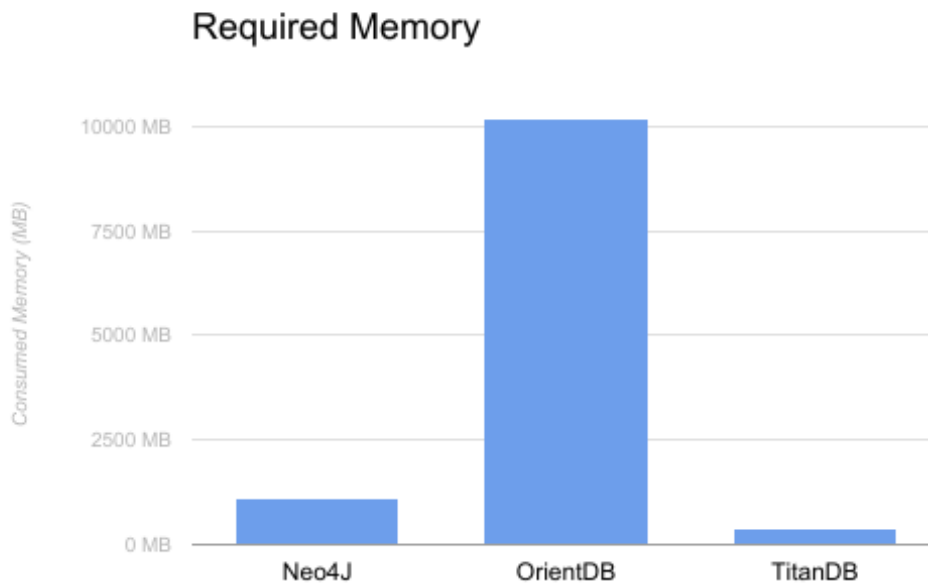


Figure 2.11 – Chart with the amount of memory required for each DB

classified according to different characteristics. Finally, we explained the definition of a Graph Database and went through a historical overview of such systems, as well as a comparison of the most popular Graph DBs nowadays. In the next chapter, we will review the most important research published that implements a OLAP system using Graph Databases.



## 3 Graph Cubes: State of the Art

This chapter presents the most important research works published in the area of OLAP systems implemented using graph databases. The first work presented here dates back to 2011 and introduces several concepts - such as graph cube, aggregated graphs and cuboid queries - that serve as basis for other papers published since then.

### 3.1 Graph Cube: On Warehousing and OLAP Multidimensional Networks

One of the main works in graph analysis using OLAP methods is described in (ZHAO et al., 2011), and it introduces several concepts that will be used by other authors to describe their work in this area. Graph Cube is one of those concepts and it is defined as a multidimensional model that extends multidimensional networks to provide decision support features. A multidimensional network is a graph  $N = (V, E, A)$ , where  $V$  is a set of vertices,  $E$  is a set of edges and  $A$  is a set of vertex-specific attributes. Each vertex in the graph is a multidimensional tuple and the attributes of the vertex define the graph cube dimensions.

A graph cube is formed by all possible aggregate networks calculated from the original multidimensional network. An aggregate network (often called cuboid) is a summarisation of the original graph with respect to one or more dimensions, which is calculated by applying an aggregate function (e.g. COUNT, SUM, AVERAGE, among others) on the vertices attributes. Consider the multidimensional network illustrated in Figure 3.1.

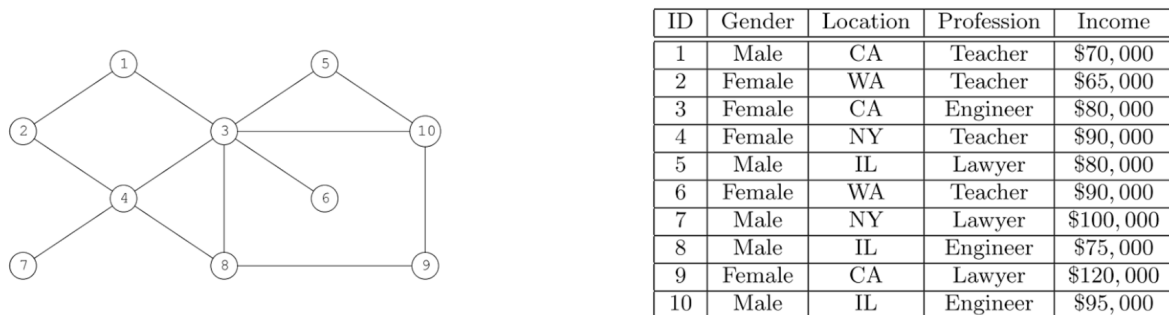


Figure 3.1 – Multidimensional network (ZHAO et al., 2011)

