Precision Control of an Autonomous Surface Vessel

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Agenda

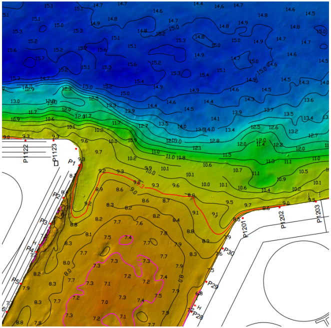
- **Introduction**
  - **Use Case**
- **System Description**
- **Model**
  - **Reference Frames**
  - **Model Equations**
  - **Model Verification**
- Control Approach
- Sensor Fusion
- Inner Controller
- Outer Controller
- Results
- Conclusion

Introduction

- Applications of an Autonomous Surface Vessel (ASV)
- Bathymetric Measurements
- Control of an ASV

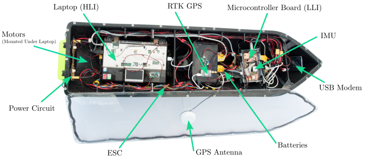
Introduction

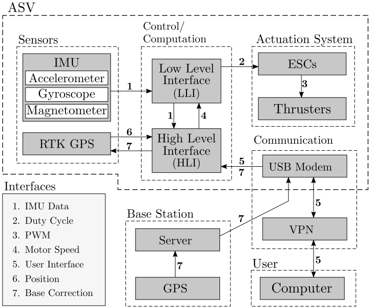
Use Case



- Depth map used by Port of Aalborg
- Problem: No recent knowledge of depths of the port
- Solution: Automate smaller unmanned vessel

