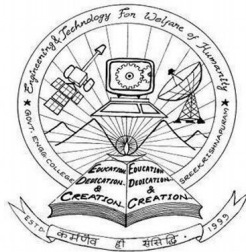


ITT201 Data Structures

Module 3: Stacks and Queues



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Acknowledgements

- All the pictures are taken from the Internet using Google search.
- Wikipedia also referred.

Lecture 13

We Saw & Will See

Till Now We Saw...

- Module 1 : Introduction to Data Structures
 - Concept, Classification - ADT, CDT, Linear/Non-linear DS
 - Searching - Linear and Binary Searches
 - $O(n^2)$ Sorting Algorithms - Bubble, Selection, Insertion
 - $O(n \log n)$ Sorting Algorithms- Merge Sort, Quick Sort

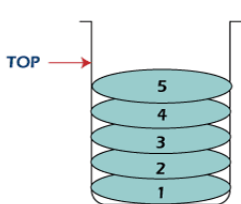
Today We Will See...

- Module 3 : Stacks and Queues
 - Stack using Array

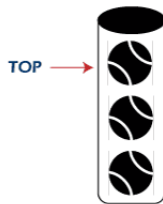
Stack Examples



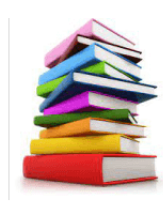
Stack of Coins



Stack of Plates

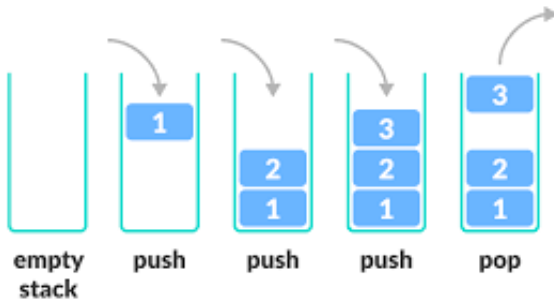


Can of Tennis Balls



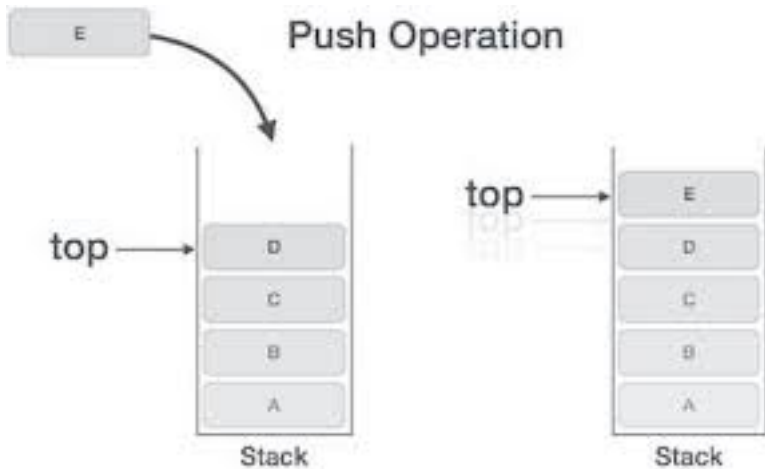
Stack of Books

Stack operations

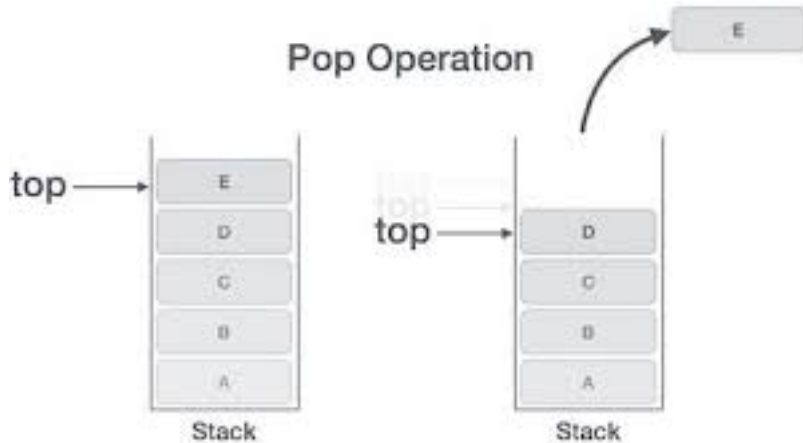


- Stack is a LIFO or FILO
- Insertion in Stack - Push
- Deletion in Stack - Pop

Push

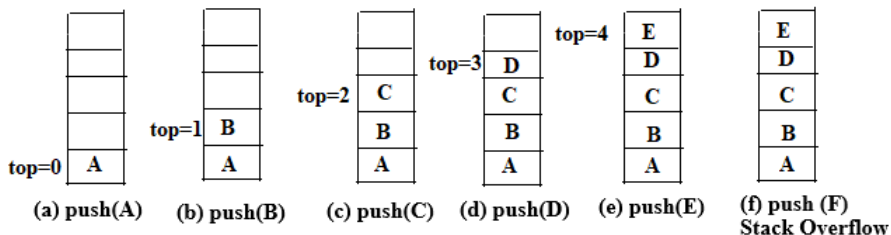


Pop



Stack Overflow

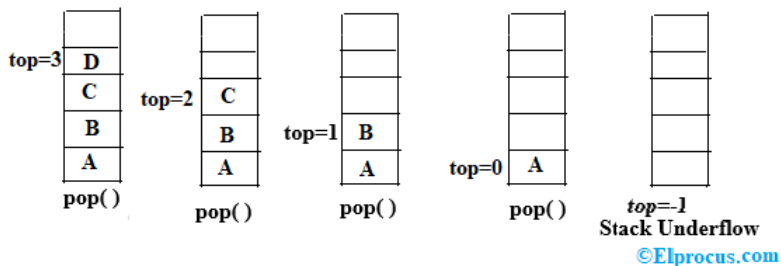
- Stack Overflow happens when we try to push an item to a stack that is full.



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Stack Underflow

