

Answer Keys

| | | | | | | | | | | | | | |
|----|------|----|-----|----|-----|----|------|----|----|----|---|----|-----|
| 1 | 5 | 2 | B | 3 | B | 4 | 2048 | 5 | 10 | 6 | A | 7 | C |
| 8 | A | 9 | 375 | 10 | 700 | 11 | A | 12 | B | 13 | D | 14 | A |
| 15 | 200 | 16 | B | 17 | A | 18 | B | 19 | D | 20 | D | 21 | C |
| 22 | 32 | 23 | C | 24 | D | 25 | B | 26 | B | 27 | D | 28 | 133 |
| 29 | 3.25 | 30 | A | 31 | C | 32 | A | 33 | A | 34 | 6 | 35 | D |
| 36 | B | 37 | D | 38 | D | 39 | D | 40 | C | 41 | B | 42 | D |
| 43 | D | 44 | B | 45 | D | 46 | B | 47 | D | 48 | 5 | 49 | 10 |
| 50 | B | 51 | A | 52 | C | 53 | B | 54 | A | 55 | A | 56 | D |
| 57 | C | 58 | D | 59 | D | 60 | B | 61 | D | 62 | B | 63 | C |
| 64 | D | 65 | C | | | | | | | | | | |

Explanations:-

- Graph G be a connected graph with n vertices and m edges. The spanning tree contains 'n-1' edges only. No. of edges that must be deleted in order to get spanning tree of G = m - n + 1 this is called circuit Rank.

So, circuit rank = 15 - 11 + 1 = 5

$$2. \sum_{x=0}^n \frac{x}{n} \cdot \binom{n}{x} p^x q^{n-x} = \frac{1}{n} \sum_{x=0}^n x \binom{n}{x} p^x q^{n-x} = \frac{1}{n} E(x) = \frac{1}{n} \cdot np = p$$

$$3. P \rightarrow (\neg r + \neg q)$$

$$P \rightarrow (r \vee \neg q)$$

$$\neg(r \vee \neg q) \rightarrow \neg p$$

$$(r \vee \neg q) \vee \neg p$$

$$\left[\begin{array}{l} \because \text{contrapositive of} \\ x \rightarrow y = \neg y \rightarrow \neg x \\ \because x \rightarrow y = \neg x \vee y \end{array} \right]$$

$$4. \text{Frame size} = 64B = 2^9 \text{ bits}$$

In 1 sec 1 Giga bit is transferred

\therefore In 1ms 1×10^{-3} Gb is transferred

$$1 \times 10^{-3} \text{ Gb} = \frac{2^{30} \times 10^{-3}}{2^9} \text{ frames} = 2048 \text{ frames}$$

$$5. \begin{array}{|c|c|c|c|c|c|c|c|c|c|c|c|} \hline P_1 & P_2 & P_3 & P_1 & P_2 & P_3 & P_1 & P_3 & P_1 & P_1 & P_1 & \\ \hline 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 \\ \hline \end{array}$$

6.

| | | BC | | | |
|---|---|----|----|----|----|
| | | 00 | 01 | 11 | 10 |
| A | 0 | 0 | X | | X |
| | 1 | X | 0 | 0 | 0 |

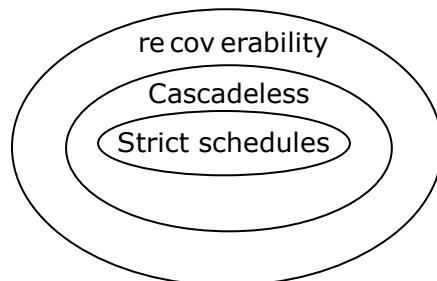
$F = \bar{A}.B$
 (or)
 $F = \bar{A}.C$

7. Number of serial schedules possible with n transactions = $n!$
 2 transactions = $2! = 2$.

No. of concurrent schedules possible with $T_1 = n_1, T_2 = n_2$

$$\text{instructions} = \frac{(n_1 + n_2)!}{n_1! n_2!} = \frac{(2 + 5)!}{2! 5!} = \frac{7!}{2! 5!} = \frac{6 \times 7}{2} = 21$$

8.



