

Q 6) As in my folder, there is kript.py. folder which give me the number of coincidence when we shift the text. According to solution most common coincidences appear when shift by 7, 14, 21. From the result, I estimate that key length is 2 when I grouped them by 7 i.

I divide the text into subgroups in my code line 13. When I apply the frequency analysis for ~~first~~ groups I've

$\begin{array}{r} 1. \\ \hline 14 \\ 0 \end{array}$ $\begin{array}{r} 18 \\ S \end{array}$ $\begin{array}{r} 20 \\ Y \end{array}$	$\begin{array}{r} 4 \\ \hline 4 \\ E \end{array}$ $\begin{array}{r} 14 \\ O \end{array}$
$k_1 = 1$ $e \quad i$	$k_4 = W$ $I \quad S$
$\begin{array}{r} 2 \\ \hline 15 \\ P \end{array}$ $\begin{array}{r} 13 \\ D \end{array}$ $\begin{array}{r} 18 \\ S \end{array}$	$\begin{array}{r} 5 \\ \hline 12 \\ A \end{array}$ $\begin{array}{r} 22 \\ W \end{array}$
$k_2 = L$ $E \quad S \quad H$	$k_5 = 8$ $4 \quad 18 \quad 14$
$\begin{array}{r} 3 \\ \hline 9 \\ E \end{array}$ $\begin{array}{r} 19 \\ T \end{array}$ $\begin{array}{r} 0 \\ A \end{array}$	$\begin{array}{r} 6 \\ \hline 22 \\ W \end{array}$ $\begin{array}{r} 6 \\ 0 \end{array}$
$k_3 = 0$	$k_6 = 5$ $e \quad 0$
	$\begin{array}{r} 7 \\ \hline 23 \\ N \end{array}$ $\begin{array}{r} 3 \\ D \end{array}$ $\begin{array}{r} 25 \\ Z \end{array}$
	$k_7 = 14 \quad 4 \quad 0$

Q1) cipher-text = N Z W O  $k=?$

N:13 plaintext  $t = 13 - k \pmod{26}$

Z:25

W:22

O:14

N Z W O

$k=1 \rightarrow$  M Y V N

$2 \rightarrow$  R X U M

$3 \rightarrow$  I K W T L

$4 \rightarrow$  J V S X

$5 \rightarrow$  F U Q J

$6 \rightarrow$  H T Q I

$7 \rightarrow$  G S P H

$8 \rightarrow$  F R O G

$9 \rightarrow$  E Q N F

$10 \rightarrow$  D P M E

$11 \rightarrow$  C O L D

$k = 8, 11$



Q2) We know  $A \rightarrow H$   
 $0 \quad 7$

$(\alpha, \beta)$

$$0: \alpha + \beta \equiv 7$$

$$\downarrow$$

$$7$$

H C  
 $\downarrow \quad \downarrow$   
 A ?  $\rightarrow$  in English C can be 'N', 'M', 'S', 'T'

"N"  $\rightarrow$  C

"M"  $\rightarrow$  C

"S"  $\rightarrow$  C

"T"  $\rightarrow$  C

$$13: \alpha + 7 \equiv 2$$

$$13: \alpha \equiv 21 \pmod{26}$$

$\downarrow$   
 we can not find  
 any  $\alpha$  value since 13  
 divides 26, remainder  
 can be 0 or 13.  
 so plain letter  
 cannot be N.

$$14: \alpha \equiv 21 \pmod{26} \quad 18: \alpha \equiv 21 \pmod{26} \quad 19: \alpha \equiv 21 \pmod{26}$$



They can not since 14  
 and 18 are even number, and  
 26 is even, remainder should  
 be even either.

LAST OPTION

If choose  $\alpha$  as 23,  
 the encryption supports.

We found  $\alpha = 23$  and  $\beta = 7$ . for decryption key:

$$23^{-1} \equiv 17 \pmod{26}$$

$$\alpha_d = 17 \quad \gamma = 11.$$

0: A $\rightarrow$ H: 7	13: N $\rightarrow$ U: 20
1: B $\rightarrow$ E: 4	14: M $\rightarrow$ X: 23
2: C $\rightarrow$ B: 1	15: O $\rightarrow$ R: 17
3: D $\rightarrow$ Y: 24	16: P $\rightarrow$ -
4: E $\rightarrow$ V: 21	17: Q $\rightarrow$ -
5: F $\rightarrow$ S: 18	18: R $\rightarrow$ I: 8
6: G $\rightarrow$ -	19: S $\rightarrow$ F: 5
7: H $\rightarrow$ M: 12	20: T $\rightarrow$ C: 12
8: I $\rightarrow$ J: 19	21: U $\rightarrow$ Z: 25
9: J $\rightarrow$ -	22: V $\rightarrow$ -
10: K $\rightarrow$ D: 3	23: W $\rightarrow$ T: 19
11: L $\rightarrow$ A: 0	24: Y $\rightarrow$ N: 13
12: M $\rightarrow$ X: 23	25: Z $\rightarrow$ -

A successful man is one who  
 can lay a firm foundation with the  
 bricks others have thrown at him.

Q3) Since an alphabet is bigram and 31 letters in it the modulo should be  $31 * 31 = 961$ . This is our modulo. And for the beta value  $\gcd(a, b) \neq 1$ .

Beta can be any value between 0-960. Because it just shifts. However, alpha can not take any value that

has  $\gcd(a, b) \neq 1$ . Since 31 is prime, only the factors of 31 can not be alpha. Since 961 is  $31 * 31$

$$\# \alpha = 961 - 31 = \underline{\underline{930}}$$

$$\text{Total key space} = 961 * 930 = 893730$$



Q5)  $\{S, A, N, I, T, Y\} = \{19, 0, 13, 8, 19, 24\}$

A R R N N W T B I G Q O E E B A Y L Q . H M L R A O A W G  
0 17 13 13 13 16 22 19 1 8 6 16 14 4 4 1 0 24 11 16 2 12 11 17 0 14 0 22 6  
-18 -0 -13 -8 -19 -24 -18 -0 -13 -8 -19 -24 -13 -0 -13 -8 -19 -24 -18 -0 -13 -8 -19

8 / 17 4 5 20 18 4 / 19 14 / 0 13 18 22 4 17 / 19 7 0 19 / 16 20 18 19 8 14 13 14 13

I REFUSE TO ANSWER THAT QUESTION ON.

R 2 E T 2 H S F D F B A Y L I Q W G ' R C N B E M F W  
17 25 4 19 25 7 18 5 3 5 1 0 24 11 8 16 22 6 17 2 13 1 4 17 1 5 22  
-24 -18 -0 -13 -8 -19 -24 -18 -0 -13 -8 -19 -24 -18 -0 -13 -8 -19 -24 -18 -14 -0 -13 -8 -19 -24 -18  
19 7 4 6 17 14 20 13 3 18 19 7 0 19 8 3 14 13 19 10 13 14 22 19 7 4

THE GROUNDS THAT I DONT KNOW THE

A A A P C J  
0 0 0 15 29  
-0 -13 -8 -19 -24 -18  
0 13 18 22 4 17  
A N S W E R .