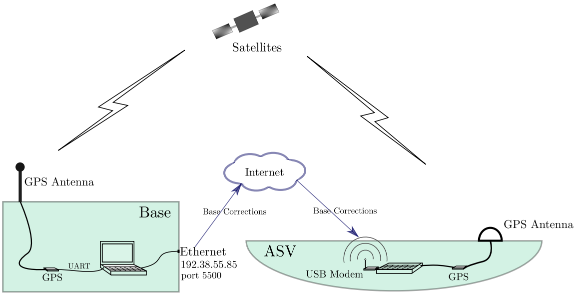
System Description

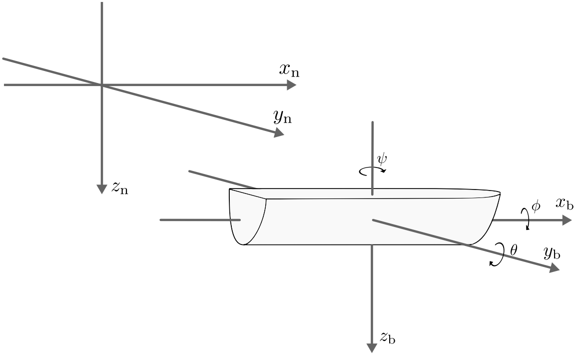




System Description

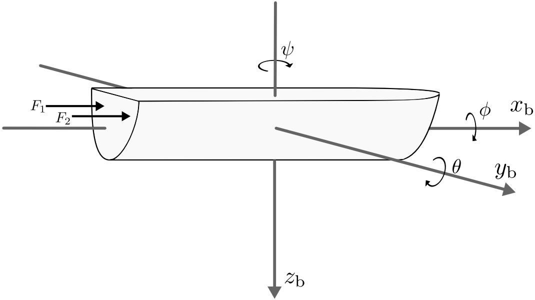
RTK GPS

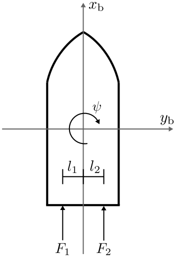




- Inertial Frame
- Body Frame

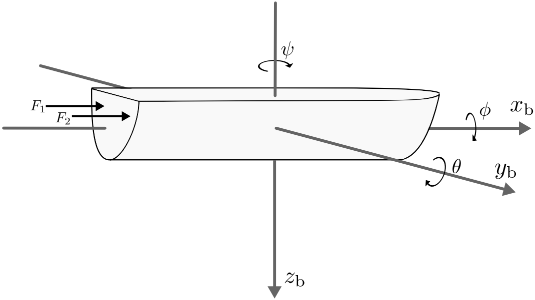
Model
Model Dynamics

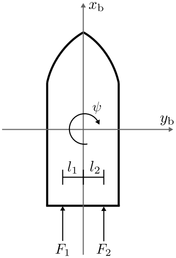




- Rigid Body Dynamics
- Hydrostatics
- Hydrodynamics

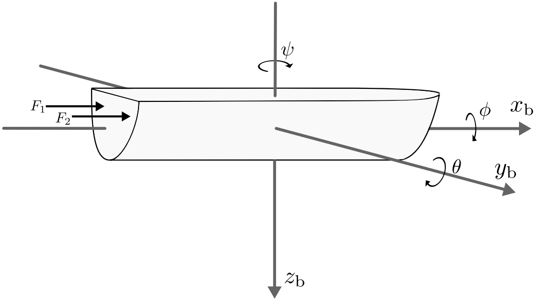
Model
Rigid Body Dynamics

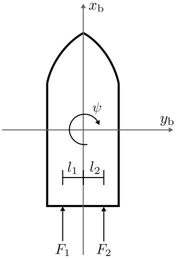




$$\sum F = m\ddot{x}$$

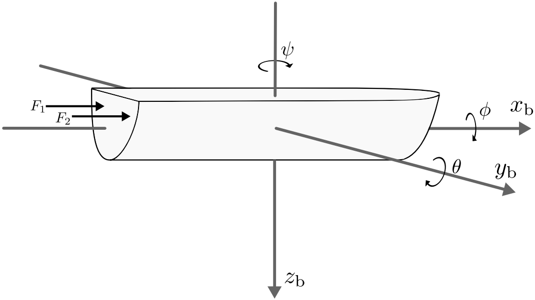
$$\sum \tau = I\ddot{\theta}$$

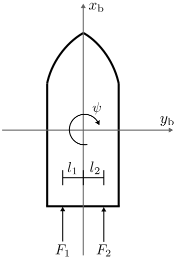




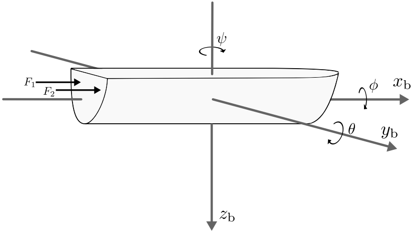
- Buoyancy Force

Model
Hydrodynamics



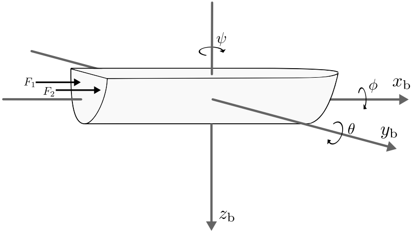


- Added mass
- Viscous Damping



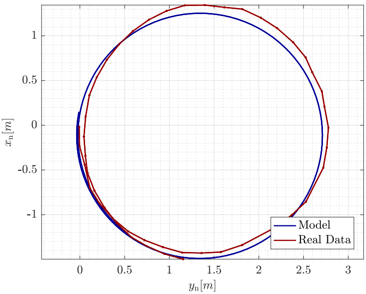
$$
\begin{aligned}
m\ddot{x}_\mathrm{b} &= F_1 + F_2 - d_{\dot{x}_\mathrm{b}}\dot{x}_\mathrm{b} + F_{x_\mathrm{b}} \\
m\ddot{y}_\mathrm{b} &= -d_{\dot{y}_\mathrm{b}}\dot{y}_\mathrm{b} + F_{y_\mathrm{b}} \\
m\ddot{z}_\mathrm{b} &= -d_{\dot{z}_\mathrm{b}}\dot{z}_\mathrm{b} + F_{z_\mathrm{b}} \\
I_\mathrm{x}\ddot{\phi} &= -d_{\dot{\phi}}\dot{\phi} + T_\phi \\
I_\mathrm{y}\ddot{\theta} &= -d_{\dot{\theta}}\dot{\theta} + T_\theta \\
I_\mathrm{z}\ddot{\psi} &= F_1 l_1 - F_2 l_2 - d_{\dot{\psi}}\dot{\psi}
\end{aligned}
$$

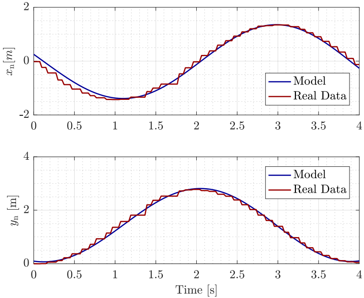
Model
Linearized Model Equations



$$
\begin{aligned}
m\ddot{x}_b &= F_1 + F_2 - d_{\dot{x}_b}\dot{x}_b \\
m\ddot{y}_b &= -d_{\dot{y}_b}\dot{y}_b \\
m\ddot{z}_b &= -d_{\dot{z}_b}\dot{z}_b - \rho g A_{wp}\tilde{z}_n \\
I_x\ddot{\phi} &= -d_{\dot{\phi}}\dot{\phi} - \rho g V\overline{GM_T}\cdot\phi \\
I_y\ddot{\theta} &= -d_{\dot{\theta}}\dot{\theta} - \rho g V\overline{GM_L}\cdot\theta \\
I_z\ddot{\psi} &= F_1 l_1 - F_2 l_2 - d_{\dot{\psi}}\dot{\psi}
\end{aligned}
$$