The vertices of the graph presented in Figure 3.1 represent individuals and the edges represent the relationship between these individuals. The table on the right side of Figure 3.1 describes the attributes of each vertex: an unique *ID*, *Gender*, *Location*,

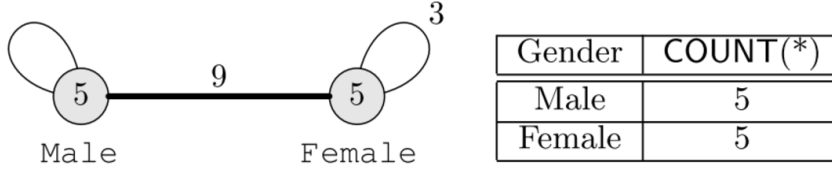


Figure 3.2 – Aggregate Network by *Gender* dimension (ZHAO et al., 2011)

*Profession* and *Income*. Figure 3.2 shows the cuboid obtained by applying the function COUNT on the attribute *Gender*: two nodes represent the possible values for the attribute (Male and Female) and they contain the number of nodes in the original graph with the respective *Gender* value. It is important to notice that the relationship between individuals was also aggregated in the resulting network, e.g. the aggregate network show that there are 9 relationships between male and female individuals in the original graph.

The dimension of a cuboid is given by the set of non-aggregate dimensions of the cuboid. For instance, the cuboid in Figure 3.2 has the dimension *Gender*. A cuboid  $A'$  is an ancestor of another cuboid  $A''$  if  $\dim(A')$  contains  $\dim(A'')$ . Given these definitions, all possible cuboids of a graph cube can be organised in a graph cube lattice, ordering the cuboids according to its ancestors. A multidimensional network  $N$  with  $n$  dimensions has  $2^n$  cuboids in the graph cube. Figure 3 shows the graph cube lattice for the multidimensional network introduced in Figure 3.1, considering only *Gender*, *Location* and *Profession* as dimensions.

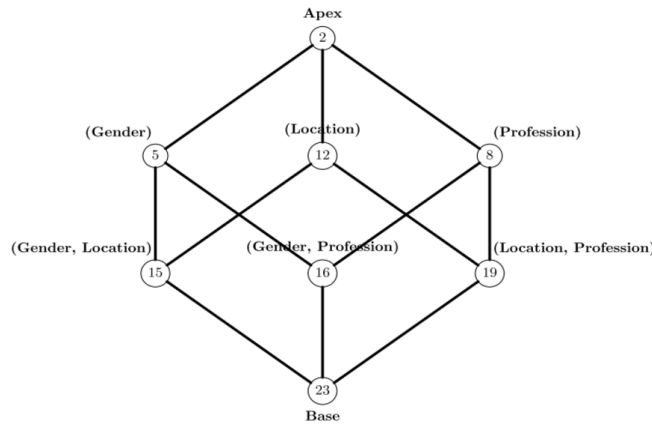


Figure 3.3 – Graph Cube Lattice (ZHAO et al., 2011)

The paper proposes two OLAP query models:

**Cuboid Query** Aggregate vertices and edges based on the dimension requested in the query and can work with any aggregate function (SUM, AVG, etc). For instance, consider a graph with nodes containing the attributes (*Gender*, *Location*, *Profession*).



A cuboid query for this graph can be  $(Gender, *, *)$  which will result in an aggregate graph showing all the vertices with the same Gender value aggregated and the edges also aggregate by the function COUNT.

**Crossboid Query** Returns the aggregate network between two or more cuboids structures. An example of a crossboid query can be the aggregate network between an user with  $ID = 3$  and all the locations

Given that the size of the graph cube lattice is exponential with respect to the number of dimensions of the original multidimensional network, the paper proposes a partial materialisation in order to process queries. The partial materialisation is implemented using a greedy algorithm that selects  $k$  cuboids ( $k < 2^n$ ) to be materialised according to the benefit of those cuboids to improve the cost for query evaluation.

