

# Cosmic magnetism revealed through Faraday rotation



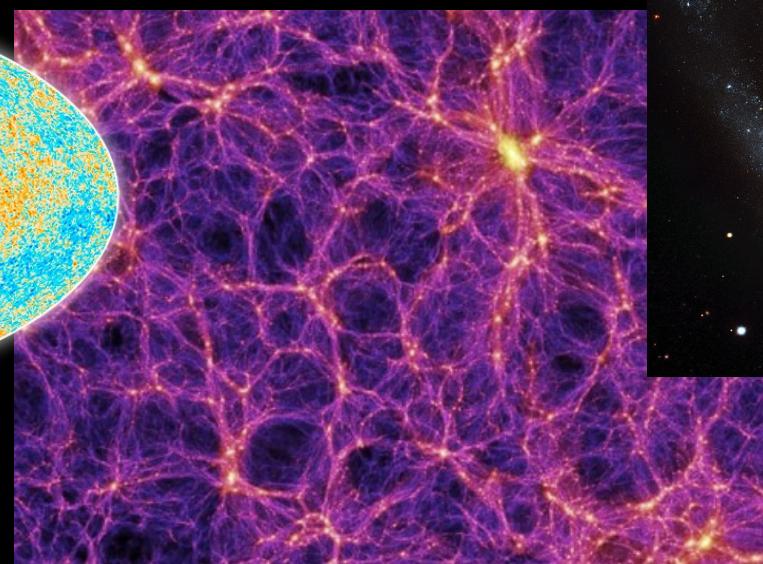
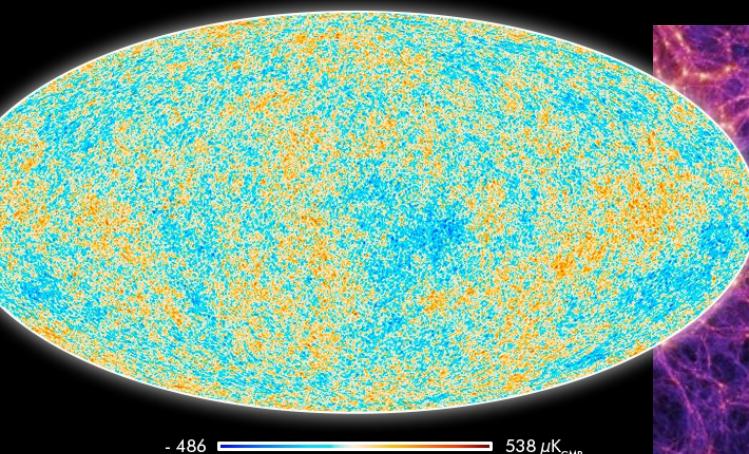
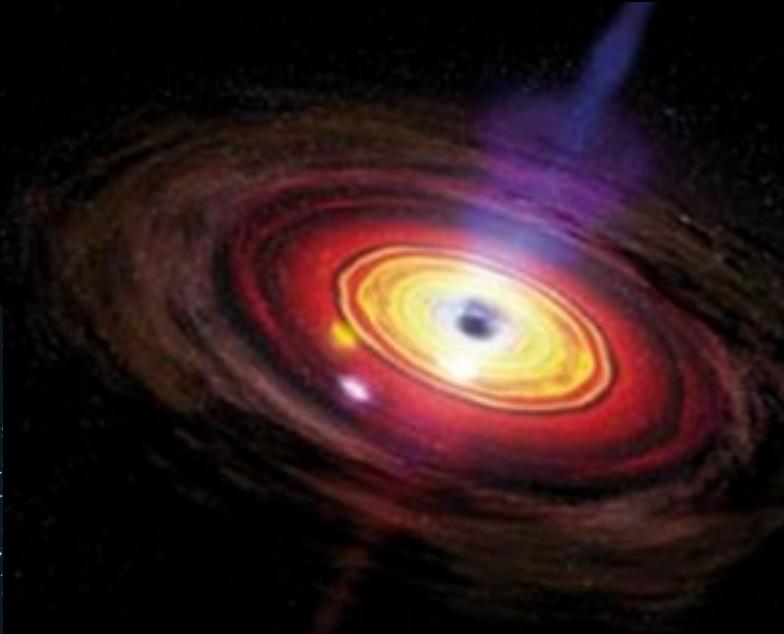
**CITA  
ICAT**

Canadian Institute for  
Theoretical Astrophysics  
L'institut Canadien  
d'astrophysique théorique

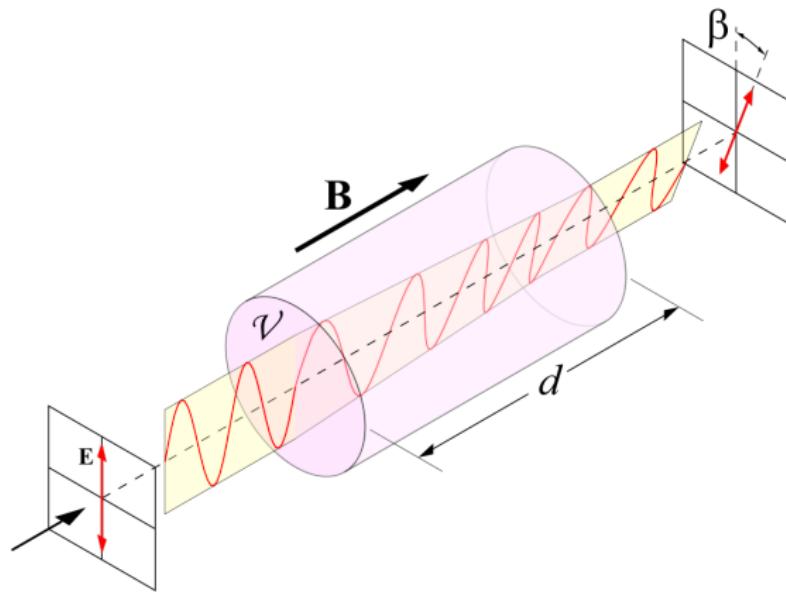
Niels Oppermann

with:

B. M. Gaensler (Toronto)  
V. Vacca, T. A. Enßlin, J. Jasche (Munich)  
J.-A. Brown, J. Stil (Calgary)  
H. Junklewitz, S. A. Mao, D. H. F. M. Schnitzeler (Bonn)  
and others



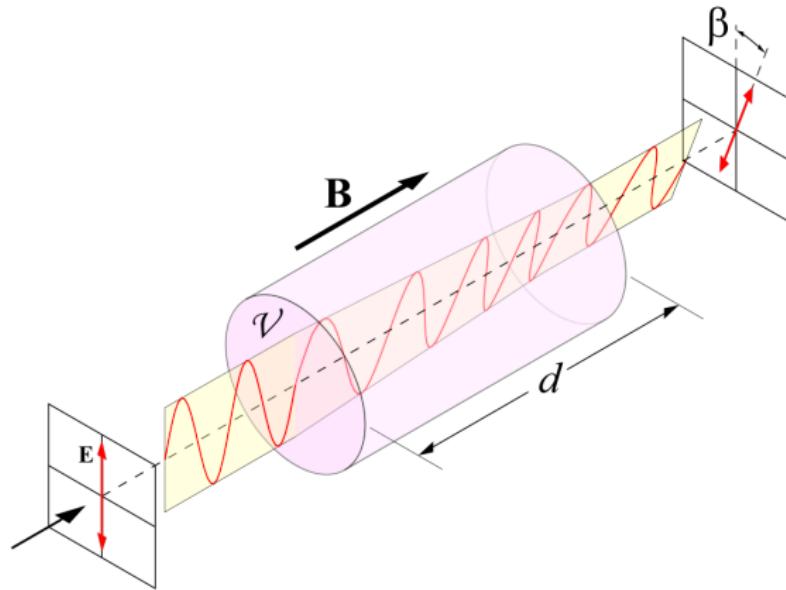
# Faraday rotation



$$d\beta \propto \lambda^2 n_e B_r dr$$

$$\Rightarrow \beta \propto \lambda^2 \int_{r_{\text{source}}}^0 (1+z)^{-2} n_e B_r dr$$

# Faraday rotation

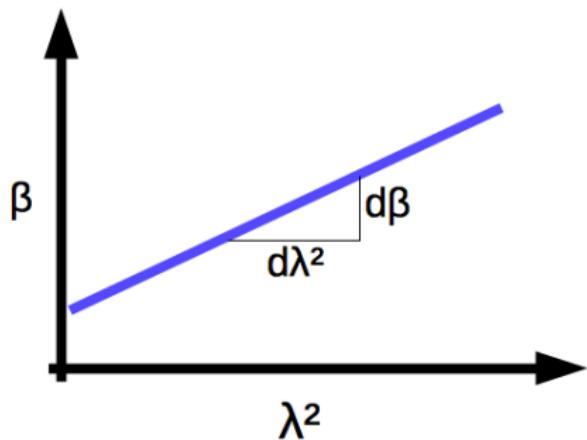


$$\text{Faraday depth: } \phi \propto \int_{r_{\text{source}}}^0 (1+z)^{-2} n_e B_r dr$$

$$\beta = \phi \lambda^2$$

## Faraday rotation

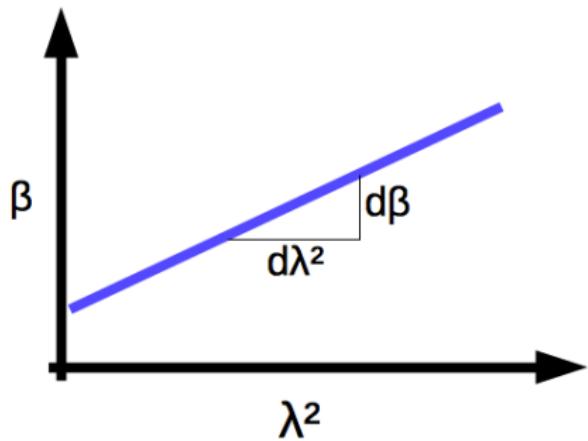
if B-fields in front of emission:



$$\phi = RM = \frac{d\beta}{d\lambda^2}$$

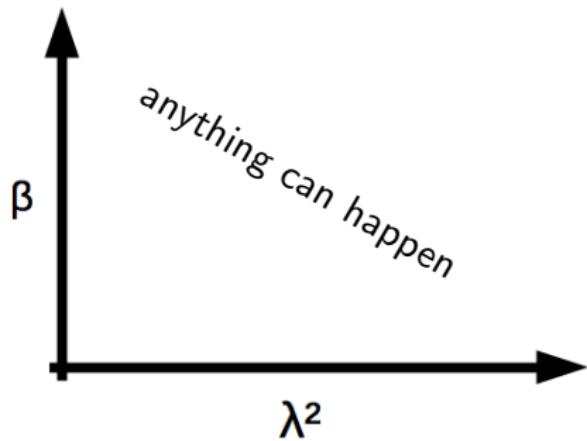
# Faraday rotation

if B-fields in front of emission:

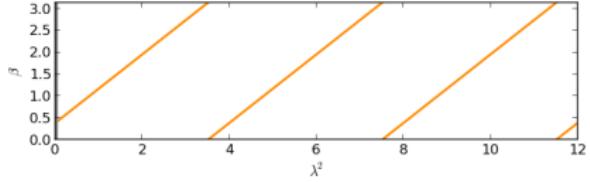
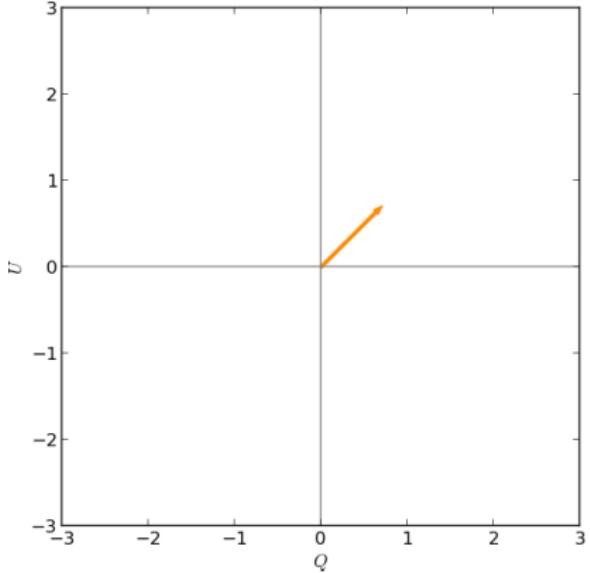
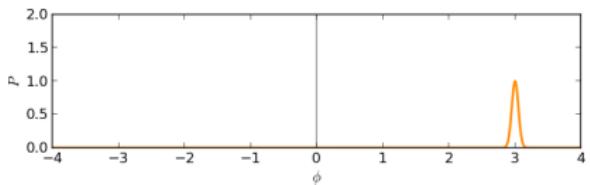
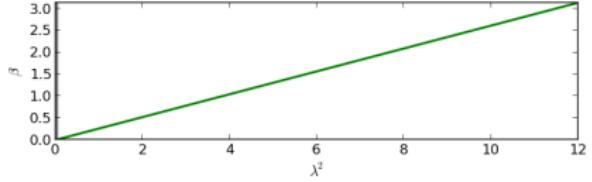
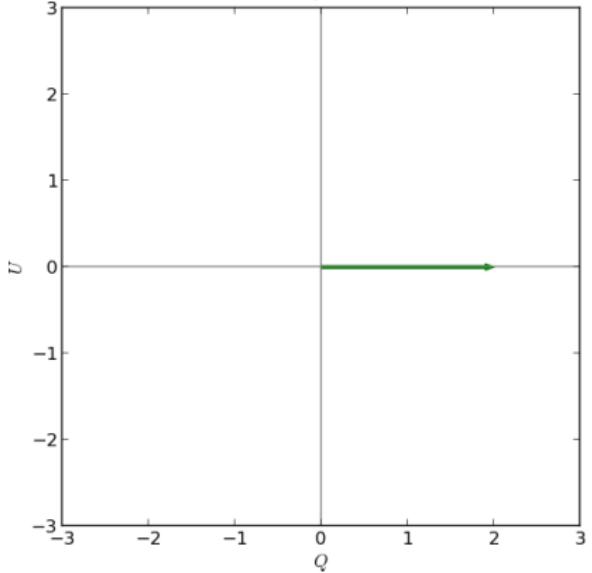
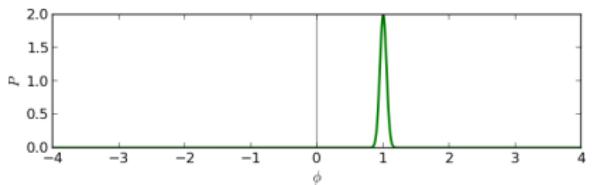


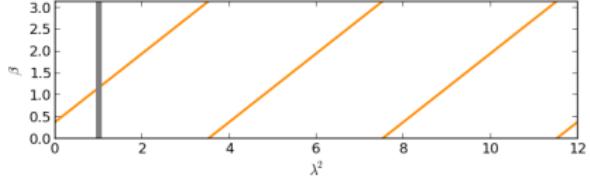
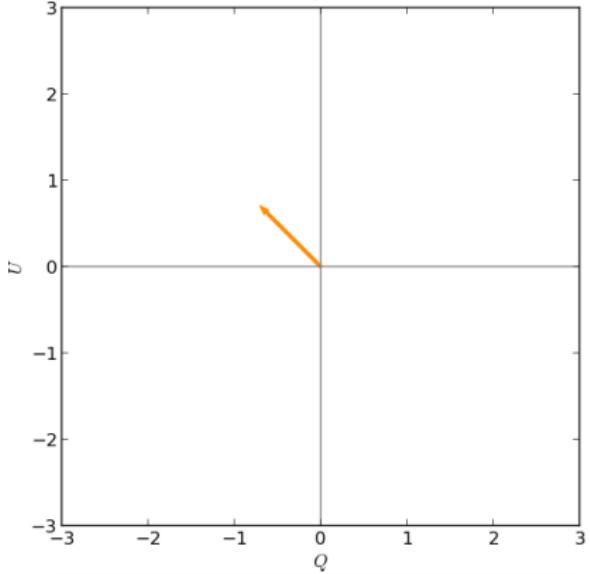
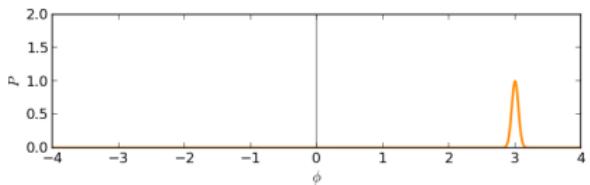
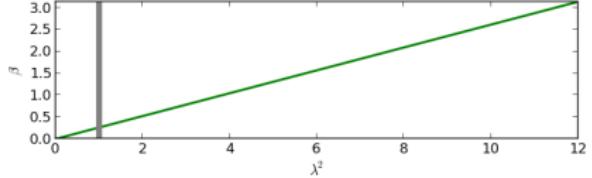
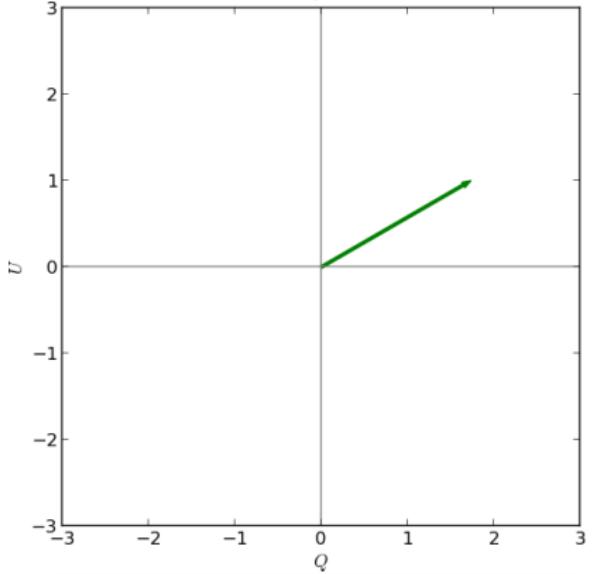
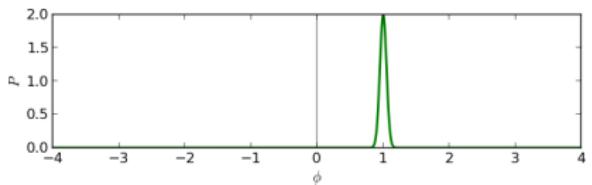
$$\phi = \text{RM} = \frac{d\beta}{d\lambda^2}$$

