### Assignment-6.R

nidhi

2020-10-20

```
#Loading Packages
library(mvtnorm)
## Warning: package 'mvtnorm' was built under R version 3.6.3
library(dplyr)
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
##
       intersect, setdiff, setequal, union
library(psych)
## Warning: package 'psych' was built under R version 3.6.3
#Loading dataset
dataset <-
read.csv("C:/Users/nidhi/OneDrive/Desktop/MVA/heart_failure_clinical_records_
dataset.csv")
View(dataset)
attach(dataset)
#Identifying different columns names
names(dataset)
## [1] "age"
                                    "anaemia"
## [3] "creatinine_phosphokinase" "diabetes"
## [5] "ejection_fraction"
                                   "high_blood_pressure"
## [7] "platelets"
                                   "serum_creatinine"
## [9] "serum_sodium"
                                   "sex"
## [11] "smoking"
                                   "time"
## [13] "DEATH_EVENT"
#Data Summary
str(dataset)
```

```
## 'data.frame': 299 obs. of 13 variables:
## $ age
                           : num 75 55 65 50 65 90 75 60 65 80 ...
                           : int 0001111101...
## $ anaemia
## $ creatinine_phosphokinase: int 582 7861 146 111 160 47 246 315 157 123
## $ diabetes
                            : int 0000100100...
## $ ejection fraction
                           : int 20 38 20 20 20 40 15 60 65 35 ...
## $ high blood pressure
                                 1000010001...
                           : int
## $ platelets
                           : num 265000 263358 162000 210000 327000 ...
                           : num 1.9 1.1 1.3 1.9 2.7 2.1 1.2 1.1 1.5 9.4
## $ serum creatinine
## $ serum_sodium
                           : int 130 136 129 137 116 132 137 131 138 133
## $ sex
                           : Factor w/ 2 levels "Female", "male": 2 2 2 2 1
2 2 2 1 2 ...
                          : int 0010010101...
## $ smoking
## $ time
                           : int 4 6 7 7 8 8 10 10 10 10 ...
                          : Factor w/ 2 levels "Death", "No Death": 2 2 2
## $ DEATH EVENT
2 2 2 2 2 2 2 ...
summary(dataset)
##
                     anaemia
                                  creatinine phosphokinase
       age
## Min. :40.00
                                  Min. : 23.0
                  Min.
                         :0.0000
## 1st Qu.:51.00
                  1st Qu.:0.0000
                                  1st Qu.: 116.5
## Median :60.00
                  Median :0.0000
                                  Median : 250.0
## Mean
                                  Mean : 581.8
        :60.83
                  Mean :0.4314
## 3rd Qu.:70.00
                  3rd Qu.:1.0000
                                  3rd Qu.: 582.0
## Max.
         :95.00
                  Max.
                        :1.0000
                                  Max. :7861.0
##
                   ejection fraction high blood pressure
      diabetes
                                                         platelets
## Min.
          :0.0000
                   Min. :14.00
                                    Min. :0.0000
                                                       Min. : 25100
## 1st Qu.:0.0000
                   1st Qu.:30.00
                                    1st Qu.:0.0000
                                                       1st Qu.:212500
## Median :0.0000
                   Median :38.00
                                    Median :0.0000
                                                       Median :262000
## Mean
         :0.4181
                   Mean :38.08
                                    Mean
                                          :0.3512
                                                       Mean
                                                             :263358
## 3rd Qu.:1.0000
                                    3rd Qu.:1.0000
                   3rd Qu.:45.00
                                                       3rd Qu.:303500
## Max.
        :1.0000
                   Max. :80.00
                                    Max. :1.0000
                                                       Max.
                                                             :850000
                                                 smoking
## serum_creatinine serum_sodium
                                      sex
## Min. :0.500
                   Min. :113.0
                                  Female:105
                                              Min.
                                                     :0.0000
## 1st Ou.:0.900
                   1st Ou.:134.0
                                  male :194
                                              1st Ou.:0.0000
## Median :1.100
                   Median :137.0
                                              Median :0.0000
## Mean
        :1.394
                   Mean :136.6
                                              Mean
                                                     :0.3211
## 3rd Qu.:1.400
                   3rd Qu.:140.0
                                              3rd Qu.:1.0000
         :9.400
## Max.
                   Max. :148.0
                                              Max.
                                                     :1.0000
##
                    DEATH EVENT
        time
## Min.
                        :203
        : 4.0
                  Death
## 1st Qu.: 73.0
                  No Death: 96
## Median :115.0
## Mean :130.3
## 3rd Qu.:203.0
## Max. :285.0
```

```
head(dataset)
     age anaemia creatinine_phosphokinase diabetes ejection_fraction
##
## 1
      75
## 2 55
               0
                                       7861
                                                   0
                                                                      38
## 3 65
               0
                                        146
                                                   0
                                                                      20
## 4 50
               1
                                        111
                                                   0
                                                                      20
               1
## 5 65
                                        160
                                                   1
                                                                      20
## 6 90
               1
                                         47
                                                   0
                                                                      40
##
     high_blood_pressure platelets serum_creatinine serum_sodium
                                                                        sex
                                                   1.9
## 1
                        1
                             265000
                                                                130
                                                                       male
## 2
                        0
                             263358
                                                  1.1
                                                                136
                                                                       male
## 3
                        0
                                                   1.3
                                                                129
                                                                       male
                             162000
## 4
                        0
                             210000
                                                  1.9
                                                                137
                                                                       male
## 5
                        0
                             327000
                                                  2.7
                                                                116 Female
## 6
                        1
                             204000
                                                  2.1
                                                                132
                                                                       male
     smoking time DEATH_EVENT
## 1
           0
                4
                      No Death
## 2
           0
                 6
                      No Death
## 3
           1
                7
                      No Death
## 4
           0
                7
                      No Death
## 5
           0
                 8
                      No Death
## 6
           1
                 8
                      No Death
dim(dataset)
## [1] 299 13
#Checking for missing values
is.null(dataset)
## [1] FALSE
##The "FALSE" output shows there is no missing data in the dataset.
#Correlation
correlation < -cor(dataset[c(1,3,5,7,8,9,12)])
View(correlation)
#From the table, we can see all the continuous variables are uncorrelated
#Principal components
dataset pca <- prcomp(dataset[c(1,3,5,7,8,9,12)],scale=TRUE)</pre>
dataset_pca
## Standard deviations (1, .., p=7):
## [1] 1.2143198 1.0842469 1.0146325 0.9829678 0.9421964 0.8587448 0.8537882
## Rotation (n \times k) = (7 \times 7):
                                                                           PC4
##
                                     PC1
                                                  PC2
                                                              PC3
                              0.4649617 -0.45213222 0.00779977 0.19809211
## age
```

```
## creatinine phosphokinase -0.1379593 0.19389349 -0.81505355 0.33440577
## ejection fraction
                            -0.1788924 -0.68147830 0.10671326 0.01299509
## platelets
                            -0.1992576 -0.24678636 -0.40331735 -0.82095373
## serum creatinine
                             0.5117770 -0.04569638 -0.10167226 -0.18226520
## serum sodium
                            -0.4474108 -0.42971962 -0.11797610 0.36260682
## time
                            ##
                                   PC5
                                              PC6
                                                            PC7
                             0.1912135 -0.6341378 0.318421659
## age
## creatinine_phosphokinase -0.2948224 -0.1008787 0.264832516
                            -0.4694857 0.3913478 0.344177806
## ejection fraction
## platelets
                             0.1807563 -0.1733047 0.007459381
                            -0.6335802 -0.1069130 -0.528757042
## serum creatinine
## serum sodium
                             0.1513990 -0.1865190 -0.641912443
## time
                            -0.4461860 -0.5985695 0.135357997
#Recreating the summary table manually
(eigen dataset <- dataset pca$sdev^2)</pre>
## [1] 1.4745726 1.1755914 1.0294792 0.9662257 0.8877341 0.7374427 0.7289544
names(eigen dataset) <- paste("PC",1:7,sep="")</pre>
eigen_dataset
##
                   PC2
                             PC3
                                       PC4
                                                 PC5
                                                           PC6
                                                                      PC7
         PC1
## 1.4745726 1.1755914 1.0294792 0.9662257 0.8877341 0.7374427 0.7289544
sumlambdas <- sum(eigen_dataset)</pre>
sumlambdas
## [1] 7
propvar <- eigen_dataset/sumlambdas</pre>
propvar
##
         PC1
                   PC2
                             PC3
                                       PC4
                                                 PC5
                                                            PC<sub>6</sub>
                                                                      PC7
## 0.2106532 0.1679416 0.1470685 0.1380322 0.1268192 0.1053490 0.1041363
cumvar dataset <- cumsum(propvar)</pre>
cumvar_dataset
                             PC3
                                       PC4
                                                 PC5
##
                   PC2
                                                           PC6
                                                                      PC7
## 0.2106532 0.3785949 0.5256633 0.6636956 0.7905147 0.8958637 1.0000000
matlambdas <- rbind(eigen dataset,propvar,cumvar dataset)</pre>
rownames(matlambdas) <- c("Eigenvalues", "Prop. variance", "Cum. prop.</pre>
variance")
round(matlambdas,6)
##
                            PC1
                                     PC2
                                              PC3
                                                       PC4
                                                                PC5
                                                                          PC6
## Eigenvalues
                       1.474573 1.175591 1.029479 0.966226 0.887734 0.737443
                       0.210653 0.167942 0.147068 0.138032 0.126819 0.105349
## Prop. variance
## Cum. prop. variance 0.210653 0.378595 0.525663 0.663696 0.790515 0.895864
```

```
##
                           PC7
## Eigenvalues
                      0.728954
## Prop. variance
                      0.104136
## Cum. prop. variance 1.000000
#Based on Option 2 rule, which says components whose Eigenvalues are larger
than 1 should be considered, so we need to keep PC1 through PC3
summary(dataset_pca)
## Importance of components:
                                                 PC4
##
                            PC1
                                   PC2
                                          PC3
                                                        PC5
                                                               PC6
                                                                      PC7
                         1.2143 1.0842 1.0146 0.9830 0.9422 0.8587 0.8538
## Standard deviation
## Proportion of Variance 0.2107 0.1679 0.1471 0.1380 0.1268 0.1053 0.1041
## Cumulative Proportion 0.2107 0.3786 0.5257 0.6637 0.7905 0.8959 1.0000
eigvec.heart<-dataset pca$rotation
print(eigvec.heart)
                                              PC2
                                                          PC3
                                                                      PC4
##
                                  PC1
## age
                            0.4649617 -0.45213222 0.00779977
                                                               0.19809211
## creatinine phosphokinase -0.1379593 0.19389349 -0.81505355
                                                               0.33440577
## ejection_fraction
                           -0.1788924 -0.68147830 0.10671326 0.01299509
                           -0.1992576 -0.24678636 -0.40331735 -0.82095373
## platelets
## serum_creatinine
                            0.5117770 -0.04569638 -0.10167226 -0.18226520
## serum_sodium
                           -0.4474108 -0.42971962 -0.11797610 0.36260682
## time
                           -0.4806034
                                      ##
                                  PC5
                                             PC6
                                                          PC7
## age
                            0.1912135 -0.6341378 0.318421659
## creatinine_phosphokinase -0.2948224 -0.1008787 0.264832516
## ejection_fraction
                           -0.4694857 0.3913478 0.344177806
## platelets
                            0.1807563 -0.1733047 0.007459381
## serum creatinine
                           -0.6335802 -0.1069130 -0.528757042
## serum sodium
                            0.1513990 -0.1865190 -0.641912443
                           -0.4461860 -0.5985695 0.135357997
## time
# Taking the first three PCs to generate linear combinations for all the
variables with three factors
pcafactors.heart <- eigvec.heart[,1:3]</pre>
pcafactors.heart
##
                                  PC1
                                              PC2
                                                          PC3
## age
                            0.4649617 -0.45213222
                                                   0.00779977
## creatinine phosphokinase -0.1379593 0.19389349 -0.81505355
## ejection fraction
                           -0.1788924 -0.68147830 0.10671326
## platelets
                           -0.1992576 -0.24678636 -0.40331735
## serum_creatinine
                            0.5117770 -0.04569638 -0.10167226
## serum sodium
                           -0.4474108 -0.42971962 -0.11797610
## time
                           -0.4806034 0.21428597
                                                   0.37056533
```

```
# Multiplying each column of the eigenvector's matrix by the square-root of
the corresponding eigenvalue in order to get the factor loadings
unrot.fact.heart <-</pre>
sweep(pcafactors.heart,MARGIN=2,dataset pca$sdev[1:3],`*`)
unrot.fact.heart
##
                                    PC1
                                                PC2
                                                             PC3
                             0.5646122 -0.49022298 0.007913901
## age
## creatinine phosphokinase -0.1675268 0.21022842 -0.826979846
## ejection_fraction
                            -0.2172326 -0.73889076 0.108274741
## platelets
                            -0.2419625 -0.26757736 -0.409218900
## serum creatinine
                             0.6214609 -0.04954616 -0.103159985
                            -0.5432998 -0.46592218 -0.119702387
## serum sodium
## time
                            -0.5836063 0.23233891 0.375987635
# Computing communalities
communalities.heart <- rowSums(unrot.fact.heart^2)</pre>
communalities.heart
##
                        age creatinine_phosphokinase
                                                             ejection_fraction
##
                  0.5591682
                                            0.7561569
                                                                     0.6048730
##
                  platelets
                                    serum creatinine
                                                                  serum sodium
##
                  0.2976036
                                           0.3993105
                                                                     0.5265868
##
                       time
                  0.5359443
##
# Performing the varimax rotation. The default in the varimax function is
norm=TRUE thus, Kaiser normalization is carried out
rot.fact.heart <- varimax(unrot.fact.heart)</pre>
View(unrot.fact.heart)
rot.fact.heart
## $loadings
##
## Loadings:
##
                            PC1
                                   PC2
                                          PC3
## age
                             0.696 -0.185 0.200
## creatinine phosphokinase
                                           -0.864
## ejection fraction
                                    -0.755 0.157
                                   -0.357 -0.412
## platelets
## serum creatinine
                             0.586 0.232
## serum sodium
                            -0.240 -0.663 -0.173
## time
                            -0.702
                                            0.201
##
##
                    PC1
                          PC2
                                PC3
## SS loadings
                  1.390 1.235 1.054
## Proportion Var 0.199 0.176 0.151
## Cumulative Var 0.199 0.375 0.526
##
## $rotmat
              [,1] [,2] [,3]
```

```
0.8660041 0.4477622 0.2225891
## [2,] -0.4270706 0.8938525 -0.1365226
## [3,] -0.2600915 0.0231679 0.9653060
# The print method of varimax omits loadings less than abs(0.1). In order to
display all the loadings, it is necessary to ask explicitly the contents of
the object $loadings
fact.load.heart <- rot.fact.heart$loadings[1:7,1:3]</pre>
fact.load.heart
##
                                     PC1
                                                  PC2
                                                              PC3
                              0.69625801 -0.18519166
## age
                                                       0.20024241
## creatinine phosphokinase -0.01977081 0.09374166 -0.86427917
## ejection_fraction
                              0.09927290 -0.75521937 0.15703997
## platelets
                              0.01116830 -0.35699707 -0.41234930
## serum creatinine
                              0.58617844 0.23158975
                                                     0.04551365
## serum sodium
                             -0.24038458 -0.66250806 -0.17287312
## time
                             -0.70242172 -0.04492927
                                                       0.20131920
# Computing the rotated factor scores for the 299 Patients
scale.heart <- scale(dataset[c(1,3,5,7,8,9,12)])</pre>
scale.heart
##
                  age creatinine_phosphokinase ejection_fraction
##
     [1,]
           1.19094867
                                    0.000165451
                                                      -1.527997920
##
     [2,] -0.49045705
                                    7.502062717
                                                      -0.007064906
##
     [3,]
                                   -0.449185725
                                                      -1.527997920
          0.35024581
##
     [4,] -0.91080848
                                   -0.485257493
                                                      -1.527997920
##
     [5,]
          0.35024581
                                   -0.434757017
                                                      -1.527997920
##
          2.45200296
                                   -0.551217299
                                                       0.161927651
     [6,]
##
     [7,]
           1.19094867
                                   -0.346123528
                                                      -1.950479313
##
     [8,] -0.07010562
                                   -0.275010613
                                                       1.851853222
##
     [9,]
           0.35024581
                                   -0.437848883
                                                       2.274334615
##
                                   -0.472890030
    [10,]
          1.61130010
                                                      -0.260553742
##
    [11,]
           1.19094867
                                   -0.516176152
                                                      -0.007064906
##
    [12,]
           0.09803495
                                   -0.361582858
                                                      -1.105516528
##
    [13,] -1.33115991
                                    0.411383614
                                                      -0.683035135
##
    [14,] -0.91080848
                                   -0.426512042
                                                      -0.007064906
##
    [15,] -0.99487877
                                   -0.517206774
                                                      -0.683035135
    [16,]
##
           1.77944067
                                   -0.209050807
                                                       1.006890437
##
    [17,]
                                                      -0.007064906
           2.19979210
                                   -0.446093859
##
    [18,] -1.33115991
                                    0.000165451
                                                      -2.034975592
##
    [19,]
           0.77059724
                                   -0.470828786
                                                      -1.105516528
##
   [20,] -1.07894905
                                    0.000165451
                                                       1.429371829
##
    [21,]
          0.35024581
                                   -0.546064189
                                                      -1.105516528
##
    [22,]
           0.35024581
                                   -0.467736920
                                                      -0.683035135
##
    [23,]
          0.60245667
                                   -0.372919699
                                                      -0.260553742
##
    [24,] -0.65859762
                                   -0.534727348
                                                       1.851853222
##
    [25,]
           1.19094867
                                    0.000165451
                                                      -0.683035135
##
    [26,]
           1.61130010
                                   -0.447124481
                                                      -0.007064906
##
   [27,] 2.87235439
                                   -0.484226871
                                                       0.161927651
```