9. Total Data to transfer = $2000 \times 4 = 8000$ B

$$10^7 \text{ B} \text{ ----- } 1 \text{ s}$$

$$8000 \text{ B} \text{ ----- } 8000/10^7 \text{ s}$$

$$8000/10^7 \text{ s} = \text{RTT} + \text{transmission time}$$

$$8000/10^7 \text{ s} = 2 * \text{prop delay} + \text{transmission time}$$

$$8000/10^7 \text{ s} = 2 * \text{prop delay} + 50 \mu\text{s}$$

$$\text{Prop delay} = 375 \mu\text{s}$$

10. Total input data for 60 sec = $50 \text{ kB} \times 10 + 10 \text{ kB} \times 50$
 = 1000 kB

$$\text{Now output rate} = 5 \text{ kB/S}$$

$$\therefore \text{Output data for 60 sec} = 5 \text{ kB} \times 60 = 300 \text{ kB}$$

$$\text{Hence Bucket size} = (1000 - 300) \text{ kB} = 700 \text{ kB}$$

11. In a perfect binary tree number of nodes will be always odd
 In a perfect binary of height h , total number of nodes = $2^{h+1} - 1$

$$\therefore n = 2^{h+1} - 1; \text{ number of internal nodes}$$

$$= 2^h - 1 = \frac{n}{2} - \frac{1}{2} = \left\lfloor \frac{n}{2} \right\rfloor \text{ (Because } n \text{ is always odd)}$$

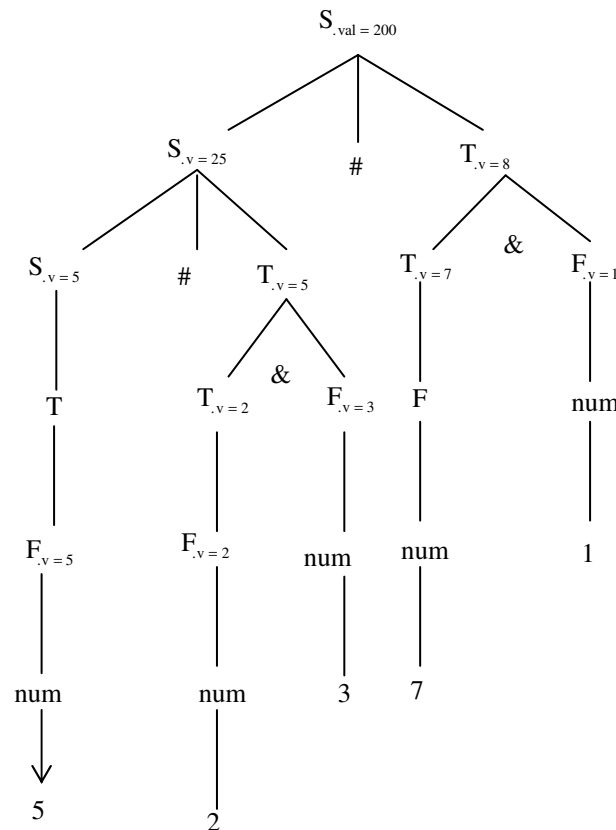
12. According to program,
 $F(n) = n + 2F(n-1)$ for $n \geq 2$
 $= 0$ for $n=1$

$$F(5) = 5 + 2(4 + 2(3 + 2(2 + 2(0)))) = 41$$

13. In a binary min heap the max element can be found among the leaf nodes. For a heap with n nodes there are at most $\text{ceil}(n/2)$ leaf nodes all of those need to be searched, hence it takes $\Theta(n)$ time.

14. Effort applied = $a_b \times (\text{KLOC})^{b_b} = 2.4 \times (64)^{1.05} \approx 189 \text{ PM}$

- 15.



16. (2) is finite, hence regular
 Let us use pumping lemma for (3)
 For $m \geq 3$, a y value of "aa" or "bb" will always pump the string. Hence (3) is regular
 (4) is regular as it can be expressed with regular expression $0(0+1)^+0+1(0+1)^+1$
17. $(R * S) *$ can produce ϵ . But $(R + S) * S$ cannot, hence they are not equivalent
18. $1 - (1 - 0.6) * (1 - 0.4) * (1 - 0.5) = 0.88$.