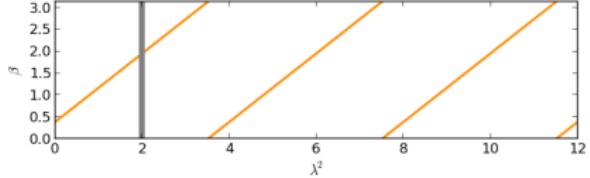
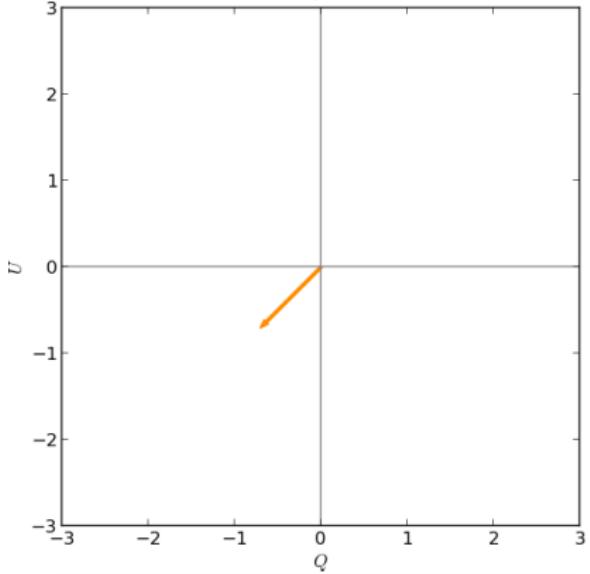
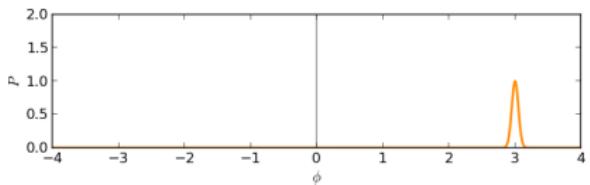
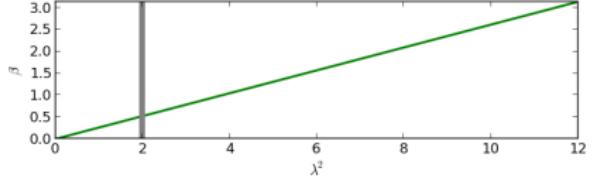
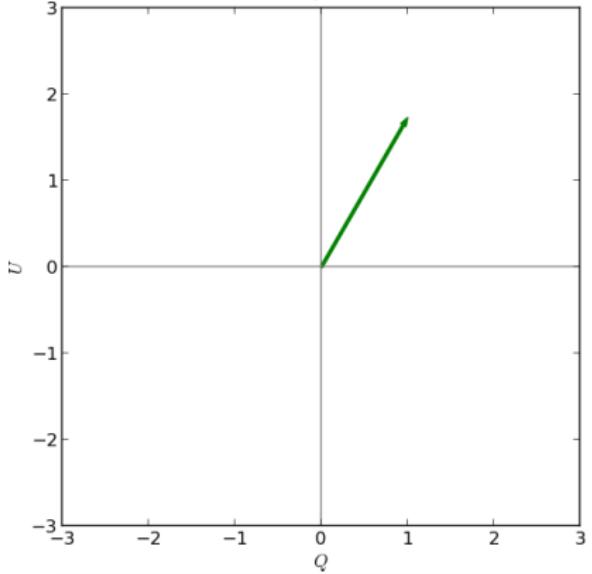
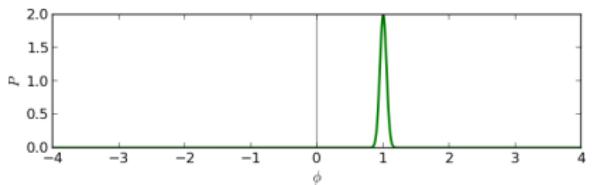
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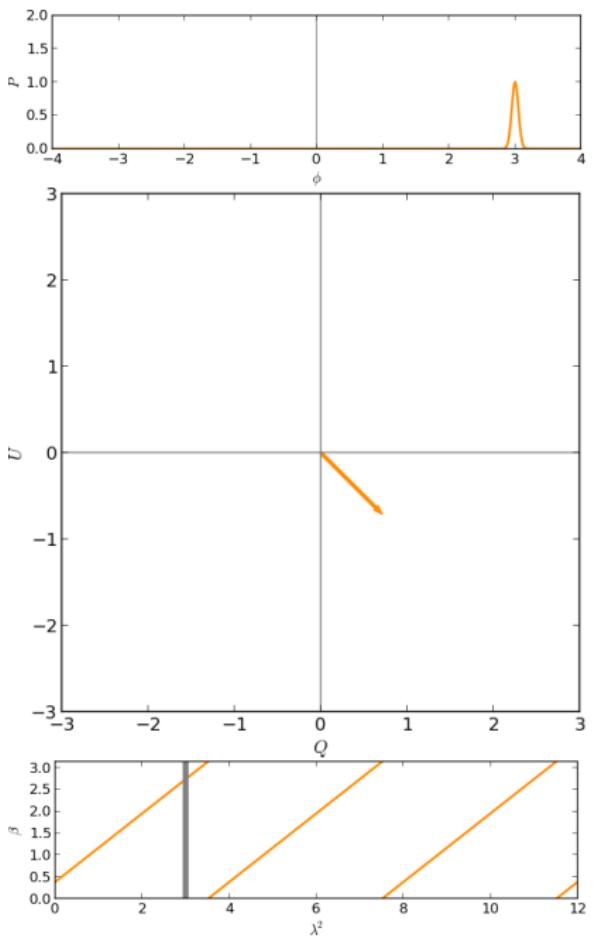
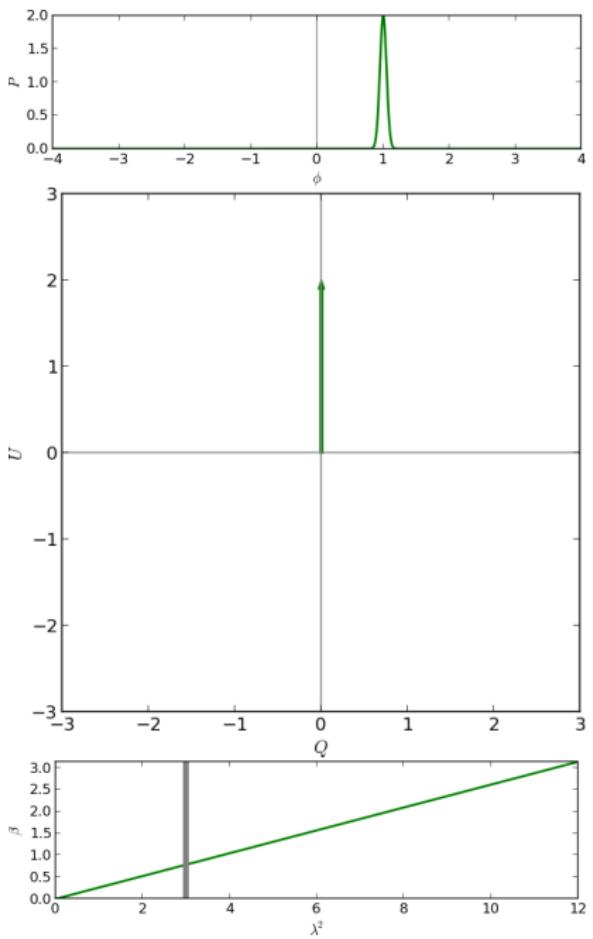


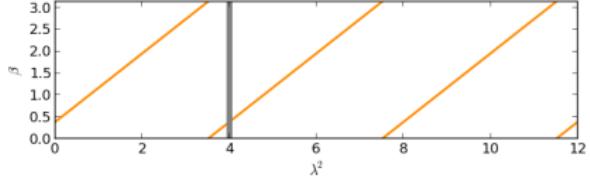
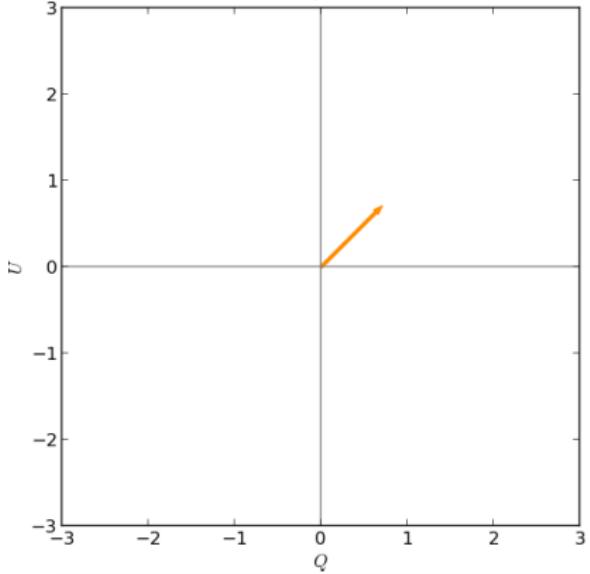
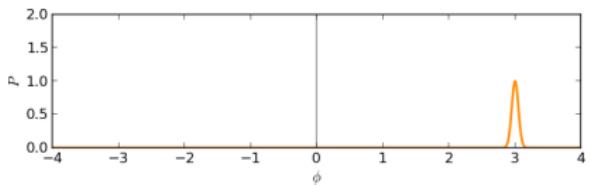
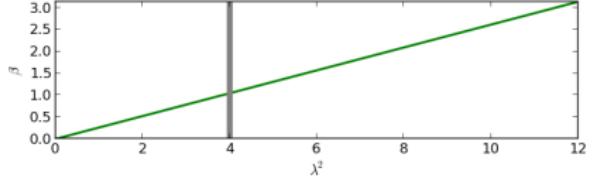
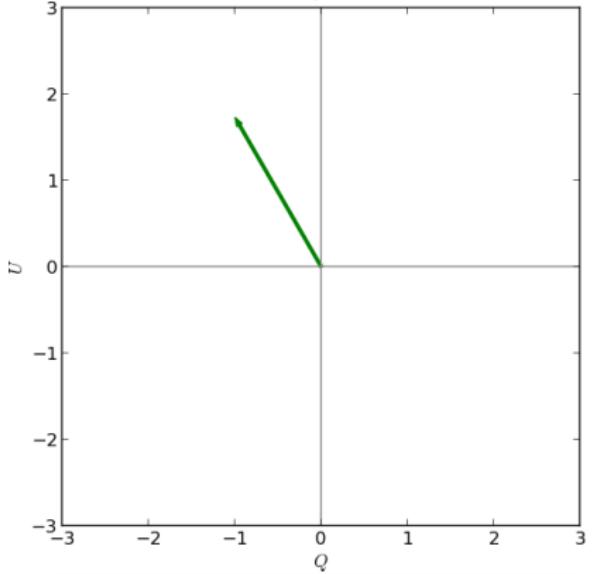
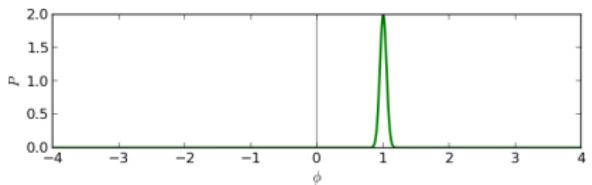
Use  $Q(\lambda)$ ,  $U(\lambda)$ ,  $I(\lambda)$ ,  
RM synthesis, . . .

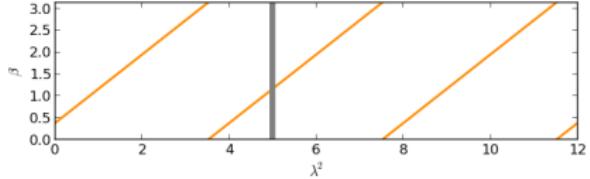
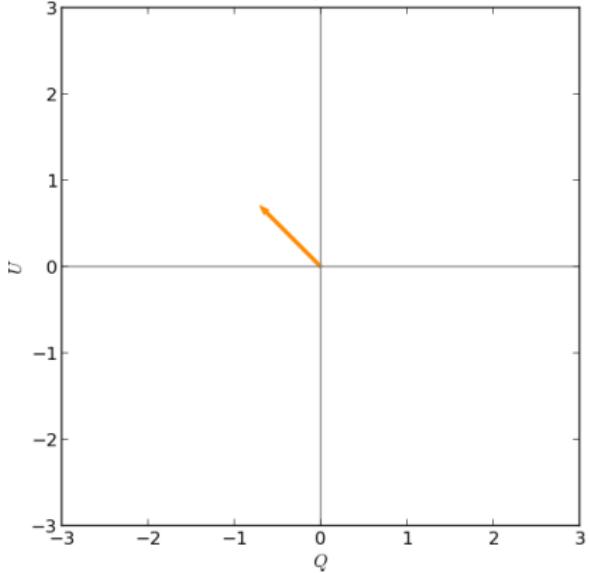
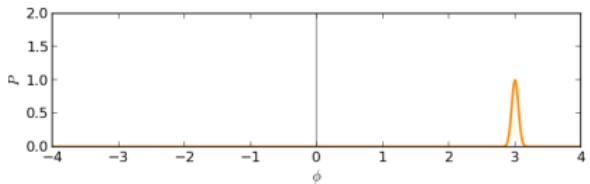
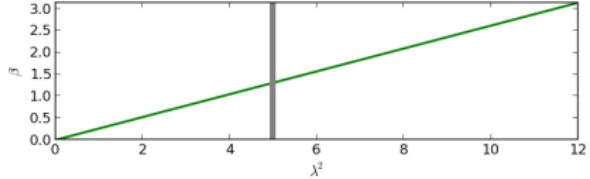
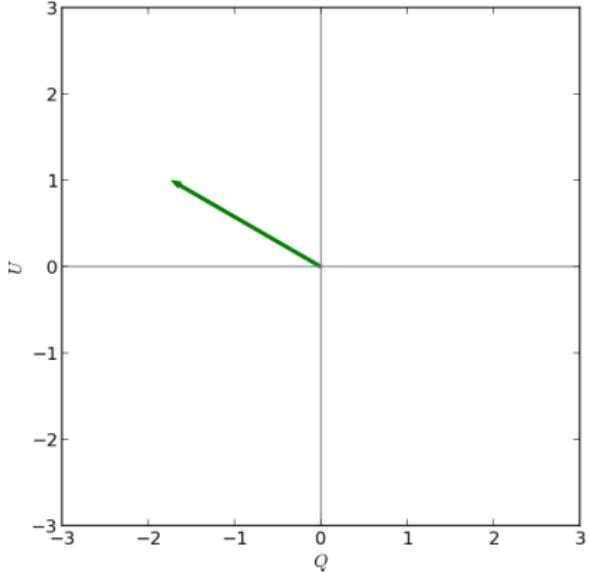
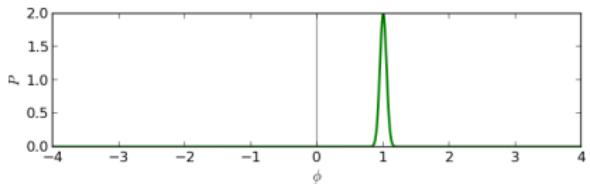


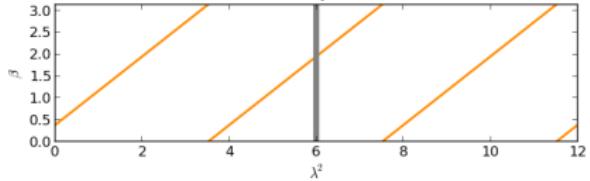
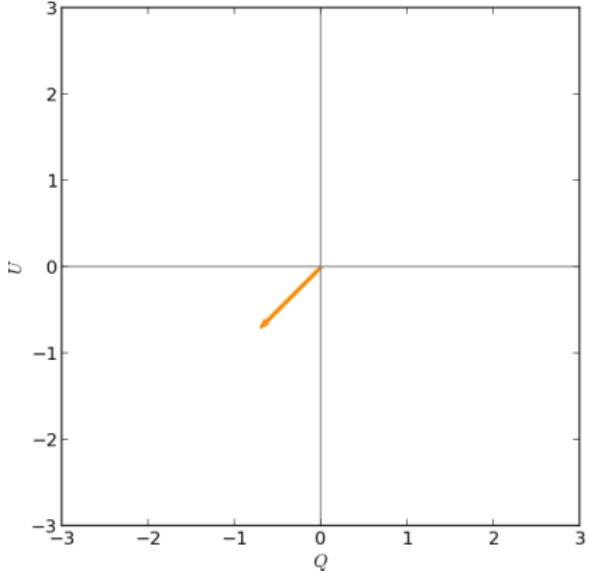
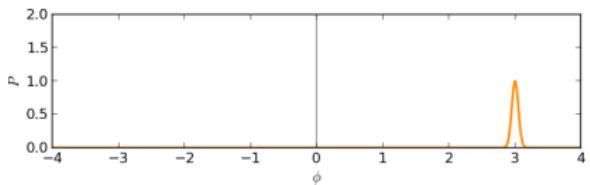
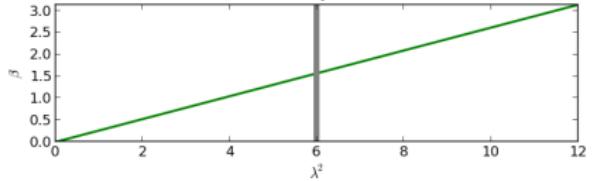
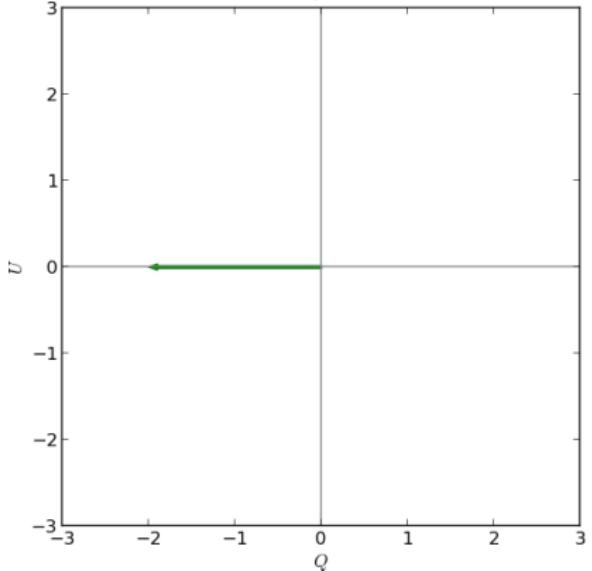
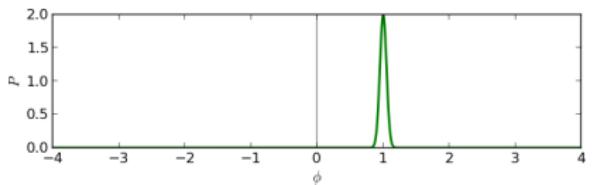