- Verified Nonlinear Model





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- Introduction
- System Description
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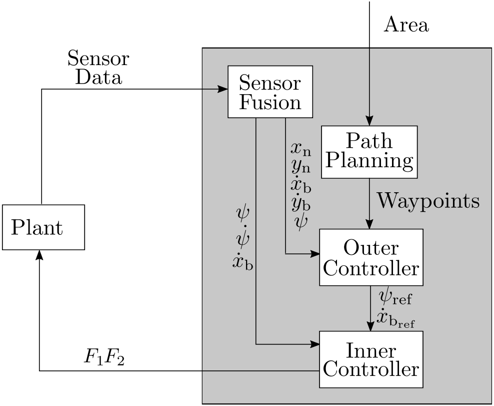
- **Control Approach**
- **Sensor Fusion**
    - **Attitude Kalman Filter**
    - **Position Kalman Filter**
- Inner Controller
- Outer Controller
- Results
- Conclusion

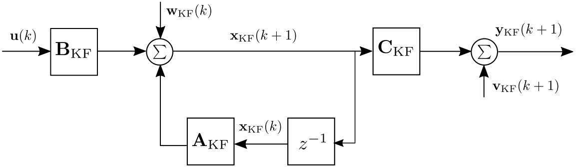
Control Approach



Sensor Fusion
Structure

- Fuses GPS and IMU data
- Achieved using a Kalman filter
- Sensor fusion contains
  - Attitude
  - Position

$$\mathbf{x}_{\mathrm{KF}}(k+1) = \mathbf{A}\mathbf{x}_{\mathrm{KF}}(k) + \mathbf{B}_{\mathrm{KF}}\mathbf{u}(k) + \mathbf{w}_{\mathrm{KF}}(k)$$
$$\mathbf{y}_{\mathrm{KF}}(k) = \mathbf{C}_{\mathrm{KF}}\mathbf{x}_{\mathrm{KF}}(k) + \mathbf{v}_{\mathrm{KF}}(k)$$



- w(k) and v(k) are assumed white Gaussian
- Matrices $\mathbf{Q}_{\mathrm{KF}}$ and $\mathbf{R}_{\mathrm{KF}}$ contain the respective covariances

- Attitude

$$\mathbf{x}_{\mathrm{att}} = \begin{bmatrix} \phi & \theta & \psi & \dot{\phi} & \dot{\theta} & \dot{\psi} & \ddot{\phi} & \ddot{\theta} & \ddot{\psi} \end{bmatrix}^{\mathrm{T}}$$

$$\mathbf{y}_{\mathrm{att}} = \begin{bmatrix} \phi_{\mathrm{acc}} & \theta_{\mathrm{acc}} & \psi_{\mathrm{mag}} & \dot{\phi}_{\mathrm{gyro}} & \dot{\theta}_{\mathrm{gyro}} & \dot{\psi}_{\mathrm{gyro}} \end{bmatrix}^{\mathrm{T}}$$

- Position

$$\mathbf{x}_{\mathrm{pos}} = \begin{bmatrix} x_{\mathrm{n}} & y_{\mathrm{n}} & \dot{x}_{\mathrm{b}} & \dot{y}_{\mathrm{b}} & \ddot{x}_{\mathrm{b}} & \ddot{y}_{\mathrm{b}} \end{bmatrix}^{\mathrm{T}}$$

$$\mathbf{y}_{\mathrm{pos}} = \begin{bmatrix} x_{\mathrm{n,GPS}} & y_{\mathrm{n,GPS}} & \ddot{x}_{\mathrm{b,acc}} & \ddot{y}_{\mathrm{b,acc}} \end{bmatrix}^{\mathrm{T}}$$

- Step 0: Initialization

$$\hat{\mathbf{x}}_{\mathrm{KF}}(0|0) = \mathbf{0}$$
$$\mathbf{P}_{\mathrm{KF}}(0|0) = \mathbf{Q}_{\mathrm{KF}}$$

- Step 1: Prediction
- Step 2: Update

- Step 0: Initialization
- Step 1: Prediction

$$\hat{\mathbf{x}}_{\mathrm{KF}}(k+1|k) = \mathbf{A}_{\mathrm{KF}}\hat{\mathbf{x}}_{\mathrm{KF}}(k|k) + \mathbf{B}_{\mathrm{KF}}\mathbf{u}(k)$$

