

b) $P(x) \times P^{-1}(x) \equiv 1 \pmod{p(x)}$ irreducible polynomial.

$$(x^7 + x^6 + x^4 + x^3 + x^2 + 1) \times (x^7 + x^6 + x^5 + x^4 + x^3)$$

$$\begin{aligned} & x^{14} + x^{13} + x^{12} + x^{11} + x^{10} + x^9 + x^8 + x^7 + x^6 + x^5 + x^4 + x^3 + x^2 + x + 1 \\ & + x^{10} + x^9 + x^8 + x^7 + x^6 + x^5 + x^4 + x^3 + x^2 + x + 1 + x^7 + x^6 + x^5 + x^4 + x^3 \end{aligned}$$

$$\equiv x^{14} + x^{11} + x^8 + x^6 + x^5 + x^3$$

$$\equiv x^7 + x^6 + x^5 + x^4 + x^3 + x^2 + x + 1 + x^7 + x^6 + x^5 + x^4 + x^3$$

$$\equiv x^5 + x^2 + x + x^6 + 1$$

$$\equiv 1$$

So they are inverse.