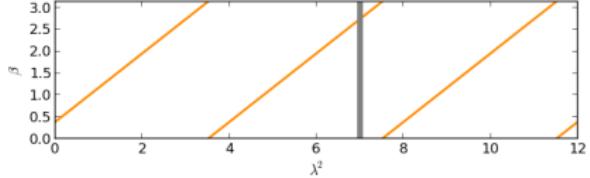
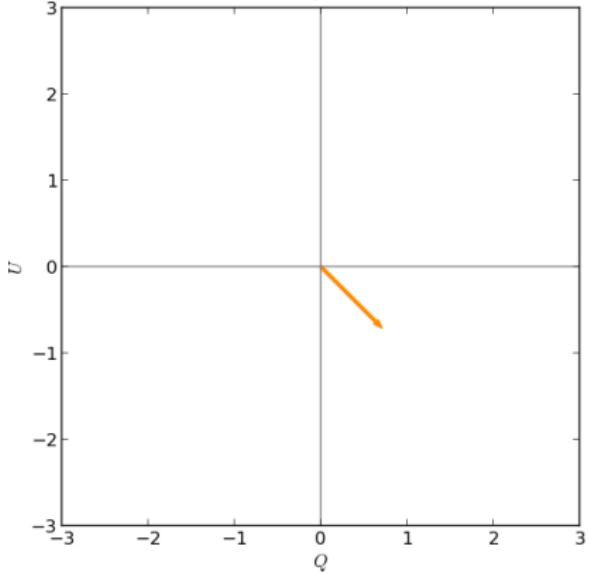
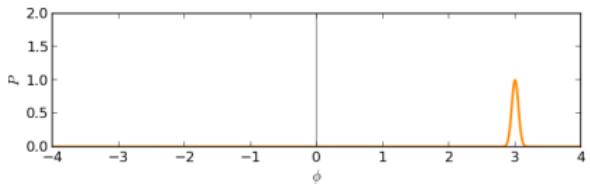
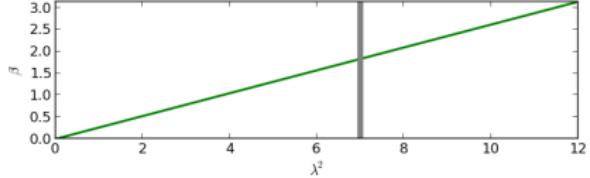
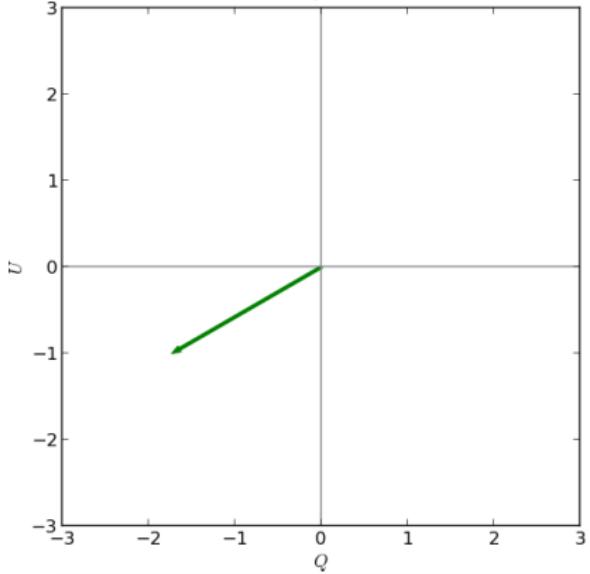
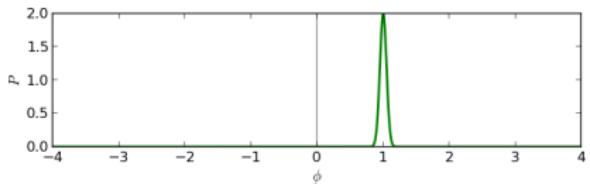


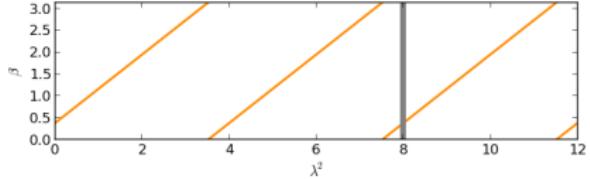
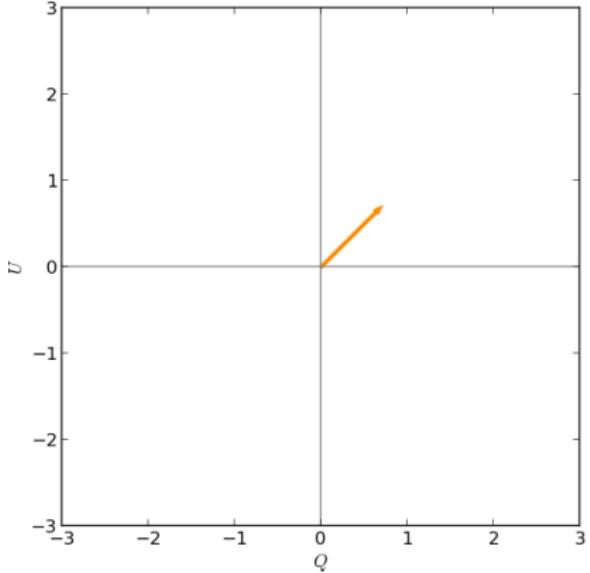
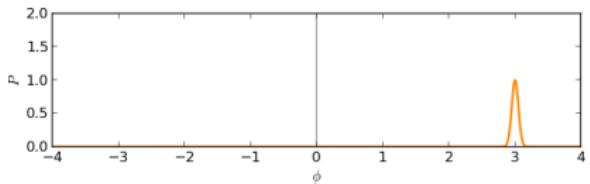
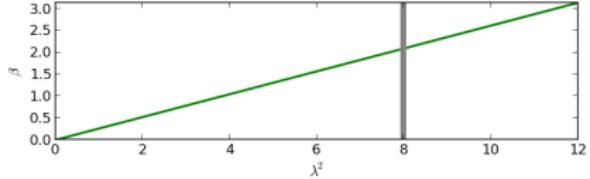
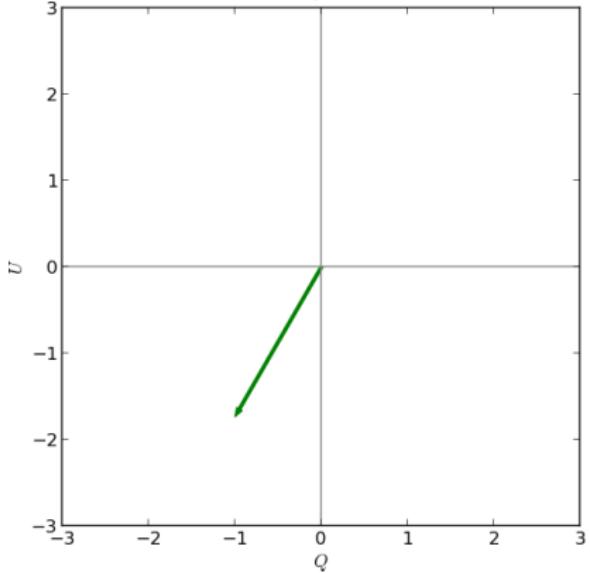
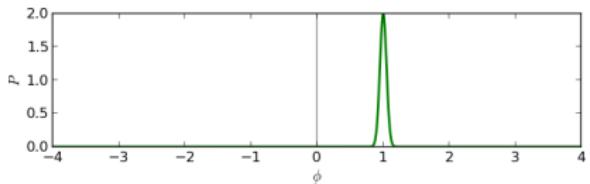


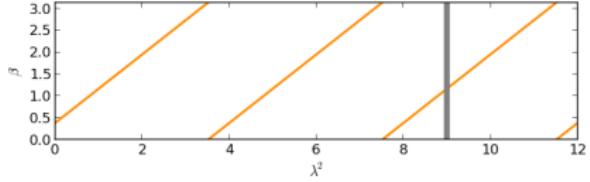
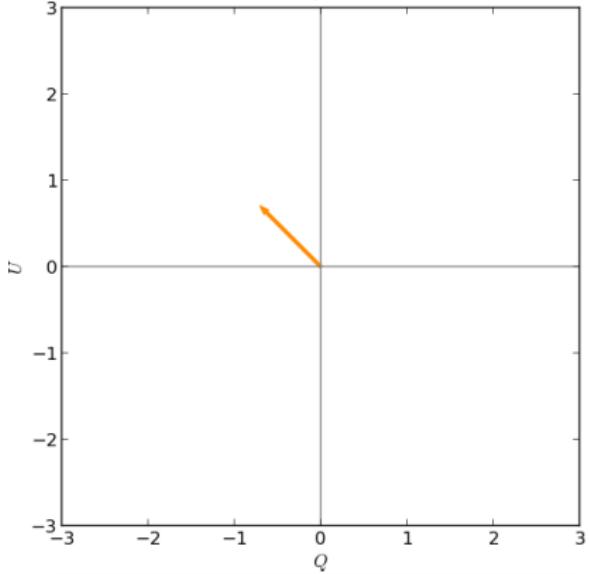
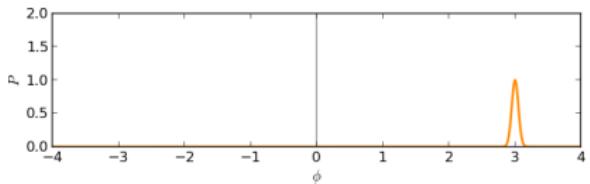
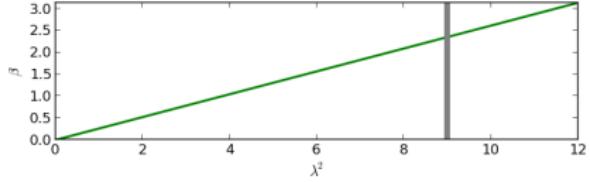
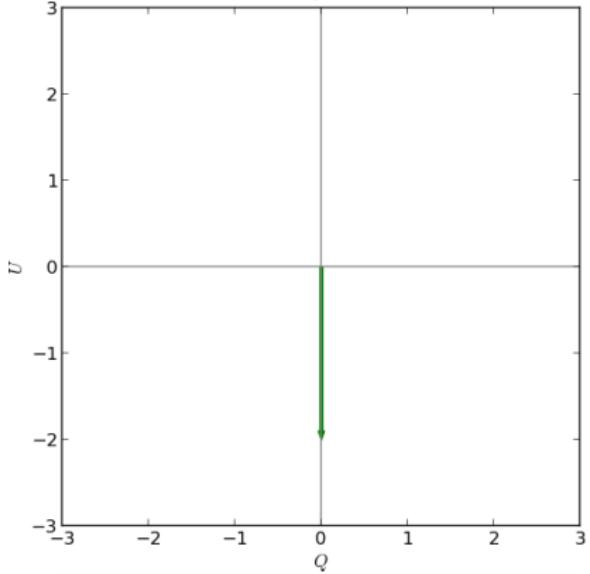
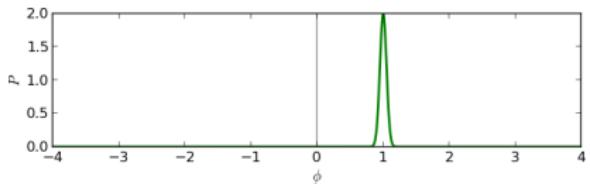


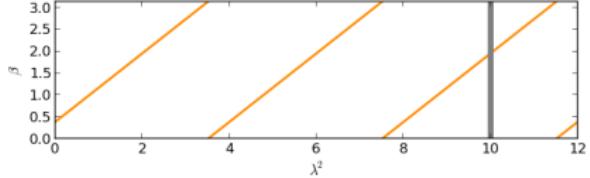
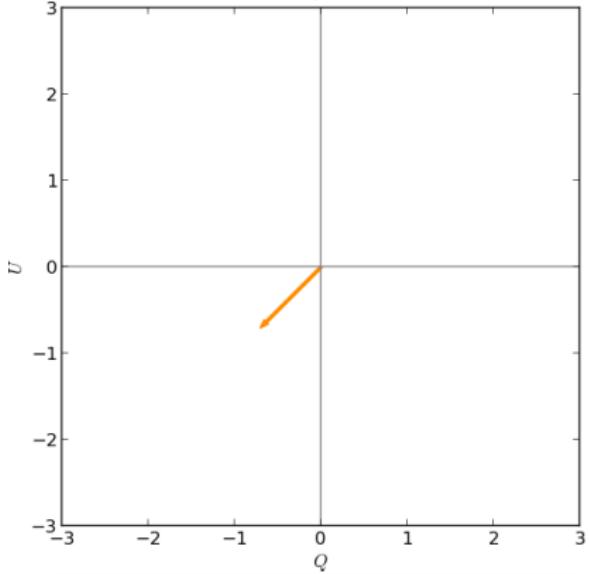
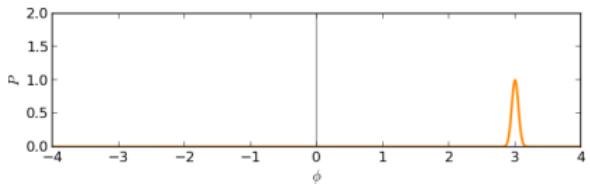
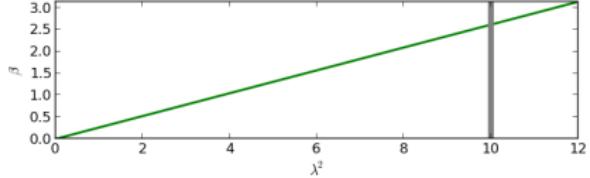
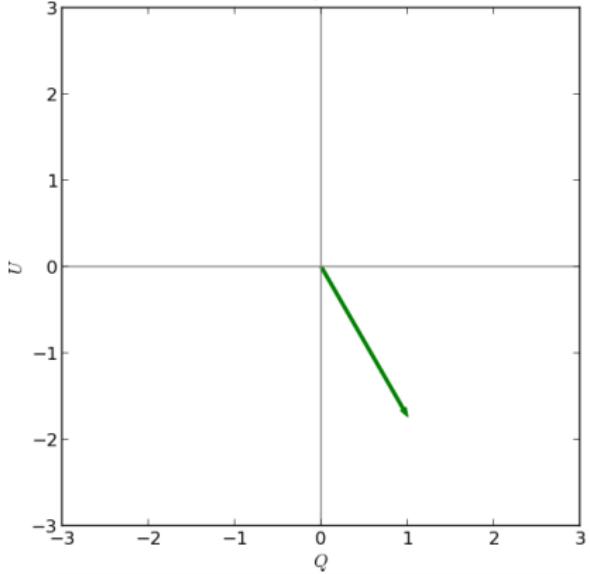
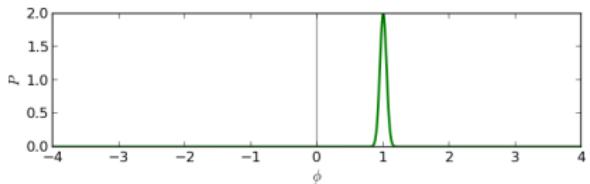