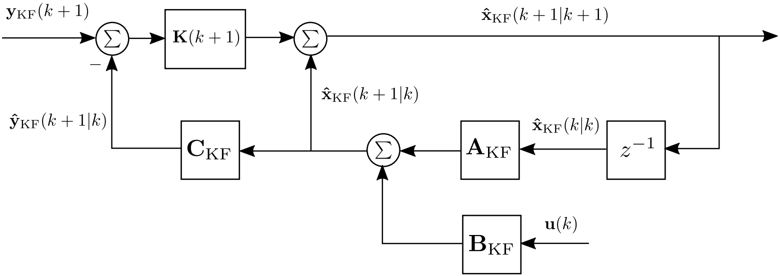
$$\mathbf{P}(k+1|k) = \mathbf{A}_{\mathrm{KF}}\mathbf{P}(k|k)\mathbf{A}_{\mathrm{KF}}^{\mathrm{T}} + \mathbf{Q}_{\mathrm{KF}}$$

- Step 2: Update

$$\hat{\mathbf{x}}_{\mathrm{KF}}(k+1|k+1) = \hat{\mathbf{x}}_{\mathrm{KF}}(k+1|k) + \mathbf{K}(k+1)\left[\mathbf{y}_{\mathrm{KF}}(k+1) - \mathbf{C}_{\mathrm{KF}}\hat{\mathbf{x}}_{\mathrm{KF}}(k+1|k)\right]$$

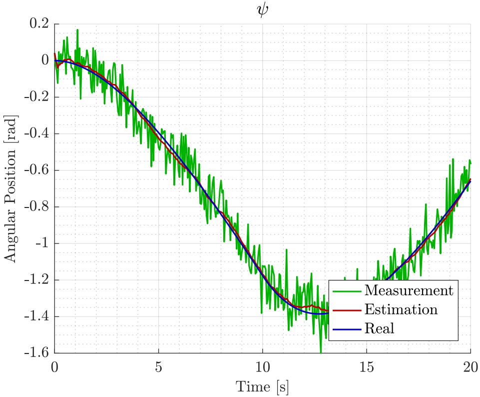
$$\mathbf{P}(k+1|k+1) = \left[\mathbf{I} - \mathbf{K}(k+1)\mathbf{C}_{\mathrm{KF}}^{\mathrm{T}}\right]\mathbf{P}(k+1|k)$$

$$\mathbf{K}(k+1) = \mathbf{P}(k+1|k)\mathbf{C}_{\mathrm{KF}}^{\mathrm{T}}\left[\mathbf{C}_{\mathrm{KF}}\mathbf{P}(k+1|k)\mathbf{C}_{\mathrm{KF}}^{\mathrm{T}} + \mathbf{R}_{\mathrm{KF}}\right]^{-1}$$



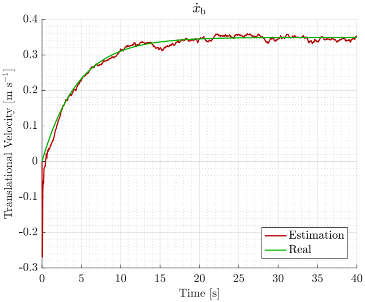
$\mathbf{y}_{\mathrm{KF}}(k+1)$
$\sum$
$-$
$\mathbf{K}(k+1)$
$\sum$
$\hat{\mathbf{x}}_{\mathrm{KF}}(k+1|k+1)$
$\hat{\mathbf{x}}_{\mathrm{KF}}(k+1|k)$
$\hat{\mathbf{y}}_{\mathrm{KF}}(k+1|k)$
$\mathbf{C}_{\mathrm{KF}}$
$\sum$
$\mathbf{A}_{\mathrm{KF}}$
$\hat{\mathbf{x}}_{\mathrm{KF}}(k|k)$
z^{-1}
$\mathbf{B}_{\mathrm{KF}}$
$\mathbf{u}(k)$