##		0.77059724	-0.473920652	0.584409044
##	[29,]	-0.23824619	-0.537819214	-0.007064906
##	[30,]	1.77944067	-0.527512994	-0.683035135
##	[31,]	2.78828410	0.000165451	-0.007064906
##	[32,]	2.03165153	-0.575952226	0.584409044
##	[33,]	-0.91080848	-0.343031663	-0.260553742
##	[34,]	-0.91080848	-0.435787639	-0.683035135
##	[35,]	0.35024581	-0.502778067	1.006890437
##	[36,]	0.68652695	0.000165451	-0.260553742
##	[37,]	2.45200296	-0.537819214	1.006890437
##	[38,]	1.77944067	0.281525247	1.006890437
##	[39,]	-0.07010562	2.137675402	-0.683035135
##	[40,]	-0.07010562	-0.357460370	-0.007064906
##	[41,]	0.77059724	0.000165451	-1.527997920
##	[42,]	-0.91080848	-0.471859408	-0.683035135
##	[43,]	0.77059724	-0.011171391	0.584409044
##	[44,]	0.93873781	-0.468767542	1.006890437
##	[45,]	-0.07010562	0.006349183	1.851853222
##	[46,]	-0.91080848	0.000165451	-0.007064906
##	[47,]	-0.82673819	0.822601777	-1.105516528
##	[48,]	-0.07010562	0.000165451	-0.007064906
##	[49,]	1.61130010	-0.029722586	-1.527997920
##	[50,]	-0.32231648	-0.466706298	-0.683035135
##	[51,]	0.60245667	-0.004987659	-1.105516528
##	[52,]	-0.65859762	-0.505869933	-1.527997920
##	[53,]	-0.07010562	3.485728929	2.020845779
##	[54,]	0.77059724	-0.528543616	1.006890437
##	[55,]	-0.07010562	-0.331694821	-0.007064906
##	[56,]	2.87235439	-0.217295783	-0.683035135
##	[57,]	0.77059724	-0.522359884	-0.260553742
##	[58,]	-0.07010562	0.025931000	0.161927651
##	[59,]	-0.99487877	0.213504197	-1.527997920
##	[60,]	0.93873781	-0.224510137	-1.527997920
##	[61,]	-1.33115991	7.338193825	-1.105516528
##	[62,]	-0.91080848	-0.271918747	0.161927651
##	[63,]	-0.49045705	-0.487318737	-0.260553742
##	[64,]	-1.33115991	0.000165451	-0.260553742
##	[65,]	-1.33115991	0.000165451	3.541778793
##		-0.07010562	-0.529574238	-1.527997920
##	[67,]	-1.58337077	-0.342001041	-1.950479313
##	[68,]	0.93873781	-0.486288115	-1.105516528
##	[69,]	0.77059724	-0.433726395	-1.105516528
##	[70,]	0.35024581	-0.483196249	-1.105516528
##	[71,]	-1.66744105	-0.447124481	0.161927651
##	[72,]	-0.23824619	0.000165451	-0.260553742
##	[73,]		5.462461853	-0.260553742
##	[74,]	0.35024581	-0.368797212	1.006890437
##	[75,]	0.68652695	0.000165451	-1.527997920
##	[76,]	-0.07010562	-0.551217299	-1.527997920
##	[77,]	0.77059724	-0.504839311	1.851853222

##		-1.58337077	-0.494533091	
##	[79,]	1.19094867	-0.390440273	
##	[80,]	-0.49045705	-0.253367552	0.584409044
##	[81,]	0.77059724	-0.528543616	0.161927651
##	[82,]	0.51838638	0.000165451	1.006890437
##	[83,]	-0.07010562	-0.521329262	-1.105516528
##	[84,]	1.52722981	-0.542972323	1.006890437
##	[85,]	-0.15417591	-0.311082382	-1.105516528
##	[86,]	-0.82673819	-0.519268018	
##	[87,]	-0.49045705	-0.551217299	-0.260553742
##	[88,]	0.35024581	-0.529574238	1.851853222
##	[89,]	-1.41523020	-0.513084286	0.161927651
##	[90,]	-0.32231648	-0.481135006	-1.105516528
##	[91,]	0.77059724	-0.531635482	0.584409044
##	[92,]	-0.07010562	0.324811369	0.584409044
##	[93,]	-1.58337077	0.000165451	1.851853222
##	[94,]	-0.07010562	-0.440940749	-1.105516528
##	[95,]	-0.23824619	-0.451246969	-0.007064906
##	[96,]	-0.23824619	-0.462583810	1.851853222
##	[97,]	0.18210524	-0.069916842	-1.105516528
##	[98,]	0.77059724	-0.538849835	1.851853222
##	[99,]	-0.07010562	-0.438879505	-1.105516528
##	[100,]	0.18210524	-0.536788592	0.161927651
##	[101,]	0.35024581	-0.285316833	-1.105516528
##	[102,]	1.19094867	0.000165451	0.584409044
		1.61130010	0.325841991	-1.105516528
##	[104,]	-1.58337077	4.768853272	-0.683035135
##	[105,]	-0.07010562	-0.545033567	1.006890437
##	[106,]	0.93873781	-0.261612528	-0.683035135
##	[107,]	-0.49045705	0.171248697	0.584409044
##	[108,]	-1.33115991	1.333790271	-0.260553742
##	[109,]	0.18210524	0.365005626	-0.007064906
##	[110,]	-1.33115991	-0.298714918	-0.260553742
##	[111,]	2.03165153	-0.466706298	1.851853222
##	[112,]	-0.49045705	-0.537819214	-0.260553742
##	[113,]	-0.91080848	-0.219357027	-1.105516528
##	[114,]	0.77059724	-0.452277591	1.851853222
##	[115,]	-0.07010562	0.177432429	0.161927651
##	[116,]	-0.23824619	-0.187407746	0.161927651
##	[117,]	-0.07010562	-0.500716823	1.851853222
##	[118,]	2.03165153	-0.494533091	1.851853222
##	[119,]	0.35024581	-0.483196249	1.851853222
##	[120,]	2.11572181	0.000165451	-0.007064906
##	[121,]	-0.07010562	0.159911855	1.851853222
##	[122,]	0.43431609	-0.529574238	-0.007064906
##	[123,]	-0.07010562	-0.500716823	-0.007064906
##	[124,]	-0.07010562	0.000165451	-0.683035135
##	[125,]	-0.07010562	0.000165451	0.161927651
##	[126,]	-1.49930048	-0.230693869	1.006890437
##	[127,]	-1.24708962	-0.426512042	-1.781486756

_	,] -0.23824619	-0.393532139	1.851853222	
_	,] 0.01396466	-0.344062285	-0.683035135	
_	,] -0.65859762	-0.321388601	-0.260553742	
_	,] -0.65859762	1.263707977	1.851853222	
_	,] -0.07010562	0.515476432	0.584409044	
## [133	,] -1.24708962	0.141360660	0.161927651	
## [134	,] 0.18210524	-0.400746492	1.851853222	
	,] 1.69537038	4.079367179	-0.260553742	
-	,] 1.19094867	0.000165451	0.161927651	
<b>-</b>	,] 0.35024581	-0.538849835	1.851853222	
_	,] 0.60245667	0.066125257	-1.105516528	
-	,] 0.09803495	-0.310051760	-0.260553742	
_	,] -0.91080848	0.995746267	-0.683035135	
_	,] 1.61130010	0.229994149	-0.007064906	
-	,] -1.24708962	-0.299745540	-0.260553742	
_	,] -0.91080848	-0.102896745	-0.683035135	
-	,] 0.01396466	-0.513084286	0.161927651	
_	,] 0.93873781	0.372219980	-1.105516528	
-	,] -0.91080848	-0.408991468	-0.683035135	
-	,] -0.74266791	-0.463614432	-0.683035135	
_	,] 0.26617552	1.059644829	1.851853222	
-	,] 1.19094867	0.000165451	-0.683035135	
-	,] -0.07010562	1.730579726	-0.260553742	
_	,] 0.93873781	-0.359521614	0.584409044	
_	,] 0.09803495	-0.568737872	1.851853222	
_	,] -0.91080848	-0.481135006	0.584409044	
_	,] -0.91080848	1.302871612	-0.260553742	
-	,] 0.35024581	-0.254398174	-0.260553742	
-	,] -0.07010562	-0.361582858	-1.105516528	
_	,] -0.74266791	-0.539880457	-0.260553742	
_	,] -0.91080848	-0.342001041	-1.105516528	
_	,] 2.03165153	0.338209455	1.006890437	
_	,] -0.15417591	-0.466706298	0.584409044	
-	,] 0.43431609	-0.525451750	0.161927651	
_	,] -1.33115991	-0.465675676	-0.260553742	
_	,] 0.18210524	0.000165451	0.161927651	
_	,] -0.91080848	1.805815130	-0.260553742	
_	,] -1.33115991	1.917122302	-0.683035135	
_	,] 1.61130010	0.200106112	-0.007064906	
_	,] -0.65859762	-0.397654627	1.851853222	
-	,] -0.15417591	-0.531635482	-1.527997920	
-	,] 0.35024581	0.000165451	0.161927651	
_	,] 0.77059724	0.260912808	-0.260553742	
_	,] -0.82673819	0.000165451	-0.260553742	
_	,] -0.74266791	3.487790173	0.161927651	
## [173		-0.423420176	1.851853222	
## [174		-0.481135006	-1.527997920	
## [175		-0.395593383	-0.260553742	
_	,] -0.07010562	-0.501747445	1.851853222	
## [177	,] 0.68652695	0.862796034	0.161927651	

		-0.99487877	-0.528543616	1.006890437	
		0.18210524	-0.473920652	1.851853222	
		-0.49045705	0.260912808		
##	[181,]	-1.75151134	-0.107019233	-0.683035135	
##	[182,]	-0.15417591	-0.418267066	-1.105516528	
##	[183,]	0.35024581	-0.192560856	-1.105516528	
##	[184,]	1.19094867	-0.497624957	-0.007064906	
##	[185,]	-0.23824619	-0.450216347	-1.105516528	
##	[186,]	-0.01403074	-0.492471847	-0.683035135	
##	[187,]	-0.91080848	0.000165451	1.006890437	
##	[188,]	-0.07010562	1.354402710	-1.105516528	
##	[189,]	-0.01403074	-0.444032615	0.161927651	
##	[190,]	-1.75151134	-0.348184772	0.584409044	
		1.61130010	0.000165451	-0.260553742	
		0.26617552	-0.535757970		
		-0.91080848		0.161927651	
		1.02280810	-0.361582858		
		-1.33115991	0.000165451		
		1.35908924	-0.168856551	0.584409044	
		-1.33115991	0.000165451	-0.007064906	
		0.35024581	-0.427542664	-0.683035135	
		-0.91080848	0.000165451	-1.527997920	
		-0.07010562	0.648426666		
		0.18210524	1.221452477		
		-1.33115991	-0.282224967		
		0.77059724	-0.499686201	1.851853222	
		-0.07010562	-0.538849835	-1.105516528	
		1.44315953	-0.533696726	0.161927651	
		-0.91080848		0.584409044	
		-1.75151134		0.161927651	
		2.03165153	-0.381164675		
		-0.07010562	1.751192166	0.161927651	
		-0.99487877	0.402108016	-0.260553742	
		0.77059724	-0.381164675	-1.781486756	
		-0.91080848	0.000165451	2.020845779	
	[213,]		-0.368797212	1.006890437	
		-1.07894905	-0.464645054	-0.683035135	
	[215,]		-0.460522566	-0.260553742	
	[216,]		0.000165451	-0.260553742	
		0.77059724	0.639151068	1.006890437	
	[218,]		-0.159580953	2.696816008	
	[219,]		0.452608493	-0.260553742	
		-0.49045705	0.000165451	-0.260553742	
		1.02280810	0.000165451	-1.527997920	
		0.35024581	-0.478043140	1.006890437	
		-1.58337077	-0.511023042	-0.260553742	
		-1.16301934	0.000165451	-1.105516528	
	[225,]		0.000165451	-1.105516528	
	[226,]		0.096013294	1.851853222	
		-0.23824619	-0.540911079	-1.105516528	
##	[22/,]	-0.23624619	-0.3403110/9	-1.103310328	

