

HYPOTHESIS TESTING FRAMEWORK - 1



*Terminologies
Everywhere !!!*

Conduct → 9:00 pm → 9:02 pm

↓ Revise

9:05/9:10 pm
~~~~~  
↓

10:10 → Break 5 mins

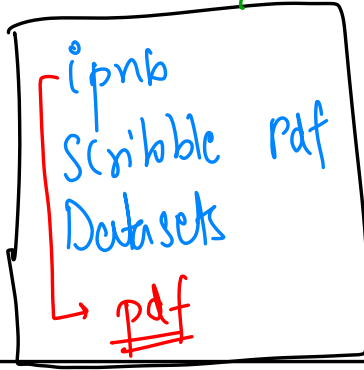
10:15

↓

11:00/11:15 → Start doubt session -

→

Google Drive



Lecture Notes

(i) Concept  
1<sup>st</sup> Repeat  
2<sup>nd</sup> Repeat

Assessments

→ ~~X~~ live class ~~X~~

Q1 ✓

Q2

Q3

50% ←

50%

# Problem Solving Class

L1 Q1 - - - Qn

⋮

L12

Attempted

Hypothesis Testing

→ most difficult module.

\* Advanced  
distribution

→ Poisson, Exponential

Chi square  
{ Correlation } →

t test

KRUSKAL

ANOVA

\* Feature Engineering

## Cricket Series Example → The captain always calls heads

1) 10 matches Series  
7 Tosses were won

Is the Coin fair?

YES  
30

NO  
14

2) 100 matches Series  
70 Tosses were won

Is the Coin fair?

YES  
94

NO  
23

3) 1000 matches Series  
700 Tosses were won

Is the Coin fair?

YES  
8

NO  
17

We need a mathematical framework  
which will Quantify this??

## Cricket Series Example

"Status Quo"

1) What is our default assumption?

$H_0$  It is a fair coin

2) When should we reject the assumption?

$H_a$  When we have conclusive evidence to prove otherwise.

# Judge in Court

Assume that you are judging a murder case.

"Innocent until proven guilty"



1) What is our default assumption?

$H_0$

Person is innocent.

2) When should we reject the assumption?

$H_a$

When we have enough conclusive evidence to prove otherwise.



# Machine Learning Model Deployment

ML algorithm is in production ( legacy ). You and your team have built a new model, and want to replace the legacy model.

1) What is our default assumption?

$H_0$  performance old model = new model

2) When should we reject the assumption?

$H_a$  When we have enough conclusive evidence to prove otherwise.

# Third Umpire

Suppose you are the third umpire.

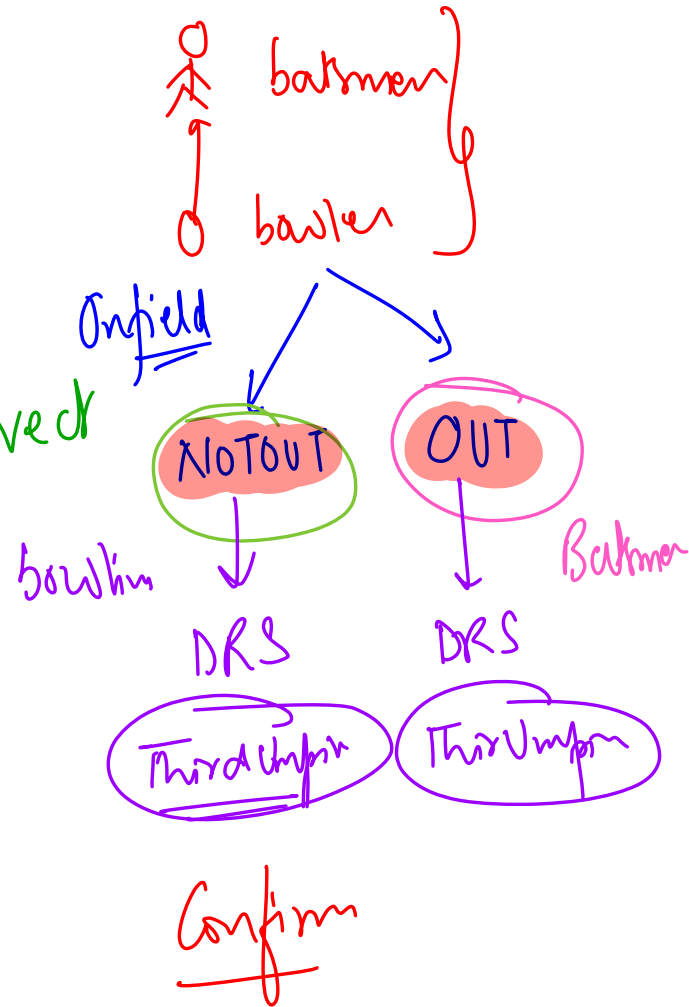
The batsmen have taken a drs on being given out.

1) What is our default assumption?

Onfield umpire is correct

2) When should we reject the assumption?

When we have enough conclusive evidence to prove otherwise.



# Fingerprint Sensor

We unlock our phones using a fingerprint scanner. A finger is placed on the scanner.