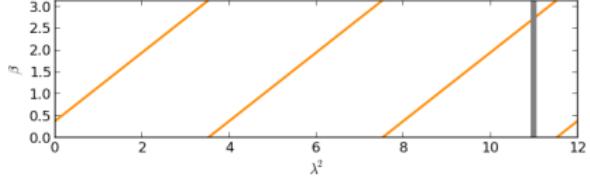
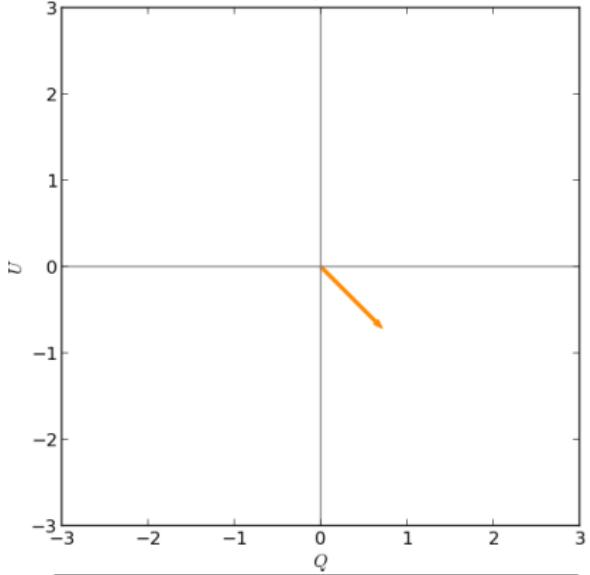
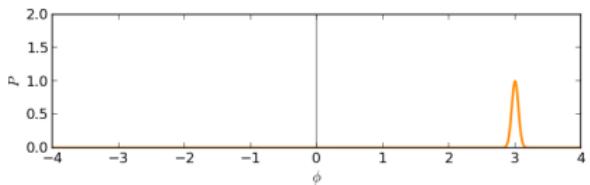
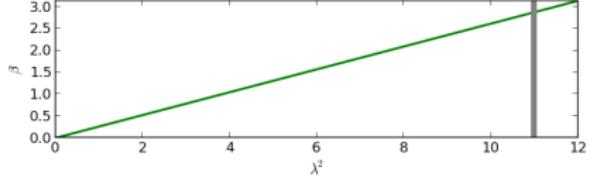
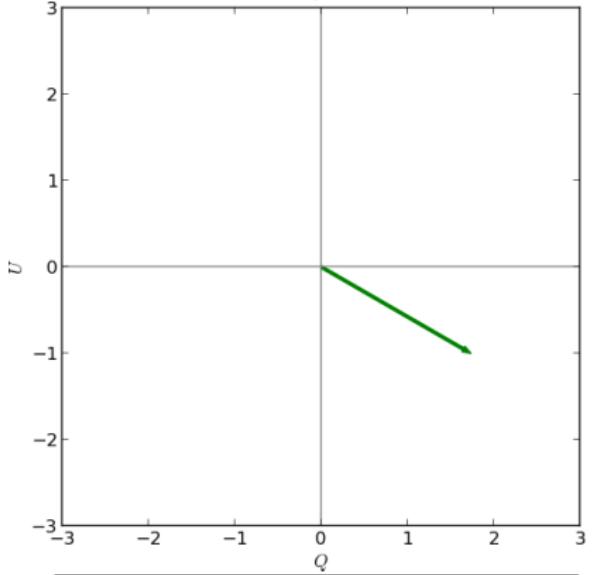
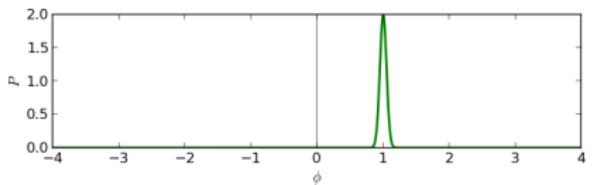


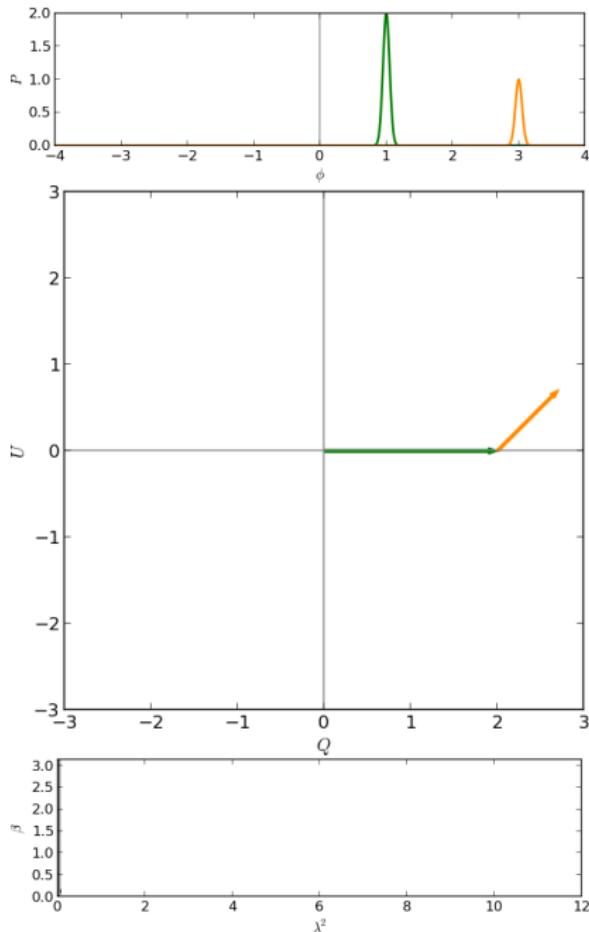


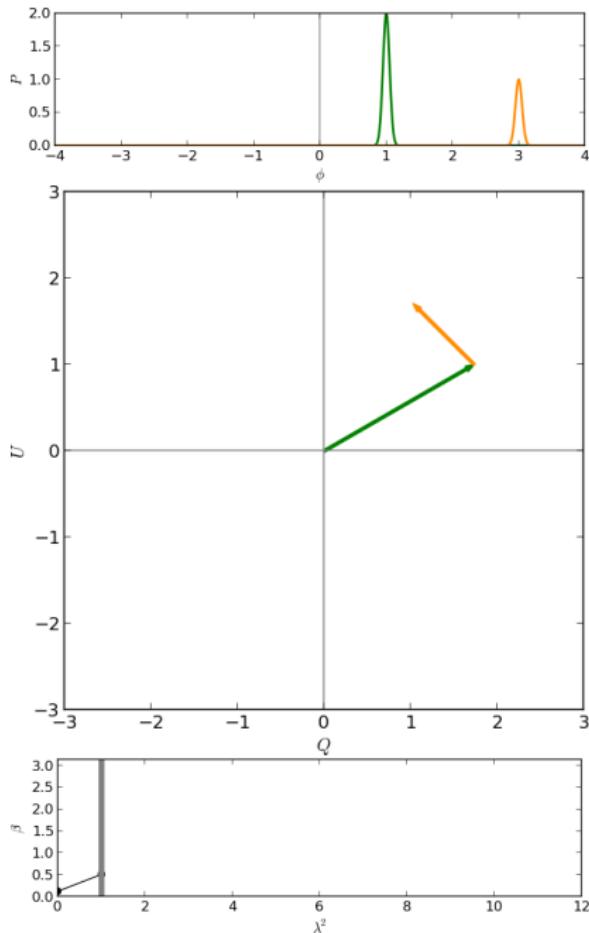


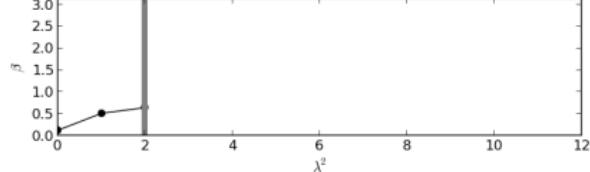
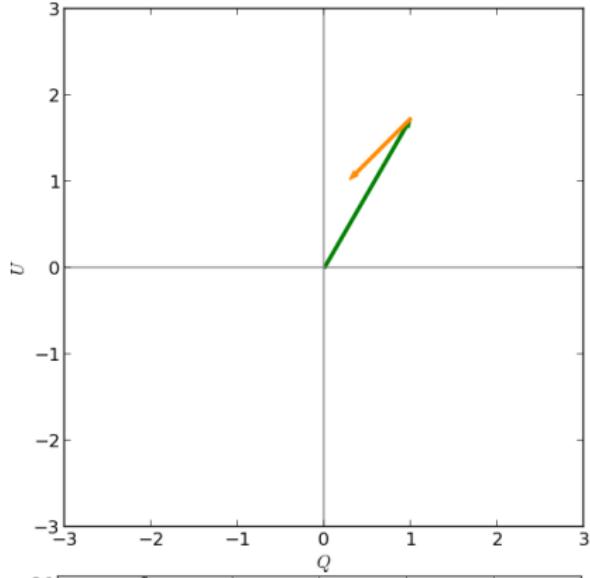
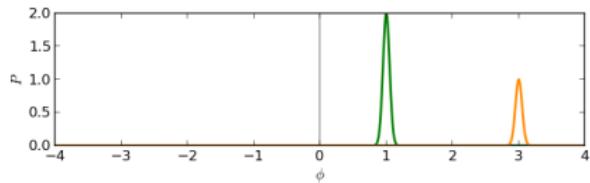


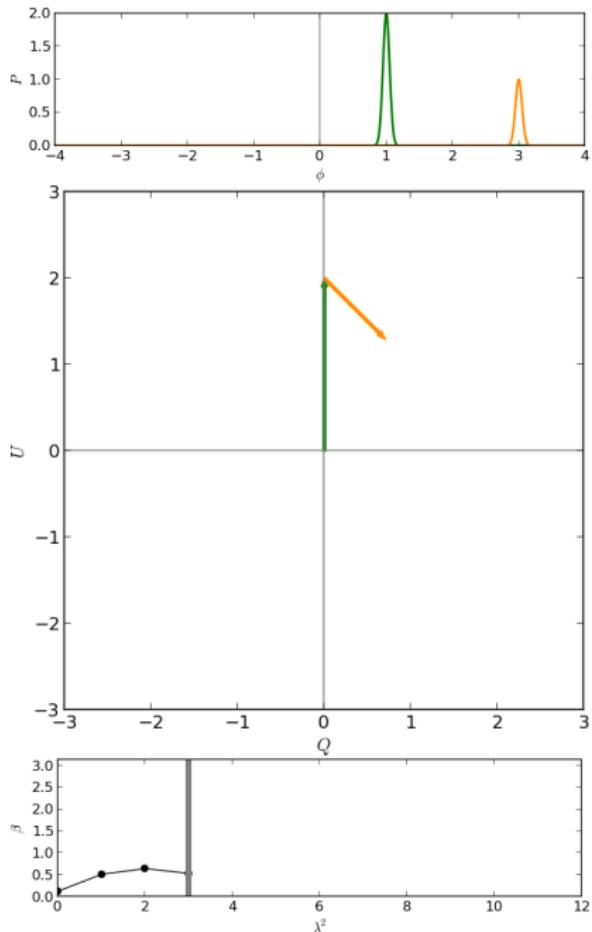


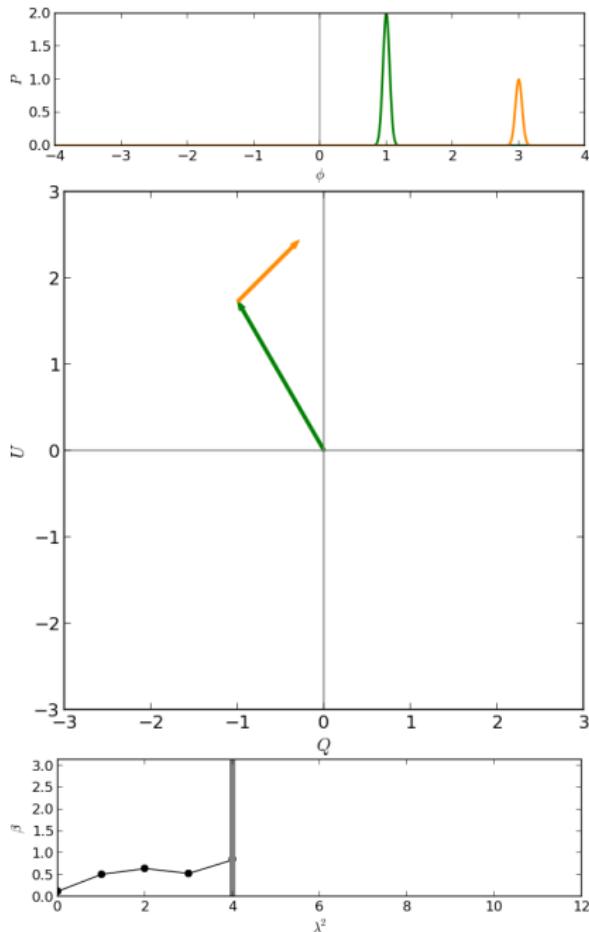


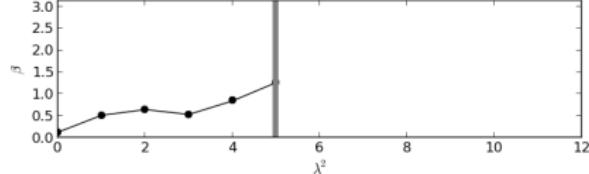
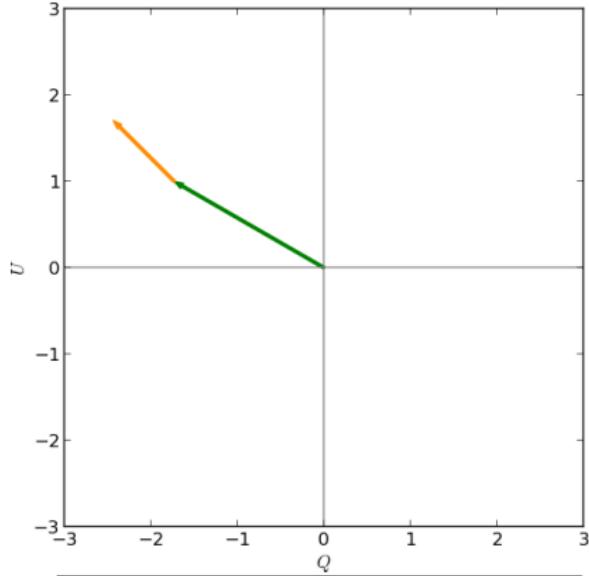
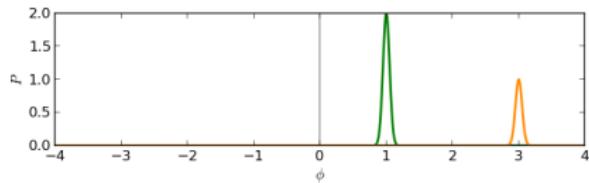


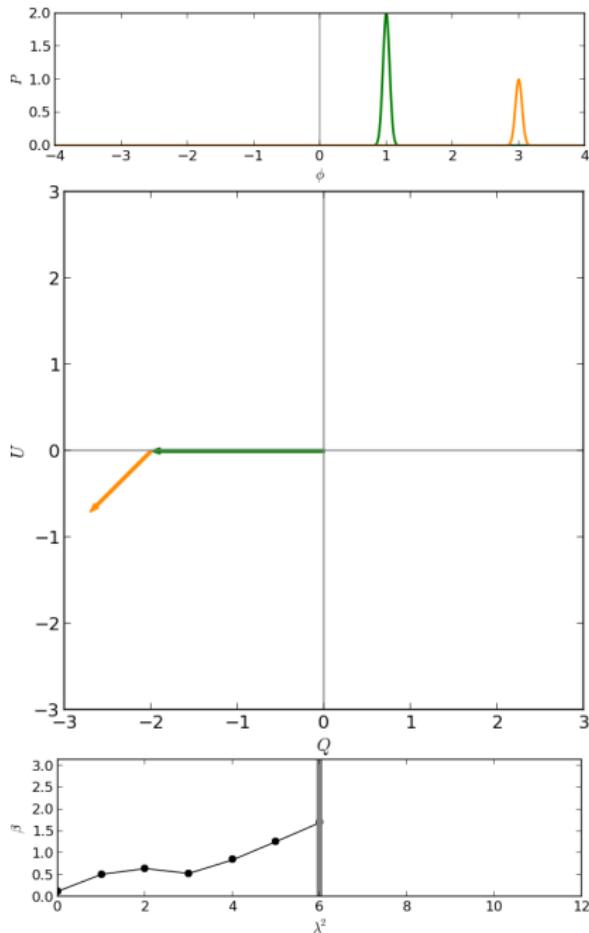


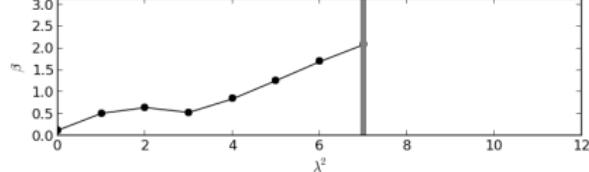
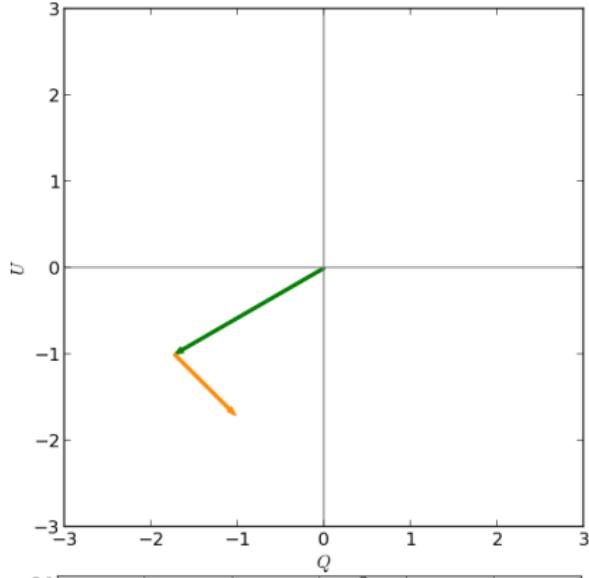
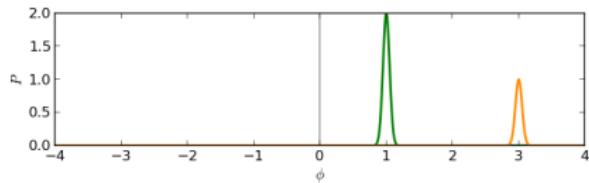