		-0.49045705	2.279901233	-0.260553742	
##	[229,]	0.35024581	-0.541941701	-1.105516528	
##	[230,]	0.93873781	-0.382195297	-1.105516528	
##	[231,]	-0.07010562	-0.428573285	-0.683035135	
##	[232,]	0.77059724	-0.503808689	-0.260553742	
##	[233,]	-1.75151134	-0.466706298	-0.260553742	
##	[234,]	-0.65859762	0.128993196	-0.007064906	
##	[235,]	-0.65859762	0.000165451	0.584409044	
##	[236,]	1.35908924	-0.487318737	1.006890437	
##	[237,]	1.19094867	-0.477012518	1.006890437	
##	[238,]	0.77059724	-0.360552236	-0.683035135	
##	[239,]	0.35024581	0.142391282	0.161927651	
##	[240,]	-0.49045705	-0.414144578	0.584409044	
##	[241,]	0.77059724	-0.516176152	-0.260553742	
##	[242,]	0.35024581	0.000165451	-0.683035135	
##	[243,]	-1.75151134	-0.506900555	-0.260553742	
##	[244,]	1.02280810	0.621630495	0.161927651	
##	[245,]	-0.57452734	0.000165451	-0.007064906	
		0.01396466	-0.517206774	-0.007064906	
##	[247,]	-0.49045705	1.479107967	-1.105516528	
		0.26617552	-0.452277591	-1.105516528	
##	[249,]	-1.75151134	0.043451573	-0.260553742	
##	[250,]	-0.65859762	-0.386317785	0.161927651	
		-0.91080848	1.999572059	-0.683035135	
		-0.49045705	-0.010140769	-0.260553742	
		-0.91080848	-0.347154150	0.584409044	
	[254,]		-0.508961799	-0.260553742	
##	[255,]	-0.65859762	-0.139999136	1.851853222	
##	[256,]	-0.74266791	-0.402807736	-0.683035135	
##	[257,]	0.35024581	-0.263673771	-0.007064906	
##	[258,]	-0.23824619	-0.463614432	-0.007064906	
##	[259,]	-1.33115991	-0.531635482	-1.105516528	
##	[260,]	-0.65859762	-0.541941701	1.006890437	
##	[261,]	-0.49045705	-0.531635482	0.161927651	
##	[262,]	0.09803495	0.075400854	0.161927651	
##	[263,]	0.35024581	-0.333756065	-1.105516528	
##	[264,]	0.60245667	-0.437848883	1.851853222	
##	[265,]	0.01396466	0.000165451	-0.007064906	
##	[266,]	-0.91080848	-0.292531186	-0.260553742	
##	[267,]	-0.49045705	0.636059202	-1.527997920	
##	[268,]	-0.40638676	-0.460522566	-0.007064906	
##	[269,]	-1.33115991	0.000165451	-0.007064906	
##	[270,]	-1.75151134	0.000165451	-0.260553742	
##	$[271, \bar{]}$	-1.41523020	0.000165451	-0.683035135	
		-0.82673819	0.000165451	0.161927651	
	[273,]		-0.380134053	-0.007064906	
##	[274, ]	-1.58337077	-0.533696726	0.161927651	
		-0.07010562	-0.334786687	-0.683035135	
		-1.33115991	0.000165451	-0.007064906	
		0.77059724	0.037267842	-0.260553742	

```
## [278,]
           0.77059724
                                     0.000165451
                                                       -0.007064906
## [279,] -0.91080848
                                     0.483527152
                                                       -0.683035135
## [280,] -0.49045705
                                    -0.513084286
                                                       -0.007064906
  [281,]
           0.77059724
                                     2.177869658
                                                        0.161927651
## [282,]
           0.77059724
                                     0.000165451
                                                        0.161927651
  [283,] -1.58337077
                                    -0.533696726
                                                       -0.683035135
##
  [284,]
           0.35024581
                                     1.140033342
                                                       -0.007064906
##
   [285,] -0.91080848
                                    -0.544002945
                                                        0.161927651
  [286,] -0.49045705
                                    -0.424450798
                                                        0.161927651
   [287,] -0.07010562
                                    -0.338909175
                                                       -0.260553742
  [288,] -1.33115991
                                     0.000165451
                                                        1.429371829
## [289,]
           0.35024581
                                     0.319658259
                                                       -0.260553742
  [290,]
           2.45200296
                                    -0.252336930
                                                       -0.007064906
## [291,] -1.33115991
                                     0.034175976
                                                        1.429371829
##
  [292,] -0.07010562
                                    -0.269857503
                                                       -0.260553742
  [293,] -0.74266791
                                    -0.403838358
                                                       -0.007064906
   [294,]
          0.18210524
                                    -0.493502469
                                                       -0.260553742
   [295,]
           0.09803495
                                    -0.536788592
                                                       -0.007064906
   [296,] -0.49045705
                                                       -0.007064906
##
                                     1.276075441
  [297,] -1.33115991
                                     1.523424712
                                                        1.851853222
   [298,] -1.33115991
##
                                     1.887234265
                                                       -0.007064906
##
   [299,] -0.91080848
                                    -0.397654627
                                                        0.584409044
##
               platelets serum_creatinine serum_sodium
                                                                 time
##
                                            -1.50151891 -1.626775212
     [1,]
           1.678834e-02
                              0.489236808
##
     [2,]
           7.523048e-09
                             -0.284076114
                                            -0.14173853 -1.601006734
##
     [3,] -1.036336e+00
                             -0.090747883
                                            -1.72814897 -1.588122495
##
     [4,] -5.455595e-01
                              0.489236808
                                             0.08489153 -1.588122495
##
     [5,]
          6.507077e-01
                              1.262549729
                                            -4.67433977 -1.575238256
##
     [6,] -6.069065e-01
                                            -1.04825878 -1.575238256
                              0.682565038
                             -0.187411999
##
     [7,]
                                             0.08489153 -1.549469778
          -1.394193e+00
##
     [8,]
           1.949220e+00
                             -0.284076114
                                            -1.27488884 -1.549469778
##
     [9,]
           7.523048e-09
                              0.102580347
                                             0.31152159 -1.549469778
##
    [10,]
           1.274403e+00
                              7.739045447
                                            -0.82162872 -1.549469778
    \lceil 11, \rceil
##
           1.069912e+00
                              2.519183227
                                            -1.27488884 -1.549469778
##
    [12,]
          -1.059057e-01
                             -0.477404344
                                             0.76478171 -1.549469778
##
    [13,] -1.302173e+00
                             -0.284076114
                                             0.08489153 -1.536585539
    [14,]
                             -0.284076114
##
           1.292579e-01
                                             0.08489153 -1.536585539
##
                                             0.31152159 -1.523701300
    [15,]
           1.673158e+00
                             -0.380740229
##
    [16,] -2.212154e+00
                             -0.090747883
                                            -0.14173853 -1.510817061
##
    [17,] -1.388518e-02
                             -0.477404344
                                             0.76478171 -1.497932822
##
    [18,] -9.954377e-01
                             -0.574068459
                                            -2.18140909 -1.497932822
##
    [19,] -2.694978e-01
                             -0.380740229
                                             0.76478171 -1.485048583
##
    [20,] -1.803174e+00
                              0.489236808
                                            -3.54118946 -1.485048583
##
    [21,]
           1.292579e-01
                             -0.090747883
                                             0.08489153 -1.472164344
##
    [22,]
                              0.199244462
                                            -0.14173853 -1.420627389
           3.439725e-01
##
    [23,]
                             -0.477404344
                                             0.76478171 -1.420627389
           2.621765e-01
##
    [24,]
           1.069912e+00
                             -0.574068459
                                            -0.36836860 -1.394858911
##
    [25,]
           7.523048e-09
                              0.421571927
                                            -0.59499866 -1.381974672
##
    [26,] -1.169254e+00
                              0.489236808
                                             1.67130196 -1.381974672
    [27,] -6.887026e-01
                             -0.380740229
                                             0.31152159 -1.369090433
```

```
##
    [28,]
           2.110540e-01
                             -0.090747883
                                            -0.14173853 -1.343321955
##
    [29,] -1.128356e+00
                              4.259137300
                                            -0.59499866 -1.343321955
##
    [30,] -6.478045e-01
                             -0.187411999
                                            -1.04825878 -1.343321955
##
    [31,]
           7.523048e-09
                              0.421571927
                                            -0.59499866 -1.330437716
           9.881164e-01
##
    [32,]
                              1.552542075
                                            -1.04825878 -1.317553477
##
    [33,]
           5.689117e-01
                             -0.380740229
                                            -1.95477903 -1.317553477
##
                                             0.31152159 -1.304669238
    [34,]
           3.950951e-01
                             -0.187411999
##
    [35,] -7.704986e-01
                             -0.380740229
                                             0.76478171 -1.304669238
##
    [36,] -3.615184e-01
                              2.035862651
                                            -0.59499866 -1.291784999
##
    [37,] -3.819674e-01
                                            -0.59499866 -1.291784999
                             -0.380740229
##
    [38,]
           5.893607e-01
                             -0.380740229
                                             1.89793202 -1.291784999
##
    [39,]
           4.257686e-01
                              0.875893269
                                             0.08489153 -1.291784999
##
    [40,]
                                             1.21804184 -1.291784999
           6.711567e-01
                              1.552542075
##
    [41,]
           7.523048e-09
                              0.421571927
                                            -0.59499866 -1.278900760
    [42,] -1.128356e+00
                                            -0.14173853 -1.266016521
##
                             -0.187411999
##
    [43,] -8.011721e-01
                             -0.187411999
                                             0.53815165 -1.253132283
##
    [44,] -4.637634e-01
                             -0.380740229
                                            -0.59499866 -1.253132283
##
    [45,] -7.091516e-01
                             -0.284076114
                                             1.21804184 -1.253132283
    [46,]
##
           4.768911e-01
                              0.489236808
                                            -0.36836860 -1.227363805
##
    [47,]
           7.813538e-02
                                            -1.50151891 -1.188711088
                             -0.477404344
##
                                             0.31152159 -1.162942610
    [48,]
           1.918546e+00
                             -0.767396690
##
    [49,] -1.261275e+00
                              2.905839687
                                            -0.82162872 -1.150058371
##
    [50,]
           1.345974e+00
                             -0.380740229
                                             0.76478171 -1.137174132
##
    [51,] -9.954377e-01
                             -0.380740229
                                             0.31152159 -1.124289893
##
    [52,]
           1.581138e+00
                              0.005916232
                                             0.53815165 -1.124289893
##
    [53,]
           7.523048e-09
                              5.225778452
                                             2.12456209 -1.124289893
##
    [54,]
                             -0.380740229
                                            -0.59499866 -1.111405654
           8.960958e-01
##
    [55,] -8.545672e-02
                              0.779229153
                                            -1.04825878 -1.098521415
##
    [56,]
           2.020792e+00
                              0.585900923
                                            -1.04825878 -1.034100221
##
    [57,] -4.126409e-01
                              1.262549729
                                             0.31152159 -0.982563265
##
    [58,] -4.842125e-01
                             -0.767396690
                                             0.31152159 -0.982563265
##
    [59,]
                                            -0.14173853 -0.969679026
           5.689117e-01
                             -0.284076114
##
    [60,] -9.568123e-02
                             -0.090747883
                                            -0.14173853 -0.918142070
##
    [61,]
          1.294852e+00
                             -0.380740229
                                             0.53815165 -0.905257831
##
    [62,] -4.842125e-01
                              0.875893269
                                            -1.27488884 -0.905257831
##
    [63,] -9.568123e-02
                             -0.284076114
                                             0.53815165 -0.905257831
    [64,]
##
           1.243729e+00
                             -0.380740229
                                             1.89793202 -0.892373592
##
           7.523048e-09
                             -0.206744822
                                             0.08489153 -0.866605114
    [65,]
##
    [66,] -1.475990e+00
                              1.455877960
                                            -2.18140909 -0.853720876
##
    [67,] -5.148860e-01
                             -0.090747883
                                            -0.14173853 -0.840836637
##
    [68,]
                                             0.76478171 -0.840836637
           1.088089e-01
                             -0.380740229
##
    [69,] -1.979263e-01
                             -0.187411999
                                             1.21804184 -0.827952398
##
    [70,]
          2.388874e+00
                              0.421571927
                                            -0.36836860 -0.815068159
##
    [71,]
           1.131259e+00
                             -0.574068459
                                             0.76478171 -0.802183920
##
    [72,] -1.445316e+00
                             -0.477404344
                                             0.53815165 -0.763531203
##
    [73,] -2.081508e-01
                             -0.380740229
                                            -1.04825878 -0.750646964
##
    [74,] -1.169254e+00
                             -0.090747883
                                             0.08489153 -0.750646964
##
    [75,]
           2.701285e-02
                             -0.187411999
                                            -0.59499866 -0.737762725
##
    [76,] -6.069065e-01
                             -0.670732575
                                             0.53815165 -0.737762725
    [77,] 5.484626e-01
                             -0.574068459
                                             0.76478171 -0.724878486
```

```
##
    [78,] -2.694978e-01
                             -0.187411999
                                             0.76478171 -0.724878486
           2.008294e-01
                                            -1.27488884 -0.724878486
##
    [79,]
                             -0.767396690
##
    [80,]
           6.200342e-01
                             -0.477404344
                                             0.76478171 -0.724878486
##
    [81,]
                              0.295908577
                                            -0.14173853 -0.711994247
           3.030745e-01
##
    [82,]
           7.523048e-09
                             -0.206744822
                                             0.08489153 -0.699110008
##
    [83,] -6.887026e-01
                              1.069221499
                                            -1.04825878 -0.686225769
##
    [84,] -9.340907e-01
                              0.392572693
                                            -0.82162872 -0.673341530
##
    [85,]
           3.950951e-01
                             -0.380740229
                                             0.99141178 -0.673341530
##
    [86,]
           1.458444e+00
                             -0.670732575
                                             0.76478171 -0.660457292
##
    [87,] -9.238662e-01
                                             0.08489153 -0.660457292
                             -0.284076114
##
    [88,]
           4.155441e-01
                             -0.574068459
                                             0.76478171 -0.660457292
    [89,] -2.899468e-01
##
                             -0.670732575
                                             0.53815165 -0.660457292
##
    [90,] -8.420702e-01
                             -0.284076114
                                             1.67130196 -0.660457292
##
    [91,] -1.468038e-01
                             -0.574068459
                                            -0.14173853 -0.647573053
    [92,]
                                            -0.82162872 -0.647573053
##
           3.439725e-01
                             -0.380740229
##
    [93,]
          7.523048e-09
                             -0.206744822
                                             0.08489153 -0.621804575
##
    [94,] -5.455595e-01
                              0.295908577
                                            -0.36836860 -0.621804575
##
    [95,]
          6.507077e-01
                             -0.670732575
                                             1.21804184 -0.608920336
##
    [96,] -4.535389e-01
                             -0.380740229
                                             0.99141178 -0.608920336
##
    [97,] -9.568123e-02
                             -0.090747883
                                            -0.59499866 -0.608920336
    [98,] -8.545672e-02
                                            -0.14173853 -0.583151858
##
                             -0.284076114
##
    [99,]
           5.586872e-01
                             -0.187411999
                                             0.08489153 -0.583151858
##
  [100,] -4.330899e-01
                             -0.284076114
                                             0.76478171 -0.570267619
   [101,]
                                             0.99141178 -0.557383380
##
           3.541970e-01
                             -0.284076114
  [102,]
           7.523048e-09
                             -0.206744822
                                             0.08489153 -0.557383380
   [103,] -1.169254e+00
                             -0.284076114
                                             1.67130196 -0.557383380
   [104,] -3.819674e-01
                                             0.76478171 -0.557383380
                             -0.380740229
##
  [105,]
           2.315030e-01
                              0.875893269
                                             1.44467190 -0.557383380
## [106,]
                              0.295908577
                                             0.31152159 -0.544499141
           3.656712e+00
## [107,] -3.660672e-03
                                             0.08489153 -0.544499141
                             -0.090747883
##
  [108,] -3.819674e-01
                             -0.477404344
                                             0.31152159 -0.544499141
## [109,]
                                            -0.82162872 -0.544499141
           4.155441e-01
                             -0.284076114
  [110,]
           5.998124e+00
                             -0.090747883
                                             1.21804184 -0.544499141
##
## [111,]
           4.359931e-01
                             -0.187411999
                                            -1.04825878 -0.518730663
   [112,] -3.615184e-01
                             -0.187411999
                                            -0.36836860 -0.518730663
  [113,] -1.161302e-01
                              0.199244462
                                            -0.14173853 -0.518730663
## [114,]
           8.960958e-01
                             -0.090747883
                                            0.08489153 -0.518730663
## [115,]
           6.609322e-01
                             -0.187411999
                                            -2.40803915 -0.505846424
## [116,] -1.015887e+00
                             -0.380740229
                                             0.53815165 -0.505846424
## [117,]
           7.813538e-02
                             -0.670732575
                                            -0.14173853 -0.467193707
                                             0.31152159 -0.467193707
## [118,]
           2.491119e+00
                              1.745870305
##
   [119,] -6.171310e-01
                             -0.477404344
                                             0.76478171 -0.467193707
## [120,]
          7.523048e-09
                              0.421571927
                                            -0.59499866 -0.454309469
  [121,] -5.455595e-01
                              0.102580347
                                            -0.36836860 -0.454309469
## [122,] -1.036336e+00
                             -0.380740229
                                            -0.14173853 -0.454309469
## [123,] -3.615184e-01
                                            0.76478171 -0.454309469
                             -0.622400517
## [124,] -1.394193e+00
                             -0.477404344
                                             1.89793202 -0.454309469
## [125,] -4.739879e-01
                              2.229190881
                                            -0.59499866 -0.441425230
## [126,] -2.694978e-01
                             -0.090747883
                                            -0.36836860 -0.428540991
## [127,] 7.813538e-02
                              0.682565038
                                           -2.86129928 -0.389888274
```

```
## [128,]
           3.746460e-01
                             -0.574068459
                                            0.08489153 -0.338351318
## [129,]
           3.723735e-02
                             -0.670732575
                                            -0.14173853 -0.338351318
## [130,] -3.717429e-01
                                             1.89793202 -0.325467079
                              1.939198536
  [131,] -1.468038e-01
                                            0.31152159 -0.312582840
                             -0.670732575
## [132,] -1.365792e-01
                              4.549129646
