

Introduction

- We will take you through successfully launching a rocket and landing it on a different body
- This is a simplified version based on our knowledge of KSP not real life per se

Jargon

Orbit An object rotating around another object is said to be in orbit

Inclined An orbit that is tilted relative to the plane of the parent body

Technicallities

delta-v

- aka: fuel budget
- how hard can i accelerate/decelerate my rocket
- dependent on:
 - fuel efficiency
 - thrust to weight ratio

Technicallities

Points on orbit

apoapsis : highest point on orbit

periapsis : Lowest point on orbit



Let's prepare for launch

Stage	TWR (k)	Δv (atm)	Time
1	2.10	279 m/s	12.9 s
2	2.07	322 m/s	15.0 s
3	2.04	380 m/s	17.8 s

Total Δv : 981 m/s

Stage	TWR (k)	Δv (vac)	Time
4	4	198	3155 m/s
5	---	---	---

Stage	TWR (k)	Δv (vac)	Time
6	6	135	2523 m/s
7	---	---	---

Stage	TWR (k)	Δv (vac)	Time
8	8	191	---

2 x Z-400 Rechargeable Battery

Mass = 20 kg
Capacity = 400 e

2 x OX-STAT Photovoltaic Panel

Mass = 5 kg
Electricity = 0.75 e/s

6 x 60° Liquid Fuel Booster

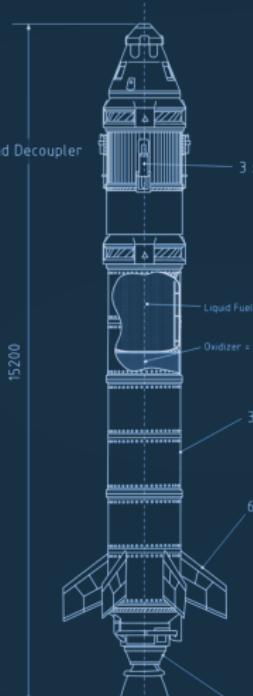
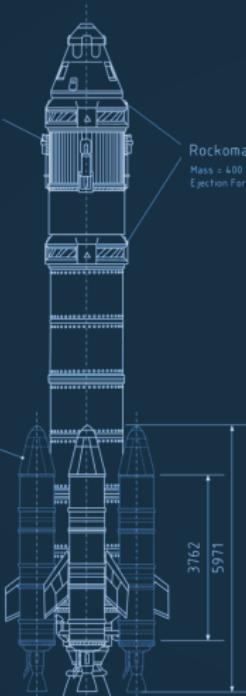
2-2-2 Asparagus Staging
6 x NCS Adapter incl. Standard NC
Mass = 400 kg

18 x FL-T400 Liquid Fuel Tank
Mass = 250 kg
Liquid Fuel = 180 L
Oxidizer = 220 L

6 x LV-T45 Liquid Fuel Engine
Mass = 1500 kg
Thrust = 200 000 N
Isp (atm) = 320 s

6 x Hydraulic Detachment Manifold
Mass = 400 kg
Ejection Force = 100 N

Total Δv (atm) = 5 404 m/s
Total Δv (vac) = 6 826 m/s
Total Mass = 131 390 kg
Part Count = 78
Total Cost = 64 820 ₣



Rockomax „Poodle“ Liquid Engine
Mass = 2 500 kg
Thrust = 220 000 N
Isp (vac) = 390 s

Mk16-XL Parachute
Mass = 300 kg
Drag
- Stowed = 0.22
- Semi-Deployed = 1
- Deployed = 500

Mk1-2 Command Pod
Mass = 4 000 kg
Required Crew = 3

Staging



How do we do it

- Split the rocket in 2 or more parts.
- Each part carries own fuel and engine
- Each stage can be separated from the rocket in sequence
- e.g. booster stage, landing stage, transfer stage, ...

6 x 60° Liquid Engine
2 x 20° Solid Rocket Motor
6 x 18° Solid Rocket Motor
18 x 6° Solid Rocket Motor
6 x Landing Leg

Thrust = 200 000 N
Isp (atm) = 320 s
6 x Hydraulic Detachment Manifold
Mass = 400 kg
Ejection Force = 100 N

Total Δv (atm) = 5 404 m/s
Total Δv (vac) = 6 826 m/s
Total Mass = 131 390 kg
Part Count = 78
Total Cost = 64 820 ₣



Rockomax "Mainsail" Liquid Engine
Mass = 6 000 kg
Thrust = 1 500 000 N
Isp (atm) = 280 s
Isp (vac) = 330 s

Mk1-2 Command Pod
Mass = 4 000 kg
Required Crew = 3

Staging



Why do we do it

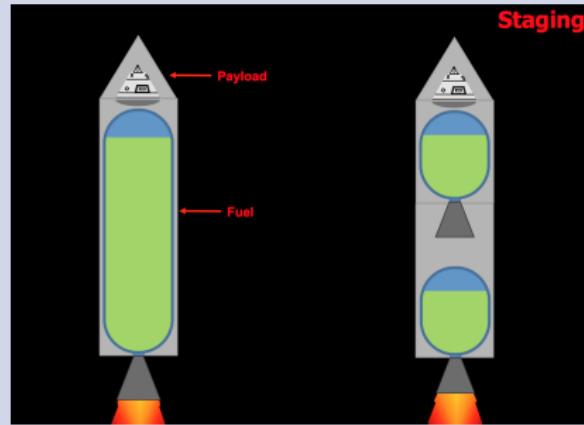
- Rocket efficiency is inversely proportional to its weight
- Delta-v goes up as total mass decreases (All else being equal)
- We want to carry as little mass as possible
- Throw away excess weight of unused engines and empty fuel tanks