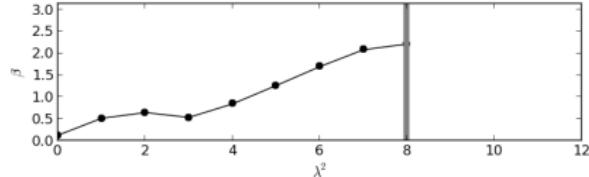
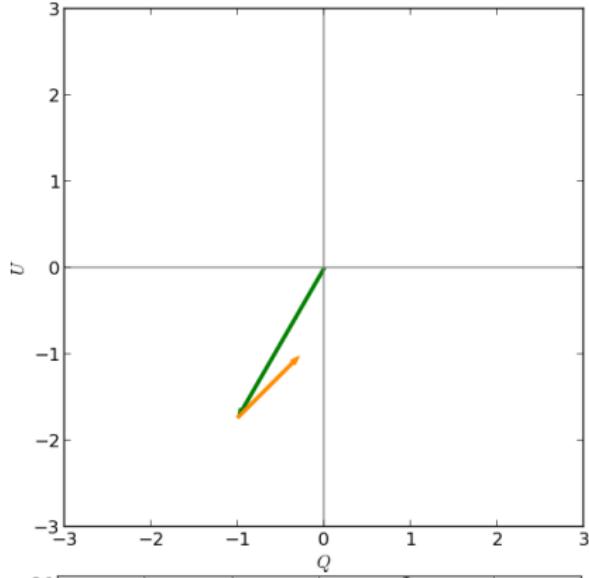
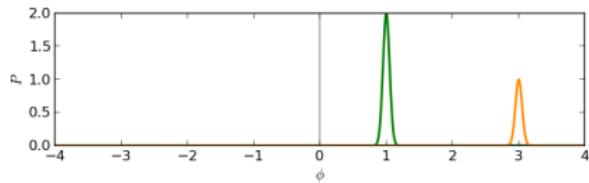


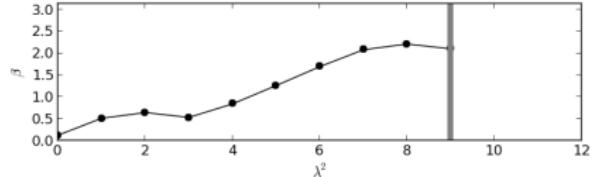
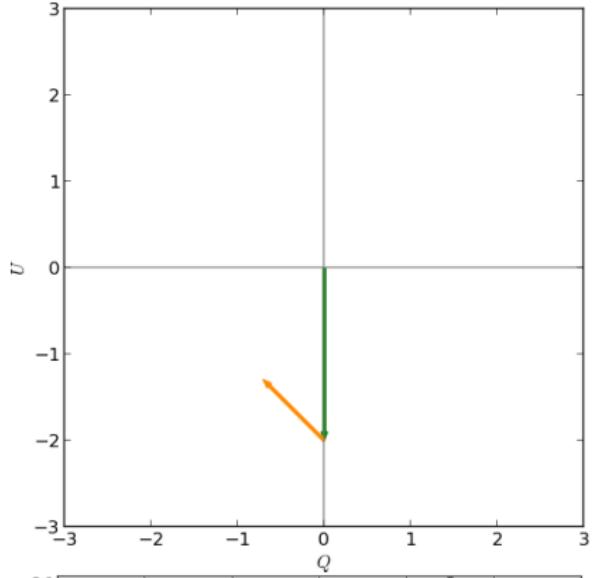
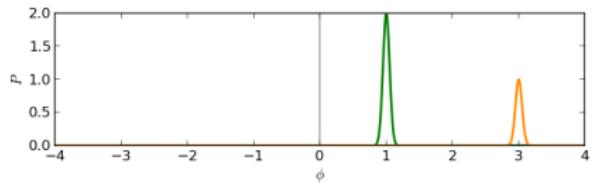


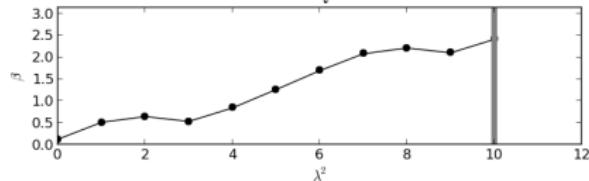
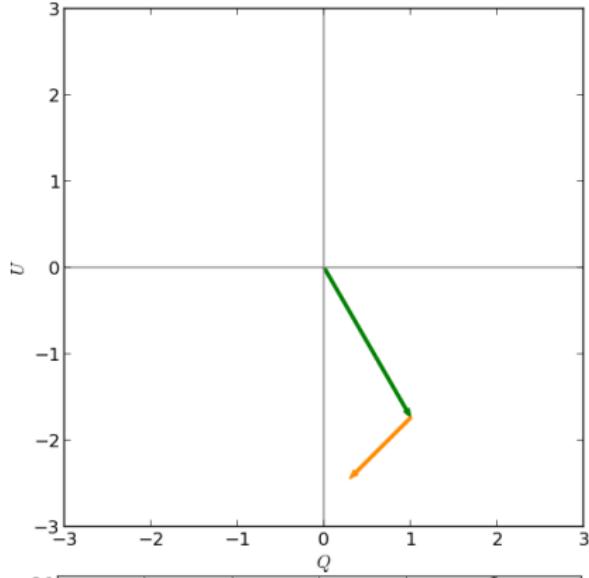
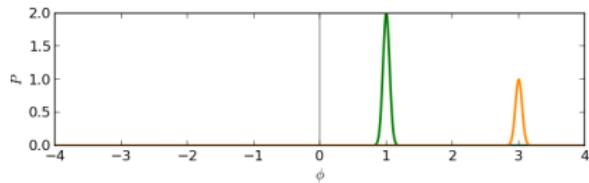


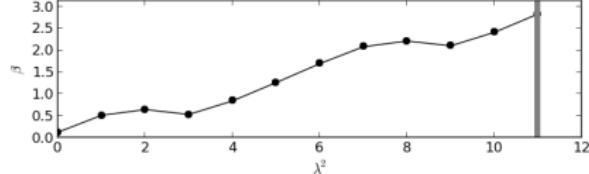
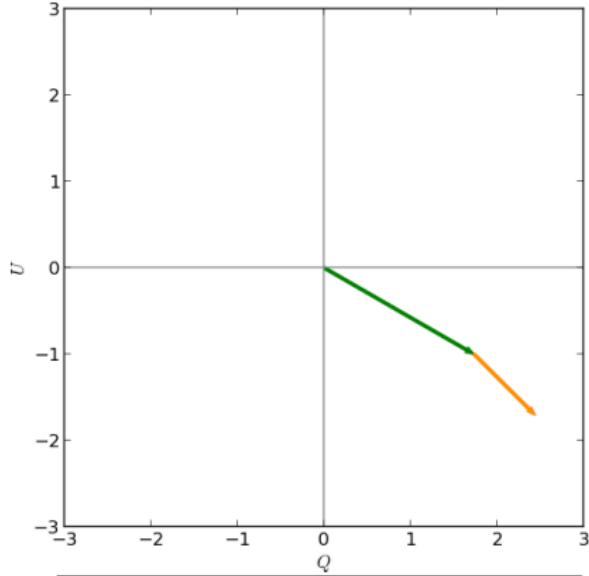
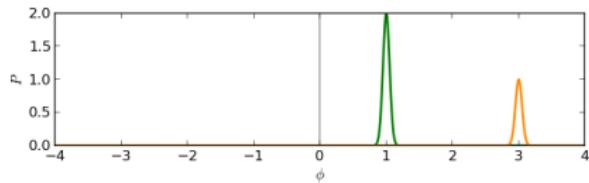




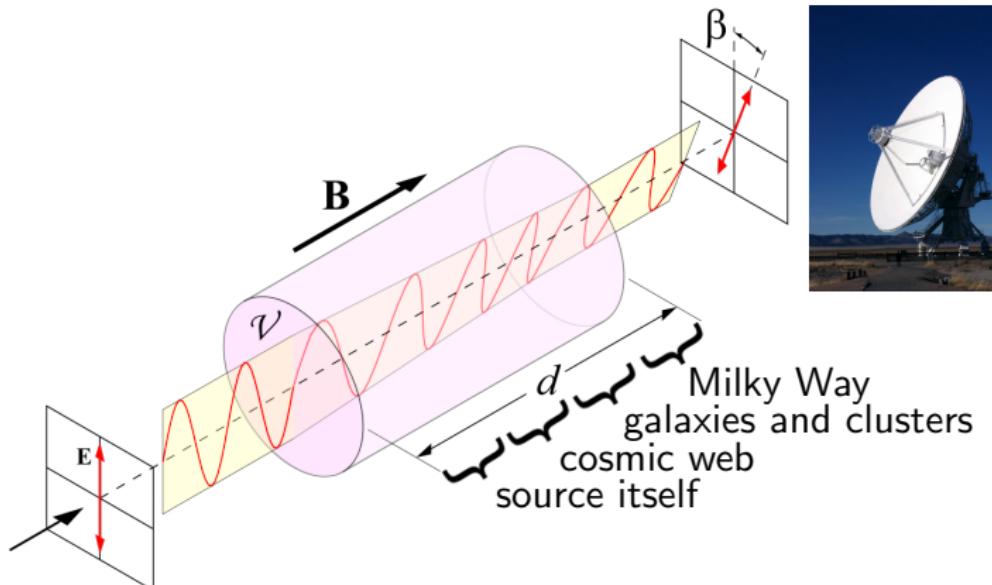








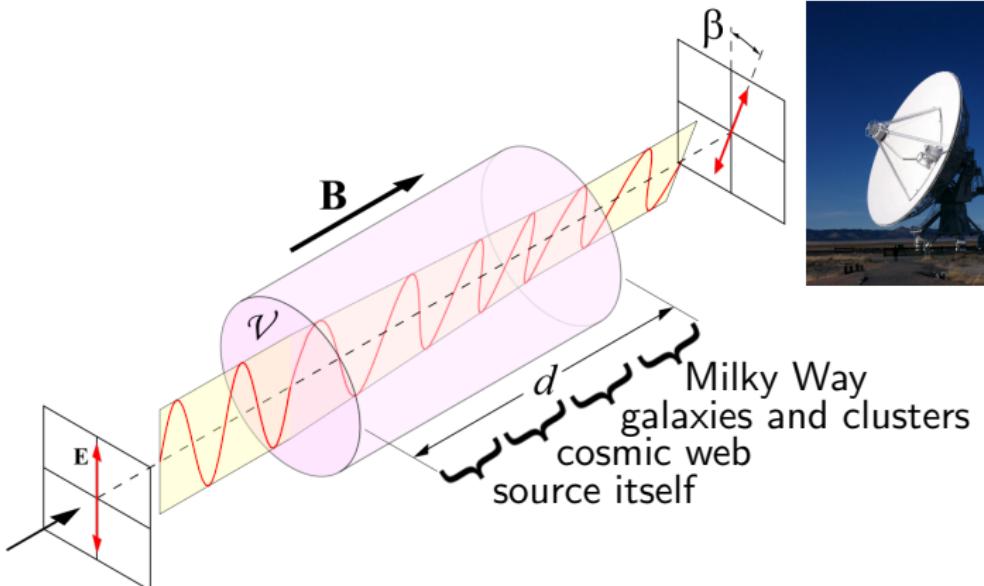
# Faraday rotation



$$\text{Faraday depth: } \phi \propto \int_{r_{\text{source}}}^0 (1+z)^{-2} n_e B_r dr$$

$$\beta = \phi \lambda^2$$

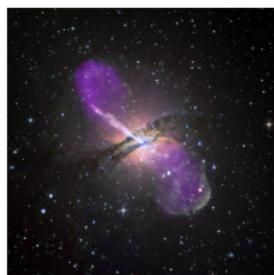
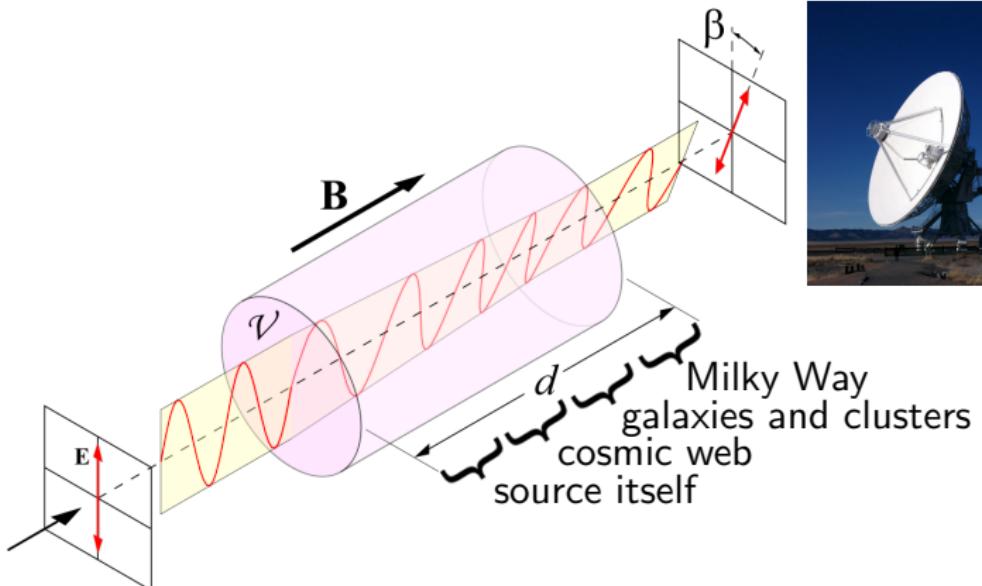
# Faraday rotation



$$\text{Faraday depth: } \phi \propto \int_{r_{\text{source}}}^0 (1+z)^{-2} n_e B_r dr$$

$$\phi = \phi_{\text{MW}} + \phi_{\text{other galaxies}} + \phi_{\text{clusters}} + \phi_{\text{filaments}} + \phi_{\text{sheets}} + \phi_{\text{voids}} + \phi_{\text{source}}$$

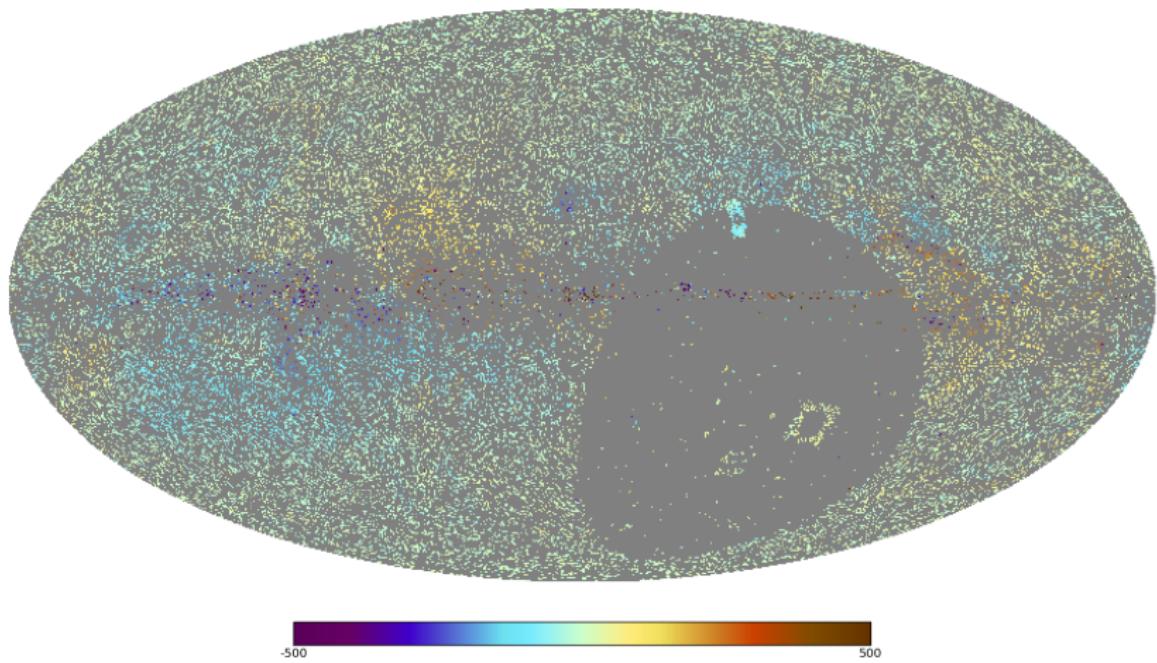
# Faraday rotation



$$\text{Faraday depth: } \phi \propto \int_{r_{\text{source}}}^0 (1+z)^{-2} n_e B_r dr$$

$$\phi = \phi_{\text{MW}} + \phi_{\text{extragalactic}}$$

$$d = \phi_{\text{MW}} + \phi_{\text{extragalactic}} + n$$

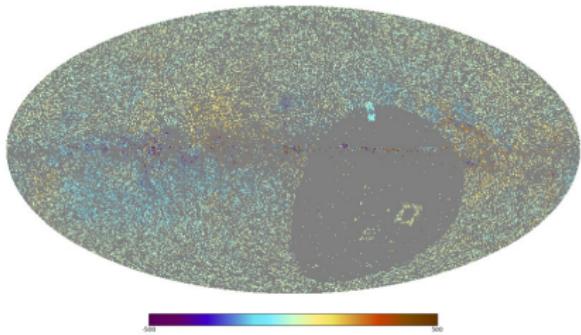


$\gtrsim 40\,000$  data points

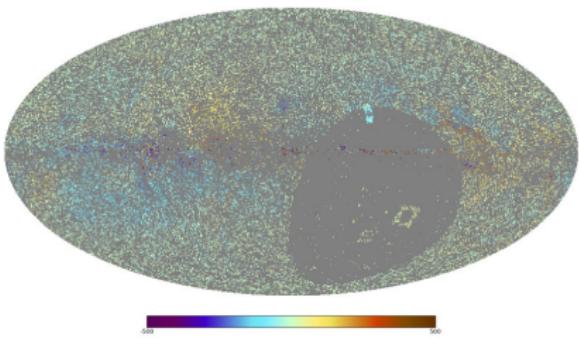
$$d = \phi_{\text{MW}} + \phi_{\text{extragalactic}} + n$$

## Challenges

- ▶ Regions without data
- ▶ Galactic/extragalactic split unknown
- ▶ Uncertain uncertainties



$$d = \phi_{\text{MW}} + \phi_{\text{extragalactic}} + n$$

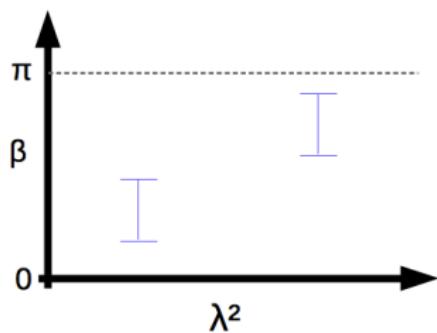
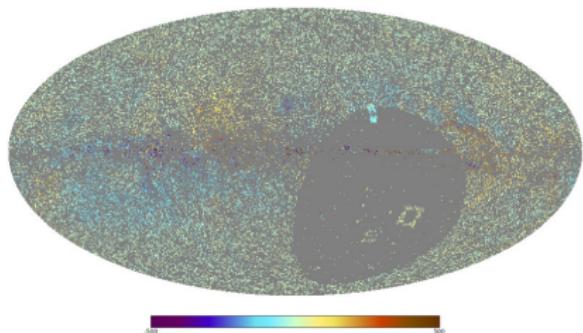