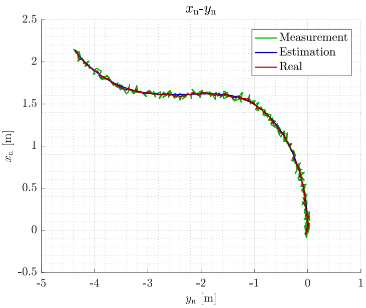
Sensor Fusion
Attitude Kalman Filter



Sensor Fusion

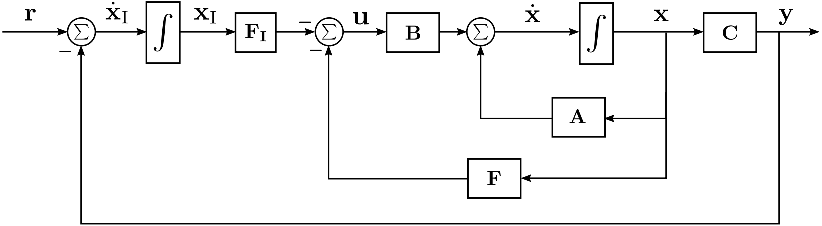
Position Kalman Filter



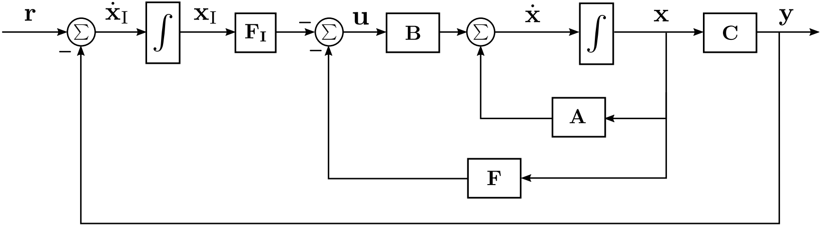


Agenda

Inner Controller



Inner Controller

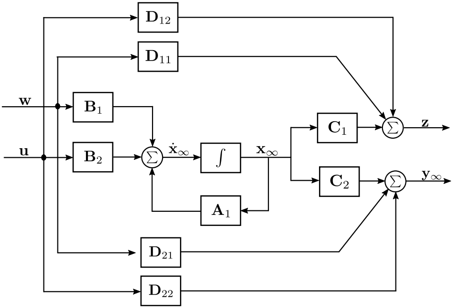


- $\mathcal{H}_\infty$ Controller
- Linear Quadratic Regulator

- Suboptimal $\mathcal{H}_\infty$ controller

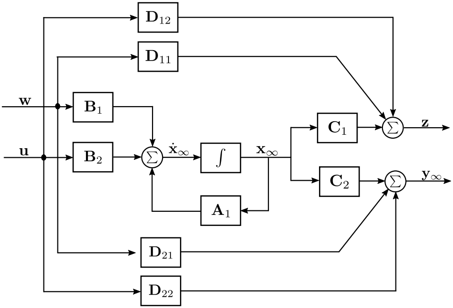
Find an internally stabilizing controller that provides a closed loop $\mathcal{H}_\infty$ norm less than some bound γ

- System structure



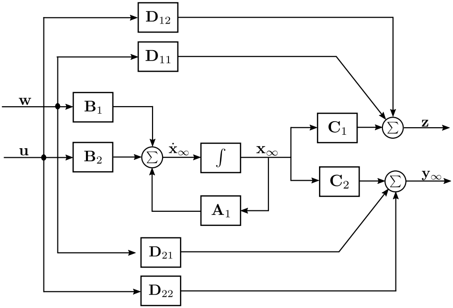
$$
\begin{aligned}
\dot{\mathbf{x}}_\infty(t) &= \mathbf{A}_1\mathbf{x}_\infty(t) + \mathbf{B}_1\mathbf{w}(t) + \mathbf{B}_2\mathbf{u}(t) \\
\mathbf{z}(t) &= \mathbf{C}_1\mathbf{x}_\infty(t) + \mathbf{D}_{11}\mathbf{w}(t) + \mathbf{D}_{12}\mathbf{u}(t) \\
\mathbf{y}_\infty(t) &= \mathbf{C}_2\mathbf{x}_\infty(t) + \mathbf{D}_{21}\mathbf{w}(t) + \mathbf{D}_{22}\mathbf{u}(t)
\end{aligned}
$$

- System structure



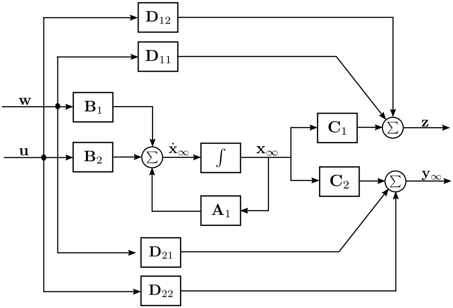
$$\mathbf{u}(t) = \begin{bmatrix} F_1 & F_2 \end{bmatrix}^{\mathrm{T}}$$

- System structure



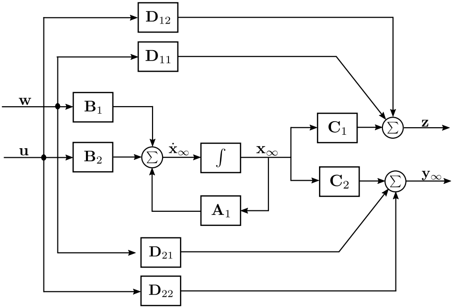
$$\mathbf{w}(t) = \begin{bmatrix} \psi_{\mathrm{ref}} & \dot{x}_{\mathrm{b,ref}} & F_{\mathrm{wc}} & \tau_{\mathrm{wc}} & F_{\mathrm{wave}} & \tau_{\mathrm{wave}} & n_\psi & n_{\dot{x}_\mathrm{b}} \end{bmatrix}^\mathrm{T}$$