The graph cube implementation described above is also studied by other works. In (DENIS; GHRAB; SKHIRI, 2013), a distributive approach is proposed using map reduce jobs to calculate each step of the aggregation process. In (KHAN et al., 2014), a new algorithm to compute the Graph Cube (iGraphCubing) is proposed, using a new pruning method based on the Structural Significance measure. This measure takes into account three factors:

- The diversity of the attribute value in the neighborhood for each vertex
- The clustering coefficient
- The density around each vertex

The work in (ZHAO et al., 2011) presents experiments evaluating the effectiveness and the efficiency of the method proposed. The effectiveness was evaluated by analysing OLAP queries submitted to the graph cube. The efficiency was evaluated by analysing the graph cube performance depending if it was fully or partially materialised in disk. In conclusion, the paper proposes an implementation of a graph cube obtained from an homogeneous attributed graph, but it does not consider heterogeneous networks neither attributed edges

## 3.2 Graph OLAP: Towards Online Analytical Processing on Graphs

The Graph OLAP framework proposed in (CHEN et al., 2008) takes as input a set of network snapshots, where each snapshot contains a graph and a set of informational attributes that describes the snapshot. In this scenario, the paper defines two dimension types: informational dimensions (formed by the informational attributes) and topological dimensions (formed by the attributes of the nodes and edges of the graph). The authors

distinguish different semantics for OLAP operations in graphs, so these operations are categorised into Informational OLAP (I-OLAP) and Topological OLAP (T-OLAP).

The framework gives as output an aggregate graph with a summarised view of the snapshots set. The type of the aggregate graph returned by the framework can also be categorised in Informational Aggregate Graph (I-aggregate graph) and Topological Aggregate Graph (T-aggregate graph).

Informational Aggregate Graph is computed based on a set of network snapshots that have informational dimensions with same values. Figure 3.4 shows an example of an i-aggregate graph composed by snapshots describing the co-author relationship between individual authors. The co-author relationship is grouped by a certain conference (*sigmod*, *vldb*, *icde*), by a class of conferences (*db-conf*), by a specific period of time (*2004*, *2005*) and by a group of time periods (*all-years*). It is important to notice that the graph in Figure 3.4 shows different levels of aggregations for each co-author relationship.

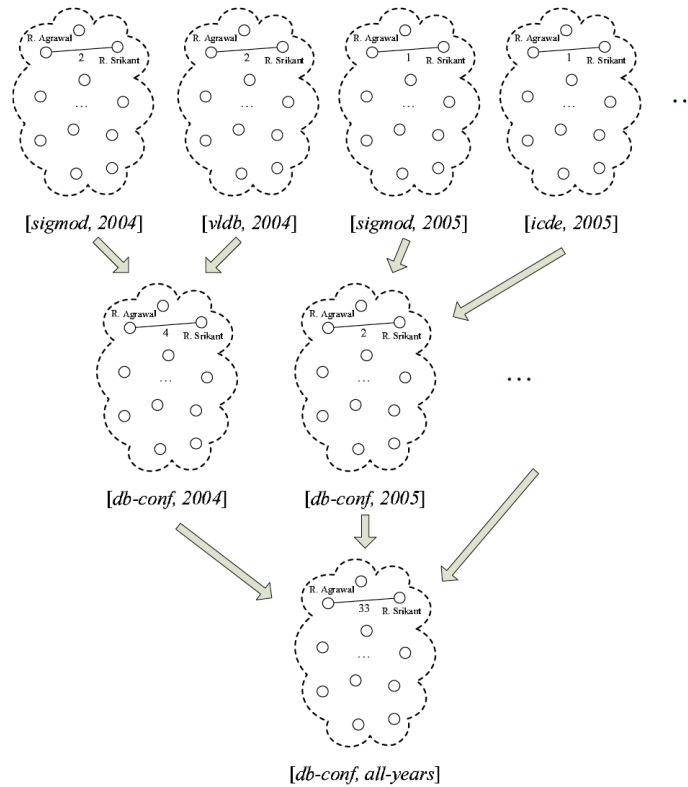


Figure 3.4 – Example of Informational Aggregate Graph (CHEN et al., 2008)

Classic OLAP operations in an i-aggregate graph can be interpreted as follows:

**Roll-up** Aggregate multiple snapshots to form a higher level summary of information

**Drill-down** Return to lower-level snapshots from aggregate graph

**Slice / dice** Select a subset of snapshots based on informational dimensions

Topological Aggregate Graph is obtained based on a single network, where the nodes are the result of applying the aggregate function to the nodes of the original network with the same attribute value. Figure 3.5 shows an example of a t-aggregate graph where the information about co-author relationship between individual authors in one snapshot was aggregated into co-author relationship between the institutions the authors belong to.