6 x 60° Liqui
2 x 20° Liqui
6 x 60° Oxide
18 x 60° Oxide
6 x 120° L.T.
6 x Hydrazine Detachment Manifold
Mass = 400 kg
Ejection Force = 100 N

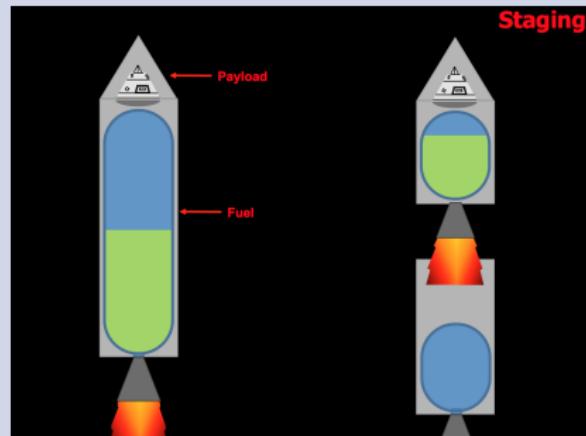


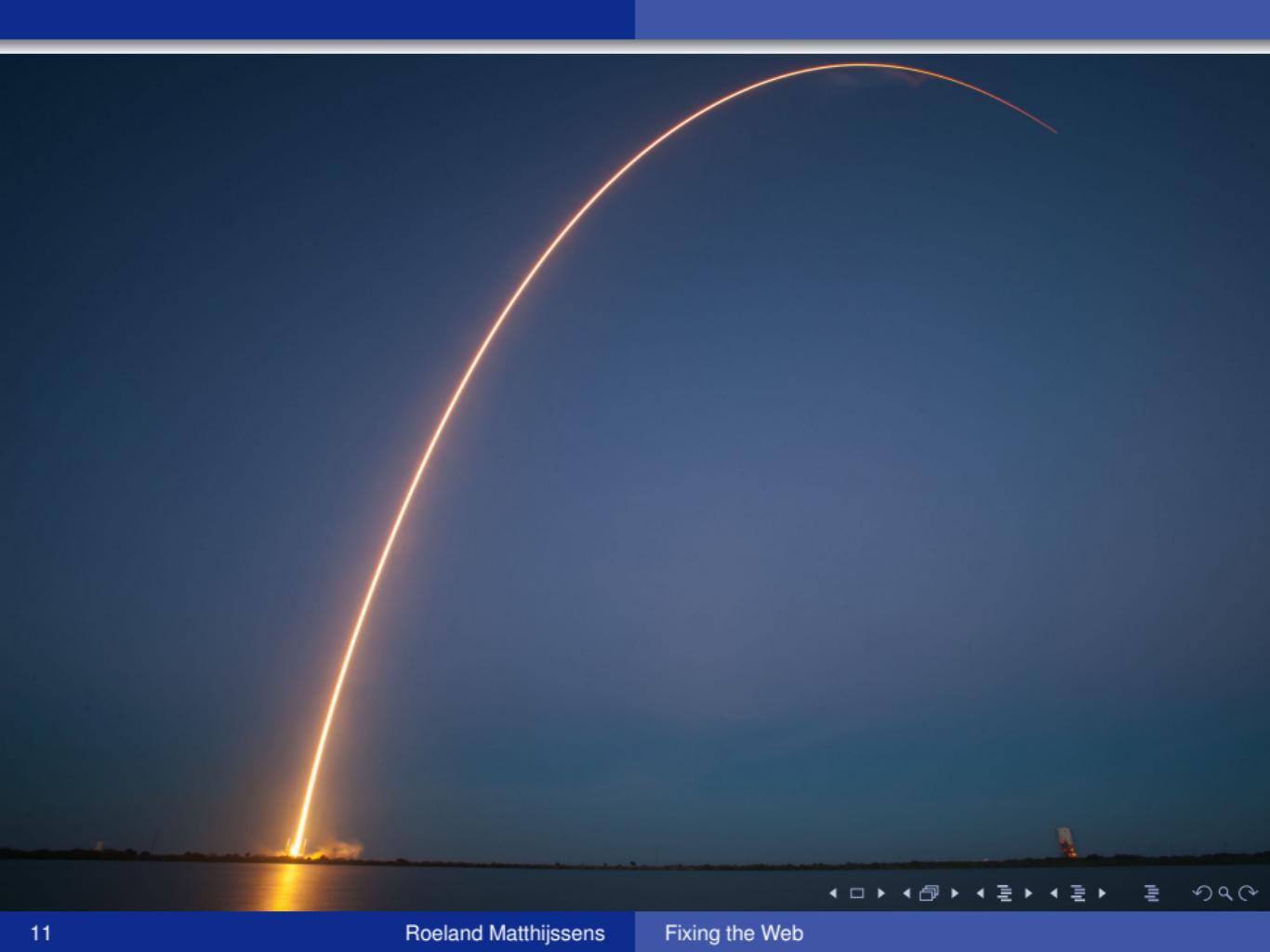
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Staging