- Stack Underflow happens when we try to pop an item from a stack that is empty.



isEmpty() & isFull()

- top is used to point to the top most element in the stack
- $\text{top} = -1$, indicates that the stack is Empty
- $\text{top} = n - 1$, indicates that a stack of size n is Full

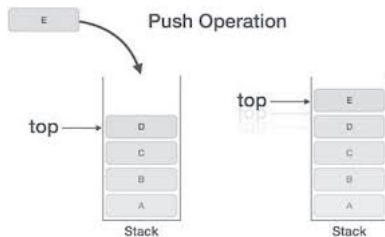
```
int isEmpty( )
{
    if(top == -1)
        return 1;
    else
        return 0;
}
```

```
int isFull()
{
    if(top == n-1)
        return 1;
    else
        return 0;
}
```

Push(int x)

Consider an integer stack $S[n]$ to which an element x is pushed

```
void push(int x)
{
    if( !isFull() ){
        top++;
        S[top] = x;
    }
}
```

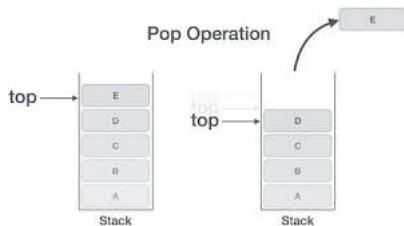


Pop()

Consider an integer stack $S[n]$ from which an element is popped

```
int pop( )
```

```
{  
    if( !isEmpty() ){  
        x = S[top];  
        top--;  
        return x;  
    }  
}
```



Lecture 14

We Saw & Will See

Till Now We Saw...

- Module 1 : Introduction to Data Structures
 - Concept, Classification - ADT, CDT, Linear/Non-linear DS
 - Searching - Linear and Binary Searches
 - $O(n^2)$ Sorting Algorithms - Bubble, Selection, Insertion
 - $O(n \log n)$ Sorting Algorithms- Merge Sort, Quick Sort
- Module 3 : Stacks and Queues
 - Stack using Array

Today We Will See...