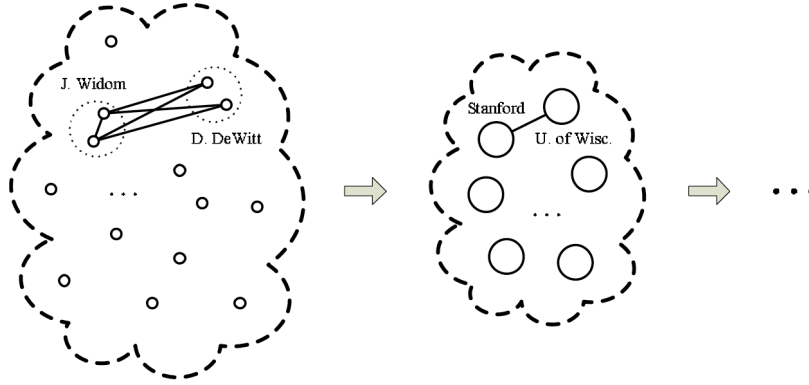


Figure 3.5 – Example of Topological Aggregate Graph (CHEN et al., 2008)

Classic OLAP operations in an t-aggregate graph can be interpreted as follows:

**Roll-up** Merge topological elements (nodes or edges) and replace them by corresponding higher-level elements

**Drill-down** Split merged elements into lower-level elements

**Slice / dice** Select a subgraph of a snapshot based on topological dimensions

The Topological OLAP is further explained in (QU et al., 2011). This work takes into consideration two properties (T-Distributiveness and T-Monotonicity) used to classify how different measures can be performed in an OLAP Graph. A measure function is considered T-Distributive if the result of the function applied to high-level nodes from the graph can be obtained by the computation of pre-computed results of the same function applied to lower-level nodes from the same graph. On the other hand, a measure is considered T-Monotone, if the data search space can be pruned given a user-defined threshold, by dropping node pairs with measures that don't satisfy the threshold. The paper shows experiments using common constraint function, proven to be T-Distributives and/or T-Monotones, such as SUM, MIN, MAX, Density, Degree Centrality, Closeness Centrality, among others.

### 3.3 HMGraph

An Heterogeneous and Multidimensional Graph OLAP framework (HMGraph OLAP) is proposed in (YIN; WU; ZENG, 2012). This framework uses a graph model similar to Graph OLAP (CHEN et al., 2008), but it adds the concept of Entity Dimensions due to the heterogeneity of the input graphs (Graph OLAP framework only handles homogeneous graphs). Figure 3.6 shows an example of a heterogeneous multidimensional network, highlighting the entity attributes of the graph.

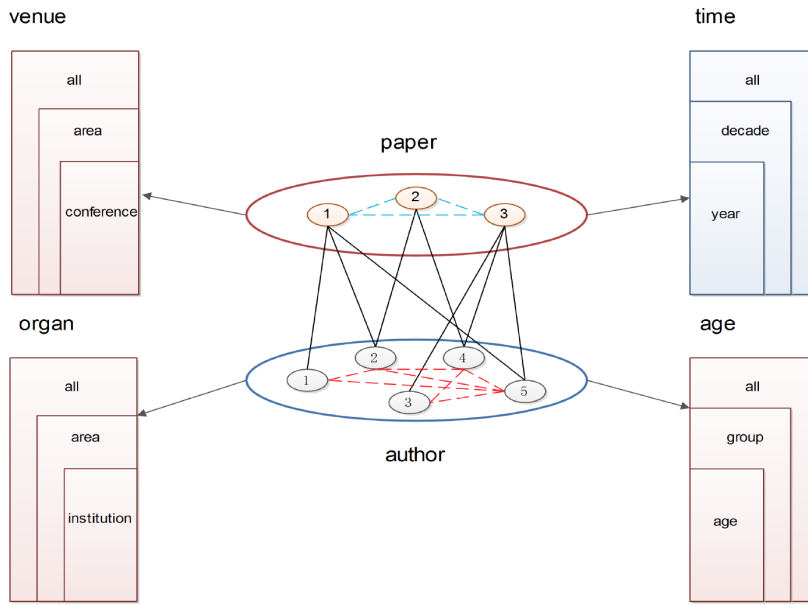


Figure 3.6 – Example of a heterogeneous multidimensional network (YIN; WU; ZENG, 2012)

Entity attributes are the attributes that describe the characteristics of an entity. In the graph illustrated in Figure 3.6, organ and age are entity attributes of author entity. Entity Dimension is related to the types of nodes in the graph.