Staging

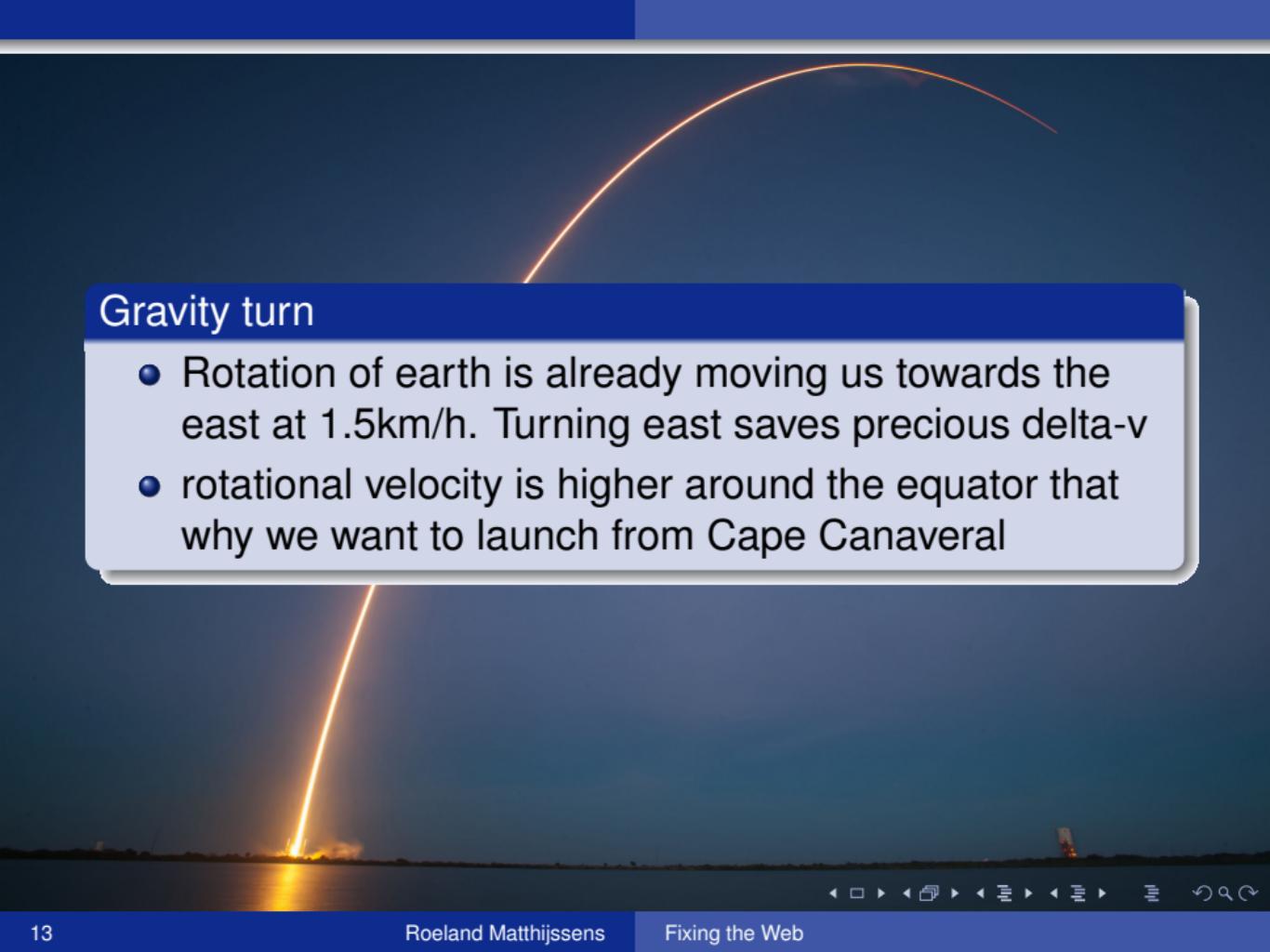




Getting into orbit

Why do we turn

- Going straight up gains altitude quickly
- But we would just fall down again
- To get into orbit we need to move lateral as well
- combining vectors is efficient: $a^2 + b^2 = c^2$



Gravity turn

- Rotation of earth is already moving us towards the east at 1.5km/h. Turning east saves precious delta-v
- rotational velocity is higher around the equator that why we want to launch from Cape Canaveral

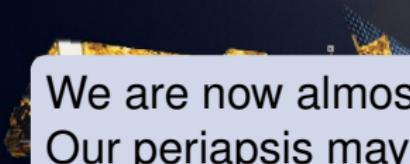
Let's Launch

How do we do it

- throttle up
- point eastwards (about 5degrees)
- don't. touch. anything. let gravity do it's work
- activate staging at the appropriate times
- keep apoapsis in front of you until desired height
- circularize orbit
- It easy, it's not ro... oh...