- System structure



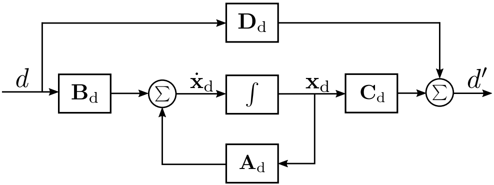
$$\mathbf{y}_\infty(t) = \begin{bmatrix} \psi & \dot{x}_\mathrm{b} & \mathbf{x}_\mathrm{I}^\mathrm{T} \end{bmatrix}^\mathrm{T}$$

- System structure



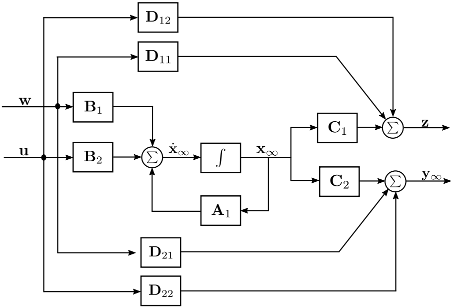
$$\mathbf{x}_\infty(t) = \begin{bmatrix} \psi & \dot{\psi} & \dot{x}_\mathrm{b} & x_{I_\psi} & x_{I_{\dot{x}_\mathrm{b}}} & x_{F_\mathrm{wc}} & x_{\tau_\mathrm{wc}} & x_{F_\mathrm{wave}} & x_{\tau_\mathrm{wave}} & x_{n_\psi} & x_{n_{\dot{x}_\mathrm{b}}} \end{bmatrix}^\mathrm{T}$$

- Disturbance model



$$\frac{d'}{d} = \frac{a}{s+a} \rightarrow \dot{d}' = -ad' + ad \rightarrow \begin{cases} \dot{x}_\mathrm{d} = -ax_\mathrm{d} + ad \\ d' = x_\mathrm{d} \end{cases}$$

- System structure



$$\mathbf{z}(t) = \begin{bmatrix} \mathbf{x}_\infty^{\mathrm{T}} & \mathbf{u}^{\mathrm{T}} \end{bmatrix}^{\mathrm{T}}$$

- Controller design parameters (γ, $\mathbf{C}_1$, $\mathbf{D}_{12}$)

$$\mathbf{C}_1 = \begin{bmatrix} \mathbf{W}_\mathrm{x} & \mathbf{0}_{3x2} & \mathbf{0}_{3x2} & \mathbf{0}_{3x2} & \mathbf{0}_{3x2} \\ \mathbf{0}_{2x3} & \mathbf{W}_\mathrm{I} & \mathbf{0}_{2x2} & \mathbf{0}_{2x2} & \mathbf{0}_{2x2} \\ \mathbf{0}_{2x3} & \mathbf{0}_{2x2} & \mathbf{W}_\mathrm{wc} & \mathbf{0}_{2x2} & \mathbf{0}_{2x2} \\ \mathbf{0}_{2x3} & \mathbf{0}_{2x2} & \mathbf{0}_{2x2} & \mathbf{W}_\mathrm{wave} & \mathbf{0}_{2x2} \\ \mathbf{0}_{2x3} & \mathbf{0}_{2x2} & \mathbf{0}_{2x2} & \mathbf{0}_{2x2} & \mathbf{W}_\mathrm{noise} \\ \mathbf{0}_{2x3} & \mathbf{0}_{2x2} & \mathbf{0}_{2x2} & \mathbf{0}_{2x2} & \mathbf{0}_{2x2} \\ \mathbf{0}_{2x3} & \mathbf{0}_{2x2} & \mathbf{0}_{2x2} & \mathbf{0}_{2x2} & \mathbf{0}_{2x2} \end{bmatrix} \qquad \mathbf{D}_{12} = \begin{bmatrix} \mathbf{0}_{2x3} \\ \mathbf{0}_{2x2} \\ \mathbf{0}_{2x2} \\ \mathbf{0}_{2x2} \\ \mathbf{0}_{2x2} \\ \mathbf{W}_\mathrm{u} \end{bmatrix}$$

- Feedback gain

$$\mathbf{X}_\infty = Ric\begin{bmatrix} \mathbf{A}_1 & \gamma^{-2}\mathbf{B}_1\mathbf{B}_1^{\mathrm{T}} - \mathbf{B}_2\mathbf{B}_2^{\mathrm{T}} \\ -\mathbf{C}_1^{\mathrm{T}}\mathbf{C}_1 & -\mathbf{A}_1^{\mathrm{T}} \end{bmatrix}$$

$$\mathbf{F}_\infty = -\mathbf{B}_2^{\mathrm{T}}\mathbf{X}_\infty$$

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- **Inner Controller**
  - Robust Controller Design
  - **Linear Quadratic Regulator Design**
  - **Controllers Comparison**
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Inner Controller