## Challenges

- ▶ Regions without data
- ▶ Galactic/extragalactic split unknown
- ▶ Uncertain uncertainties
  - ▶  $n\pi$  ambiguity
  - ▶ multiple components along a LOS
  - ▶ ionosphere
  - ▶ ...

$$d = \phi_{\text{MW}} + \phi_{\text{extragalactic}} + n$$

## Challenges

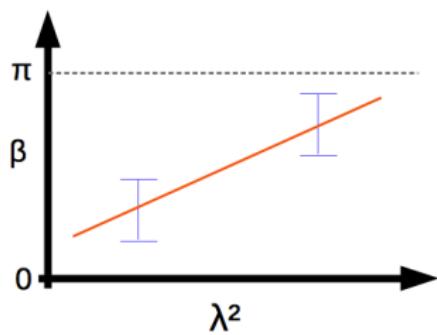
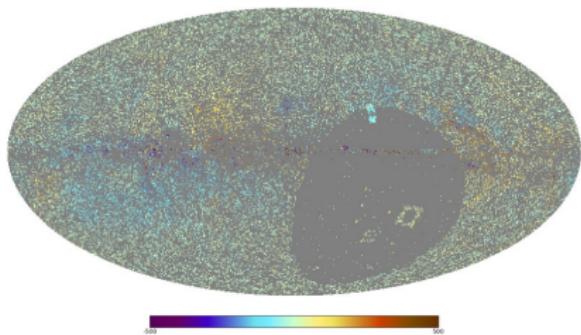


- ▶ Regions without data
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  - ▶ ...

$$d = \phi_{\text{MW}} + \phi_{\text{extragalactic}} + n$$

## Challenges

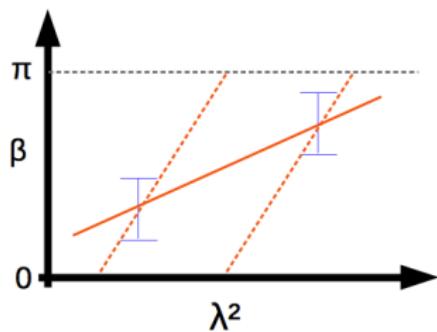
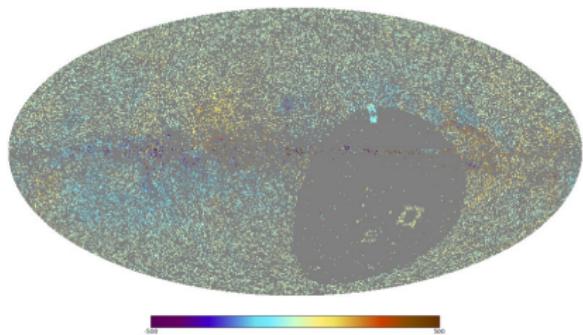
- ▶ Regions without data
- ▶ Galactic/extragalactic split unknown
- ▶ Uncertain uncertainties
  - ▶  $n\pi$  ambiguity
  - ▶ multiple components along a LOS
  - ▶ ionosphere
  - ▶ ...



$$d = \phi_{\text{MW}} + \phi_{\text{extragalactic}} + n$$

## Challenges

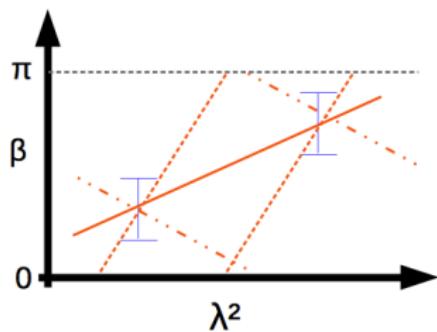
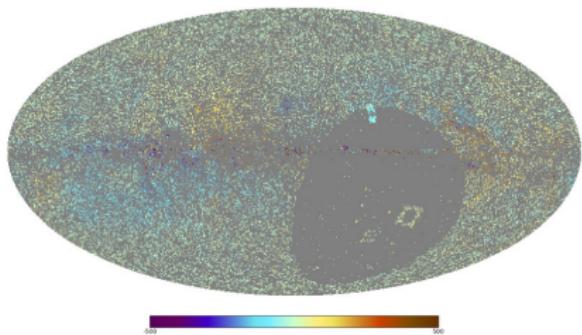
- ▶ Regions without data
- ▶ Galactic/extragalactic split unknown
- ▶ Uncertain uncertainties
  - ▶  $n\pi$  ambiguity
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  - ▶ ...



$$d = \phi_{\text{MW}} + \phi_{\text{extragalactic}} + n$$

## Challenges

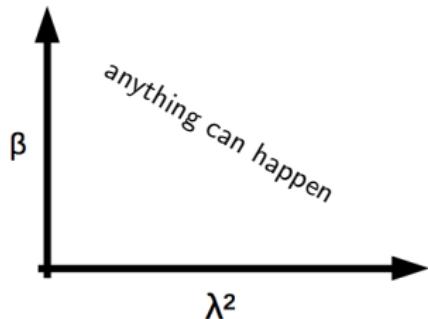
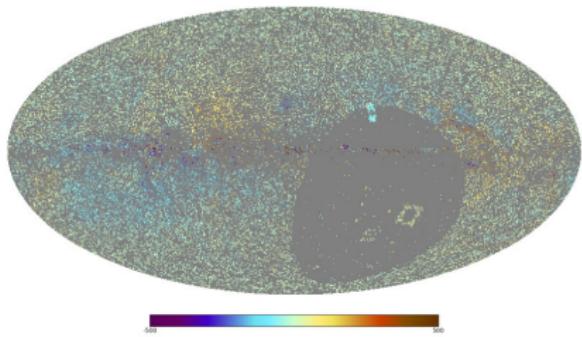
- ▶ Regions without data
- ▶ Galactic/extragalactic split unknown
- ▶ Uncertain uncertainties
  - ▶  $n\pi$  ambiguity
  - ▶ multiple components along a LOS
  - ▶ ionosphere
  - ▶ ...



$$d = \phi_{\text{MW}} + \phi_{\text{extragalactic}} + n$$

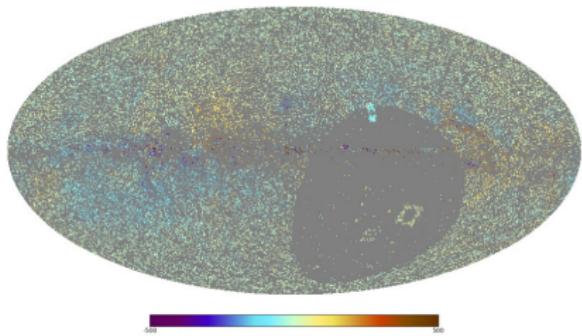
## Challenges

- ▶ Regions without data
- ▶ Galactic/extragalactic split unknown
- ▶ Uncertain uncertainties
  - ▶  $n\pi$  ambiguity
  - ▶ multiple components along a LOS
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  - ▶ ...



$$d = \phi_{\text{MW}} + \phi_{\text{extragalactic}} + n$$

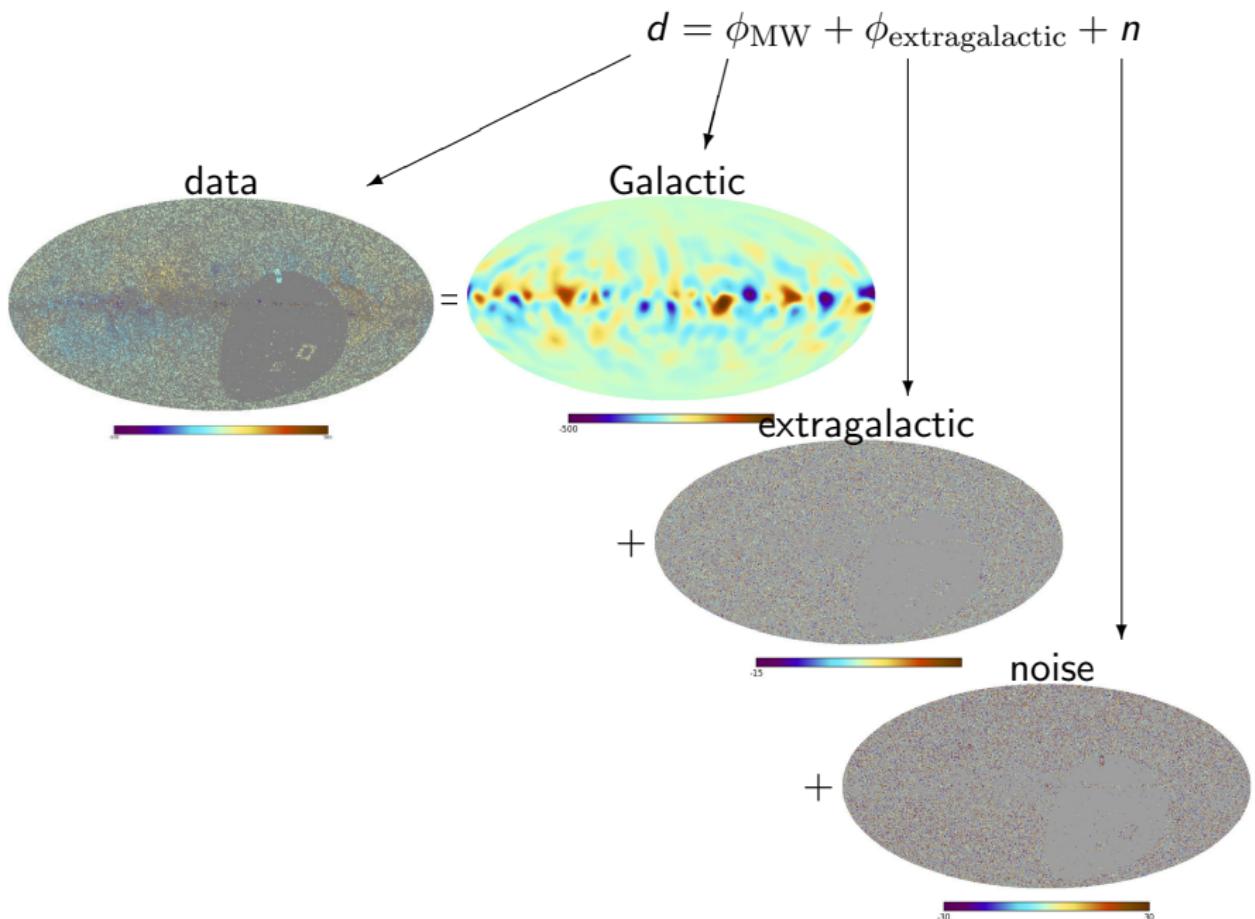
## Challenges

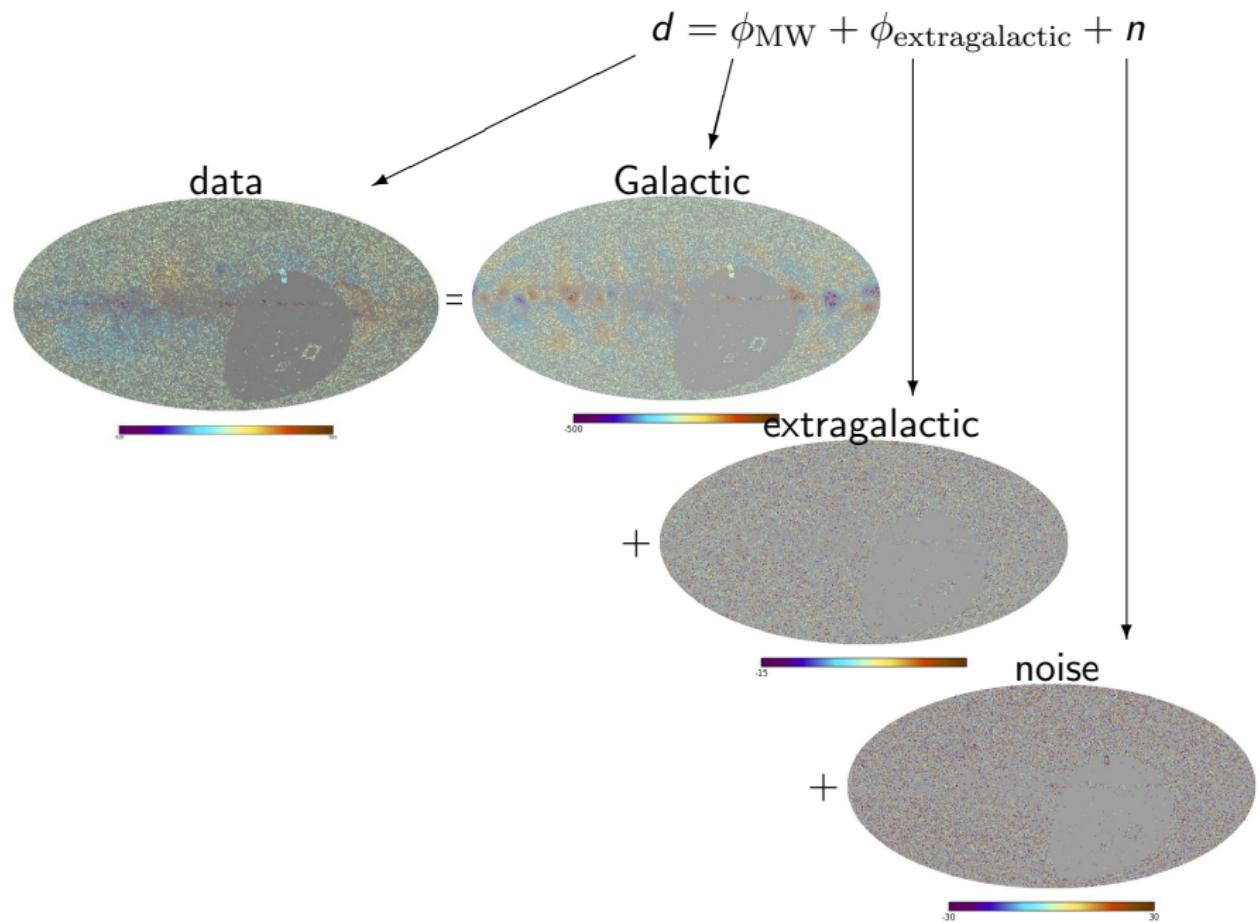


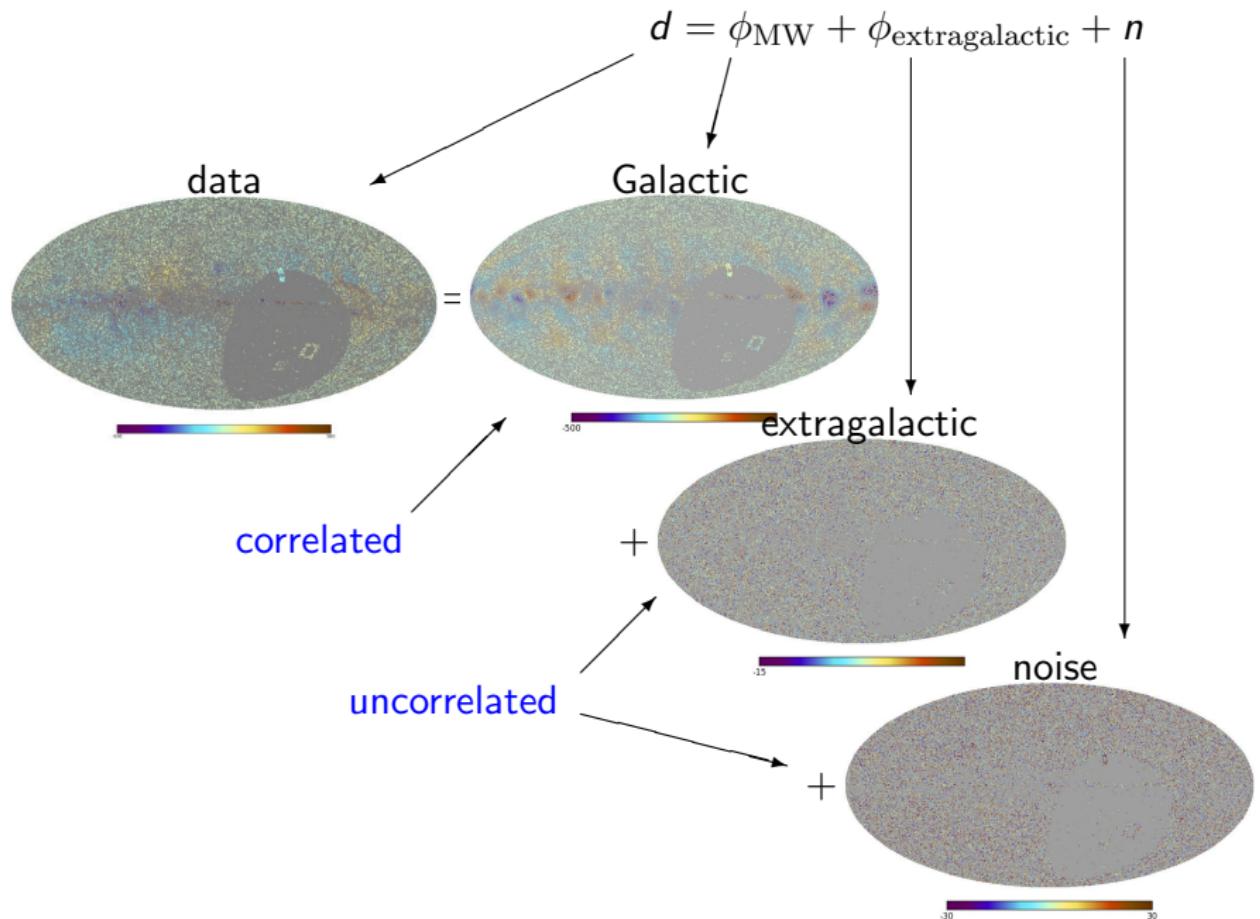
- ▶ Regions without data
- ▶ Galactic/extragalactic split unknown
- ▶ Uncertain uncertainties
  - ▶  $n\pi$  ambiguity
  - ▶ multiple components along a LOS
  - ▶ ionosphere
  - ▶ ...