About that circulizing



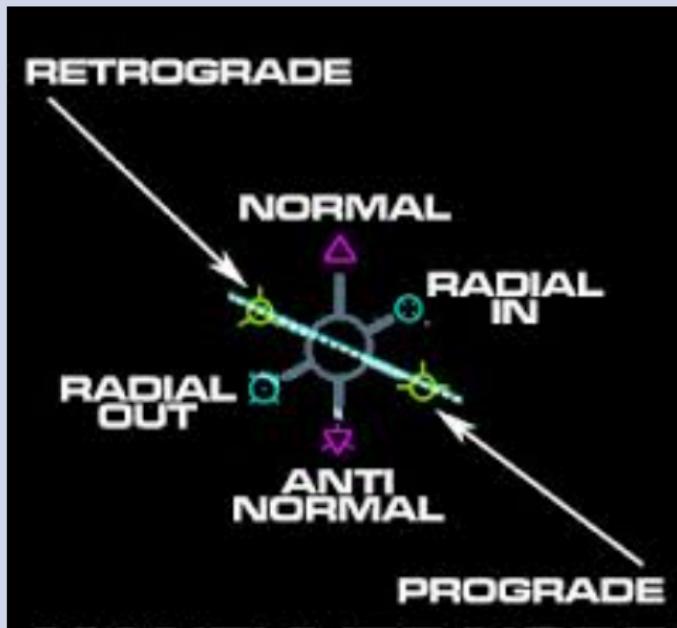
We are now almost in low earth orbit but still falling down. Our periapsis may still be within the atmosphere. So we need to learn how to manipulate our orbit while in space.

Basics

Movement on an orbit generally affects the opposite side of the orbit.

Adjusting Orbits

At any point on the orbit you can burn in 3 directions.
up/down, left/right, forwards/backwards



