

PageRank with random walkers

- Start random surfers **at all pages** with **equal probability** $\frac{1}{n}$

$$\vec{v}_0 = [1/n, 1/n, \dots, 1/n].$$

- **After one step**, the distribution will be

$$\vec{v}_1 = M\vec{v}_0.$$

- **After k steps:**

$$\vec{v}_k = M^k \vec{v}_0.$$

- **Markov process:** The distribution approaches a limiting distribution \vec{v} such that $\vec{v} = M\vec{v}$ if
 - The graph is **strongly connected**: can get from a node to any other node.
 - No **dead ends**: nodes that have no out-links.