

1) $\text{sum}(\text{theta})/n$

theta is a vector of n values drawn from $p(\text{theta}|y)$

$g(\text{theta})$ and $p(\text{theta})$ are not required in this case

```
In [1]: using Distributions;
        using Gadfly;
```

2

a) $p(x) = \text{unif}(1,7) = 1/6;$
 $g(x) = 6 f(x) = 6 x^2 e^{-x}$

b)

1) $p(x) \geq 0;$

2) $\int p(x) dx = 1$

3) $g(x)$ is a factor of x such that $g(x)$

c)

1) Initialize x_1, \dots, x_n to 0's

2) for $i = 1 \dots n$ times

3) Draw $x_i \sim \text{unif}(1,7)$

4)end

5) $sn = 6 * \text{sum}(x_1, \dots, x_n)/n$

6) return sn

d)

```
In [2]: n=10000;
        delta=6;
        f(x) = (x^2.7)*(e^-x);
        x = rand(Uniform(1, 7), n);
        S = sum(delta.*f.(x))/n
```

Out[2]: 3.797650977086129

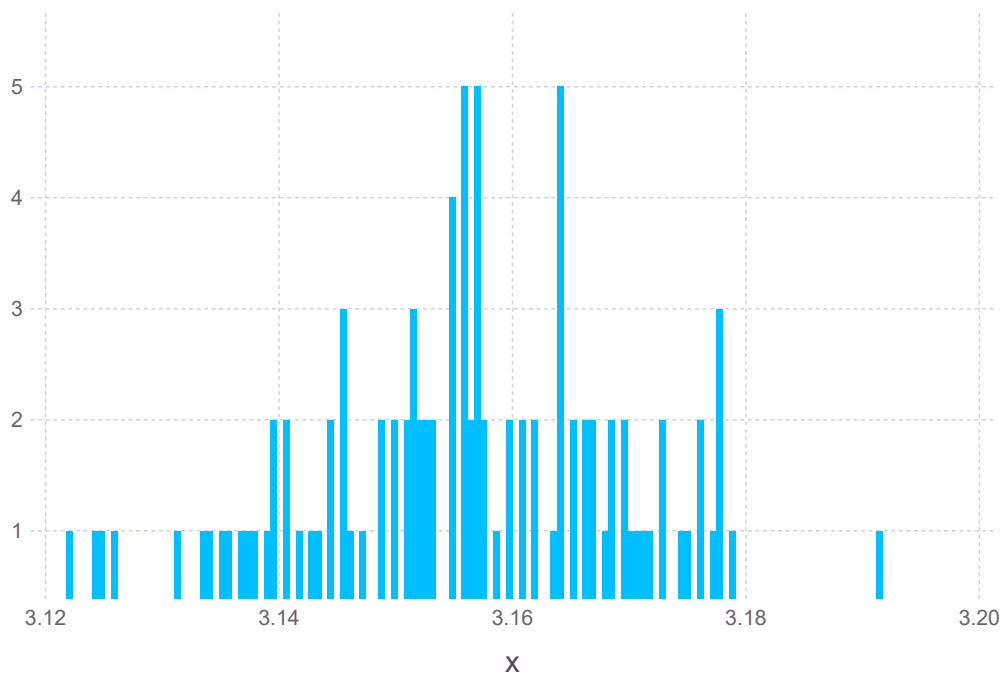
e)

```
In [14]: n = 10000;
delta = 5;
S = zeros(100);
for i= 1:100
    x = rand(Uniform(1, 7), n);
    S[i] = sum(delta.*f.(x))/n;
end
mean(S), var(S)
```

Out[14]: (3.1556872756238556, 0.00015674075078885727)

```
In [5]: plot(layer(x=S, Geom.histogram))
```

Out[5]:

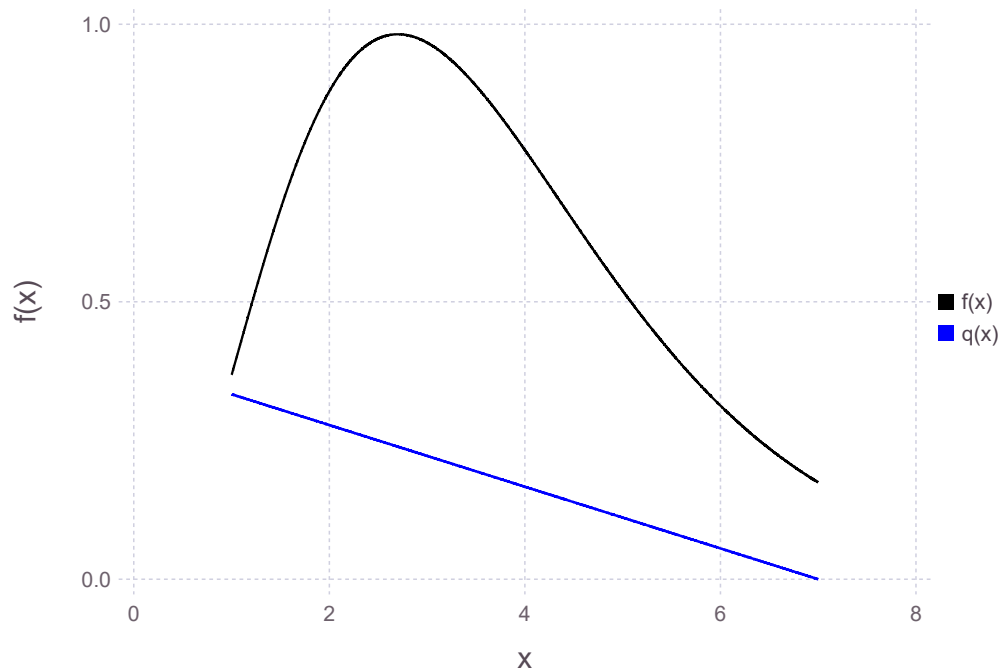


3) a)

```
In [6]: x = collect(1:0.01:7);
f(x) = (x^2.7)*(e^-x);
q(x) = (7-x)/18;
```

```
In [15]: plot(  
  layer(x=x,y=f.(x),Geom.line,Theme(default_color=colorant"black")),  
  layer(x=x,y=q.(x),Geom.line,Theme(default_color=colorant"blue")),  
  Guide.ylabel("f(x)"),Guide.xlabel("x"),Coord.Cartesian(xmin=0, xmax=8),  
  Guide.manual_color_key("", ["f(x)", "q(x)"], ["black", "blue"]))
```

Out[15]:



b)

1) Initialize x_1, \dots, x_n to 0's

2) for $i = 1 \dots n$ times

3) Draw $x_i \sim q(x)$

4)end

5) $s_n = \sum (f(x_i)/q(x_i))/n$

6) return s_n

$$f(x) = (x^{2.7}) * (e^{-x});$$

$$q(x) = (7-x)/18;$$

c)

```
In [10]: function accept_reject_method(n)
    x = 1:0.01:7;
    f(x) = (7-x)/18;
    g(x) = pdf(Uniform(1,7),x);
    M = maximum(f.(x)./g.(x));
    count = 0;
    samples = [];
    while(count < n)
        y = rand(Uniform(1,7));
        u = rand(Uniform(0,1));
        if(u < f(y)/(M*g(y)))
            samples = [samples; y];
            count += 1;
        end
    end
    return samples;
end
```

Out[10]: accept_reject_method (generic function with 1 method)

```
In [11]: f(x) = (x^2.7)*(e^-x);
    q(x) = (7-x)/18;
    n = 10000;
    x = accept_reject_method(n);
    S = sum(f.(x)./(q.(x)))/length(x)
```

Out[11]: 3.776183033867579

d)

```
In [13]: n = 10000;
    f(x) = (x^2.7)*(e^-x);
    p(x) = (7-x)/18;
    S = zeros(100);
    for i = 1:100
        x = accept_reject_method(n);
        S[i] = sum(f.(x)./(p.(x)))/n;
    end
    mean(S), var(S)
```

Out[13]: (3.7841925791854165, 0.0004192997783983889)

4)

Ordinary Monte Carlo Integration has less variance compared to estimate generated by importance sampling because shaoe factor is not solely responsible for reducing variance.