- Queue using Array

Queue Example



Queue operations



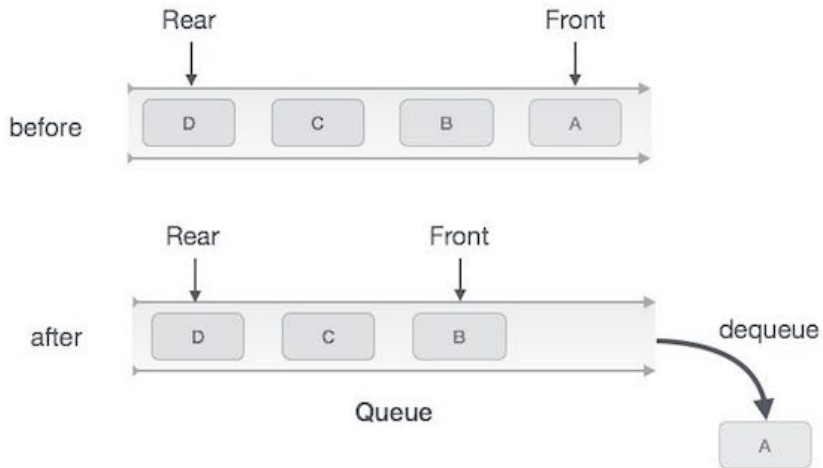
- Queue is a FIFO or LILO
- Insertion in Queue - EnQueue
- Deletion in Queue - DeQueue

EnQueue



Queue Enqueue

DeQueue



Queue Dequeue

Queue Overflow and Underflow

- Queue Overflow happens when we try to EnQueue an item to a Queue that is Full.
- Queue Underflow happens when we try to DeQueue an item from a Queue that is empty.

isQEmpty() & isQFull()

- **front** is used to point to the item at the start of the Queue
- **rear** is used to point to the item at the end of the Queue
- $\text{front} = -1$ & $\text{rear} = -1$, indicates that the Queue is Empty
- $\text{rear} = n - 1$, indicates that Queue of size n is Full

```
int isQEmpty( )
{
    if(front == -1)
        return 1;
    else
        return 0;
}
```

```
int isQFull( )
{
    if(rear == n-1)
        return 1;
    else
        return 0;
}
```

EnQueue(int x)

Consider an integer Queue $Q[n]$ to which an element x is enqueued .

```
void EnQueue(int x)
{
    if( !isFull() ){
        rear++;
        Q[rear] = x;
    }
    if(front == -1)
        front = 0;
}
```

DeQueue()

Consider an integer Queue $Q[n]$ from which an element is dequeued.

Try Writing this by your own! Submit to me in Whatsapp.

- Think if we need to check for any extra condition similar to the one we did in EnQueue() !

```
int DeQueue( )
{
    if( !isEmpty() ){
        x = Q[front];
        front++;
        return x;
    }
    if(front > rear)
        front = rear = -1;
}
```

Lecture 15

We Saw & Will See

Till Now We Saw...

- Module 1 : Introduction to Data Structures
 - Concept, Classification - ADT, CDT, Linear/Non-linear DS
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- Module 3 : Stacks and Queues
 - Stack using Array
 - Queue using Array

Today We Will See...