Like Graph OLAP, HMGraph can perform I-OLAP and T-OLAP operations, but it can also perform rotate and stretch operations. The rotate operation is done by changing nodes into edges and edges into nodes, as shown in Figure 3.7. The stretch operation is done by changing edges into entities and adding edges between the recently created entity and the nodes previously connected to the transformed edge, as shown in Figure 3.8.

Even though the work presented in (YIN; WU; ZENG, 2012) draws attention to the importance of heterogeneous networks in real world application, the paper does not provide further implementation detail on how the framework can be used with real data.

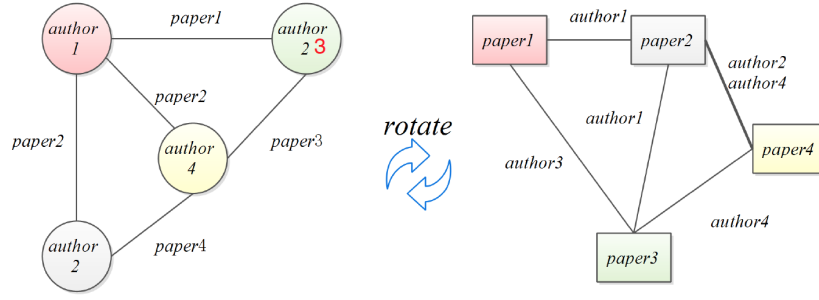


Figure 3.7 – Example of rotate operation (YIN; WU; ZENG, 2012)

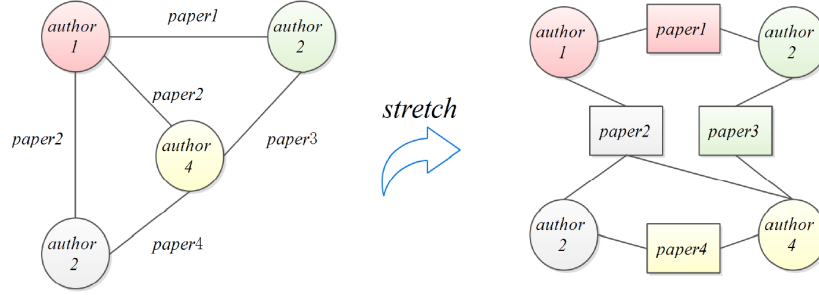


Figure 3.8 – Example of stretch operation (YIN; WU; ZENG, 2012)

### 3.4 Pagrol: PArallel GGraph OLap over Large-scale Attributed Graphs

The work presented in (WANG et al., 2014) proposes a parallel Graph OLAP system, adopting the Hyper Graph Cube model that extends attributed graphs to support decision making services. The model proposed in this paper is similar to the Graph Cube described in (ZHAO et al., 2011), with the main difference being the presence of attributes also in the graph edges. In this scenario, there are two types of dimensions: vertex dimensions and edge dimensions. Figure 3.9 shows an example of an attributed graph.

Given an attributed graph with  $n$  vertex dimensions and  $m$  edge dimensions, the Hyper Graph Cube will contain  $2^{n+m}$  aggregate graph obtained as described by the work of (ZHAO et al., 2011). This Hyper Graph Cube can be seen as the cartesian product between all the vertex-aggregate networks (when one or more vertex dimensions are aggregated) and the edge-aggregate networks (when one or more edge dimensions are aggregated). This cube arrangement can support the following query categories:

**Category 1** Queries answered by information stored either in a vertex or in a edge attributes. For example: “How many relationships appeared in 2012?” or “What is the percentage of users in each different professions in this network?”