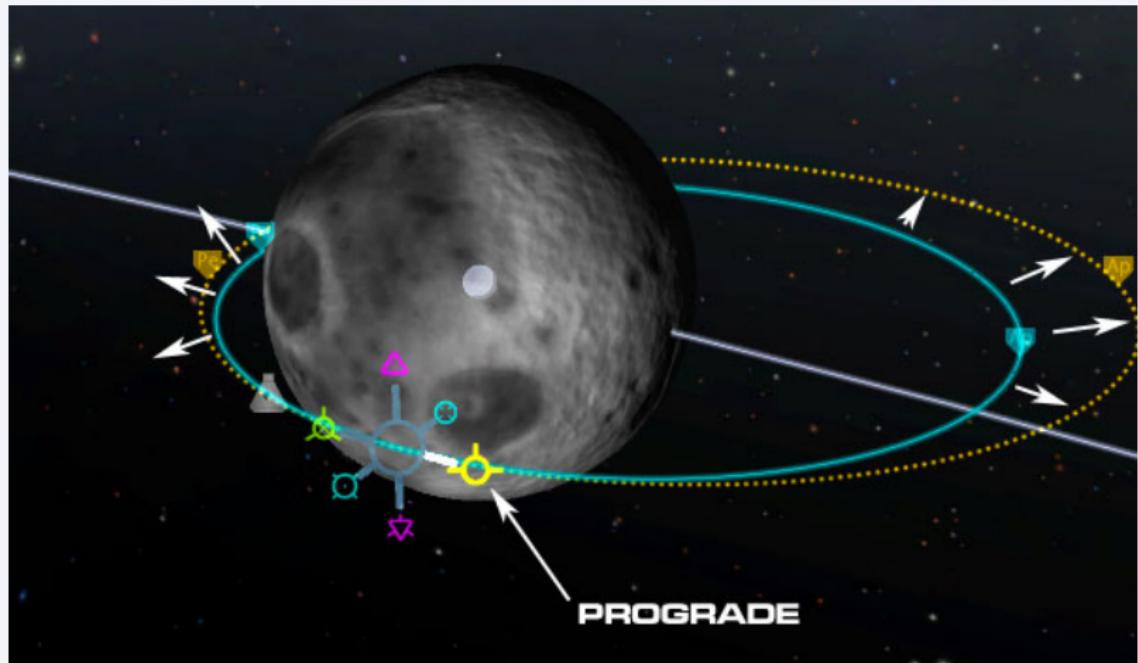
Low Orbit

Maneuvering in space

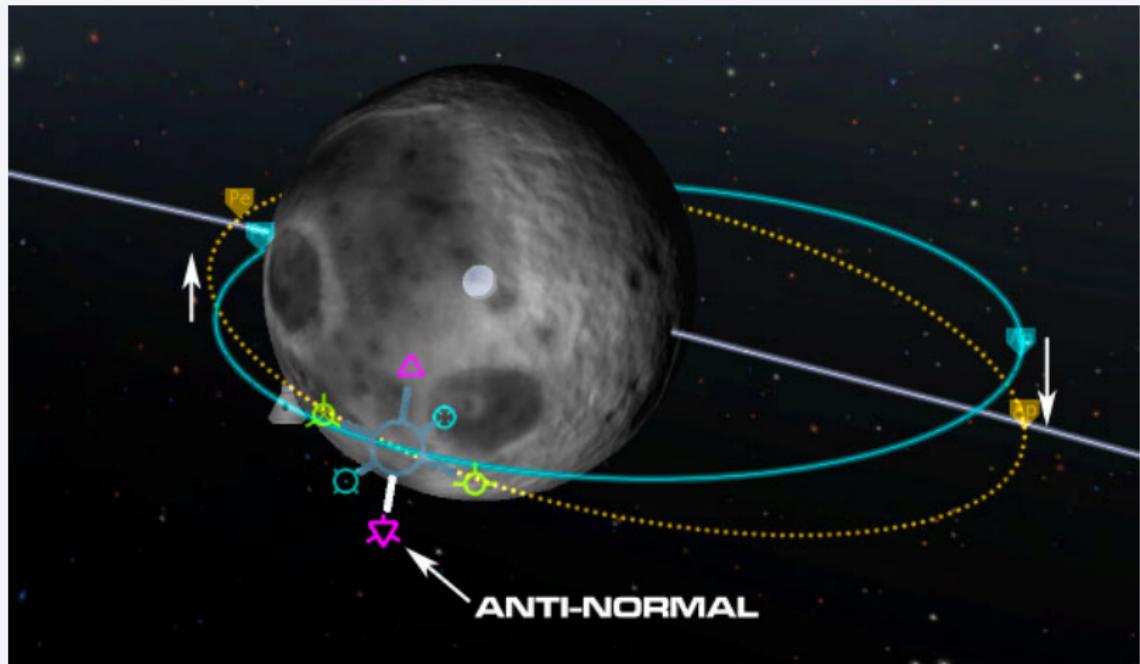
- prograde Along your movement vector, used to increase orbit altitude
- retrograde Opposite your movement vector, used to decrease orbit altitude
- normal Perpendicular to orbit, used to increase/decrease inclination
- anti-normal perpendicular to orbit, used to increase/decrease inclination
- radial Towards parent body, Used to shift orbit around
- anti-radial Away from parent body, used to shift orbit around



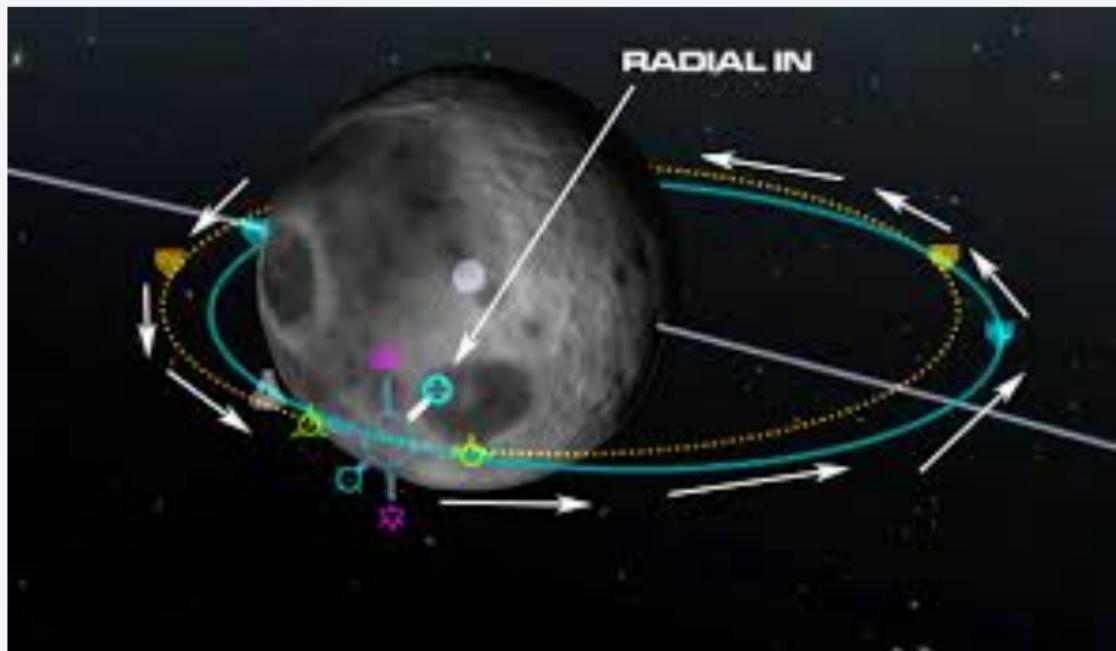
Prograde



Normal



Radial



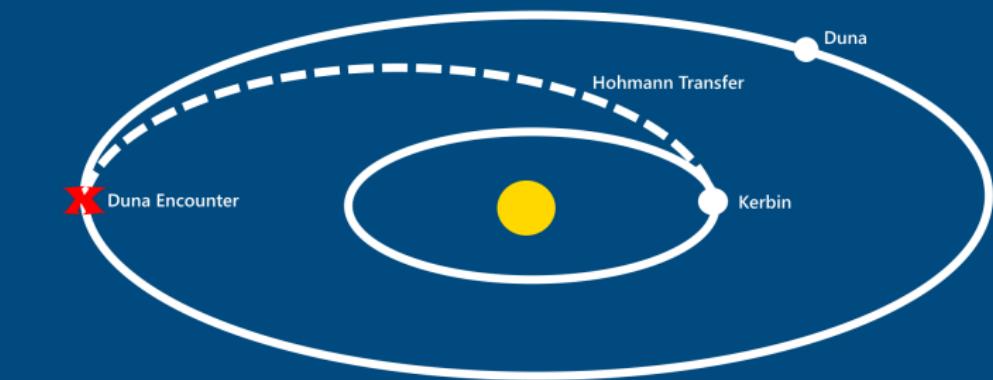
Planning Transfe

Finally achieved a stable low earth orbit. We need to plan our transfer to our target body