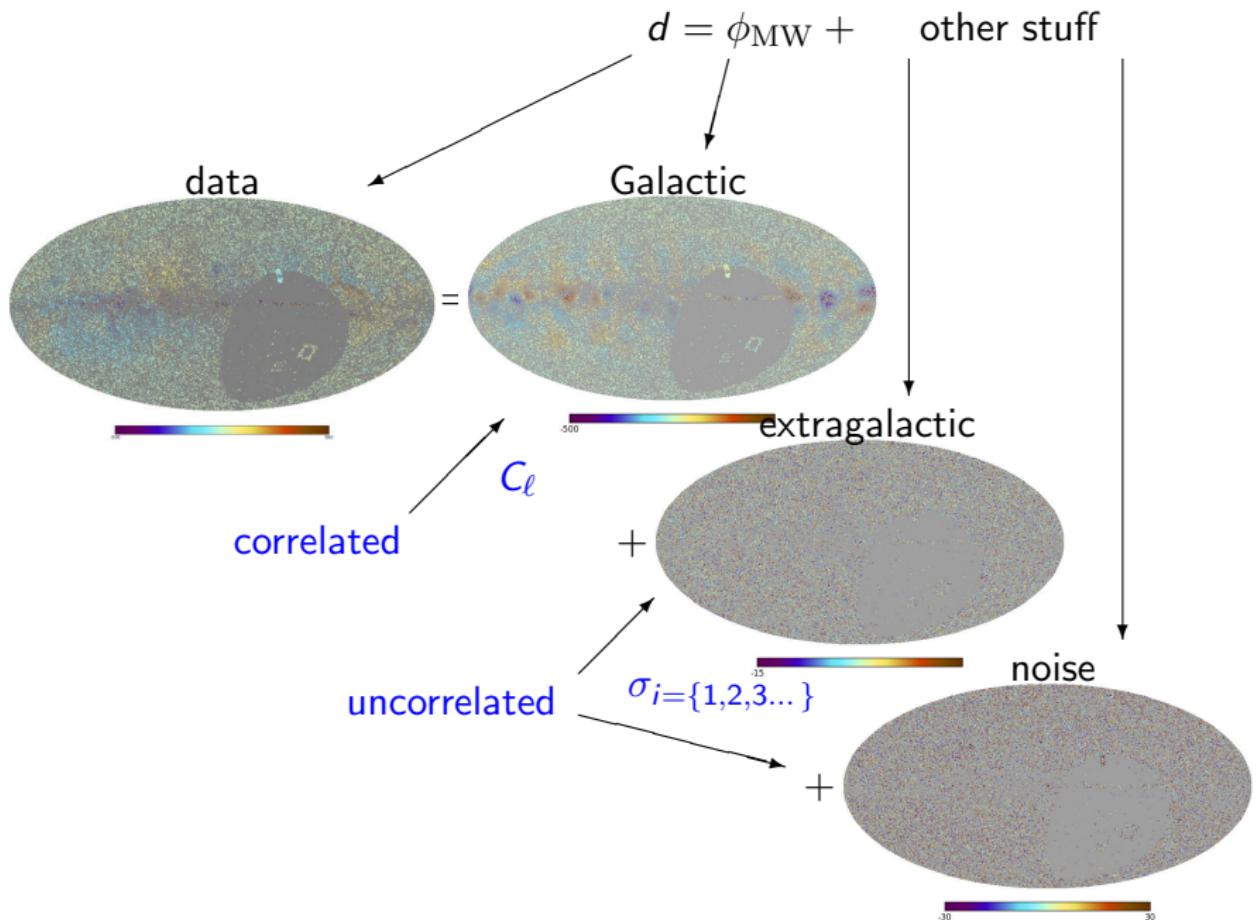
$$d = \phi_{\text{MW}} + \phi_{\text{extragalactic}} + \phi_{\text{ionosphere}}(t) + n$$

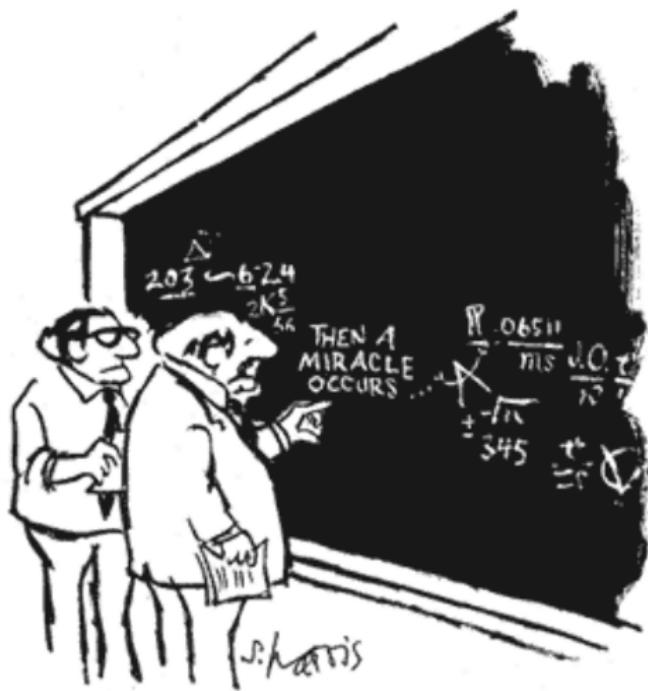
$$d = \phi_{\text{MW}} + \phi_{\text{extragalactic}} + n$$





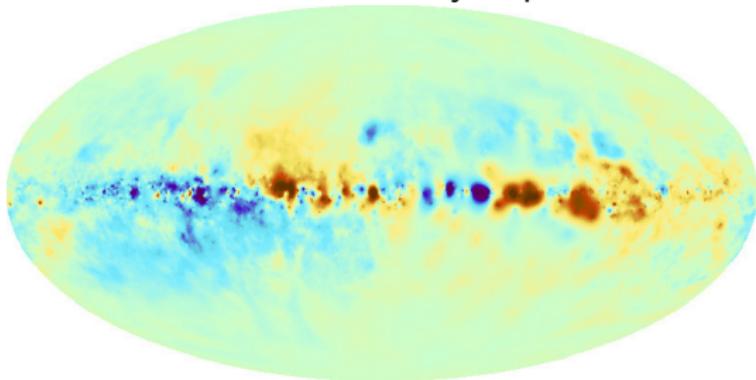




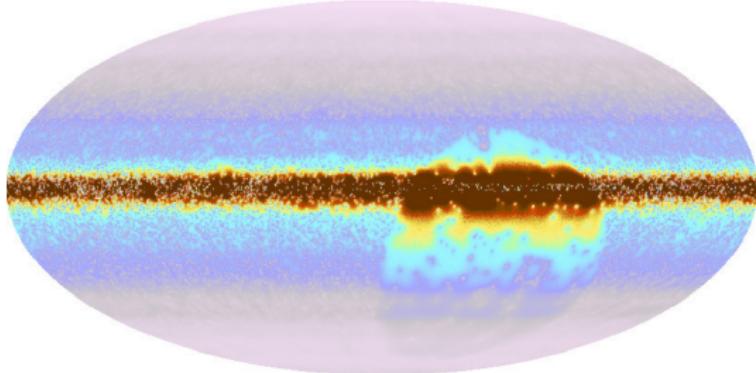


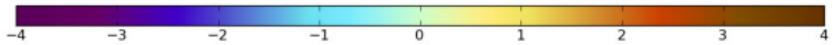
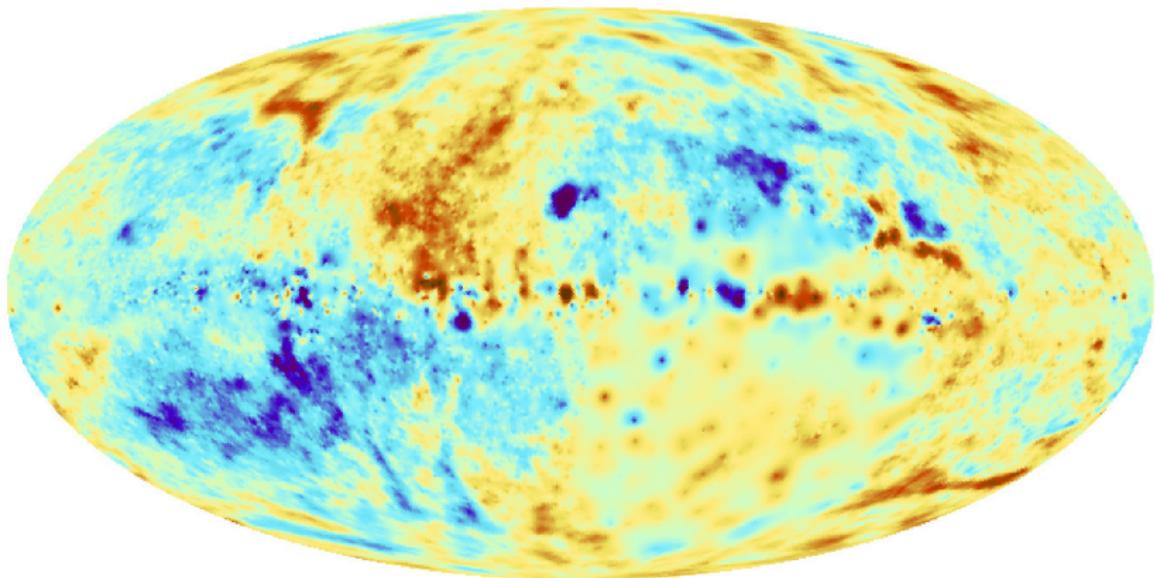
"I THINK YOU SHOULD BE MORE EXPLICIT HERE IN STEP TWO."