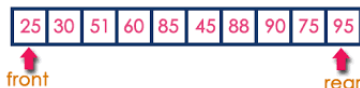
- Circular Queue using Array

Queue Example



Limitation of Queue using Array

Queue is Full



Queue is Full (Even three elements are deleted)



- Queue is Full when $\text{rear} = n - 1$, irrespective of where front is.
- There may still be some vacant spaces, in worst case it is $n - 1$

Solution:

- Fix $\text{front} = 0$, shift all elements left after a DeQueue (Not Efficient)
- Use **Circular Queue!** ✓

Circular Queue Using Array Example

Circular Queues in Data Structure

Size = 6

front, rear = -1



Enqueue (10)



Enqueue (20)



Enqueue (30)



Enqueue (40)



Enqueue (50)



Dequeue()



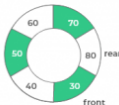
Dequeue()



Enqueue(60)



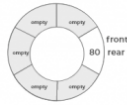
Enqueue(70)



Enqueue(80)



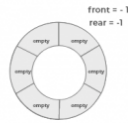
Enqueue(90)



Dequeue() - 5 times



Dequeue()



Dequeue()

Can't Enqueue Overflow !

Can't Dequeue Underflow !

EnQueue & DeQueue in Circular Queue

Circular Queue using Array in C



Enqueue (50)

Enqueue() $\text{rear} = (\text{rear} + 1) \% \text{SIZE};$

Dequeue() $\text{front} = (\text{front} + 1) \% \text{SIZE};$



Dequeue()

Queue Overflow and Underflow

- Circular Queue Overflow happens when we try to EnQueue an item to a Circular Queue that is Full, i.e with n items.
- Circular Queue Underflow happens when we try to DeQueue an item from a Circular Queue that is empty.

isCQEmpty() & isCQFull()

- **front** is used to point to the item at the start of the Queue
- **rear** is used to point to the item at the end of the Queue
- Conditions for Circular Queue being Full and Empty ??

```
int isCQFull( )
{
    if((rear+1)%n == front)
        return 1;
    else
        return 0;
}
```

```
int isCQEmpty( )
{
    if(front == -1)
        return 1;
    else
        return 0;
}
```

EnQueue(int x)

Consider an integer Queue $Q[n]$ to which an element x is enqueued .

```
void EnQueue(int x)
{
    if( !isCQFull() ){
        rear= (rear+1)%n;;
        Q[rear] = x;
    }
    if(front == -1)
        front = 0;
}
```


DeQueue()

Consider an integer Circular Queue $Q[n]$ from which an element is dequeued.

```
int DeQueue( )
{
    if( !isCQEmpty() ){
        x = Q[front];
        front=(front+1)%n;
        return x;
    }
    if((rear+1)%n == front)
        front = rear = -1;
}
```

Lecture 16

We Saw & Will See

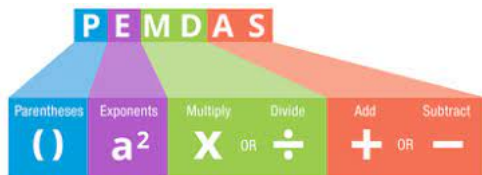
Till Now We Saw...

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 - $O(n \log n)$ Sorting Algorithms- Merge Sort, Quick Sort
- Module 3 : Stacks and Queues
 - Stack using Array
 - Queue, Circular Queue using Array

Today We Will See...

- Infix, Prefix and Postfix Expressions

PEMDAS rule



Order of Operations

PEMDAS

P	P arenthesis, $()$
E	E xponents, a^n
M D	M ultiplication or D ivision (Left to right)
A S	A ddition or S ubtraction (Left to Right)

Evaluation example

Evaluate the expression:

$$9^2 + 3 \bullet (9-5)^2 / 4$$

$$9^2 + 3 \bullet \underline{(9-5)}^2 / 4$$

Parenthesis

$$\underline{9}^2 + 3 \bullet \underline{4}^2 / 4$$

Exponents

$$\downarrow \quad \downarrow$$

$$81 + 3 \bullet \underline{16} / 4$$

Multiplication

$$\downarrow$$

$$81 + \underline{48 / 4}$$

Division

Steps to find Prefix/Postfix expression from any given Infix Expression

- Identify the order of expression evaluation in the given Infix expression using PEMDAS rule.
- Put Parenthesis corresponding to each operation in that order. i.e. for each operator identify the two parts in the given expression that is involved and put parenthesis

Prefix Expression

- Replace all open parenthesis with its corresponding operator. Then remove all closing parenthesis as well as operators to get the Prefix expression.