1) What is our default assumption?

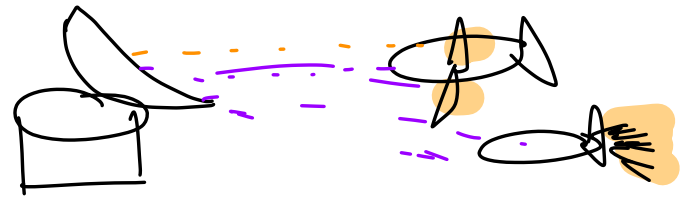
No fingerprint <sup>doesn't</sup> matches with the owner.

2) When should we reject the assumption?

No When we have enough conclusive evidence to prove otherwise.

# Radar Example

A Radar has to detect a plane.



1) What is our default assumption?

RADAR

~~Default~~  
~~There is an enemy plane.~~

$H_0$  Sky is clear, There is no enemy plane.

2) When should we reject the assumption?

$H_a$  sky is not clear.

When we have enough conclusive evidence to prove otherwise.

## Terminologies

$H_0$ : NULL HYPOTHESIS

- ① Coin is fair
- ② Person is innocent
- ③ ML model old = new
- ④ Radar → Sky is clear
- ⑤ Fingerprint → doesn't match
- ⑥ Thunderstorm is correct

$H_a$ : ALTERNATE HYPOTHESIS

When we have enough conclusive evidence to prove otherwise.

## Judge in Court

Ho. Person is innocent

When we have sufficient evidence to prove otherwise.

Data :

- ① Person was carrying a knife. "he is a chef" ✗
- ② There was blood on knife. "blood belonged to victim" ✗
- ③ Blood group matches with "person is a friend" ✗  
the victim

Verdict :

- ④ Fingerprint & blood of dead person was found on T-shirt ✗
- ⑤ Eye witness "Eye witness lying" ✗
- ⑥ CCTV FOOTAGE "DEEP FAKE" ✗

Reject Ho

$P[\text{data} \mid H_0 \text{ is true}] \rightarrow \text{pvalue}$   
evidences person is innocent.  $\rightarrow$  Very low

pvalue

Probability of observing/seeing the data/evidence  
as extreme as was observed, under the assumption  
that  $H_0$  is true

## Deep Dive : Coin toss Example



# Coin toss

Case 1 : 10 match series, 7 heads were observed. Would you believe that the coin is fair?

1) What is the random variable?

$X \rightarrow$  No. of heads

2) What is the distribution?

Binomial

3) What is the observed value?

7

4) What is probability of our observation assuming  $H_0$  is true?

$P = [0.1171]$

$${}^n C_k p^k (1-p)^{n-k}$$

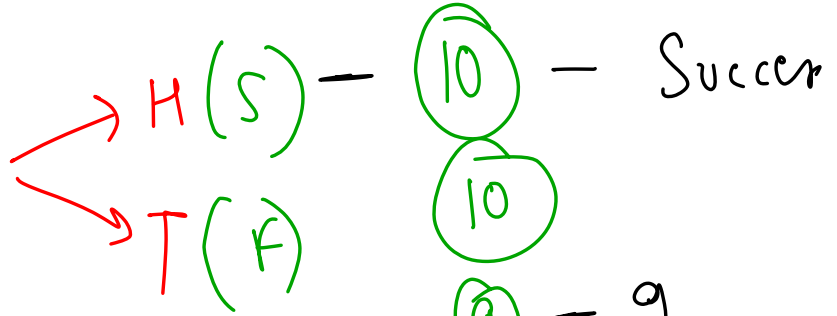
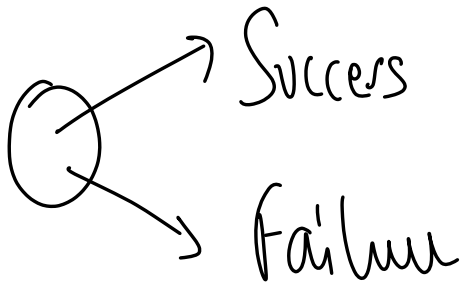
$H_0$ : Coin is fair

$H_a$ : Coin is biased.

$$n = 10$$

$$k = 7$$

$$p = 0.5$$



bernoulli trial

$$P[X=k] = {}^n C_k (p)^k (1-p)^{n-k}$$

$$= {}^{10} C_7 (0.5)^7 (1-0.5)^3$$