                                            -1.27488884 -0.299698601
  [133,]
           7.523048e-09
                             -0.206744822
                                            0.08489153 -0.299698601
##
  [134,]
           3.235235e-01
                             -0.090747883
                                            1.89793202 -0.299698601
##
   [135,] -3.308449e-01
                             -0.206744822
                                            0.08489153 -0.299698601
  [136,]
          7.523048e-09
                             -0.206744822
                                            0.08489153 -0.299698601
   [137,] -9.340907e-01
                                            0.08489153 -0.299698601
                             -0.477404344
## [138,]
          4.257686e-01
                              0.682565038
                                            -1.50151891 -0.286814362
## [139,] -4.330899e-01
                             -0.380740229
                                            -0.14173853 -0.286814362
  [140,] -5.353350e-01
                             -0.574068459
                                            0.31152159 -0.286814362
## [141,]
           7.523048e-09
                             -0.284076114
                                            -0.59499866 -0.273930123
##
  [142,]
           8.654223e-01
                             -0.477404344
                                            0.76478171 -0.273930123
  [143,]
          6.711567e-01
                             -0.477404344
                                            -1.04825878 -0.273930123
   [144,] -3.512939e-01
                             -0.477404344
                                            0.99141178 -0.261045885
  [145,]
           7.631773e-01
                              0.295908577
                                            0.53815165 -0.248161646
   [146,]
           2.701285e-02
                             -0.670732575
                                            0.99141178 -0.235277407
##
## [147,] -4.637634e-01
                             -0.670732575
                                            -0.14173853 -0.235277407
## [148,] -2.183753e-01
                             -0.380740229
                                            0.08489153 -0.222393168
## [149,] -3.921919e-01
                              0.421571927
                                            -0.59499866 -0.222393168
## [150,] -3.615184e-01
                             -0.477404344
                                            -0.14173853 -0.196624690
  [151,] -2.899468e-01
##
                              1.069221499
                                            -0.36836860 -0.196624690
## [152,] -1.979263e-01
                             -0.477404344
                                            0.53815165 -0.170856212
   [153,] -8.113966e-01
                             -0.477404344
                                            -0.59499866 -0.157971973
  [154,]
          7.523048e-09
                             -0.206744822
                                            0.08489153 -0.145087734
##
  [155,] -2.899468e-01
                             -0.574068459
                                            -0.14173853 -0.132203495
## [156,] -7.091516e-01
                                            0.76478171 -0.132203495
                              0.295908577
## [157,]
          1.394824e-01
                              0.005916232
                                            -0.14173853 -0.132203495
##
  [158,] -1.388518e-02
                             -0.380740229
                                            -0.14173853 -0.132203495
## [159,] -2.899468e-01
                             -0.090747883
                                            -0.59499866 -0.119319256
   [160,]
          1.008565e+00
                             -0.284076114
                                            0.53815165 -0.119319256
##
  [161,] -2.183753e-01
                             -0.187411999
                                            -0.59499866 -0.119319256
   [162,] -9.136417e-01
                             -0.574068459
                                            0.53815165 -0.119319256
  [163,]
                             -0.477404344
                                            0.08489153 -0.093550778
          1.887873e+00
  [164,] -1.925868e+00
##
                             -0.477404344
                                            1.21804184 -0.054898062
  [165,]
          7.222792e-01
                             -0.284076114
                                            0.53815165 -0.016245345
## [166,] -7.296006e-01
                             -0.090747883
                                            -0.36836860 -0.003361106
## [167,] -4.433144e-01
                             -0.670732575
                                            -0.82162872
                                                         0.048175850
## [168,] -1.976990e+00
                              0.972557384
                                            -0.59499866
                                                         0.061060089
##
   [169,]
           6.791087e-02
                             -0.380740229
                                            0.31152159
                                                         0.125481284
  [170,]
           4.257686e-01
                             -0.574068459
                                            -0.82162872
                                                         0.189902478
##
  [171,]
           7.523048e-09
                              0.102580347
                                            -0.14173853
                                                         0.189902478
## [172,]
           6.302587e-01
                             -0.477404344
                                            0.76478171
                                                         0.202786717
## [173,] -8.931927e-01
                             -0.284076114
                                            1.89793202
                                                         0.202786717
## [174,] -7.602741e-01
                             -0.574068459
                                            0.53815165
                                                         0.202786717
## [175,]
           1.803804e-01
                             -0.477404344
                                            0.08489153
                                                         0.202786717
##
  [176,]
           7.529528e-01
                             -0.380740229
                                            0.31152159
                                                         0.202786717
## [177,] -1.619133e+00
                             -0.380740229
                                           -0.36836860 0.215670956
```

```
## [178,] -1.343071e+00
                              -0.380740229
                                             0.76478171
                                                          0.215670956
  [179,]
           3.723735e-02
                             -0.187411999
                                             1.89793202
                                                          0.215670956
   [180,]
           1.599314e-01
                             -0.670732575
                                             0.76478171
                                                          0.215670956
##
##
   [181,]
                             -0.477404344
           4.053196e-01
                                            -0.14173853
                                                          0.228555195
                                                          0.254323673
##
   [182,]
          -4.330899e-01
                             -0.380740229
                                            -0.14173853
   [183,]
                             -0.187411999
                                            -0.14173853
                                                          0.305860629
##
           1.678834e-02
##
   [184,]
          -4.024164e-01
                              1.069221499
                                            -0.59499866
                                                          0.408934540
                                             0.08489153
##
   [185,]
          -4.535389e-01
                              -0.187411999
                                                          0.512008452
   [186,]
           1.284627e+00
                              0.102580347
                                             -0.14173853
                                                          0.524892691
   [187,] -1.128356e+00
##
                              -0.767396690
                                            -0.59499866
                                                          0.537776929
   [188,]
           1.039239e+00
                              0.682565038
                                             1.67130196
                                                          0.537776929
##
   [189,]
          -6.375800e-01
                             -0.380740229
                                            -0.14173853
                                                          0.537776929
   [190,]
                                                          0.563545407
##
           1.190334e-01
                             -0.477404344
                                             0.76478171
##
  [191,]
           8.858713e-01
                              0.682565038
                                            -0.59499866
                                                          0.563545407
##
   [192,]
           4.666666e-01
                              0.102580347
                                            -0.36836860
                                                          0.563545407
                                                          0.576429646
   [193,] -3.433419e-02
                              -0.670732575
                                            -1.50151891
   [194,] -1.056785e+00
                              -0.206744822
                                             1.21804184
                                                          0.640850841
   [195,] -1.404418e+00
                              0.199244462
                                             -0.36836860
                                                          0.640850841
   [196,]
          -4.126409e-01
##
                              0.392572693
                                              1.89793202
                                                          0.640850841
   [197,]
           7.523048e-09
                             -0.206744822
                                             0.08489153
                                                          0.705272036
   [198,]
##
          -4.455870e-02
                             -0.574068459
                                              0.31152159
                                                          0.718156275
##
   [199,]
           1.599314e-01
                             -0.380740229
                                            -0.59499866
                                                          0.718156275
##
   [200,]
           7.523048e-09
                              0.392572693
                                            -5.35422996
                                                          0.718156275
   [201,] -1.946317e+00
##
                             -0.670732575
                                             0.08489153
                                                          0.718156275
  [202,]
           1.161933e+00
                             -0.380740229
                                            -0.14173853
                                                          0.718156275
   [203,]
          -4.433144e-01
                              -0.477404344
                                             0.31152159
                                                          0.718156275
   [204,] -5.251105e-01
                              2.035862651
                                            -0.14173853
                                                          0.731040513
##
   [205,]
           1.394824e-01
                             -0.670732575
                                             0.08489153
                                                          0.731040513
   [206,]
                             -0.380740229
                                                          0.731040513
           1.008565e+00
                                            -0.14173853
   [207,]
          -3.819674e-01
                             -0.574068459
                                             0.99141178
                                                          0.731040513
##
   [208,]
          -7.909476e-01
                             -0.477404344
                                            -0.14173853
                                                          0.731040513
  [209,]
##
           2.008294e-01
                             -0.380740229
                                             0.99141178
                                                          0.731040513
   [210,]
           4.746186e-02
                             -0.574068459
                                            -1.50151891
                                                          0.731040513
##
  [211,]
           1.284627e+00
                             -0.380740229
                                            -0.14173853
                                                          0.743924752
   [212,]
          -1.189703e+00
                              -0.574068459
                                             0.76478171
                                                          0.795461708
   [213,]
           2.225282e+00
                                             0.31152159
                                                          0.795461708
                              0.005916232
   [214,] -1.979263e-01
##
                              0.199244462
                                            -1.50151891
                                                          0.808345947
##
   [215,]
           2.724010e-01
                             -0.574068459
                                            -0.59499866
                                                          0.821230186
  [216,]
          -6.171310e-01
                             -0.090747883
                                            -0.59499866
                                                          0.834114425
##
   [217,]
           9.676674e-01
                             -0.477404344
                                             0.99141178
                                                          0.846998664
   [218,]
          -1.148805e+00
                              7.352388986
                                              0.08489153
                                                          0.846998664
##
   [219,]
           7.813538e-02
                              -0.284076114
                                            -0.59499866
                                                          0.859882903
  [220,]
           1.100586e+00
                             -0.670732575
                                              0.76478171
                                                          0.859882903
##
   [221,]
           7.523048e-09
                              0.421571927
                                            -0.59499866
                                                          0.872767142
                                             1.89793202
   [222,]
         -7.091516e-01
                                                          0.898535620
                             -0.284076114
  [223,]
                             -0.284076114
##
           1.039239e+00
                                             0.53815165
                                                          0.911419859
   [224,] -1.363520e+00
                                            -0.59499866
##
                             -0.574068459
                                                          0.911419859
## [225,]
           2.460445e+00
                             -0.380740229
                                              0.31152159
                                                          0.962956814
##
   [226,]
           1.678834e-02
                              0.005916232
                                            -2.63466921
                                                          0.962956814
## [227,] -7.602741e-01
                             -0.090747883
                                            -1.04825878
                                                          0.962956814
```

```
## [228,] -1.251050e+00
                             -0.380740229
                                             0.76478171
                                                          0.975841053
  [229,] -2.694978e-01
                              3.485824379
                                            -1.50151891
                                                          0.988725292
  [230,]
           1.088089e-01
                             -0.187411999
                                            -0.59499866
                                                          0.988725292
   [231,] -2.058786e+00
                              0.295908577
                                            -2.18140909
                                                          0.988725292
   [232,] -8.011721e-01
                             -0.284076114
                                            -0.59499866
                                                          1.001609531
   [233,] -8.545672e-02
                             -0.477404344
                                             0.08489153
                                                          1.014493770
##
   [234,]
           6.813812e-01
                              0.005916232
                                             0.08489153
                                                          1.014493770
##
   [235,]
           4.257686e-01
                             -0.284076114
                                             0.08489153
                                                          1.014493770
   [236,]
           1.458444e+00
                             -0.284076114
                                             0.08489153
                                                          1.014493770
   [237,] -1.570283e-01
                             -0.284076114
                                             2.57782221
                                                          1.014493770
   [238,] -9.238662e-01
                             -0.187411999
                                            -1.04825878
                                                          1.027378009
   [239,] -6.500771e-02
                             -0.380740229
                                            -0.14173853
                                                          1.027378009
   [240,]
           7.523048e-09
                             -0.206744822
                                             0.08489153
                                                          1.040262248
##
  [241,]
           2.756956e+00
                             -0.090747883
                                             0.53815165
                                                          1.053146487
   [242,] -1.468038e-01
##
                             -0.090747883
                                            -0.14173853
                                                          1.053146487
                             -0.284076114
   [243,] -8.545672e-02
                                            -0.14173853
                                                          1.053146487
   [244,] -4.433144e-01
                             -0.477404344
                                             0.99141178
                                                          1.066030726
   [245,]
           6.563834e-03
                              0.392572693
                                            -0.59499866
                                                          1.066030726
   [246,]
           1.906049e-01
##
                              0.005916232
                                             0.08489153
                                                          1.066030726
   [247,]
##
           5.177891e-01
                             -0.284076114
                                             0.31152159
                                                          1.078914965
  [248,] -1.774773e-01
##
                              0.972557384
                                            -0.36836860
                                                          1.078914965
##
   [249,]
           3.848706e-01
                             -0.380740229
                                                          1.078914965
                                             1.21804184
  [250,] -4.126409e-01
                             -0.187411999
                                            -1.50151891
                                                          1.078914965
   [251,]
           1.437995e+00
##
                             -0.864060805
                                             0.53815165
                                                          1.078914965
  [252,] -3.308449e-01
                             -0.574068459
                                             1.44467190
                                                          1.091799204
   [253,]
           1.088089e-01
                             -0.380740229
                                            -0.82162872
                                                          1.091799204
   [254,] -2.797223e-01
                             -0.187411999
                                            -1.04825878
                                                          1.091799204
##
   [255,]
           7.523048e-09
                             -0.380740229
                                             0.53815165
                                                          1.091799204
   [256,]
           7.222792e-01
                             -0.380740229
                                             1.21804184
                                                          1.104683443
   [257,]
           3.132990e-01
                              0.295908577
                                             0.53815165
                                                          1.156220398
##
   [258,] -1.059057e-01
                             -0.380740229
                                             0.53815165
                                                          1.285062788
   [259,] -3.103959e-01
                             -0.574068459
                                            -0.36836860
                                                          1.285062788
   [260,]
           4.564421e-01
                             -0.670732575
                                                          1.297947027
##
                                            -0.36836860
  [261,] -6.171310e-01
                             -0.380740229
                                             0.31152159
                                                          1.323715505
   [262,]
           2.008294e-01
                             -0.670732575
                                            -0.82162872
                                                          1.323715505
   [263,] -6.682536e-01
                              0.005916232
                                            -1.72814897
                                                          1.349483982
   [264,] -5.660085e-01
##
                             -0.380740229
                                             0.76478171
                                                          1.375252460
   [265,] -1.189703e+00