**Category 2** Queries answered by integrating the knowledge stored in both vertex and edges attributes. For example: “What is the trend of the number of relations appearing

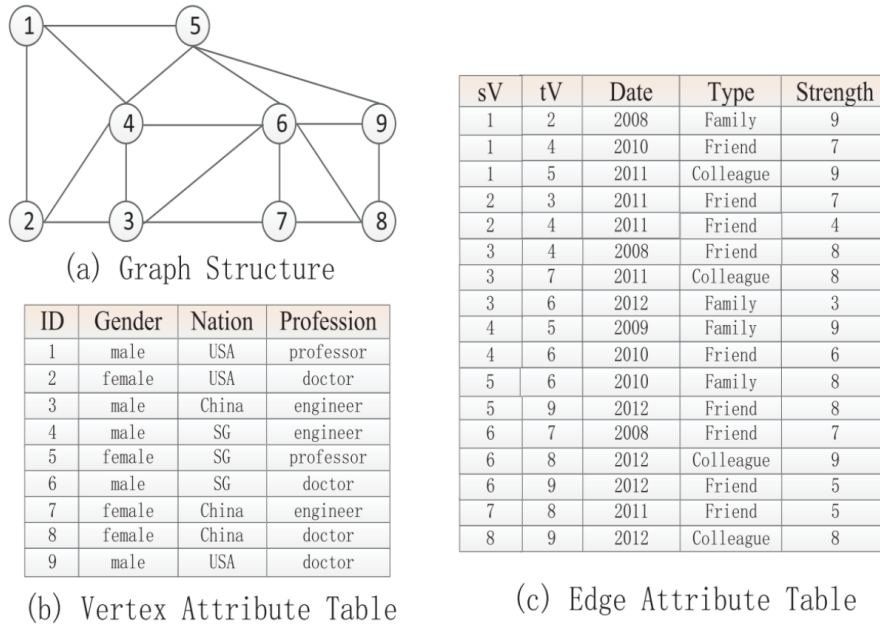


Figure 3.9 – Example of attributed graph (WANG et al., 2014)

between USA and SG (Singapore) in the last 3 years?”

**Category 3** Queries answered by an aggregate graph, that provides a summarised view of the data along some dimensions. For example: “What is the graph structure as grouped by users’ gender as well as relationship type?”

The Hyper Graph Cube also supports roll-up and drill-down operations, along both vertex and edge dimensions. For instance, if we have an aggregate graph along Location dimension according to City value, we can roll up to obtain an aggregate graph according to State value.

The materialisation for the Hyper Graph Cube is done using Map-Reduce (MR) jobs. Since vertex and edges are stored in two different tables in the distributed file system (DFS), the materialisation is done in two steps: first the two tables are joined into one flat table containing all the dimensions and the second step performs the cube computation. This process is optimised using self-contained joins and batching techniques.

### 3.5 GRAD Graph Cubes

One of the most recent works in this area is presented in (GHRAB et al., 2015). This paper proposes a new technique for extracting multidimensional concepts and building OLAP cubes from heterogeneous property graphs. The authors propose a new classification of graph measures based on the aggregation type and computation algorithm:

**Content-based measure** Calculated based on graph’s nodes and edges attributes. They are similar to traditional OLAP measures.

**Graph-specific measure** Obtained by applying graph algorithms. They capture topological properties of the graph.

**Graph as measure** Different aggregation levels of a graph can be considered measures.

Given a property graph with two distinct classes of nodes, the authors explore candidate dimensions, measures and cubes that can be obtained from the graph. The example used throughout the paper is a movie graph: it has movie nodes linked to nodes representing the actors that acted in the movie, as shown in Figure 3.10. The dimensions obtained by a subset of nodes and edges attributes are called inter-class dimensions.