Postfix Expression

- Replace all close parenthesis with its corresponding operator. Then remove all opening parenthesis as well as operators to get the Postfix expression.

Lecture 17

We Saw & Will See

Till Now We Saw...

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 - $O(n \log n)$ Sorting Algorithms- Merge Sort, Quick Sort
- Module 3 : Stacks and Queues
 - Stack using Array
 - Queue, Circular Queue using Array
 - Infix, Prefix and Postfix Expressions

Today We Will See...

- Evaluation of Postfix Expression
- Infix to Postfix using Stack

Algorithm to Evaluate a Postfix Expression

```

opndstk = the empty stack
/* scan the input string reading one element */
/* at a time into symb */
while (not end of input) {

    symb = next input character;

    if (symb is an operand)
        push(opndstk, symb)

    else {
        /* symb is an operator */
        op2 = pop(opndstk);
        op1 = pop(opndstk);
        value = result of applying symb to op1 & op2
        push(opndstk, value);
    } /* end else */

} /* end while */
return (pop(opndstk));

```

Example:

Postfix Expression: 6 2 3 + - 3 8 2 / + * 2 \$ 3 +

symb	opnd1	opnd2	value	opndstk
6				6
2				6,2
3				6,2,3
+	2	3	5	6,5
-	6	5	1	1
3	6	5	1	1,3
8	6	5	1	1,3,8
2	6	5	1	1,3,8,2
/	8	2	4	1,3,4
+	3	4	7	1,7
*	1	7	7	7
2	1	7	7	7,2
\$	7	2	49	49
3	7	2	49	49,3
+	49	3	52	52

Infix to Postfix Algorithm

- Scan the infix expression from left to right.
- If the scanned character is an operand, output it.
- Else,
 - If the precedence operator is greater than the precedence of the operator in the stacktop(or if stack is empty or contains a '('), then Push it.
 - Else, Pop all the operators from the stack which are greater than or equal to in precedence . After doing that ,Push the scanned operator to the stack. (If you encounter parenthesis while Pop, then stop there and Push the scanned operator in the stack.)
- If the scanned character is an '(', push it to the stack.
- If the scanned character is an ')', pop the stack and output it until a '(' is encountered, and discard both the parenthesis.
- Repeat the process until the infix expression is fully scanned.
- Pop and output from the stack until it is not empty.

Infix to Postfix using Stack - Example1

	RPN	Stack	Input Expression		RPN	Stack	Input Expression
①			A+(B*(C-D)/E)	⑨	ABC	(* (D)/E)
②	A		+(B*(C-D)/E)	⑩	ABCD	(* (+) /E)
③	A	+	(B*(C-D)/E)	⑪	ABCD-	* (+	/E)
④	A	(+	B*(C-D)/E)	⑫	ABCD-*	/ (+	E)
⑤	AB	(+	*(C-D)/E)	⑬	ABCD-*E	/ (+)
⑥	AB	* (+	(C-D)/E)	⑭	ABCD-*E/	+	
⑦	AB	(* (+	C-D)/E)	⑮	ABCD-*E/+		
⑧	ABC	(* (+	-D)/E)				

Infix to Postfix using Stack - Example2

Suppose we want to convert $2*3/(2-1)+5*3$ into Postfix form,

Expression	Stack	Output
2	Empty	2
*	*	2
3	*	23
/	/	23*
(/(23*
2	/(23*2
-	/(-	23*2
1	/(-	23*21
)	/	23*21-
+	+	23*21-/
5	+	23*21-/5
*	++	23*21-/53
3	++	23*21-/53
	Empty	23*21-/53*+