                             -0.187411999
                                             0.99141178
                                                          1.375252460
## [266,]
           1.008565e+00
                             -0.477404344
                                             0.76478171
                                                          1.413905177
##
   [267,]
           7.523048e-09
                              0.421571927
                                            -0.59499866
                                                          1.426789416
                              0.295908577
   [268,] -1.332846e+00
                                             0.76478171
                                                          1.465442133
   [269,]
           3.950951e-01
                             -0.477404344
                                             0.76478171
                                                          1.465442133
##
   [270,] -4.228654e-01
                             -0.380740229
                                            -1.04825878
                                                          1.465442133
   [271,]
##
          7.523048e-09
                              0.199244462
                                            -1.50151891
                                                          1.465442133
   [272,] -4.330899e-01
                             -0.477404344
                                            -0.59499866
                                                          1.465442133
  [273,] -4.944370e-01
                             -0.187411999
                                            -0.82162872
                                                          1.478326372
   [274,] -7.602741e-01
                                             0.76478171
                                                          1.478326372
##
                             -0.670732575
## [275,] -1.159030e+00
                             -0.380740229
                                             0.08489153
                                                          1.478326372
##
   [276,]
           1.622036e+00
                             -0.574068459
                                             0.08489153
                                                          1.478326372
## [277,] 6.507077e-01
                             -0.284076114
                                             1.21804184
                                                          1.478326372
```

```
## [278,] -2.436071e+00
                             -0.284076114
                                            0.76478171
                                                        1.491210611
## [279,] -3.206204e-01
                             -0.670732575
                                           -0.14173853 1.491210611
## [280,]
          1.918546e+00
                             -0.090747883
                                           -0.14173853
                                                        1.491210611
## [281,] -2.285998e-01
                             -0.380740229
                                            0.08489153 1.504094850
## [282,] -2.171256e+00
                             1.262549729
                                           -0.14173853
                                                        1.542747566
## [283,] -4.944370e-01
                              2.325854996
                                           -1.95477903
                                                        1.542747566
           7.523048e-09
                                            0.31152159
## [284,]
                            -0.284076114
                                                        1.542747566
## [285,]
           1.599314e-01
                             -0.574068459
                                            0.99141178
                                                        1.542747566
## [286,]
           7.427283e-01
                             -0.187411999
                                           -0.36836860
                                                        1.542747566
## [287,]
           1.599314e-01
                                            0.76478171
                                                        1.542747566
                             0.295908577
## [288,]
           2.859201e+00
                            -0.380740229
                                           -1.04825878 1.542747566
## [289,]
           7.523048e-09
                            -0.284076114
                                            1.21804184
                                                        1.620053000
                            -0.477404344
## [290,]
           1.294852e+00
                                            1.67130196
                                                       1.620053000
## [291,] -4.228654e-01
                            -0.574068459
                                            0.99141178 1.632937239
## [292,] -1.332846e+00
                             0.005916232
                                            0.53815165
                                                        1.645821478
## [293,]
          1.213056e+00
                             -0.380740229
                                            0.76478171 1.645821478
## [294,] -8.625192e-01
                             -0.477404344
                                           -0.14173853
                                                        1.800432345
## [295,] -1.107907e+00
                            -0.284076114
                                            1.44467190
                                                       1.800432345
          6.791087e-02
## [296,]
                             -0.187411999
                                            0.53815165
                                                        1.813316584
## [297,]
          4.893878e+00
                            -0.574068459
                                            0.31152159
                                                        1.903506257
## [298,] -1.261275e+00
                             0.005916232
                                            0.76478171
                                                        1.929274734
## [299,] 1.345974e+00
                             0.199244462
                                           -0.14173853
                                                       1.993695929
## attr(,"scaled:center")
##
                         age creatinine phosphokinase
                                                              ejection fraction
##
                   60.83389
                                            581.83946
                                                                       38.08361
##
                  platelets
                                     serum_creatinine
                                                                   serum sodium
                                                                      136.62542
##
               263358.02926
                                              1.39388
##
                       time
##
                  130.26087
   attr(,"scaled:scale")
##
                        age creatinine_phosphokinase
                                                              ejection_fraction
                                           970.287881
##
                  11.894809
                                                                      11.834841
##
                  platelets
                                     serum creatinine
                                                                   serum sodium
##
               97804.236869
                                             1.034510
                                                                       4.412477
##
                       time
##
                  77.614208
as.matrix(scale.heart)%*%fact.load.heart%*%solve(t(fact.load.heart)%*%fact.lo
ad.heart)
##
                   PC1
                                 PC2
                                               PC3
##
           1.661261807
                        1.554800886 -0.2391648108
     [1,]
           0.743266680
##
     [2,]
                        0.800052166 -6.6257827317
##
     [3,]
           0.927179080
                        2.016941671
                                     0.4549872007
##
     [4,]
           0.334885605 1.266839858 -0.1473115437
##
     [5,]
           1.925456863
                       3.274592726
                                     0.2063397138
##
     [6,]
           2.435918328
                        0.165636681
                                      0.8575735122
##
           1.012119703
                        1.263416904
                                      0.3244895181
     [7,]
##
     [8,]
           1.124477246 -1.115611048 -0.4460294461
##
     [9,]
          1.234722890 -1.691814397 0.3538296415
```

```
##
    [10,]
           4.919709448
                         0.999011928 -0.1358685604
##
    [11,]
           2.640695114
                         0.439924198 0.0044503303
##
    [12,]
           0.428072549
                         0.186827135 -0.2931060423
##
                         1.005910129 -0.5149623433
    [13,] -0.139463181
    [14,]
           0.205750073
##
                         0.013367351 -0.2133024344
##
           0.100190044 -0.129530927 -0.8853088186
    [15,]
##
    [16,]
           1.649820322 -0.324891744
                                     1.1159824597
##
    [17,]
           1.595345623 -0.956323503 0.2371917548
##
    [18,] -0.156822106
                        2.866432703 -0.1779870700
    [19,]
                         0.103388790 -0.0231261139
##
           0.762120879
##
    [20,]
           0.907950332
                         1.748387342 0.9061044026
##
    [21,]
           0.762655848
                         0.465114447 -0.0799383657
##
                         0.308381123 -0.1180144130
    [22,]
           0.944646930
##
    [23,]
           0.733921935 -0.548331547 -0.1903647967
           0.457662548 -1.284173827 -0.0687137964
##
    [24,]
##
           1.492282733
                         0.549949036 -0.1711517403
    [25,]
##
           1.455420414 -0.835943301
                                      0.5028730340
    [26,]
##
    [27,]
           1.941662073 -0.755655310
                                      0.7523795208
##
    [28,]
           1.134926967 -0.573778900
                                      0.2150997676
##
                        1.259927295
                                      0.6226136569
    [29,]
           2.308580309
##
    [30,]
           1.520043263
                         0.715581081
                                      0.6753536792
##
           2.353027773 -0.193596104
                                      0.1844817096
    [31,]
##
    [32,]
           2.584217212 -0.341226598
                                      0.3233372990
##
                        1.105549289 -0.1548664887
    [33,]
           0.295532144
##
           0.035612527
                         0.257097226 -0.3899811986
    [34,]
##
    [35,]
           0.663877522 -0.991149461
                                      0.5046204217
##
                         0.731427455 -0.0146293253
    [36,]
           1.876218740
##
    [37,]
           1.908293478 -0.818363037 0.8903389408
##
           1.353571970 -2.188128649 -0.6137036191
    [38,]
##
                         0.588312865 -2.3617777846
    [39,]
           1.007463177
##
    [40,]
           1.154552043 -0.620878762 -0.4508776138
##
    [41,]
           1.129162665
                        1.163688178 -0.3401328031
##
    [42,] -0.020711589
                         0.926623118
                                      0.3053509355
##
    [43,]
           0.923607487 -0.610849610
                                      0.1530495710
##
    [44,]
           1.117429820 -0.484077775
                                      0.6480190259
##
    [45,]
           0.525787658 -1.628332541
                                      0.0773460918
##
    [46,]
           0.449719713
                         0.306472980 -0.5615070471
                        1.612860316 -1.0768836850
##
    [47,]
           0.092432608
##
    [48,]
           0.331904065 -0.816335765 -1.0803374958
##
    [49,]
           2.457169977
                        1.841559436 0.3705196143
##
           0.168206595 -0.400124857 -0.6707819730
    [50,]
##
    [51,]
           0.516047584
                         0.626436159 -0.0009576655
##
    [52,]
           0.092532663
                         0.300954180 -0.8749494801
##
    [53<sub>,</sub>]
           2.783428934 -1.275225506 -3.1242865473
##
           1.035561944 -0.843644912 0.1766442263
    [54,]
##
    [55,]
                         0.667315954 0.1836188315
           0.964937677
##
           2.396441039 -0.122309343 -0.3800272497
    [56,]
##
    [57,]
           1.311884637
                         0.096229075 0.3931885056
##
    [58,]
           0.117242708 -0.230750573 -0.0975868884
   [59,] -0.230865053 1.036172140 -0.9937338718
```

```
##
    [60,]
           0.749126012
                       0.827038561 -0.0716641805
##
    [61,] -0.222187227
                        0.906990443 -7.2203194356
##
    [62,]
          0.501754161
                        0.984400714
                                    0.2677696975
##
    [63,] -0.008689059 -0.085367104
                                     0.0345107941
##
    [64,] -0.549357130 -0.979474617 -1.2025062067
##
          0.083935800 -2.028983076
                                     0.1298242971
    [65,]
##
    [66,]
          0.988680110
                       2.692397650
                                     0.8718446516
##
    [67,] -0.648148747
                       1.708399982 -0.2357704108
##
    [68,]
          0.532711245 -0.034977861
                                     0.0205406501
    [69,]
##
           0.449358882 -0.116363372
                                     0.0114748486
##
          0.817628362
                       0.142198633 -0.7901497375
    [70,]
##
    [71,] -0.684673449 -0.620888501 -0.5949996183
##
    [72,] -0.096008591
                       0.266505695
                                    0.2283303489
##
    [73,]
           1.537899958
                        0.792079545 -4.1950500318
##
    [74,]
          0.555768980 -0.462584538
                                     0.7769184732
##
                       1.086577298 -0.2364415509
    [75,]
          0.556411378
##
    [76,] -0.216828225
                       0.707001512
                                     0.1918664146
##
    [77,]
          0.668441464 -2.005827437
                                     0.3236278154
##
    [78,] -0.607749063 -0.183163996
                                     0.0212675426
##
                       0.217708128
    [79,]
          0.819260082
                                     0.4254147686
##
    [80,] -0.063297651 -0.943013569 -0.2959498846
##
          0.919009855 -0.278359780
                                     0.3100879741
    [81,]
##
    [82,]
           0.647771674 -0.814464099
                                     0.0545080160
##
    [83,]
          0.701850273
                       1.556076413
                                     0.5038258391
##
          1.426833013 -0.236687990
                                     1.1519445673
    [84,]
##
    [85,] -0.113963882
                       0.001775022 -0.3909018947
##
    [86,] -0.258837308 -1.431743479 -0.3730824376
    [87,] -0.132936474
##
                       0.384334804
                                     0.5311877910
##
          0.412780099 -1.884983446
                                     0.3481862241
    [88,]
##
    [89,] -0.728453310 -0.165887725
                                     0.1153721621
##
    [90,] -0.325982563
                       0.033839181
                                     0.1137702233
##
    [91,]
          0.551045835 -0.542978350
                                    0.5658370679
##
          0.342583850 -0.0533331595 -0.3617566227
    [92,]
##
    [93,] -0.363720014 -0.919551965 -0.1109323635
##
    [94,]
          0.281720144
                       1.053032127
                                    0.2996120563
##
    [95,] -0.201173206 -0.914928165 -0.2348252272
##
    [96,]
           0.090540886 -1.601030602 0.5241222915
##
    [97,]
          ##
    [98,]
          0.783213325 -1.310128264 0.7599096037
##
    [99,]
           0.157269661 -0.508384870 0.4203188124
## [100,]
## [101,]
           0.119602956 -0.070347549 -0.2929838037
## [102,]
          0.867269604 -0.684410717 0.1234748027
## [103,]
          0.610298824 -0.187678958 -0.1110579911
## [104,] -0.696897702 0.825599986 -4.3693073628
## [105,]
           0.550164436 -1.359203255 0.1724102706
## [106,]
          0.972097738 -0.954499910 -1.3444474338
## [107,]
          0.060003135 -0.312400494 -0.2643827297
## [108,] -0.630359888
                       0.422572840 -1.3656024435
## [109,] 0.394779402 0.264159990 -0.4517056571
```

```
## [110,] -0.263211207 -1.966140938 -2.6273981587
## [111,]
          1.570689585 -1.218400716
                                      0.8286984171
## [112,] -0.079851430
                        0.476705134
                                     0.3987411216
                        0.987410715 -0.1836507253
## [113,] -0.232857424
## [114,]
           0.861926056 -1.672184717
                                      0.2905798137
## [115,]
           0.502907066
                        0.964718479 -0.1722577393
## [116,] -0.124361588 -0.121099491
                                      0.3427441451
           0.148570664 -1.241001991
## [117,]
                                      0.5654697557
## [118,]
           2.291232248 -2.230747174 -0.1209613524
## [119,]
           0.292592223 -1.569407098
                                      0.7579634732
## [120,]
           1.554116575 -0.051411596
                                      0.2919360483
## [121,]
           0.471353622 -0.769453621
                                      0.3000942339
## [122,]
           0.239404523
                        0.179511841
                                      0.8150414891
## [123,] -0.183468621 -0.418602246
                                      0.3254376420
## [124,] -0.379654647 -0.225010617
                                      0.0511604751
                                      0.1837383744
## [125,]
          1.168530259
                        0.687054723
## [126,] -0.439853331 -0.096473505
                                      0.1761735895
## [127,] -0.020406232
                        2.895762575
                                      0.1700108754
## [128,]
                                     0.3355970649
          0.029381207 -1.385234054
                        0.354127757
## [129,] -0.160749776
                                      0.1035501859
## [130,]
          0.339556664 -0.332058477 -0.0667005248
## [131,] -0.237984674 -1.134193809 -0.9177089771
## [132,]
                        1.073871848 -0.1719603923
           2.210066656
## [133,] -0.548148785
                        0.084896488 -0.3618093076
## [134,]
          0.200275116 -2.329893544 0.1807820612
## [135,]
           1.012954927
                        0.207848181 -3.1075914230
## [136,]
           0.684773385 -0.418180700
                                     0.1193766853
## [137,]
           0.265991270 -1.127564425
                                     1.0622916315
## [138,]
                        1.337238996 -0.1567333112
           0.816047289
## [139,] -0.004758957
                        0.254210240 0.3494468499
## [140,] -0.659513150
                        0.603226065 -0.9684829433
## [141,]
          0.923062231 -0.032713985 0.0676803357
## [142,] -0.766013551 -0.333299547 -0.4898487459
## [143,] -0.431084079
                        0.882918765 -0.3375768085
## [144,] -0.190133535 -0.640424682
                                     0.3848998983
## [145,]
                        0.078962400 -0.7680732406
          0.594737173
## [146,] -0.822369651 -0.053442218 -0.1115508170
## [147,] -0.632086337
                        0.639659696 0.3084664918
## [148,]
          0.318971640 -1.156013079 -0.5291490901
## [149,]
           0.863876747
                        0.671332644
                                    0.2568422316
## [150,] -0.102833245
                        0.438284149 -1.3662033639
## [151,]
           1.097728686 -0.154049087
                                      0.6481837510
## [152,]
          0.058513888
                       -1.525735600
                                      0.7298158827
## [153,] -0.501623706
                        0.244712801
                                     0.7113591605
                        0.387641116 -1.2984836637
## [154,] -0.466410671
## [155,] -0.026249918
                                     0.3217130039
                        0.140029667
## [156,] -0.116271543
                        0.519456212
                                     0.2552566197
## [157,] -0.328502961
                        0.297409376
                                     0.2283230337
## [158,] -0.670127696
                        0.863873950 -0.0320977323
## [159,] 1.236631450 -0.628600664 0.3480628341
```

```
## [160,] -0.087149306 -0.989271375 -0.0447048996
## [161,]
           0.264931050
                        0.108130352
                                      0.6630592328
## [162,] -1.011591855
                        0.282794292
                                      0.3950346566
          0.064674548 -0.794095498 -0.7180245971
## [163,]
## [164,] -0.855164135
                        0.353179379 -1.1021613126
## [165,] -0.817630171
                        0.338158269 -2.2477161022
## [166,]
          0.790071410
                        0.085952387
                                      0.4093134146
## [167,] -0.364973805
                       -0.605203649
                                      0.8129999106
## [168,]
           0.051590540
                        1.959827996
                                      1.0494779489
## [169,] -0.058338220 -0.409337783
                                      0.0359104234
## [170,]
          0.159737156
                        0.254669123 -0.1473645979
## [171,] -0.489533321
                        0.419949638 -0.0988150804
## [172,] -0.595220420 -0.285623727 -3.2696000954
## [173,]
          0.085653123 -2.126932185
                                      0.8797935760
## [174,] -1.101774379
                        0.948102234
                                      0.2916000702
                                      0.3032487590
## [175,] -0.166037172 -0.108567577
## [176,] -0.097398428 -1.622331214
                                      0.4001096589
## [177,]
          0.077392575
                         0.439270324
                                      0.1476584803
## [178,] -0.847221750 -0.547109788
                                      0.9085380018
## [179,] -0.127606139 -2.264892371
                                      0.4746835928
## [180,] -0.690762926 -0.522014464 -0.3837300635
## [181,] -1.244346835
                        0.658517059 -0.3641916993
## [182,] -0.514946965
                        0.827817681
                                      0.3989361780
## [183,] -0.172665628
                        0.647201739
                                      0.1258618235
## [184,]
          0.858257113
                         0.307871855
                                      0.9277885573
## [185,] -0.642483481
                        0.760191790
                                      0.4506613356
## [186,] -0.241494042
                         0.111254457
                                     -0.0564260901
## [187,] -0.937666219
                        0.077076546
                                      0.6672609206
## [188,] -0.255431065 -0.236095185
                                    -1.8079088692
## [189,] -0.460797704
                         0.065475798
                                      0.7839240452
## [190,] -1.408796077 -0.544433129
                                      0.0945931696