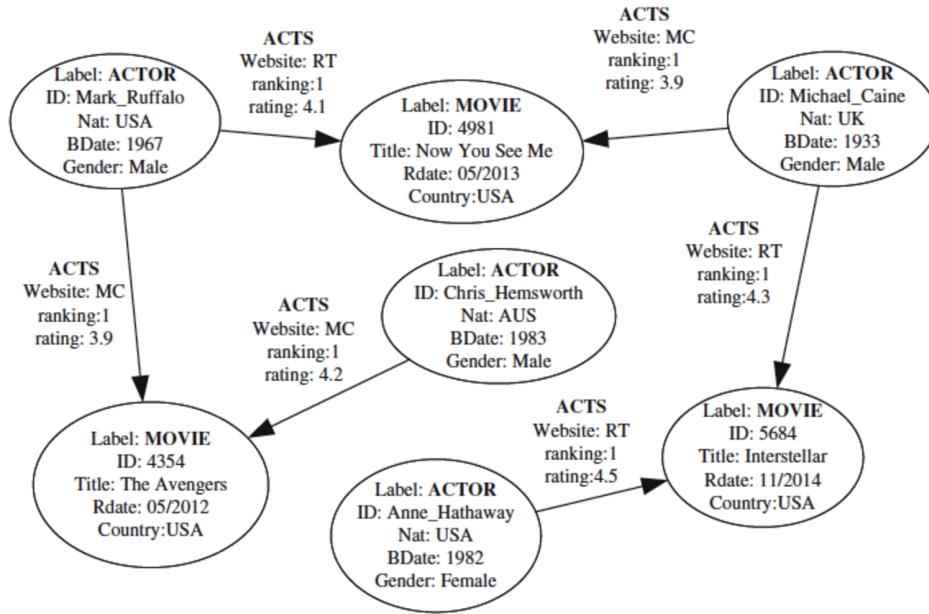


Figure 3.10 – Original movie graph (GHRAB et al., 2015)

Once the dimensions are selected, a graph lattice is defined by all possible OLAP aggregations obtained by aggregating the intra-class dimensions. The inter-class measures fall back in one of the aforementioned categories (content-based, graph-specific or graph as measure).

Figure 3.11 shows the aggregate graph obtained by grouping movies by their release date and actors by their birth date and gender. The graph shows the average ranking and rating of the ACTS relationship between grouped actors and movies.

This paper also proposes a technique for building OLAP cubes extracted from a graph modelled according to the analysis-oriented graph database model GRAD. This model provides advanced graph structures, integrity constraints and graph algebra. According to the authors, traditional property graphs only support OLAP analysis of inter-class

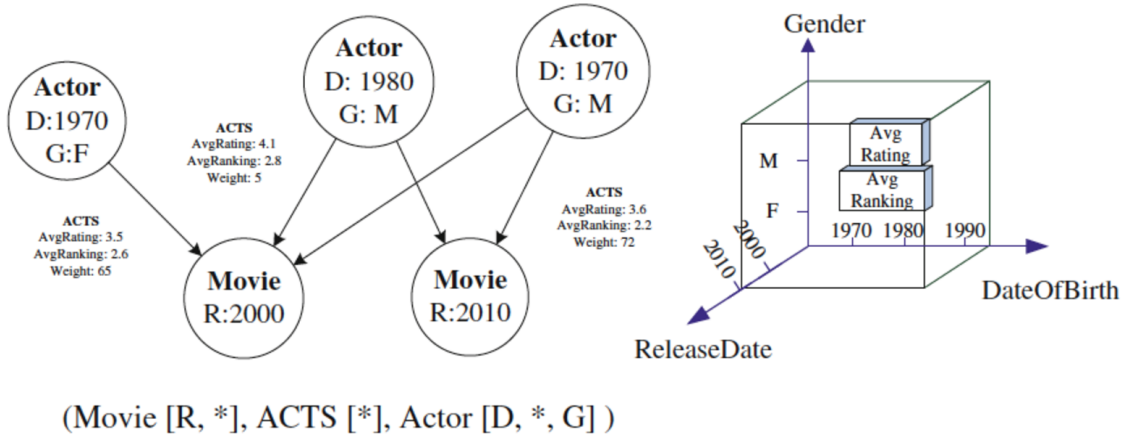


Figure 3.11 – Aggregate Graph for inter-class dimensions (GHRAB et al., 2015)

dimensions, while additional capabilities brought by GRAD allows the analysis of information stored within each node.

The GRAD model consider heterogeneous, attributed, labelled graphs and supports complex type attributes on the nodes. This model introduces special analytical structures called hypernodes, that represent real world entities grouped by classes. Each hypernode is a subgraph formed by an entity node - which contains the label and the identifier attributes - attributes nodes - linked to the entity node and represent the non-identifier attribute - and literal nodes - which stores the effective value of its attribute node. Figure 3.12 shows an example of a movie graph modelled with GRAD.