So, the Postfix Expression is $23*21-/53*+$

Lecture 18

We Saw & Will See

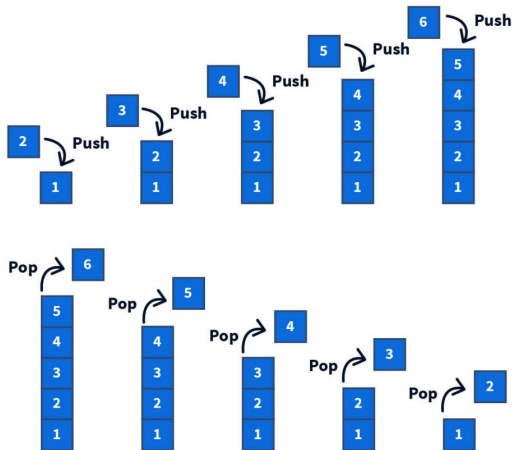
Till Now We Saw...

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 - Queue, Circular Queue using Array
 - Infix, Prefix and Postfix Expressions
 - Evaluation of Postfix Expression
 - Infix to Postfix using Stack

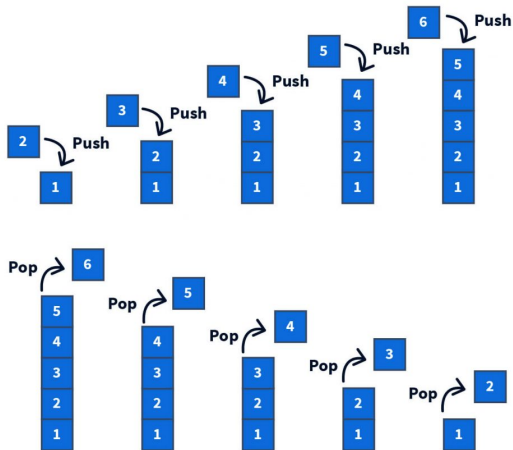
Today We Will See...

- Stack Applications - Reversal, Parenthesis Matching
- More on Queues - Double Ended Queue, Priority Queue

Reversal using Stack



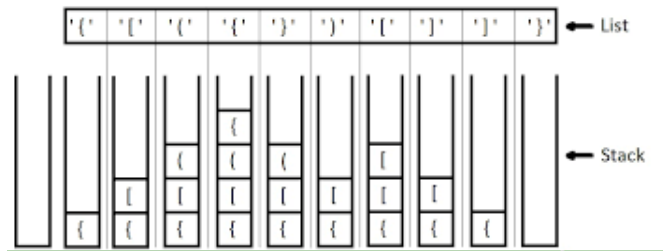
Reversal using Stack



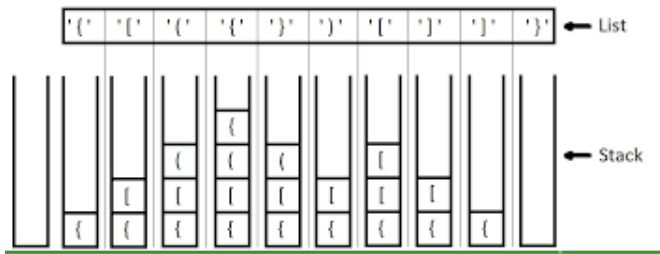
SCALER
By InterviewBit

- Push all characters of string from left to right to the Stack
- Pop all the items from the Stack

Parenthesis Matching using Stack



Parenthesis Matching using Stack



- Push all the opening brackets in the stack. Whenever you hit a closing bracket, search if the top of the stack is the opening bracket of the same nature.
- If so, Pop the stack and continue the iteration
- If not, then brackets are not well-ordered
- in the end if the stack is empty, it means all brackets are well-formed

Double Ended Queue



- Both insert and delete at both ends
- Variants : Input Restricted, Output Restricted

Priority Queue

- Every item has a priority associated with it.
- An element with high priority is dequeued before an element with low priority.
- If two elements have the same priority, they are served according to their order in the queue.

Priority queue can be implemented using the following data structures:

- Arrays
- Linked list
- Heap data structure
- Binary search tree

Is it possible to implement Queue using Stack?? Clue: Stacks!