19. output equation is $\bar{x}.1 + xy = \bar{x} + y$ [absorption law $\bar{x} + xy = \bar{x} + y$]
 $\Rightarrow \bar{x} + y = a + b \Rightarrow x = \bar{a} \& y = b$

20.

| | | | | | | |
|--|---|----|----|----|----|----|
| | | yz | | | | |
| | x | | 00 | 01 | 10 | 11 |
| | 0 | | | | 1 | 1 |
| | 1 | | 1 | 1 | 1 | 1 |

This is the K – MAP for expression $y + x.\bar{y}$

| | | | | | | |
|--|---|----|----|----|----|----|
| | | yz | | | | |
| | x | | 00 | 01 | 10 | 11 |
| | 0 | | 0 | 1 | 3 | 2 |
| | 1 | | 4 | 5 | 7 | 6 |

So answer is (d) $\sum m(2,3,4,5,6,7)$

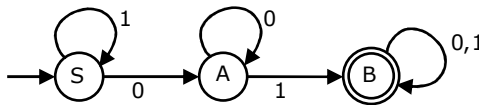
21. Given number = 1111 1111 1011
 2's complement of the given number = 00101 = $(-5)_{10}$
 So $(-15)_{10}$ is divisible by $(-5)_{10}$
 Because 2's complement of 1001 = $(-15)_{10}$

22. Size of required address is 20 bit, so 16 chips of 64k words makes 2^{20} words each of size 4 bits. As we need word size as 8 bits and available is 4 bits so we need to put another 16 chips in parallel.

23. The DFA corresponding to option (C) is

$$1 * 00 * 1(0 + 1)^*$$

$$= 1 * 0 * 01(0 + 1)^*$$



So, this DFA accepts all string with a sub string 01.

24. $\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} = \begin{bmatrix} l_{11} & 0 \\ l_{21} & l_{22} \end{bmatrix} \begin{bmatrix} 1 & u_{12} \\ 0 & 1 \end{bmatrix}$

Solving, we get $L = \begin{bmatrix} 1 & 0 \\ 3 & -2 \end{bmatrix}, U = \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix}$

25. $V(2x + 3) = 2^2 V(x) = 4 \times 6 = 24$

26. Main memory size = 2^{21} words
 Cache memory size = 32 kb
 Word size = 16 bit = 2B
 Block size = $1\text{kw} = 2^{11}\text{B} = 2\text{B} \times 2^{10}$
 For word addressable memory, physical address bits = 21 bits
 So bytes in main memory = 2^{21} words = $2^{21} \times 2\text{B} = 2^{22}$ bytes
 For byte addressable memory, physical address bits = 22 bits
 \therefore Number of blocks $M = \frac{2^{22}\text{B}}{2^{11}\text{B}} = 2048$ blocks

27. % CPU free time = $\frac{\text{data transfer time}}{\text{total time}}$
 total time = initialization time + termination time + data transfer time
 Initial set up time = 1000 clocks * 1 clock cycle time = $\frac{1000}{2 * 10^9} \text{ s} = 0.5\mu\text{s}$
 Termination time = $700 * \frac{1}{2 * 10^9} \text{ sec} = 0.35\mu\text{s}$
 Data transfer time for 16kB = $\frac{16\text{kB}}{4000\text{kB}} \text{ sec} = 4 * 10^{-3} \text{ sec} = 4000\mu\text{s}$
 % CPU free = $\frac{4000\mu\text{s}}{(0.5\mu\text{s} + 0.35\mu\text{s} + 4000\mu\text{s})} * 100 = 99.97\%$.

- 28.
-
- $2 + 12 + 13 + 14 + 8 + 3 + 62 + 19 = 133.$

29. Response time = first response time – arrival time

Gant chart:

| | | | | |
|----------------|----------------|----------------|----------------|----|
| P ₁ | P ₂ | P ₂ | P ₄ | |
| 0 | 5 | 6 | 8 | 13 |

So, response time of

$$P_1 = 0 - 0 = 0$$

$$P_2 = 5 - 1 = 4$$

$$P_3 = 6 - 2 = 4$$

$$P_4 = 8 - 3 = 5$$

$$\text{The average response time} = \frac{0 + 4 + 4 + 5}{4} = 3.25$$

30. Minimum number of nodes = $1 + 2 + 2 \cdot \left\lceil \frac{k}{2} \right\rceil + \dots + 2 \cdot \left\lceil \frac{k}{2} \right\rceil^{h-1}$

$$= 1 + 2 \left[\frac{\left\lceil \frac{k}{2} \right\rceil^h - 1}{\left\lceil \frac{k}{2} \right\rceil - 1} \right]$$

$$1 + 2 \left[\frac{3^4 - 1}{3 - 1} \right] = 81.$$

$$\begin{aligned} \text{Maximum number of nodes} &= 1 + k + k^2 + \dots + k^h \\ &= \frac{k^{h+1} - 1}{k - 1} = \frac{5^{4+1} - 1}{5 - 1} = \frac{5^5 - 1}{4} = \frac{3125 - 1}{4} = \frac{3124}{4} = 781 \end{aligned}$$