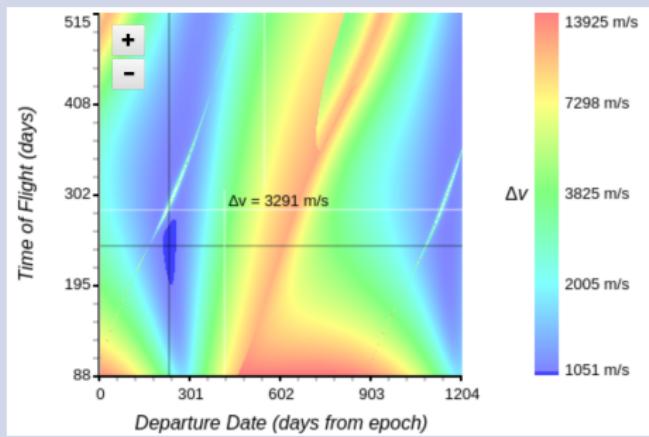
Hohmann transfer

Now that we know our target and know the delta-v required to get there we need to plan the encounter



Hohmann transfer window

To be able to transfer with the least amount of delta-v as possible we need to launch when the target body is at an exact position relative to us. If we are on a strict delta-v budget we need to wait for a good window



Oberth Effect

$$V = V_0 + at$$

$$X = X_0 + V_0 t + at^2/2$$

$$V^2 - V_0^2 = 2a(X - X_0)$$

$$\bar{V} = \frac{V_f + V_i}{2}$$

$$\Delta X = \bar{V} \Delta t$$

~~$$\vec{F}_{\text{tot}} = m \vec{a}$$~~

$$W = F d_{\parallel} = F_I d$$

$$W_{\text{tot}} = \Delta(\text{KE})$$

$$\Delta U = -W_{\text{if}}$$

$$\frac{1}{2} kx^2$$

$$\omega = \sqrt{\frac{k}{m}}$$

$$p = m v$$

$$\vec{P}_{\text{int}} = \vec{P}_{\text{final}}$$

$$\left(\sum_i m_i \vec{v}_j \right) = \left(\sum_i m_i \vec{v}_j \right)$$

$$v_x = v \cos(\theta)$$

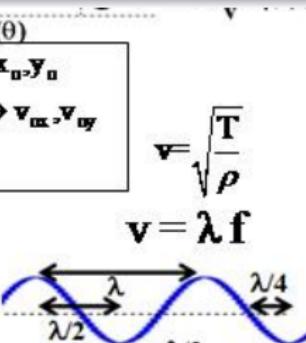
$$x \rightarrow x, y \quad x_0 \rightarrow x_0, y_0$$

$$v \rightarrow v_x, v_y \quad v_0 \rightarrow v_{0x}, v_{0y}$$

$$a \rightarrow a_x, a_y$$

$$\mu N$$

$$a = \frac{v^2}{R}$$



$$E = K + U$$

$$E_i = E_f$$

$$\frac{1}{2}mv^2$$

$$\Delta Q = (\text{quant.}) C_{\text{cond.}} \Delta T$$

$$\Delta Q_{\text{intro}} = \Delta W_{\text{by}} + \Delta E$$

$$\frac{RT}{2} \mid_{\text{deg freedom}}$$

$$C_p = C_v + R$$

$$x = A \cos(\omega t) \quad \text{(or)} \quad x = A \sin(\omega t)$$

$$v = A\omega \sin(\omega t) \quad \text{(or)} \quad v = A\omega \cos(\omega t)$$

$$a = A\omega^2 \cos(\omega t) \quad \text{(or)} \quad a = -A\omega^2 \sin(\omega t)$$