Linear Quadratic Controller Design

Inner Controller
Comparison of the Controllers

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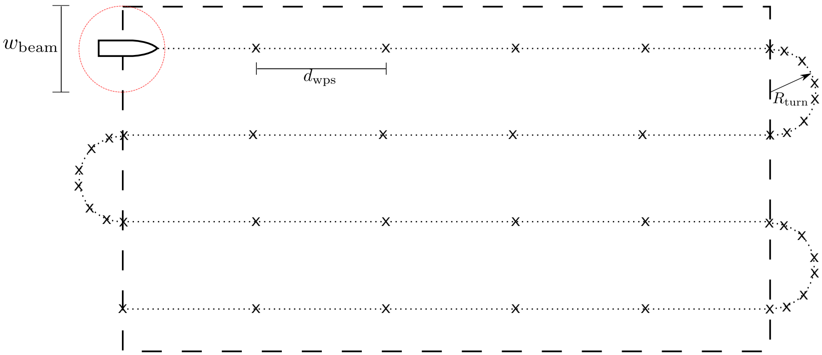
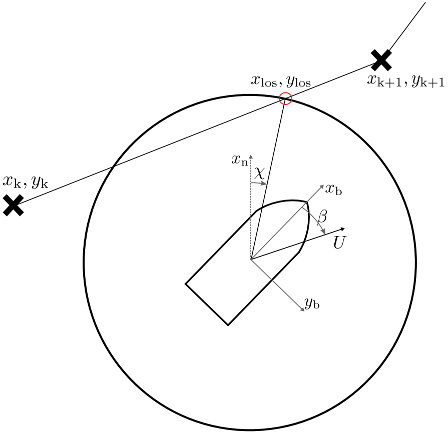
- **Outer Controller**
  - **Path Generation Algorithm**
  - **Path Following Algorithm**
- **Results**
  - **Controller Results**
  - **Implementation Results**
- **Conclusion**

Outer Controller
Path Generation Algorithm

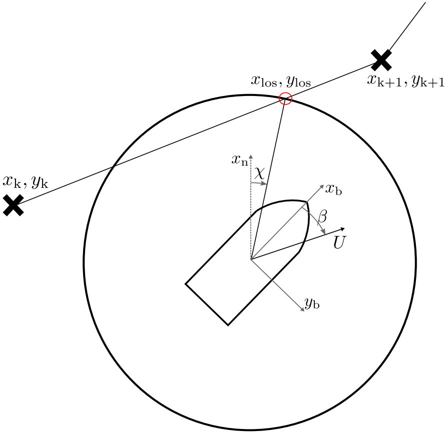


Outer Controller
Path Following Algorithm



Outer Controller

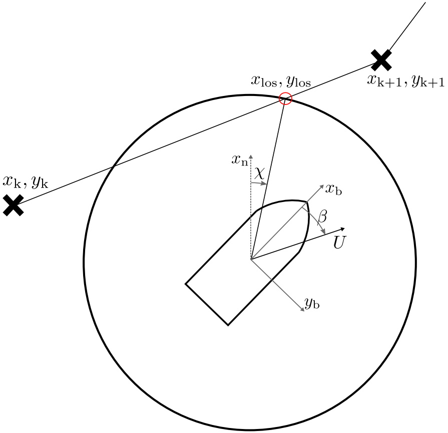
Path Following Algorithm



$$\chi = \arctan\left(\frac{y_{\mathrm{LOS}} - y_{\mathrm{n}}}{x_{\mathrm{LOS}} - x_{\mathrm{n}}}\right)$$

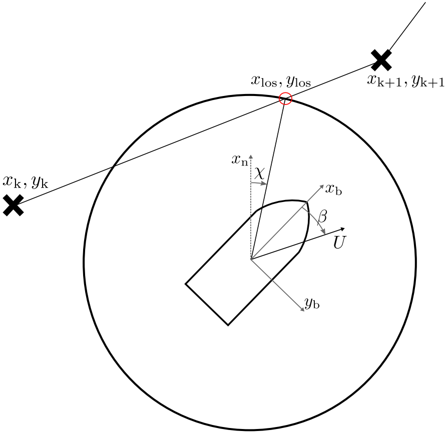
Outer Controller

Path Following Algorithm



$$\chi = \arctan\left(\frac{y_{\mathrm{LOS}} - y_{\mathrm{n}}}{x_{\mathrm{LOS}} - x_{\mathrm{n}}}\right)$$

$$\beta = \arctan\left(\frac{\dot{y}_{\mathrm{b}}}{\dot{x}_{\mathrm{b}}}\right)$$