31. The output table is

| A | B | C | D |
|---|---|------|------|
| 1 | 2 | 3 | 1 |
| 1 | 2 | 4 | 1 |
| 2 | 1 | 3 | 5 |
| 3 | 1 | 3 | null |
| 4 | 2 | null | 1 |
| 3 | 2 | null | 1 |

33. $g(0)=0$
 $g(1)=30$
 //Item 3
 $g(2)=\max[64 + g(0), 30 + g(1)]=64$
 //Item 1
 $g(3)=\max[64 + g(1), 81 + g(0), 30 + g(2)]=94$
 //Item 1,3
 $g(4)=\max[64 + g(2), 81 + g(1), 30 + g(3)]=128$
 //Item 1
 $g(5)=\max[64 + g(3), 81 + g(2), 30 + g(4), 25 + g(0)]=158$
 //Item 1,3
34. $45 \bmod 20 = 5$; No collision
 $25 \bmod 20 = 5 \rightarrow 9 \bmod 20 = 9$; 1 collision
 $10 \bmod 20 = 10$; No collision
 $5 \bmod 20 = 5 \rightarrow 9 \bmod 20 = 9 \rightarrow 13 \bmod 20 = 13$; 2 collisions
 $9 \bmod 20 = 9 \rightarrow 13 \bmod 20 = 13 \rightarrow 17 \bmod 20 = 17$; 2 collisions
 $30 \bmod 20 = 10 \rightarrow 14 \bmod 20 = 14$; 1 collision
35. Total $1 + 2 + 2 + 1 = 6$ collisions
 $T(n) = 1$ if $n \leq 4$
 $T(n) = T(\sqrt{n}) + \log n$ if $n > 4$
 Taking $m = \log n$, the equation becomes
 $T(2^m) = 2 T(2^{m/2}) + m$,
 Now renaming $S(m) = T(2^m)$, the recurrence relation becomes
 $S(m) = 2 S(m/2) + m$.
 Using Master's theorem,
 $S(m) = T(2^m) = \Theta(m \log m) = \Theta(\log n \log \log n)$
36. Propagation time $= 45000 \times 10^3 / (2 \times 10^8) = 0.225$ s
 So $RTT = 2 \times 0.225 = 0.45$ s
 So bandwidth delay product $= 1 \text{ Mbps} \times 0.45 \text{ s}$
 So Bandwidth utilization $= 127 \times 150 \times 8 / \text{bandwidth delay product} = 33.87\%$
38. The mask is $255.255.255.0 = 11111111. 11111111. 11111111. 00000000$
 which is same as the default class C mask. Hence no. of subnet bits = 0.
 \therefore Maximum no. of subnets = $2^0 = 1$ and no. of host bits = $32 - 24 = 8$. Hence
 host per subnet = $2^8 - 2 = 254$
39. Copy propagation reduces the copying of variable values. It replaces all the uses of j directly by s and thus $j=s$ may be eliminated.

40. (A) $(1 + 01) * (0 + \lambda)$

$(11)(\lambda) = (11)$

(B) $(1 + 01) * (0 + \lambda)$

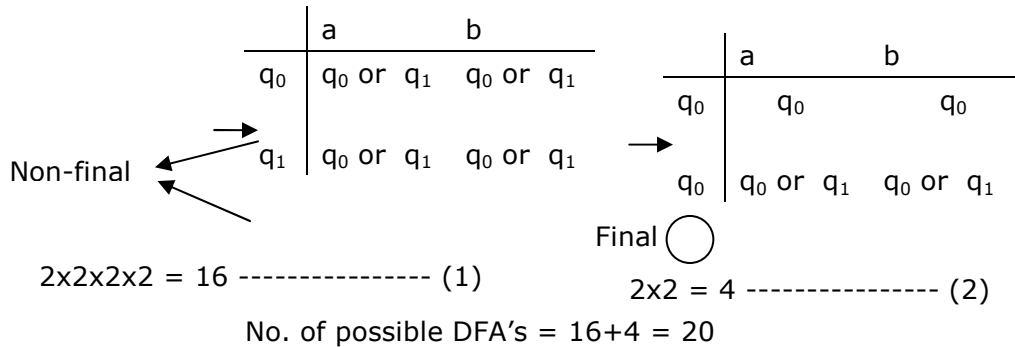
$(01)(\lambda) = 01$

(D) $(1 + 01) * (0 + \lambda)$

10

(C) In the given regular expression '00' never comes as a substring or string.