$$M_e = 5.97(10)^{24} \text{ Kg}$$

$$R_e = 6.37(10)^6 \text{ m}$$

$$\frac{GM_e}{R_e} = g R_e$$

$$\frac{GMm}{r^2}$$

$$\frac{GMm}{r}$$

$$V = \omega r$$

$$a = \alpha r$$

$$\omega = \omega_0 + \alpha t$$

$$I = \sum_i m_i r_i^2$$

$$\theta = \theta_0 + \omega_0 t + \frac{1}{2} \alpha t^2$$

$$\omega^2 - \omega_0^2 = 2\alpha(\theta - \theta_0)$$

$$L = I p = m v r_\perp$$

$$L = I \omega$$

$$\tau = \frac{\Delta L}{\Delta t}$$

$$\frac{1}{2} I \omega^2$$

$$\sum_i \vec{F}_i = 0$$

$$\sum_i \tau_i = 0$$

$$\Delta S \geq 0$$

$$\Delta Q = 1 \Delta (\text{quant.})$$

$$PV = nRT$$

$$e = \frac{\Delta W}{\Delta Q}$$

$$e = 1 - \frac{T_L}{T_H}$$

$$P = \frac{F}{A}$$

$$M = \rho V$$

$$P_1 = P_2$$

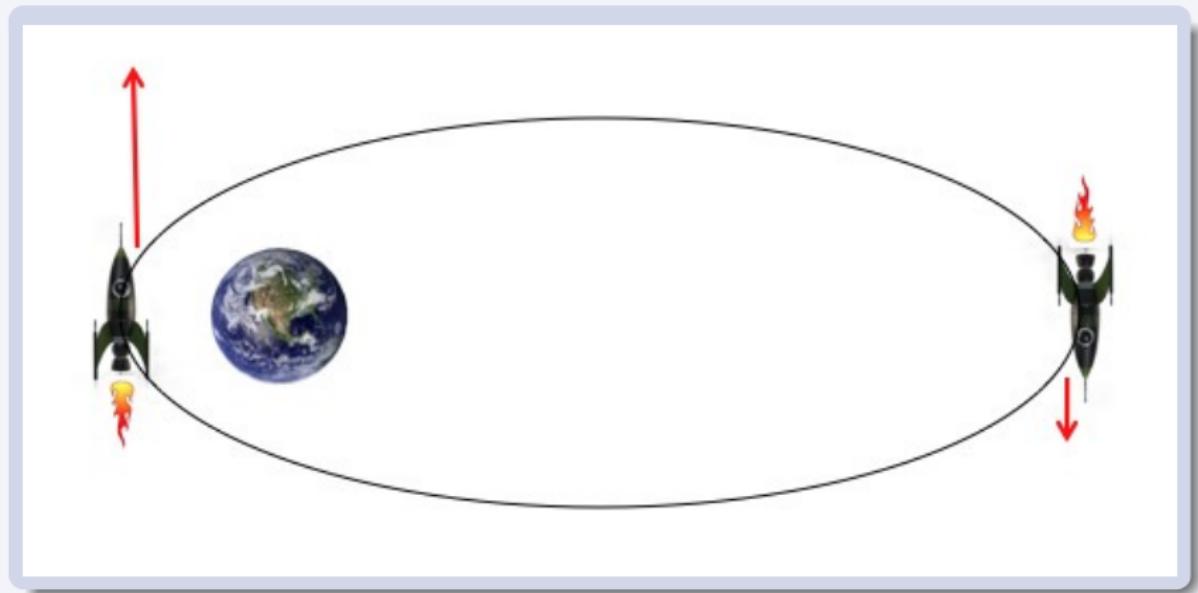
$$\Delta P = \rho g \Delta h$$

$$B = \rho_{\text{liq}} V_{\text{disp}} g$$

$$A_1 v_1 = A_2 v_2$$

$$p + \frac{1}{2} \rho v^2 = \text{const}$$

JK, Oberth Effect



Oberth Effect explained

- things that go fast have higher energy

- $KE = 0.5 * m * v^2$

- mass is a form of energy

- $E = MC^2$

- Newton's third law

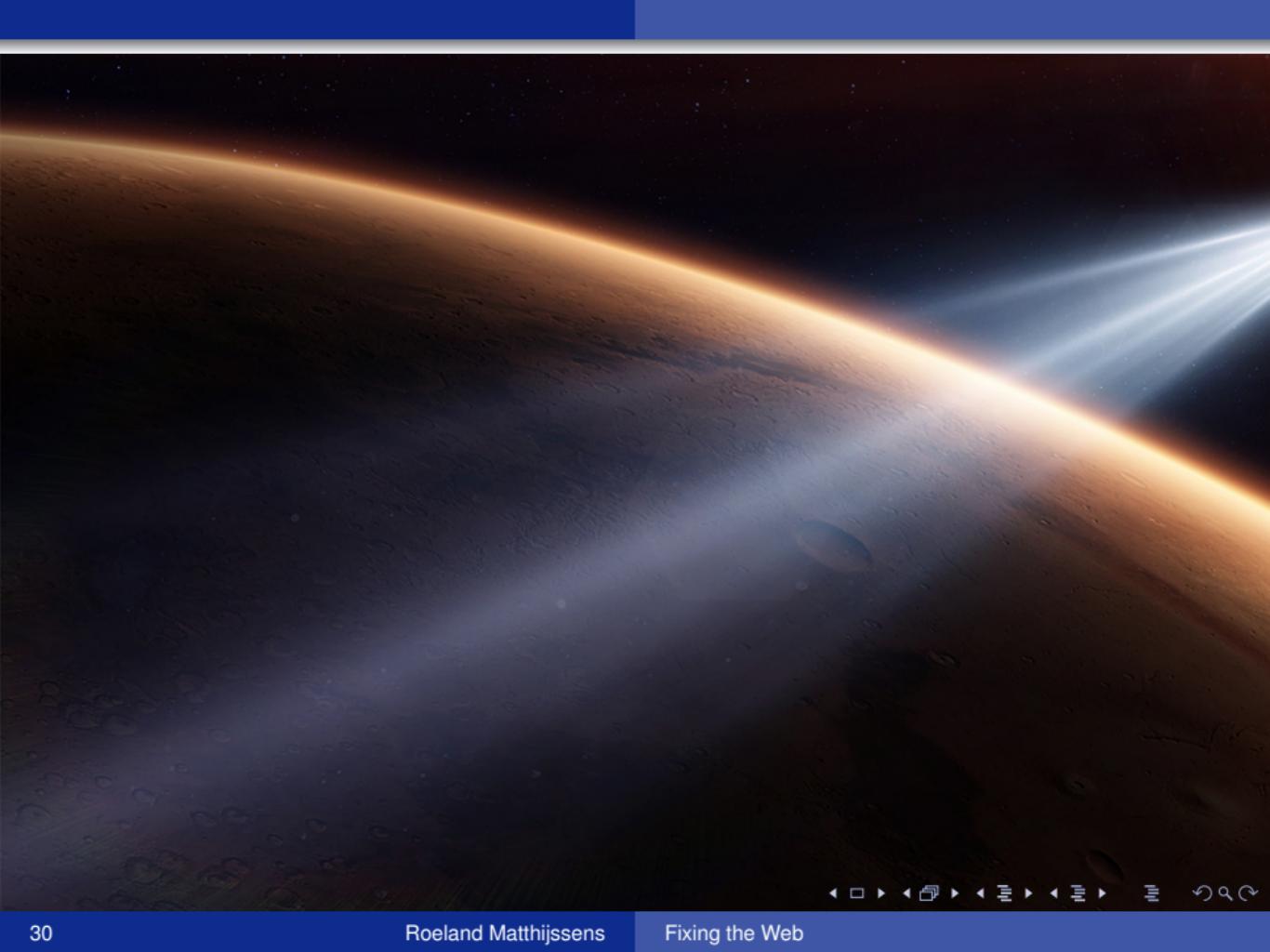
- $F_a = -F_b$

Dumping mass (fuel) while deep in the gravity well (going fast) gives more kinetic energy to the ship This is an oversimplification

Escape

Now that we know how to make optimal use of the Oberth effect we can begin our escape burn and start our transfer orbit

- decelerate to drop periapsis deeper into the gravity well
- wait for periapsis (maximal use of Oberth effect)
- make transfer burn and coast to encounter



Sphere Of Influence

Sphere Of Influence(SOI) is the region around a planet in which the gravitational pull from the planet is bigger than any other body's gravitational pull. Which planet/body has the most gravitational influence on you