## [191,]
           0.896368333
                         0.001930967
                                      0.0750159818
## [192,]
                       -1.181534430
           0.146044715
                                      0.7722082772
## [193,] -0.858056614
                         0.737315437
                                      0.6394594140
## [194,] -0.197251951
                       -0.170279072
                                      0.7379426061
## [195,] -1.140428526
                        1.852050166
                                      0.3155272212
## [196,]
          0.325426969
                       -1.463111748
                                      0.4808327148
## [197,] -1.139571685
                        0.202664970 -0.0453437056
## [198,] -0.563968269
                        0.088513773
                                      0.4422084068
## [199,] -1.086028156
                        1.352543347
                                     -0.1819051765
## [200,]
          0.382812764
                        3.094221200
                                      0.3362310993
## [201,] -0.572810886
                        0.126824436
                                      0.0238687266
## [202,] -0.921088541 -1.225260712
                                      0.0570952712
## [203,] -0.049124158 -1.459231030
                                      1.1118129779
## [204,]
           0.257805972
                        1.189500127
                                      0.6668767422
## [205,]
           0.074748808 -0.617912310
                                      0.7867845639
## [206,] -0.872191759 -0.486364167
                                      0.1067486746
## [207,] -1.645178492 -0.281541525
                                      0.3536193491
## [208,]
          0.411305453 -0.203541128
                                      1.1172313308
## [209,] -0.601616408 -0.554671402 -1.4750001020
```

```
## [210,] -0.955119693 1.089864345 -0.1569386064
## [211,] -0.276077959
                        0.580271097 -0.1500176716
## [212,] -1.044240318 -1.218357423 0.7190084888
## [213,] 0.514319443 -1.745361381 -0.0449525080
## [214,] -0.813768250
                       1.478470608
                                     0.5964264070
                        0.204602604
## [215,] -0.444032668
                                     0.5628851690
## [216,]
          0.052099177
                        0.437476293
                                     0.6339590882
## [217,] -0.172145649 -1.585499295 -0.5722453206
## [218,]
          2.496763775 -0.200777416
                                     1.1196635080
## [219,] -0.197712351
                        0.335412570 -0.0672413174
## [220,] -1.028972799 -0.545444230 -0.4469534152
## [221,]
          0.133728397
                        1.129970941
                                     0.2085540954
## [222,] -0.578029718 -1.566105155
                                     0.8250059417
## [223,] -1.446534248 -0.178091687 -0.1196636579
## [224,] -1.435219779
                        1.547758563
                                     0.4838741521
## [225,] -0.798291149 -0.176369046 -0.9801923146
## [226,]
          0.633708473 -0.010070080
                                     0.9765007437
## [227,] -0.723949834
                        1.449128438
                                     0.9110323577
## [228,] -1.030544496
                        0.377486823 -1.3845133459
                        1.958924376
## [229,]
          1.107193215
                                     0.8886990582
## [230,] -0.177352212
                        0.727349896
                                     0.5602343511
                        2.181949995
## [231,] -0.382554098
                                     1.5801305215
## [232,] -0.270465487
                        0.467890423
                                     1.1229275581
                        0.390174384
## [233,] -1.674866120
                                     0.3437570553
## [234,] -0.828338660 -0.081849356 -0.2421741564
## [235,] -0.899183143 -0.433349049
                                     0.0541855242
                                     0.4216441943
## [236,] 0.216850133 -1.442856753
## [237,] -0.260734248 -2.247006891
                                     0.6672969538
## [238,] -0.240412393 1.031285447
                                     1.0570939845
## [239,] -0.477973585 -0.114754991
                                     0.2479793462
## [240,] -0.834705507 -0.371072459
                                     0.5932273199
## [241,] -0.146097282 -1.113592351 -0.3975691472
## [242,] -0.478350273
                        0.467514588
                                     0.2735254772
## [243,] -1.590244047
                        0.533883949
                                     0.4184106249
## [244,] -0.337491933 -0.703958612 -0.0495325011
## [245,] -0.616985393
                        0.495454082
                                     0.2479309897
## [246,] -0.564588356 -0.134668438
                                     0.5948572768
## [247,] -1.010428348
                        0.579147470 -1.4544247652
## [248,] -0.137655299
                        0.993127257
                                     0.6218160308
## [249,] -1.759514498 -0.274842579 -0.4034560489
## [250,] -0.813783277
                        0.878697260
                                     0.8719692563
## [251,] -1.368612816 -0.021316492 -2.2729743066
## [252,] -1.275899254 -0.475442827
                                     0.0786717985
## [253,] -1.029142756
                        0.136056729
                                     0.5715204228
## [254,] -0.193496871
                        0.569879346
                                     1.0094653812
## [255,] -0.919133283 -1.367103676
                                     0.4859672953
## [256,] -1.304260771 -0.350205504 -0.0748085330
## [257,] -0.360695064 -0.407225800
                                     0.3469299128
## [258,] -1.034864271 -0.286602875
                                     0.6156970433
## [259,] -1.699350741 1.116851998 0.5446641225
```

```
## [260,] -1.119929739 -0.573998136 0.6845877600
## [261,] -1.169037355 -0.082835319
                                     0.9001028427
## [262,] -0.784809716
                                     0.3269090559
                        0.167920028
## [263,] -0.493708629
                        1.695450884
                                     0.9796642972
## [264,] -0.497304930 -1.601722724
                                     1.1761804108
## [265,] -0.976574569 -0.192412282
                                     0.6509580136
## [266,] -1.467961242 -0.427896169 -0.1003924068
## [267,] -0.902077101
                       1.496147172 -0.4109312622
## [268,] -1.036389744
                        0.082329109
                                     1.0784647253
## [269,] -1.705386507 -0.299483803 -0.1146301416
## [270,] -1.739073319 1.138271940
                                     0.3559990233
## [271,] -1.300129495
                        1.536663050
                                     0.2416124330
## [272,] -1.315969968
                        0.440075513
                                     0.4998004636
## [273,] -0.529848105
                        0.419933966
                                     1.0482014072
## [274,] -1.985877359 -0.100740767
                                     0.7664031671
## [275,] -1.130127906
                        0.653364324
                                     0.9493329437
## [276,] -1.598593607 -0.309970406 -0.4940385513
## [277,] -0.632759027 -0.841159617 -0.0294273529
## [278,] -0.738333683
                        0.116872897 1.3081957816
                        0.731749724 -0.1439136175
## [279,] -1.578182522
## [280,] -0.953911115 -0.420001999 -0.0239870270
## [281,] -0.480593516 -0.083066046 -1.2235734344
## [282,]
          0.010452664
                        0.638979802
                                    1.3749238633
## [283,] -0.548950968
                       2.217153856
                                     0.9372928135
## [284,] -0.743013091 -0.155648639 -0.5674839806
## [285,] -1.612155439 -0.603633903
                                     0.5012124553
## [286,] -1.039827166 -0.076912746
                                     0.4303027182
## [287,] -0.843330937 -0.242317466
                                     0.4266714040
## [288,] -1.182272798 -0.941536117 -0.5788535918
## [289,] -0.948575182 -0.543794864 -0.0384268999
## [290,]
         0.070130052 -1.812508190
                                    0.2191244979
## [291,] -1.743137930 -1.091959585
                                     0.4053547510
## [292,] -1.073623081 0.267028528
                                     1.0060410433
## [293,] -1.427227293 -0.672588422
                                     0.0315439986
## [294,] -1.122843832
                       0.345719829
                                     1.1758990412
## [295,] -1.263199681 -0.528831385
                                     1.1119318115
## [296,] -1.290036191 -0.095482767 -0.7991514192
## [297,] -1.393302226 -2.385879900 -2.6677123780
## [298,] -1.782271248  0.420525876 -0.9155996847
## [299,] -1.273483991 -0.483974683 0.2522706621
fit.pc <- principal(dataset[c(1,3,5,7,8,9,12)], nfactors=3, rotate="varimax")</pre>
fit.pc
## Principal Components Analysis
## Call: principal(r = dataset[c(1, 3, 5, 7, 8, 9, 12)], nfactors = 3,
       rotate = "varimax")
## Standardized loadings (pattern matrix) based upon correlation matrix
##
                              RC1
                                    RC2
                                          RC3
                                                h2
                                                      u2 com
## age
                             0.70 0.19 -0.20 0.56 0.44 1.3
```

```
## creatinine_phosphokinase -0.02 -0.09 0.86 0.76 0.24 1.0
## ejection fraction
                             0.10 0.76 -0.16 0.60 0.40 1.1
## platelets
                             0.01 0.36 0.41 0.30 0.70 2.0
                             0.59 -0.23 -0.05 0.40 0.60 1.3
## serum creatinine
## serum_sodium
                            -0.24 0.66 0.17 0.53 0.47 1.4
                            -0.70 0.04 -0.20 0.54 0.46 1.2
## time
##
##
                          RC1 RC2 RC3
## SS loadings
                         1.39 1.24 1.05
## Proportion Var
                         0.20 0.18 0.15
## Cumulative Var
                         0.20 0.38 0.53
## Proportion Explained 0.38 0.34 0.29
## Cumulative Proportion 0.38 0.71 1.00
## Mean item complexity = 1.3
## Test of the hypothesis that 3 components are sufficient.
## The root mean square of the residuals (RMSR) is 0.16
## with the empirical chi square 326.89 with prob < 1.5e-70
##
## Fit based upon off diagonal values = -1.65
round(fit.pc$values, 3)
## [1] 1.475 1.176 1.029 0.966 0.888 0.737 0.729
fit.pc$loadings
##
## Loadings:
                            RC1
                                   RC2
                                          RC3
                             0.696 0.185 -0.200
## age
## creatinine phosphokinase
                                           0.864
## ejection_fraction
                                    0.755 -0.157
                                    0.357
                                           0.412
## platelets
## serum creatinine
                             0.586 -0.232
                            -0.240 0.663 0.173
## serum sodium
## time
                            -0.702
                                          -0.201
##
##
                    RC1
                          RC2
                                RC3
## SS loadings
                  1.390 1.235 1.054
## Proportion Var 0.199 0.176 0.151
## Cumulative Var 0.199 0.375 0.526
# Loadings with more digits
pc.load.heart <- fit.pc$loadings[1:7,1:3]</pre>
print(pc.load.heart)
##
                                    RC1
                                                RC2
                                                             RC3
                             0.69625801 0.18519166 -0.20024241
## age
## creatinine_phosphokinase -0.01977081 -0.09374166 0.86427917
```

```
## ejection fraction
                             0.09927290 0.75521937 -0.15703997
## platelets
                             0.01116830 0.35699707 0.41234930
## serum_creatinine
                             0.58617844 -0.23158975 -0.04551365
## serum sodium
                            ## time
                            # Communalities
fit.pc$communality
##
                       age creatinine phosphokinase
                                                            ejection fraction
##
                 0.5591682
                                           0.7561569
                                                                   0.6048730
##
                  platelets
                                   serum_creatinine
                                                                serum_sodium
##
                 0.2976036
                                           0.3993105
                                                                   0.5265868
##
                      time
##
                 0.5359443
# Rotated factor scores
fit.pc$scores
##
                   RC1
                               RC2
                                              RC3
##
     [1,]
          1.661261807 -1.554800886
                                    0.2391648108
##
     [2,]
          0.743266680 -0.800052166
                                    6.6257827317
##
     [3,]
          0.927179080 -2.016941671 -0.4549872007
##
     [4,]
          0.334885605 -1.266839858 0.1473115437
##
          1.925456863 -3.274592726 -0.2063397138
     [5,]
##
     [6,]
          2.435918328 -0.165636681 -0.8575735122
##
          1.012119703 -1.263416904 -0.3244895181
     [7,]
##
     [8,]
          1.124477246 1.115611048 0.4460294461
##
     [9,]
          1.234722890 1.691814397 -0.3538296415
##
    [10,]
          4.919709448 -0.999011928 0.1358685604
##
    [11,]
          2.640695114 -0.439924198 -0.0044503303
##
          0.428072549 -0.186827135
                                    0.2931060423
   [12,]
##
    [13,] -0.139463181 -1.005910129
                                    0.5149623433
##
          0.205750073 -0.013367351
                                     0.2133024344
    [14,]
##
          0.100190044 0.129530927
                                    0.8853088186
   [15,]
##
    [16,]
          1.649820322
                       0.324891744 -1.1159824597
##
                       0.956323503 -0.2371917548
    [17,]
          1.595345623
##
    [18,] -0.156822106 -2.866432703
                                    0.1779870700
##
    [19,]
          0.762120879 -0.103388790
                                    0.0231261139
##
          0.907950332 -1.748387342 -0.9061044026
    [20,]
##
   [21,]
          0.762655848 -0.465114447
                                    0.0799383657
##
   [22,]
          0.944646930 -0.308381123
                                    0.1180144130
                       0.548331547
##
    [23,]
          0.733921935
                                    0.1903647967
##
   [24,]
          0.457662548
                      1.284173827
                                    0.0687137964
##
    [25,]
          1.492282733 -0.549949036
                                    0.1711517403
##
          1.455420414 0.835943301 -0.5028730340
   [26,]
##
    [27,]
          1.941662073
                       0.755655310 -0.7523795208
                       0.573778900 -0.2150997676
##
    [28,]
          1.134926967
##
    [29,]
          2.308580309 -1.259927295 -0.6226136569
##
          1.520043263 -0.715581081 -0.6753536792
   [30,]
          2.353027773 0.193596104 -0.1844817096
##
   [31,]
```

```
##
    [32,]
           ##
    [33,]
           0.295532144 -1.105549289
                                     0.1548664887
##
    [34,]
           0.035612527 -0.257097226
                                    0.3899811986
##
                        0.991149461 -0.5046204217
    [35,]
           0.663877522
##
    [36,]
           1.876218740 -0.731427455
                                     0.0146293253
##
           1.908293478
                        0.818363037 -0.8903389408
    [37,]
##
    [38,]
           1.353571970
                        2.188128649
                                     0.6137036191
##
    [39,]
           1.007463177 -0.588312865
                                     2.3617777846
##
    [40,]
           1.154552043
                        0.620878762
                                     0.4508776138
    [41,]
##
           1.129162665 -1.163688178
                                     0.3401328031
##
    [42,]
         -0.020711589 -0.926623118 -0.3053509355
##
    [43,]
           0.923607487
                        0.610849610 -0.1530495710
                        0.484077775 -0.6480190259
##
    [44,]
           1.117429820
##
    [45,]
           0.525787658
                        1.628332541 -0.0773460918
##
    [46,]
           0.449719713 -0.306472980
                                     0.5615070471
##
           0.092432608 -1.612860316
                                     1.0768836850
    [47,]
##
    [48,]
           0.331904065
                        0.816335765
                                     1.0803374958
##
    [49,]
           2.457169977 -1.841559436 -0.3705196143
##
    [50,]
           0.168206595
                        0.400124857
                                     0.6707819730
##
           0.516047584 -0.626436159
    [51,]
                                      0.0009576655
##
    [52,]
           0.092532663 -0.300954180
                                     0.8749494801
##
           2.783428934
                       1.275225506
                                     3.1242865473
    [53,]
##
    [54,]
           1.035561944
                        0.843644912 -0.1766442263
##
           0.964937677 -0.667315954 -0.1836188315
    [55,]
##
           2.396441039
                        0.122309343 0.3800272497
    [56,]
##
    [57,]
           1.311884637 -0.096229075 -0.3931885056
##
    [58,]
           0.117242708
                        0.230750573
                                     0.0975868884
##
    [59,] -0.230865053 -1.036172140
                                     0.9937338718
##
          0.749126012 -0.827038561
                                      0.0716641805
    [60,]
##
    [61,] -0.222187227 -0.906990443
                                     7.2203194356
##
    [62,]
          0.501754161 -0.984400714 -0.2677696975
##
    [63,] -0.008689059
                        0.085367104 -0.0345107941
##
    [64,] -0.549357130
                        0.979474617
                                     1.2025062067
##
    [65,]
          0.083935800
                       2.028983076 -0.1298242971
##
    [66,]
           0.988680110 -2.692397650 -0.8718446516
##
    [67,] -0.648148747 -1.708399982 0.2357704108
##
    [68,]
           0.532711245
                        0.034977861 -0.0205406501
##
                        0.116363372 -0.0114748486
    [69,]
          0.449358882
##
    [70,]
          0.817628362 -0.142198633 0.7901497375
##
    [71,] -0.684673449
                        0.620888501
                                     0.5949996183
##
    [72,] -0.096008591 -0.266505695 -0.2283303489
##
    [73,]
           1.537899958 -0.792079545
                                     4.1950500318
##
    [74,]
          0.555768980
                        0.462584538 -0.7769184732
##
    [75,]
          0.556411378 -1.086577298 0.2364415509
##
    [76,] -0.216828225 -0.707001512 -0.1918664146
##
    [77,]
                       2.005827437 -0.3236278154
           0.668441464
##
    [78,] -0.607749063
                        0.183163996 -0.0212675426
##
    [79,]
          0.819260082 -0.217708128 -0.4254147686
##
    [80,] -0.063297651
                        0.943013569 0.2959498846
    [81,] 0.919009855 0.278359780 -0.3100879741
```

```
##
    [82,]
           0.647771674
                        0.814464099 -0.0545080160
##
    [83,]
           0.701850273 -1.556076413 -0.5038258391
##
    [84,]
                        0.236687990 -1.1519445673
           1.426833013
##
    [85,] -0.113963882 -0.001775022 0.3909018947
##
    [86,] -0.258837308
                        1.431743479 0.3730824376
##
    [87,] -0.132936474 -0.384334804 -0.5311877910
##
    [88,]
          0.412780099
                        1.884983446 -0.3481862241
                        0.165887725 -0.1153721621
##
    [89,] -0.728453310
##
    [90,] -0.325982563 -0.033839181 -0.1137702233
    [91,]
##
           0.551045835
                        0.542978350 -0.5658370679
##
    [92,]
          0.342583850
                        0.053331595 0.3617566227
##
    [93,] -0.363720014
                        0.919551965
                                     0.1109323635
##
    [94,]
          0.281720144 -1.053032127 -0.2996120563
##
    [95,] -0.201173206
                        0.914928165
                                    0.2348252272
##
    [96,]
           0.090540886
                        1.601030602 -0.5241222915
##
                       -0.967996687
    [97,]
           0.310968078
                                      0.1101564113
##
    [98,]
           0.783213325
                        1.310128264 -0.7599096037
##
   [99,]
           0.074300534
                       -0.429114466
                                      0.1875312235
## [100,]
                        0.508384870 -0.4203188124
           0.157269661
## [101,]
           0.119602956
                        0.070347549
                                     0.2929838037
## [102,]
           0.867269604
                        0.684410717 -0.1234748027
## [103,]
           0.610298824
                                      0.1110579911
                        0.187678958
## [104,] -0.696897702 -0.825599986
                                     4.3693073628
## [105,]
           0.550164436
                        1.359203255 -0.1724102706
## [106,]
           0.972097738
                        0.954499910
                                      1.3444474338
## [107,]
           0.060003135
                        0.312400494
                                      0.2643827297
## [108,] -0.630359888
                       -0.422572840
                                      1.3656024435
## [109,]
           0.394779402 -0.264159990
                                      0.4517056571
## [110,] -0.263211207
                        1.966140938
                                      2.6273981587
## [111,]
           1.570689585
                        1.218400716 -0.8286984171
## [112,] -0.079851430 -0.476705134 -0.3987411216
## [113,] -0.232857424 -0.987410715
                                    0.1836507253
                        1.672184717 -0.2905798137
## [114,]
           0.861926056
## [115,]
          0.502907066 -0.964718479 0.1722577393
## [116,] -0.124361588
                        0.121099491 -0.3427441451
## [117,]
                        1.241001991 -0.5654697557
           0.148570664
## [118,]
           2.291232248
                        2.230747174 0.1209613524
## [119,]
           0.292592223
                        1.569407098 -0.7579634732
## [120,]
           1.554116575
                        0.051411596 -0.2919360483
## [121,]
           0.471353622
                        0.769453621 -0.3000942339
## [122,]
           0.239404523 -0.179511841 -0.8150414891
## [123,] -0.183468621
                        0.418602246 -0.3254376420
## [124,] -0.379654647
                        0.225010617 -0.0511604751
## [125,]
          1.168530259 -0.687054723 -0.1837383744
## [126,] -0.439853331
                        0.096473505 -0.1761735895
## [127,] -0.020406232 -2.895762575 -0.1700108754
## [128,]
                        1.385234054 -0.3355970649
          0.029381207
## [129,] -0.160749776 -0.354127757 -0.1035501859
## [130,] 0.339556664
                        0.332058477
                                     0.0667005248
## [131,] -0.237984674 1.134193809 0.9177089771
```