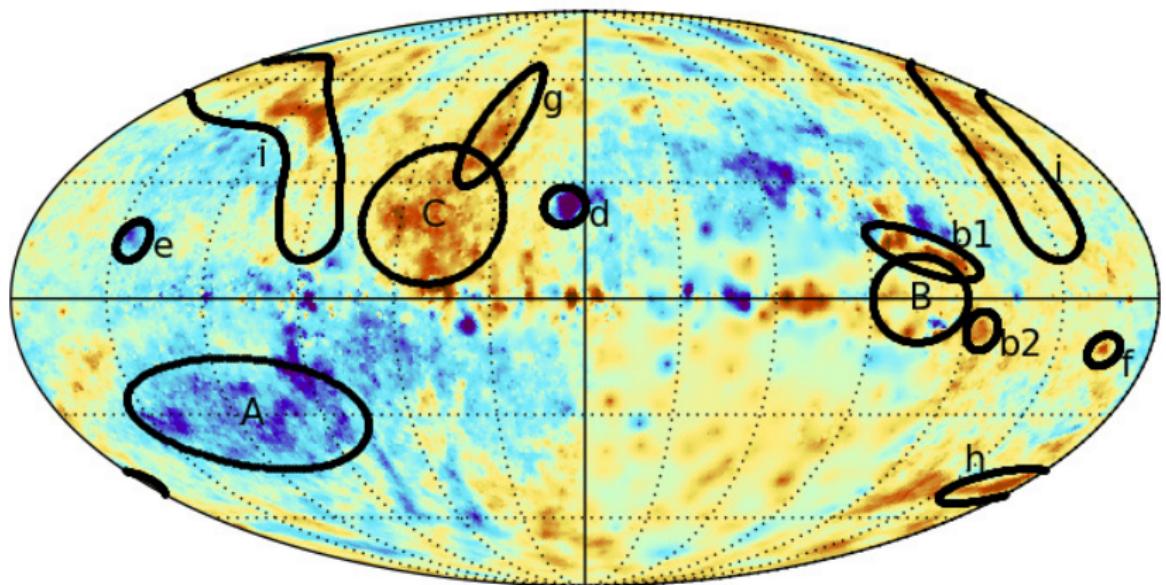
# Galactic Faraday depth

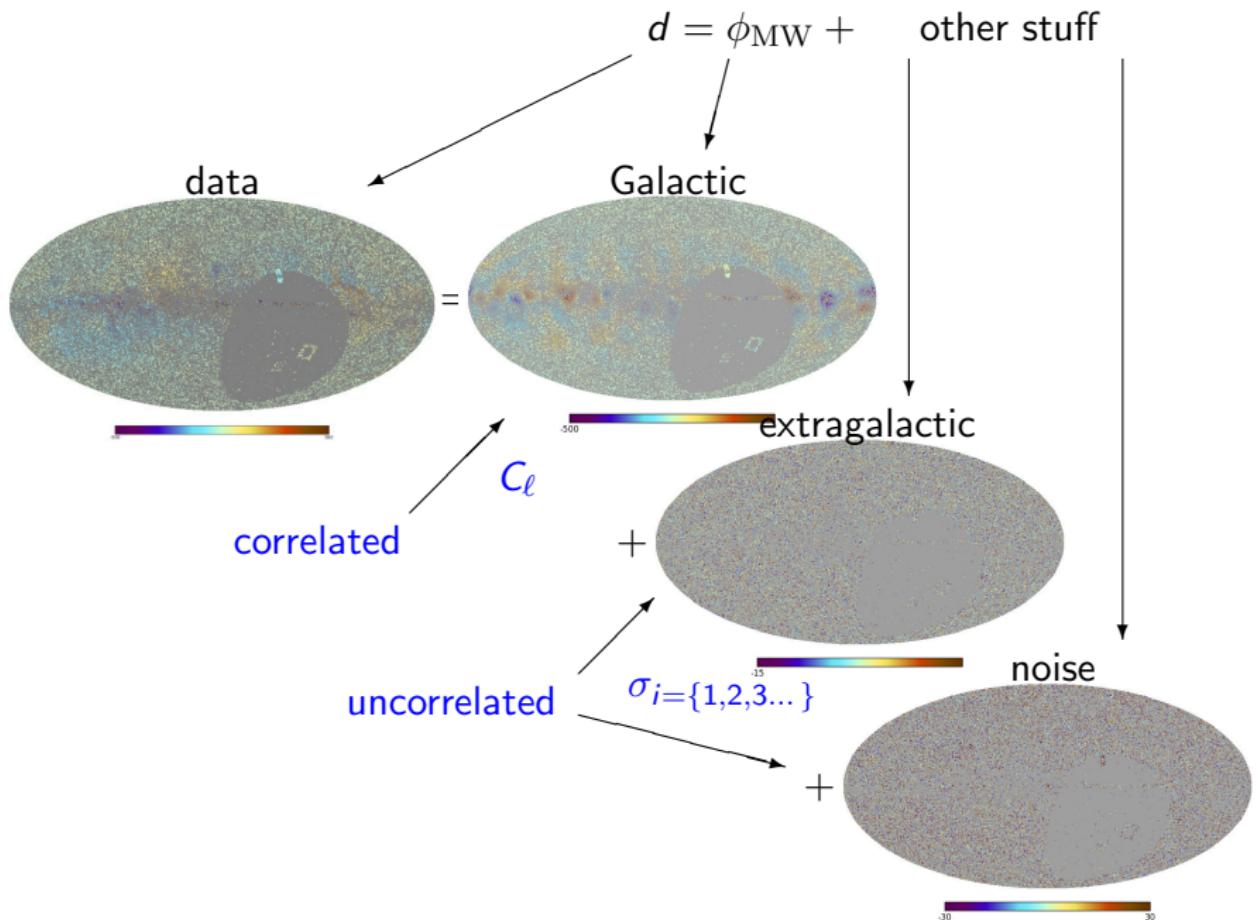


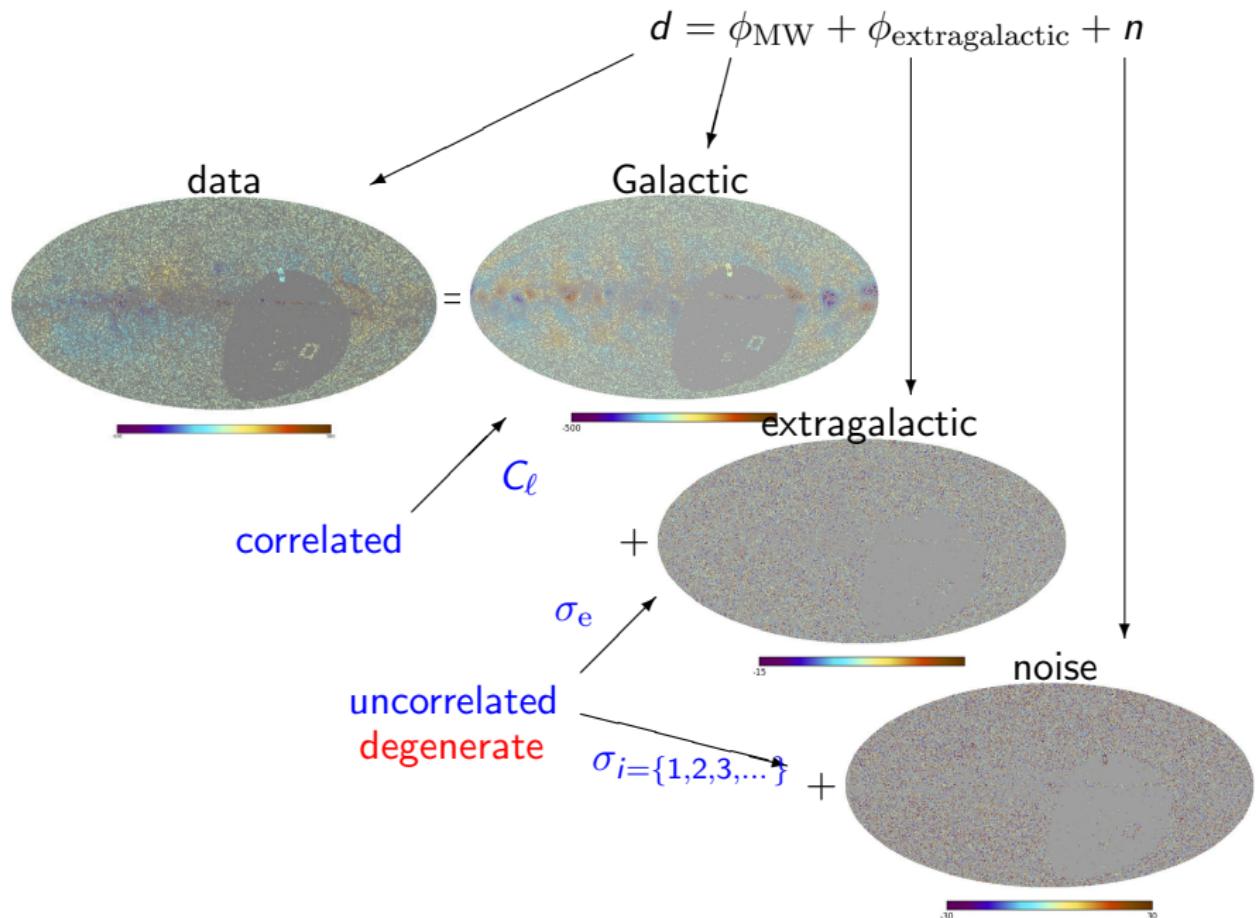
uncertainty

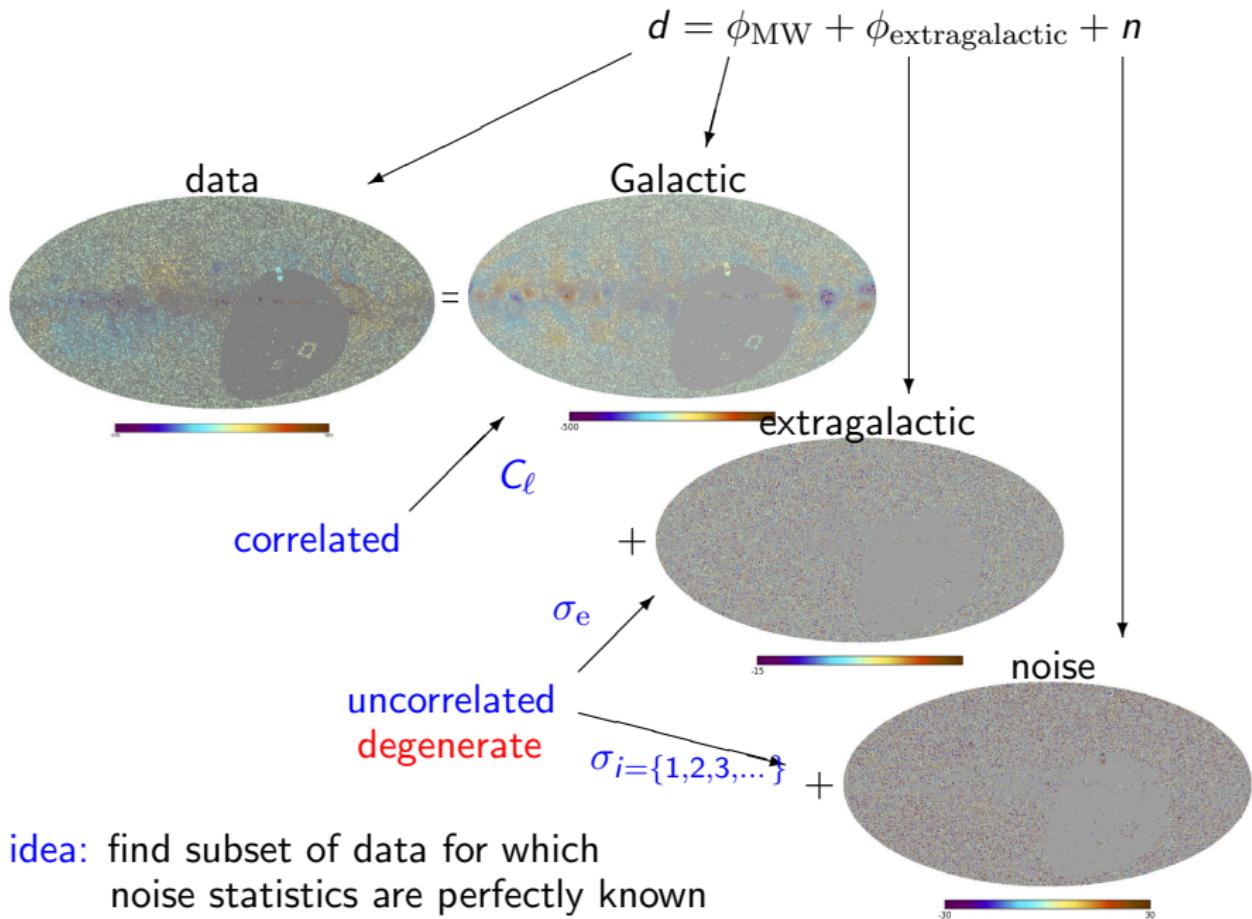












**idea:** find subset of data for which noise statistics are perfectly known

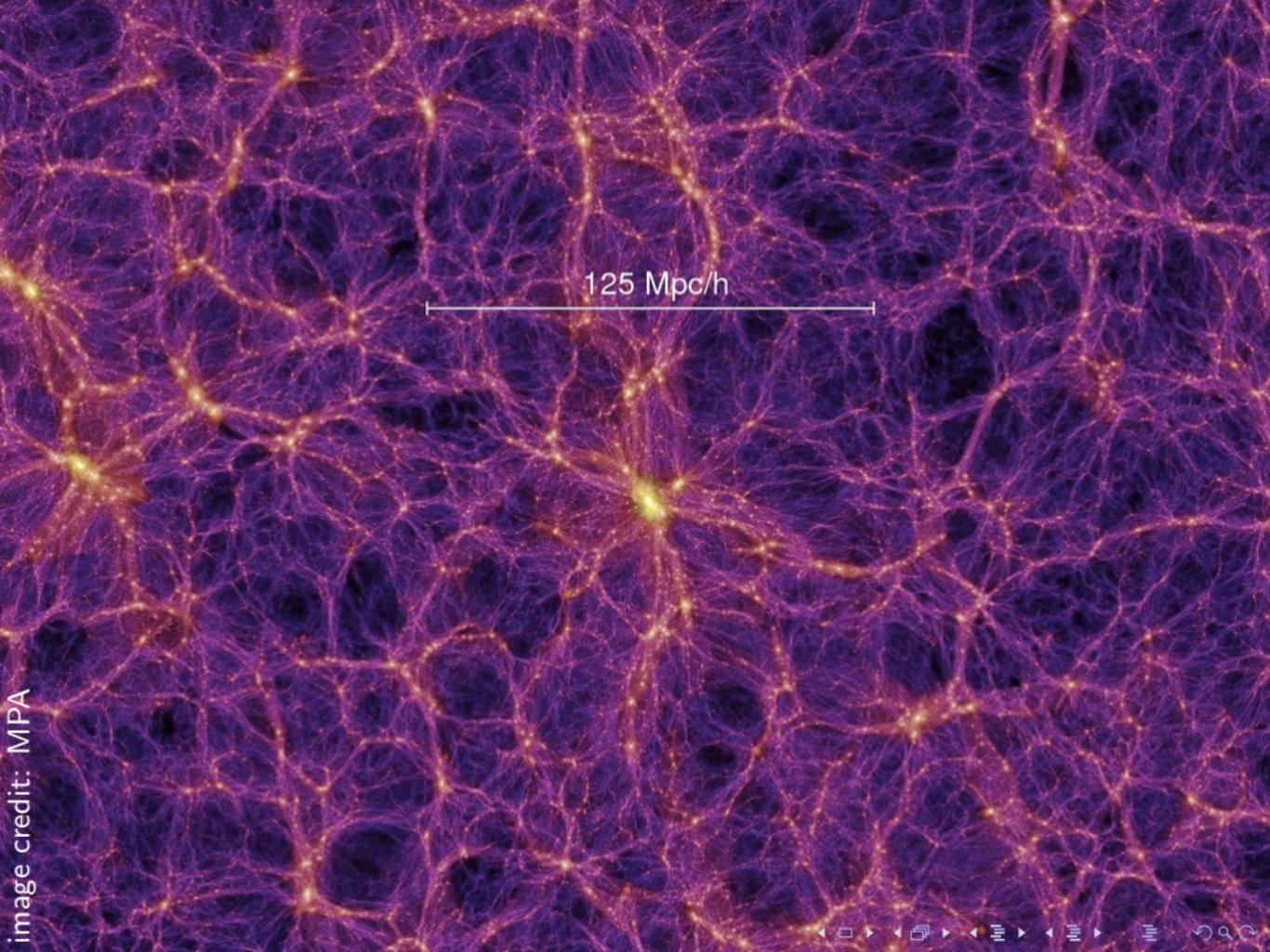
## Results:

- ▶  $\sigma_e \lesssim 7 \text{ rad/m}^2$
- ▶ constraints on extragalactic contributions for individual sources very weak

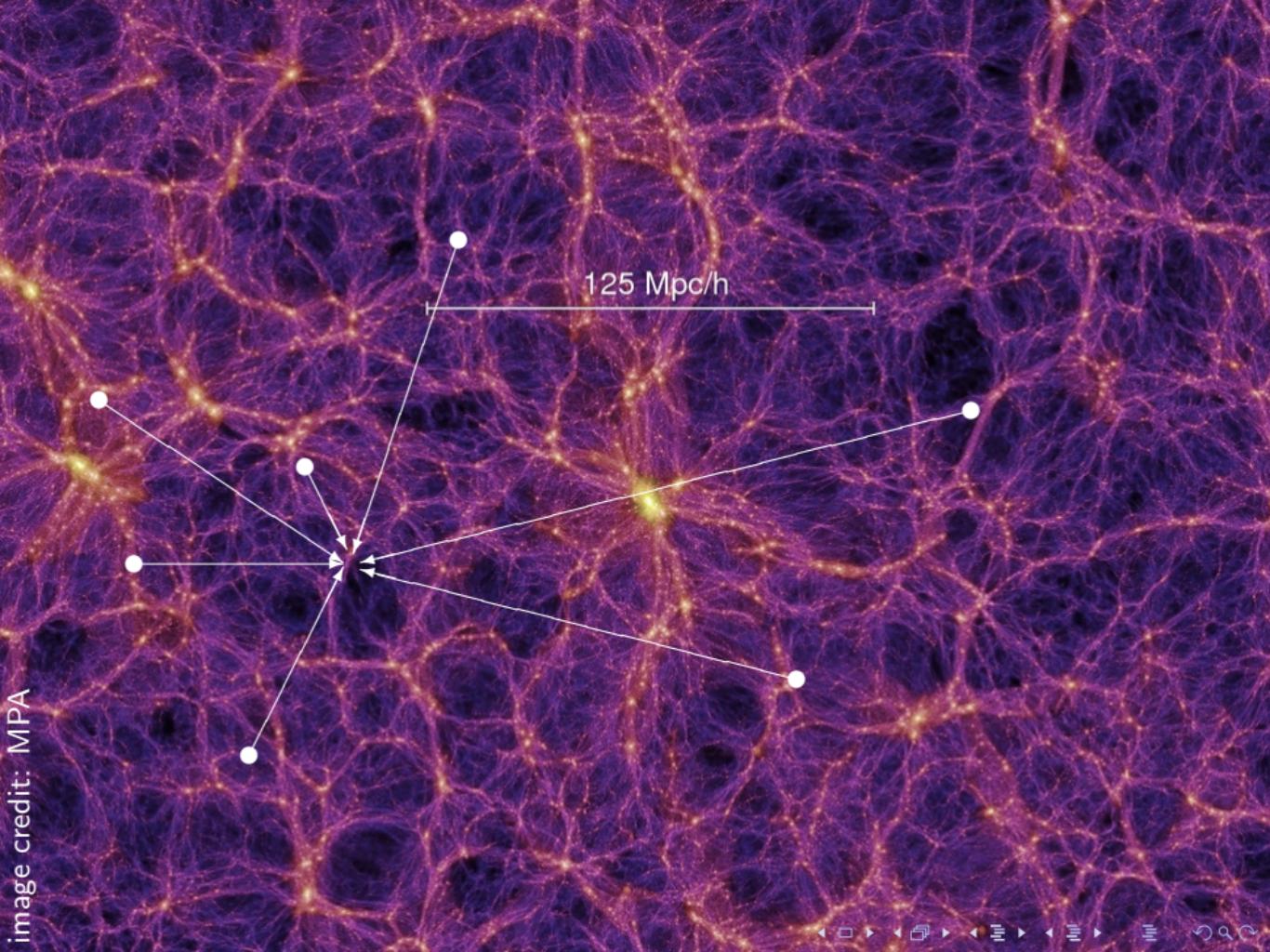
What magnetic fields is this due to?

Results:

- ▶  $\sigma_e \lesssim 7 \text{ rad/m}^2$
- ▶ constraints on extragalactic contributions for individual sources very weak

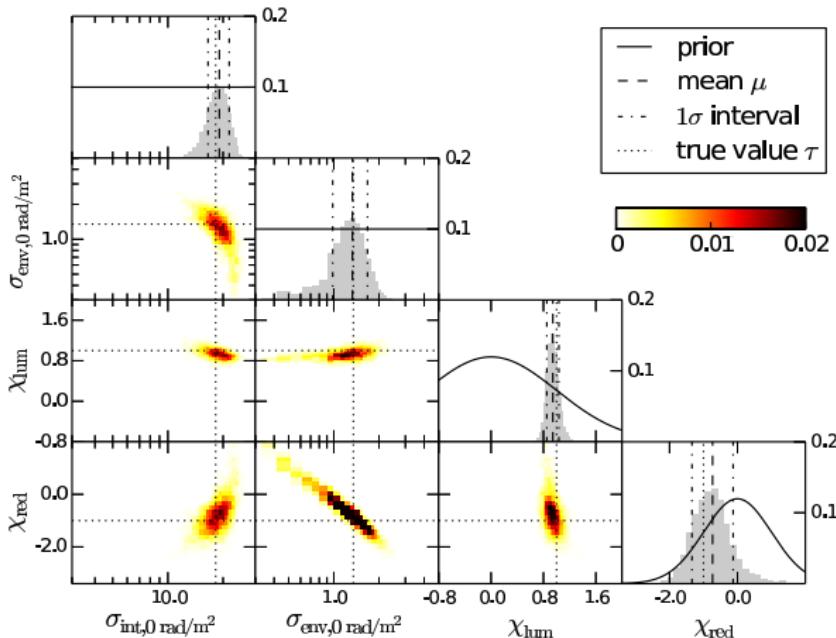


125 Mpc/h



$$\sigma_{e,i}^2 \propto \left(\frac{L}{L_0}\right)^{\chi_{\text{lum}}} \frac{\sigma_{\text{int}}^2}{(1+z_i)^4} + \frac{D_i}{D_0} \sigma_{\text{env}}^2$$

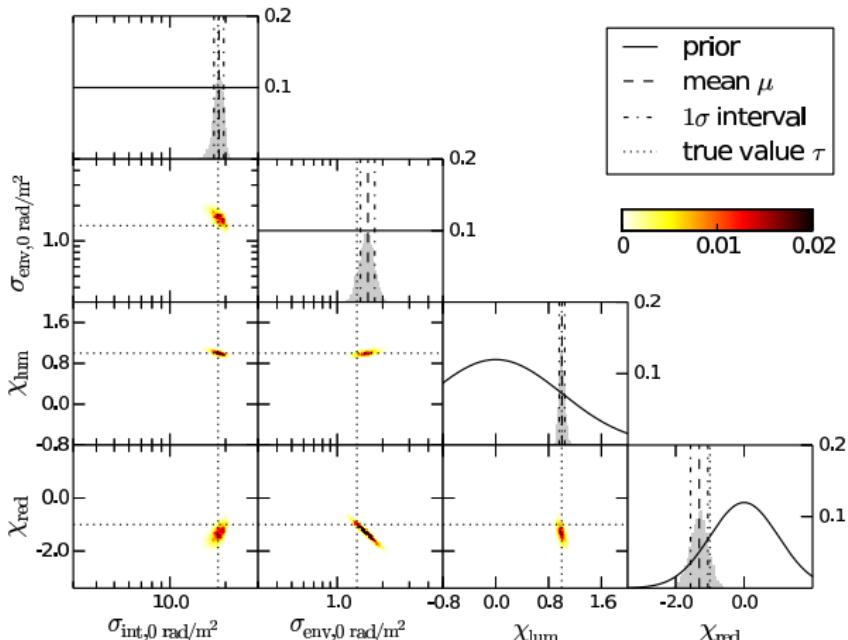
$$D_i = \int_0^{z_i} \frac{c}{H(z)} (1+z)^{4+\chi_{\text{red}}} dz$$



4003 lines of sight

$$\sigma_{e,i}^2 \propto \left(\frac{L}{L_0}\right)^{\chi_{\text{lum}}} \frac{\sigma_{\text{int}}^2}{(1+z_i)^4} + \frac{D_i}{D_0} \sigma_{\text{env}}^2$$

$$D_i = \int_0^{z_i} \frac{c}{H(z)} (1+z)^{4+\chi_{\text{red}}} dz$$



41632 lines of sight

## Summary

- ▶ Faraday rotation probes  $B$ -fields on (almost) all scales
- ▶ Galactic contribution (correlated) can be separated from rest (uncorrelated)
- ▶ Rest can be statistically split into extragalactic and noise
- ▶ Uncertainties are large and need to be understood

## Outlook

- ▶ Large-scale structure information to be included
- ▶ More sophisticated treatment of observational uncertainties desirable

Results: <http://www.mpa-garching.mpg.de/ift/faraday/>