- We are in the SOI of the sun
- The moon is also influenced by the gravity of the sun
- but it is close enough to earth so that our gravitational influence is higher than the sun's
- therefore we say that the moon is within the SOI of earth

Intercept

When we are within the gravitational sphere of influence of the target planet we need to slow down to be captured by the planet.

- Burn retrograde to slow down
- Keep slowing down until you fall into a highly elliptical orbit
- keep dropping periapsis to desired height
- wait for periapsis and then circularize orbit

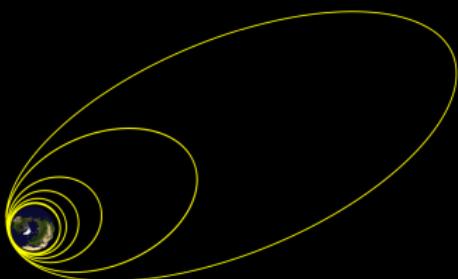
Intercept

Aerobreaking

Instead of having to circularize your orbit (which takes a fair amount of delta-v) we can make use of the body's atmosphere to slow down to do this you need to

- drop periapsis just inside of the atmosphere
- not too deep because you can burn up
- not too shallow because slowing down would take a very long time
- just wait a couple of orbits
- the apoapsis should drop on every orbit because atmospheric drag slows you down while at periapsis

Aerobraking

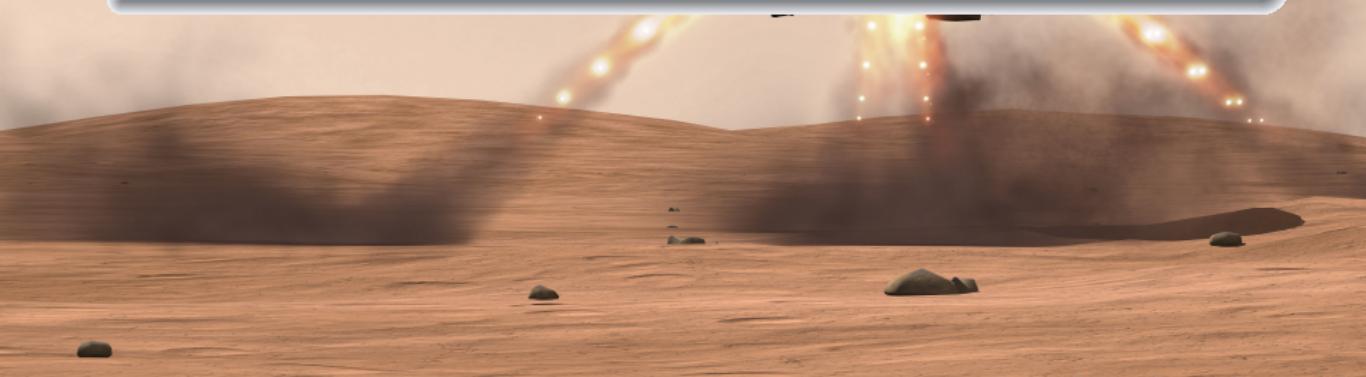




Landing

Entering atmosphere

- determine entry angle
- not to steep => too much atmospheric drag => burning up
- not to shallow => won't slow down quickly enough => skipping out of atmosphere



Landing

Suicide Burn

We need to slow down our descent before we hit the ground. At the last possible second we fire all engines at 100% throttle.

Why?

- Gravity is an accelerating force adding $\alpha m/s^2$
- Every second spent decelerating needs to be compensated for gravity
- Slowing down means burning an additional α delta-v every second
- Slowing down quickly saves fuel.

