

Positive Linear System

- ▶ The spectrum of the matrix \mathbf{A} (e.g., the Perron-Frobenius eigenvalue and eigenvectors) provides insights on fairness, rate of convergence and transient response: ¹⁴

$$\lim_{k \rightarrow \infty} w(k) = \left(\frac{\alpha_1}{1 - \beta_1}, \dots, \frac{\alpha_n}{1 - \beta_n} \right)^T,$$

which, if specialized to the case of $\alpha_i = 1$ and $\beta_i = 0.5$ for all i , is proportional to the all-ones vector as it should be

- ▶ Fairness line as Perron-Frobenius right eigenvector
- ▶ Classical power method algorithm can simulate AIMD and to visualize the iterates as shown in Figure 2

¹⁴Abraham Berman, Robert Shorten, and Douglas Leith. Positive matrices associated with synchronised communication networks. *Linear Algebra and its Applications*, 393:47–54, 2004.