

```

1  What is a Monad ?
2
3  1. Background
4
5  (see Hutton, https://www.youtube.com/watch?v=t1e8gqXLbsU)
6
7  on Maybe monads
8
9  -----
10
11 2. IO Monad
12
13 a. Recall that, for any type a, we have a corresponding type
14
15     IO a
16
17     where their members are actions (or programs) that yield a
18     result of type a . Note that the notation () denotes the
19     type with the single value () (the 0-ary tuple).
20
21     Hence, many IO actions are represented as functions of
22     the type:
23
24     t -> IO () (t is a type such as String, Char etc.)
25
26     Examples include: putChar, putStr, putStrLn, print, return
27
28     IO actions are members in IO a
29
30     Examples include: getChar, getLine etc.
31
32
33 b. One way to think of the type IO a is
34
35     type IO a = World -> (a,World)
36
37     Hence, when we compose multiple actions, it is not obvious
38     that associative laws hold. We will revisit this point later.
39
40 c. IO monad
41
42     IO and Maybe examples of monads. In essence, Monad is a type
43     class where a list of operations must be provided and the
44     operations must satisfy a number of algebraic laws (called the
45     Monad laws, see bird 243).
46
47     Here is the definition of Monad
48     [from: https://wiki.haskell.org/Monad]
49
50 class Monad m where
51
52     (>>=)  :: m a -> ( a -> m b) -> m b
53     (>>)   :: m a -> m b           -> m b
54     return :: a                   -> m a
55     fail   :: String -> m a
56
57 and all instances of Monad should obey the Monad Laws:
58
59 return a >>= k                = k a
60 m >>= return                  = m
61 m >>= (\x -> k x >>= h)      = (m >>= k) >>= h
62
63
64 It is equivalent to say that the following operation (>=>)
65
66 (>=>) :: Monad m => (a -> m b) -> (b -> m c) -> a -> m c

```

```
67 (m >=> n) x = do
68             y <- m x
69             n y
70
71 satisfy
72
73 1. (>=>) has a left identity (which is, the return function)
74 2. (>=>) has a right identity (which is, the return function)
75 3. (>=>) is an associative operations
76
77 Exercise:
78
79 Verify 1, 2 and 3.
80
81 (see https://wiki.haskell.org/Monad\_laws)
82
83 Note:
84
85 1. Monad laws are also discussed in Bird Chapter 10,
86 section 2. Note that the term Monoid is not the same
87 as Monads. Also, Parser is a Monad defined in Chapter 11
88 and the source code Parsing.lhs (given by Bird).
89
90
91 We will not go through some of the materials stated
92 therein (e.g. leapfrog rule) this semester.
93
94 -----
95
```