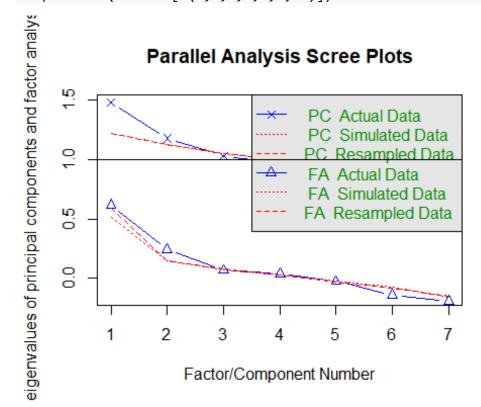
```
## [132,]
         2.210066656 -1.073871848 0.1719603923
## [133,] -0.548148785 -0.084896488 0.3618093076
## [134,]
         0.200275116 2.329893544 -0.1807820612
          1.012954927 -0.207848181
                                   3.1075914230
## [135,]
## [136,]
          ## [137,]
          0.265991270 1.127564425 -1.0622916315
## [138,]
         0.816047289 -1.337238996 0.1567333112
## [139,] -0.004758957 -0.254210240 -0.3494468499
## [140,] -0.659513150 -0.603226065 0.9684829433
## [141,]
         0.923062231
                       0.032713985 -0.0676803357
## [142,] -0.766013551
                       0.333299547
                                    0.4898487459
## [143,] -0.431084079 -0.882918765
                                  0.3375768085
## [144,] -0.190133535
                       0.640424682 -0.3848998983
## [145,]
         0.594737173 -0.078962400 0.7680732406
## [146,] -0.822369651
                       0.053442218 0.1115508170
## [147,] -0.632086337 -0.639659696 -0.3084664918
## [148,]
         0.318971640 1.156013079 0.5291490901
## [149,]
         0.863876747 -0.671332644 -0.2568422316
## [150,] -0.102833245 -0.438284149 1.3662033639
                       0.154049087 -0.6481837510
## [151,]
         1.097728686
## [152,]
         0.058513888 1.525735600 -0.7298158827
## [153,] -0.501623706 -0.244712801 -0.7113591605
## [154,] -0.466410671 -0.387641116 1.2984836637
## [155,] -0.026249918 -0.140029667 -0.3217130039
## [156,] -0.116271543 -0.519456212 -0.2552566197
## [157,] -0.328502961 -0.297409376 -0.2283230337
## [158,] -0.670127696 -0.863873950 0.0320977323
         1.236631450 0.628600664 -0.3480628341
## [159,]
## [160,] -0.087149306 0.989271375 0.0447048996
## [161,]
         0.264931050 -0.108130352 -0.6630592328
## [162,] -1.011591855 -0.282794292 -0.3950346566
## [163,] 0.064674548 0.794095498 0.7180245971
## [164,] -0.855164135 -0.353179379 1.1021613126
## [165,] -0.817630171 -0.338158269 2.2477161022
## [166,]
         0.790071410 -0.085952387 -0.4093134146
## [167,] -0.364973805 0.605203649 -0.8129999106
## [168,]
         0.051590540 -1.959827996 -1.0494779489
                       0.409337783 -0.0359104234
## [169,] -0.058338220
## [170,]
         0.159737156 -0.254669123 0.1473645979
## [171,] -0.489533321 -0.419949638 0.0988150804
## [172,] -0.595220420
                      0.285623727
                                   3.2696000954
## [173,]
         0.085653123 2.126932185 -0.8797935760
## [174,] -1.101774379 -0.948102234 -0.2916000702
## [175,] -0.166037172
                      0.108567577 -0.3032487590
## [176,] -0.097398428
                      1.622331214 -0.4001096589
## [177,]
         0.077392575 -0.439270324 -0.1476584803
## [178,] -0.847221750 0.547109788 -0.9085380018
## [179,] -0.127606139
                       2.264892371 -0.4746835928
## [180,] -0.690762926
                       0.522014464 0.3837300635
## [181,] -1.244346835 -0.658517059 0.3641916993
```

```
## [182,] -0.514946965 -0.827817681 -0.3989361780
## [183,] -0.172665628 -0.647201739 -0.1258618235
## [184,] 0.858257113 -0.307871855 -0.9277885573
## [185,] -0.642483481 -0.760191790 -0.4506613356
## [186,] -0.241494042 -0.111254457 0.0564260901
## [187,] -0.937666219 -0.077076546 -0.6672609206
## [188,] -0.255431065 0.236095185 1.8079088692
## [189,] -0.460797704 -0.065475798 -0.7839240452
## [190,] -1.408796077 0.544433129 -0.0945931696
## [191,]
         0.896368333 -0.001930967 -0.0750159818
## [192,] 0.146044715 1.181534430 -0.7722082772
## [193,] -0.858056614 -0.737315437 -0.6394594140
## [194,] -0.197251951 0.170279072 -0.7379426061
## [195,] -1.140428526 -1.852050166 -0.3155272212
## [196,] 0.325426969 1.463111748 -0.4808327148
## [197,] -1.139571685 -0.202664970 0.0453437056
## [198,] -0.563968269 -0.088513773 -0.4422084068
## [199,] -1.086028156 -1.352543347 0.1819051765
## [200,]
         0.382812764 -3.094221200 -0.3362310993
## [201,] -0.572810886 -0.126824436 -0.0238687266
## [202,] -0.921088541 1.225260712 -0.0570952712
## [203,] -0.049124158 1.459231030 -1.1118129779
## [204,] 0.257805972 -1.189500127 -0.6668767422
## [205,] 0.074748808 0.617912310 -0.7867845639
## [206,] -0.872191759 0.486364167 -0.1067486746
## [207,] -1.645178492 0.281541525 -0.3536193491
## [208,] 0.411305453
                      0.203541128 -1.1172313308
## [209,] -0.601616408
                       0.554671402 1.4750001020
## [210,] -0.955119693 -1.089864345 0.1569386064
## [211,] -0.276077959 -0.580271097 0.1500176716
## [212,] -1.044240318
                      1.218357423 -0.7190084888
## [213,] 0.514319443
                       1.745361381 0.0449525080
## [214,] -0.813768250 -1.478470608 -0.5964264070
## [215,] -0.444032668 -0.204602604 -0.5628851690
## [216,]
         0.052099177 -0.437476293 -0.6339590882
## [217,] -0.172145649 1.585499295 0.5722453206
         2.496763775
## [218,]
                       0.200777416 -1.1196635080
## [219,] -0.197712351 -0.335412570 0.0672413174
## [220,] -1.028972799 0.545444230 0.4469534152
## [221,] 0.133728397 -1.129970941 -0.2085540954
                      1.566105155 -0.8250059417
## [222,] -0.578029718
## [223,] -1.446534248 0.178091687 0.1196636579
## [224,] -1.435219779 -1.547758563 -0.4838741521
## [225,] -0.798291149 0.176369046 0.9801923146
## [226,] 0.633708473
                      0.010070080 -0.9765007437
## [227,] -0.723949834 -1.449128438 -0.9110323577
## [228,] -1.030544496 -0.377486823 1.3845133459
## [229,] 1.107193215 -1.958924376 -0.8886990582
## [230,] -0.177352212 -0.727349896 -0.5602343511
## [231,] -0.382554098 -2.181949995 -1.5801305215
```

```
## [232,] -0.270465487 -0.467890423 -1.1229275581
## [233,] -1.674866120 -0.390174384 -0.3437570553
## [234,] -0.828338660 0.081849356 0.2421741564
## [235,] -0.899183143  0.433349049 -0.0541855242
## [236,] 0.216850133 1.442856753 -0.4216441943
## [237,] -0.260734248 2.247006891 -0.6672969538
## [238,] -0.240412393 -1.031285447 -1.0570939845
## [239,] -0.477973585 0.114754991 -0.2479793462
## [240,] -0.834705507
                       0.371072459 -0.5932273199
## [241,] -0.146097282 1.113592351 0.3975691472
## [242,] -0.478350273 -0.467514588 -0.2735254772
## [243,] -1.590244047 -0.533883949 -0.4184106249
## [244,] -0.337491933
                       0.703958612 0.0495325011
## [245,] -0.616985393 -0.495454082 -0.2479309897
## [246,] -0.564588356
                       0.134668438 -0.5948572768
## [247,] -1.010428348 -0.579147470 1.4544247652
## [248,] -0.137655299 -0.993127257 -0.6218160308
## [249,] -1.759514498
                       0.274842579 0.4034560489
## [250,] -0.813783277 -0.878697260 -0.8719692563
                       0.021316492 2.2729743066
## [251,] -1.368612816
## [252,] -1.275899254
                       0.475442827 -0.0786717985
## [253,] -1.029142756 -0.136056729 -0.5715204228
## [254,] -0.193496871 -0.569879346 -1.0094653812
## [255,] -0.919133283 1.367103676 -0.4859672953
## [256,] -1.304260771
                       0.350205504 0.0748085330
## [257,] -0.360695064
                       0.407225800 -0.3469299128
                       0.286602875 -0.6156970433
## [258,] -1.034864271
## [259,] -1.699350741 -1.116851998 -0.5446641225
## [260,] -1.119929739
                       0.573998136 -0.6845877600
## [261,] -1.169037355
                       0.082835319 -0.9001028427
## [262,] -0.784809716 -0.167920028 -0.3269090559
## [263,] -0.493708629 -1.695450884 -0.9796642972
## [264,] -0.497304930 1.601722724 -1.1761804108
## [265,] -0.976574569
                       0.192412282 -0.6509580136
## [266,] -1.467961242 0.427896169 0.1003924068
## [267,] -0.902077101 -1.496147172 0.4109312622
## [268,] -1.036389744 -0.082329109 -1.0784647253
                       0.299483803 0.1146301416
## [269,] -1.705386507
## [270,] -1.739073319 -1.138271940 -0.3559990233
## [271,] -1.300129495 -1.536663050 -0.2416124330
## [272,] -1.315969968 -0.440075513 -0.4998004636
## [273,] -0.529848105 -0.419933966 -1.0482014072
## [274,] -1.985877359 0.100740767 -0.7664031671
## [275,] -1.130127906 -0.653364324 -0.9493329437
## [276,] -1.598593607 0.309970406 0.4940385513
## [277,] -0.632759027
                       0.841159617 0.0294273529
## [278,] -0.738333683 -0.116872897 -1.3081957816
## [279,] -1.578182522 -0.731749724 0.1439136175
## [280,] -0.953911115
                       0.420001999 0.0239870270
## [281,] -0.480593516  0.083066046  1.2235734344
```

```
0.010452664 -0.638979802 -1.3749238633
## [283,] -0.548950968 -2.217153856 -0.9372928135
## [284,] -0.743013091
                        0.155648639
                                    0.5674839806
## [285,] -1.612155439
                        0.603633903 -0.5012124553
## [286,] -1.039827166
                        0.076912746 -0.4303027182
## [287,] -0.843330937
                        0.242317466 -0.4266714040
## [288,] -1.182272798
                        0.941536117
                                     0.5788535918
## [289,] -0.948575182
                        0.543794864
                                     0.0384268999
## [290,]
          0.070130052
                        1.812508190 -0.2191244979
## [291,] -1.743137930
                        1.091959585 -0.4053547510
## [292,] -1.073623081 -0.267028528 -1.0060410433
## [293,] -1.427227293
                        0.672588422 -0.0315439986
## [294,] -1.122843832 -0.345719829 -1.1758990412
## [295,] -1.263199681
                        0.528831385 -1.1119318115
## [296,] -1.290036191
                        0.095482767
                                     0.7991514192
## [297,] -1.393302226
                        2.385879900
                                     2.6677123780
## [298,] -1.782271248 -0.420525876
                                     0.9155996847
## [299,] -1.273483991
                        0.483974683 -0.2522706621
# Factor Analysis utilities
```