42.



43. $Z(p, q, r, s) = \bar{r}\bar{s} + \bar{r}sq + rs = \sum m(0, 3, 4, 5, 7, 8, 11, 12, 13, 15)$

44. Inner query returns total number of departments and outer query groups WORKS_IN table by the attribute eno. And it filters the groups based on number of tuples in each group (this number should be equal to total number of departments returned by outer query then only that respective eno of the group will be selected)

45. Let $f(u) = \tan x = \frac{x^3 + y^3}{x - y}$

$\therefore f(u)$ is a homogenous function of degree 2

$\therefore x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = n \frac{f(u)}{f'(u)}$

$= 2 \frac{\tan u}{\sec^2 u} = 2 \frac{\sin u}{\cos u} \cos^2 u = \sin 2u$

46. If $(x_m - x_n)$ divisible by 7, then we will have 7 possible remainders $\{0, 1, 2, 3, 4, 5, 6\}$.

If $(y_m - y_n)$ is divisible by 3, then we have 3 possible remainders $\{0, 1, 2\}$. So by pigeon hole principle it can be proved that least number of pairs required $= (7 \times 3) + 1 = 22$

$x_m - x_n$ is divisible by 7 iff

$x_m \text{ remainder } 7 = x_n \text{ remainder } 7$

Remainder option

x
0
1
2
3
4
5
6

Remainder option

y
0
1
2

21 options, so after 21 such pair 22nd pair will definitely match any of these, hence satisfy the given condition.

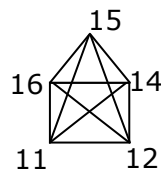
47.

| X | Y | Q_n | Q_{n+1} | J | K |
|---|---|-------|-----------|---|---|
| 0 | 0 | 0 | 1 | 1 | × |
| 0 | 0 | 1 | 0 | × | 1 |
| 0 | 1 | 0 | 1 | 1 | × |
| 0 | 1 | 1 | 1 | × | 0 |
| 1 | 0 | 0 | 0 | 0 | × |
| 1 | 0 | 1 | 1 | × | 0 |
| 1 | 1 | 0 | 0 | 0 | × |
| 1 | 1 | 1 | 0 | × | 1 |

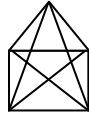
| X | YQ_n | | | |
|---|--------|----|----|----|
| | 00 | 01 | 11 | 10 |
| 0 | × | 1 | | × |
| 1 | × | | 1 | × |

$$\begin{aligned} K &= \overline{X}\overline{Y} + XY \\ &= \overline{X \oplus Y} \\ &= X \odot Y \end{aligned}$$

48. Number of elements in maximum clique of graph = clique number of graph
(Any subset of a graph in which all the vertices are connected to each other directly is called clique of a graph and largest possible subset is called maximum clique. So in the given graph maximum clique is as follows)



49. Number of vertices in the line Graph of



is equal to the number of edges in graph $\frac{5(5-1)}{2} = 10$.

50. eg: $A = \{5, 4, 3, 2, 1\}$
Here $(1,2), (1,3), (1,4), (1,5)$
 $(2,3), (2,4), (2,5)$
 $(3,4), (3,5)$
 $(4,5)$ are inversions.

Hence, maximum number of inversions $= (n-1) + (n-2) + \dots + 1 = \frac{n(n-1)}{2}$

51. Algorithm steps:

1. Use merge sort to sort A & store the output in B.
 2. Consider an element from A, starting From 1st index
 3. Find the position of A[1] in B using binary-search.
 4. The (position-1) will give no. of inversions w.r.t A[1] in A.
 5. Remove A[1] from A & B
 6. Repeat 2 to 5 for all elements. (steps)
- This requires $\theta(n \log n)$ time.