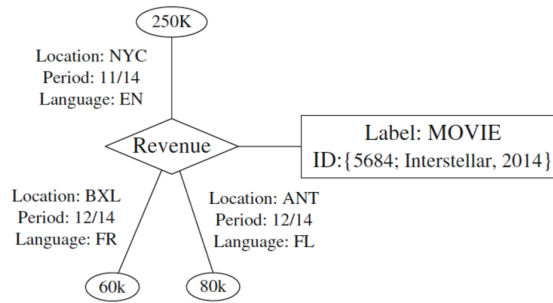


Figure 3.12 – Movie graph on GRAD model (GHRAB et al., 2015)

Based on this model, the paper defines Intra-class Dimensions as a subset of attributes nodes. The Intra-class Measures are identified by the attribute node label and are calculated in a similar way as the measures in property graph model. Figure 3.13 shows the result of applying aggregation function to the original GRAD graph in order to calculate the revenue measure, aggregating the Location according to the Country Name (CN) attribute.

This framework's implementation used Neo4J for the graph storage and HDFS



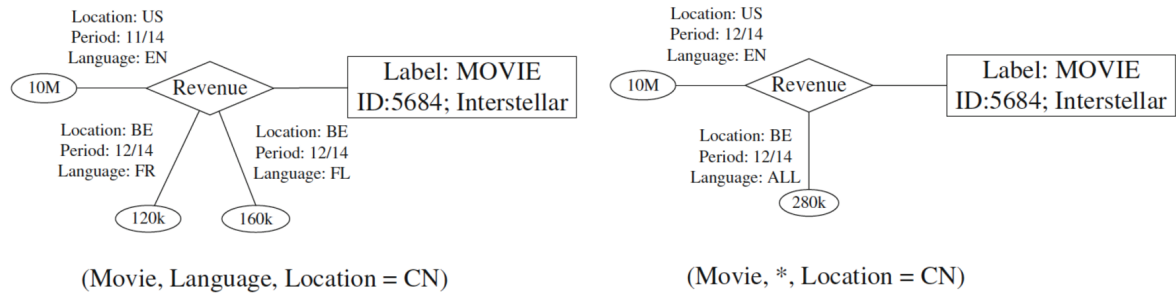


Figure 3.13 – Aggregate Graph for intra-class dimensionl (GHRAB et al., 2015)

(Hadoop Distributed File System) for distributed processing. The architecture is also composed by a middleware layer that is responsible for computing the aggregate graph and measures, using GraphX<sup>1</sup> library to calculate graph-specific measures.

## 3.6 Framework Comparison

The first works done in OLAP analysis on graph focused on homogeneous graph datasets and defined ground concept of this area, such as aggregate graphs and graph lattice. Several operators were proposed and, in general, three types of measures were taken into consideration:

**Informational / Content-based / Attribute-based measure** Similar to traditional OLAP measures, this information is obtained by applying an aggregate function on the node's attributes.

**Topological / Aggregate Graph measure** This type of measure gives information about the topology of the graph and is obtained by applying aggregate function on nodes and edges, generating a graph as a measure.

**Graph-based / specific measure** This type of measure is based on graph analysis theory and can be represented by a number or a subgraph.

One relevant characteristic of the works presented so far is the little explanation given on how the framework was indeed implemented, which made their understanding rather difficult. The Table 1 shows a comparison between all the frameworks presented in this chapter, regarding the type of graph, dimensions and operations supported by each one.

The work proposed here will be focused in heterogeneous graph datasets and will support the three types of measures described previously, in a similar way as presented by

<sup>1</sup> <https://spark.apache.org/graphx/>

Table 1 – Comparison of studied frameworks

Framework	Graph	Dimensions	Operations
Graph Cube	Homogeneous	Vertex Attributes	Cuboid and Crossboid Query
Graph OLAP	Homogeneous	Informational and Topological	I-OLAP and T-OLAP Operations
HMGraph	Heterogeneous	Informational, Topological and Entity	I-OLAP, T-OLAP, Rotate and Stretch Operations
Pagrol	Homogeneous	Vertex and Edge Attributes	3 Query Category and Roll-up/Drill-down Operations
GRAD Graph Cubes	Heterogeneous	Inter-class and Intra-class	-

the work on GRAD Graph Cubes. In addition to that, this work will also explore OLAP operations on graph cubes and will perform further experiments comparing graph OLAP with traditional relational OLAP.

### 3.7 Final Considerations

In this chapter, we presented the main research works published related to OLAP system using Graph Databases. The majority of the works available only supported homogeneous graph, but they introduced important concepts of the area, such as graph cubes and aggregate graph. The implementations that actually gave support to heterogeneous graph, proposed different graph models in order to answer analytical queries. In the next chapter, we will specify a simple OLAP system using Graph Database without the need to define a new graph model.

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