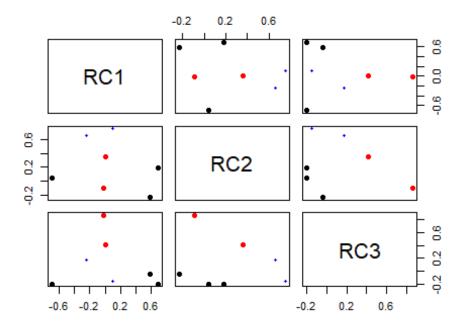
fa.parallel(dataset[c(1,3,5,7,8,9,12)])



## Parallel analysis suggests that the number of factors = 0 and the number of components = 1

#Based on the plot, we should retain two factors(based on the first elbow)
fa.plot(fit.pc)

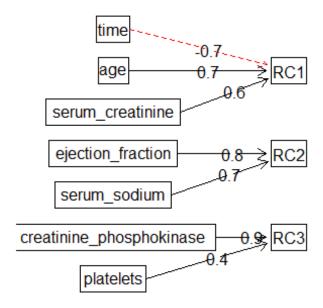
# **Principal Component Analysis**



#Based on the plot, we can confirm that there is no correlation between RCs

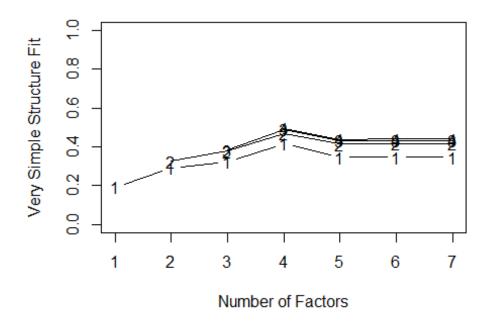
fa.diagram(fit.pc)

# **Components Analysis**



#This diagram visualizes the relationship
vss(dataset[c(1,3,5,7,8,9,12)])

# **Very Simple Structure**



```
##
## Very Simple Structure
## Call: vss(x = dataset[c(1, 3, 5, 7, 8, 9, 12)])
## VSS complexity 1 achieves a maximimum of 0.42 with 4 factors
## VSS complexity 2 achieves a maximimum of 0.47 with 4 factors
## The Velicer MAP achieves a minimum of NA with 1 factors
## BIC achieves a minimum of NA with 1 factors
## Sample Size adjusted BIC achieves a minimum of NA with 2 factors
##
## Statistics by number of factors
     vss1 vss2
                          chisq prob sqresid fit RMSEA BIC SABIC complex
               map dof
## 1 0.19 0.00 0.035 14 2.1e+01 0.095
                                          6.0 0.19 0.042 -59 -14.1
                                                                       1.0
## 2 0.29 0.33 0.075
                     8 5.0e+00 0.760
                                         5.0 0.33 0.000 -41 -15.3
                                                                       1.3
## 3 0.33 0.38 0.134
                     3 1.9e+00 0.589
                                          4.6 0.38 0.000 -15
                                                              -5.7
                                                                       1.5
## 4 0.42 0.47 0.251 -1 3.0e-02
                                   NA
                                          3.7 0.49
                                                      NA
                                                         NA
                                                                NA
                                                                       1.5
## 5 0.35 0.42 0.417 -4 2.0e-08
                                   NA
                                          4.1 0.44
                                                      NA NA
                                                                NA
                                                                       1.4
## 6 0.35 0.42 1.000 -6 2.6e-13
                                   NA
                                         4.1 0.45
                                                      NA NA
                                                                NA
                                                                       1.4
## 7 0.35 0.42
                 NA -7 2.6e-13
                                   NA
                                         4.1 0.45
                                                      NA NA
                                                                NA
                                                                       1.4
##
      eChisq
                SRMR eCRMS eBIC
## 1 3.7e+01 5.4e-02 0.066
                           -43
## 2 7.8e+00 2.5e-02 0.040
                           -38
## 3 3.0e+00 1.6e-02 0.041
                           -14
## 4 4.7e-02 1.9e-03
                            NA
                       NA
## 5 2.6e-08 1.4e-06
                       NA
                            NA
## 6 5.0e-13 6.3e-09
                       NA
                            NA
## 7 5.0e-13 6.3e-09
                            NA
                       NA
#The Very Simple Structure recommends to retain 4 factors to achieve the
maximum fit
detach(dataset)
```