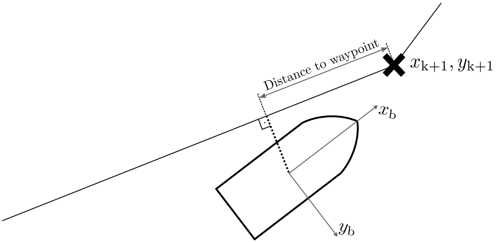


$$\chi = \arctan\left(\frac{y_{\rm LOS} - y_{\rm n}}{x_{\rm LOS} - x_{\rm n}}\right)$$

$$\beta = \arctan\left(\frac{\dot{y}_{\rm b}}{\dot{x}_{\rm b}}\right)$$

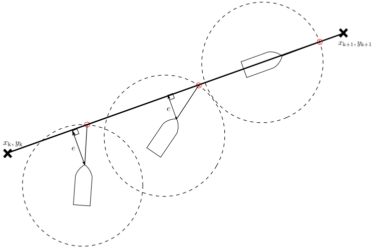
$$\psi_{\rm ref} = \chi - \beta$$

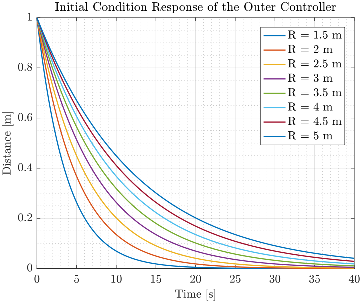
- Change active waypoints



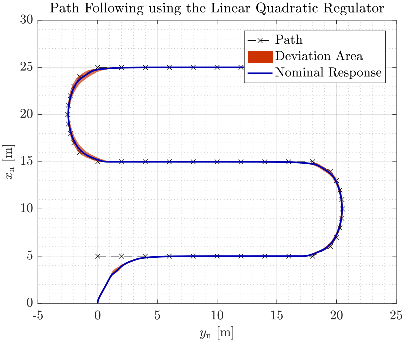
Outer Controller
Path Following Algorithm

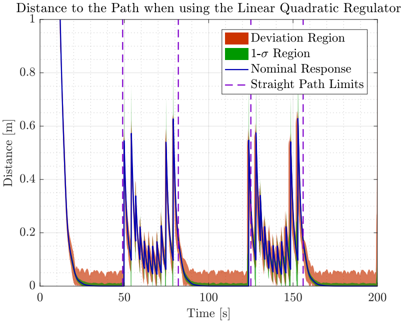
- Convergence to the path



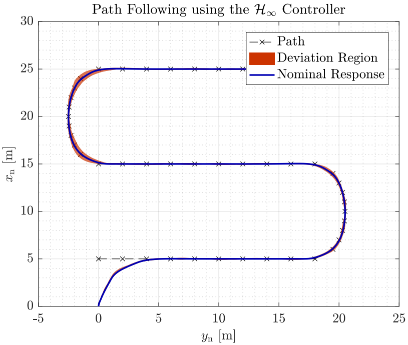


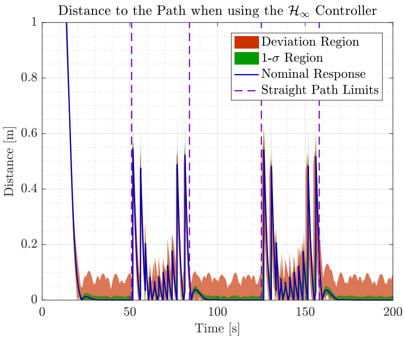
- LQR as inner controller



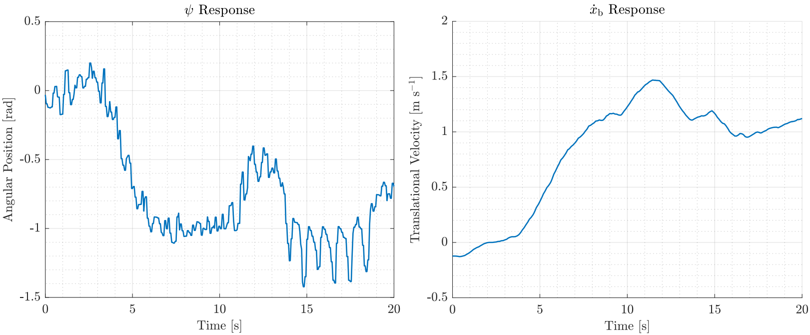


- Robust controller as inner controller





- Inner controller test



Conclusion

- The estimator has been tuned and tested through simulation.
- The controller has also been analyzed though simulations that include disturbances, noise and varying parameters.
- The simulated results have not been fully replicated in the real vessel, but they show a promising behavior of the control system.

Precision Control of an Autonomous Surface Vessel

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