52. If $X = Y = 0$, available will be $(0, 0, 2, 0)$ with this P_4 then P_2 can be executed then any of the remaining processes can be executed

- 53.

| | Allocation | Max | Need | Available |
|-------|------------|---------|---------|-----------|
| | A B C D | A B C D | A B C D | |
| P_1 | 0 2 1 4 | 1 2 1 4 | 1 0 0 0 | 0 0 2 0 |
| P_2 | 1 3 5 4 | 1 6 5 5 | 0 3 0 1 | |
| P_3 | 2 0 6 4 | 3 0 6 4 | 1 0 0 0 | |
| P_4 | 0 6 3 2 | 0 6 5 2 | 0 0 2 0 | |
| P_5 | 1 0 1 4 | 2 0 1 5 | 1 0 0 1 | |

With $(0, 0, 2, 0)$ only P_4 can be executed then only P_2 can be executed then any of the remaining processes can be executed, so number of sequences $= \underline{P_4} \underline{P_2} \underline{3} \times \underline{2} \times \underline{1} = 6$

54. Disk size = $16 * 1024 * 1024 * 1 \text{ kB}$
 $= 16 * 2^{30} \text{ byte}$
 $= 16 \text{ GB.}$
55. Initial time = $300 * \frac{1}{600 * 10^6} = 0.5\mu\text{s}$
 terminate time = $900 * \frac{1}{600 * 10^6} = 1.5\mu\text{s}$
 time for 1 revolution = $\frac{60}{3000} \text{ sec}$
 In 1 revolution or in $\frac{60}{3000} \text{ sec}$, data transfer is $\longrightarrow 1024 \text{ kB}$
 so in 1 sec data transfer is $\rightarrow \frac{1024 * 3000}{60} \text{ kB} = 50 \text{ MB / sec (data transfer rate)}$
 Data transfer time for 20kB = $\frac{20 \text{ kB}}{50 \text{ MB}} \text{ sec} = 0.4 * 10^{-3} \text{ s} = 400\mu\text{s}$
 $\% \text{ CPU consumed} = \frac{\text{Initial time} + \text{termination time}}{\text{total time}} * 100$
 $= \frac{0.5\mu\text{s} + 1.5\mu\text{s}}{(0.5\mu\text{s} + 1.5\mu\text{s} + 400\mu\text{s})} \Rightarrow \frac{2\mu\text{s}}{402\mu\text{s}} * 100 = 0.49\%$
59. If the same noun is repeated after preposition, the noun will be singular
60. Let the smaller number be x
 Then largest number = $(x + 4245)$
 $\therefore x + 4245 = 8x + 45 \Rightarrow 7x = 4200 \Rightarrow x = 600$
 $\therefore \text{smaller number} = 600$
62. Anshu 1 day work = $1/16$
 Satish 1 day work = $1/20$
 Anshu+Satish's 1 day work = $\left(\frac{1}{16} + \frac{1}{20}\right) = \left(\frac{5+4}{80}\right) = \frac{9}{80}$
 $\therefore \text{Gulshan 1 day work} = (\text{Anshu} + \text{Satish} + \text{Gulshan})$
 $= 1 \text{ day work} - (\text{Anshu} + \text{satish 1 day work})$
 $= \frac{1}{5} - \frac{9}{80} = \frac{7}{80}$
 $\therefore \text{Gulsan can finish the work in } 80/7 \text{ days.}$

63. Possible cases =
 $2B \text{ \& } 2G = {}^6C_2 \times {}^4C_2 \text{ --- (i)}$
 $3B \text{ \& } 1G = {}^6C_3 \times {}^4C_1 \text{ --- (ii)}$
 $4B = {}^6C_4 \text{ --- (iii)}$
 Adding (i), (ii), (iii)
 $90 + 80 + 15 = 185$
64. We need to find out no. of students who take at least one of 3 subjects & subtract from 120.
 $A \cup B \cup C = A + B + C - (A \cap B + B \cap C + C \cap A) + (A \cap B \cap C)$
 $= 60 + 24 + 17 - (A \cap B + B \cap C + C \cap A) + (A \cap B \cap C)$
 $A \cap B = ?$
 $10^{\text{th}}, 20^{\text{th}}, 30^{\text{th}}$, no. of students opted both physics & chemistry
 $= 120 / 10 = 12$
 $C \cap A = \frac{120}{14} = 8 \quad B \cap C = \frac{120}{35} = 3$
 $A \cap B \cap C = \frac{120}{70} = 1$
 $A \cup B \cup C = 60 + 24 + 17 - (12 + 3 + 8) + 1 = 79$
 None of 3 subjects opted by students = $120 - 79 = 41$.
65. Required ratio =
 $(272 + 240 + 236 + 256 + 288) : (280 + 179 + 148 + 160 + 193)$
 $= 1292 : 960 = 323 : 240$