Contents


```
set nocompatible

set enc=utf-8
set fenc=utf-8

set tabstop=4
set softtabstop=4
set shiftwidth=4
set backspace=2
set autoindent
set cindent

syntax on
set t_Co=256
set number
set showmatch
set hls

autocmd FileType cpp nnoremap <F9> :w <bar> :! g++ % -std=c++11 -
    O2 -Wall && ./a.out<CR>
```

1 Java

```
class Scan {
  BufferedReader buffer;
  StringTokenizer tok;
  Scan() {
    buffer = new BufferedReader(new InputStreamReader(System.in))
     ;
  }
  boolean hasNext() {
    while(tok == null || !tok.hasMoreElements())
      try {
        tok = new StringTokenizer(buffer.readLine());
      } catch (Exception ex) {
        return false;
      }
    return true;
  }
  String next() {
    if(hasNext())
      return tok.nextToken();
    return null;
  }
  String nextLine() {
    if(hasNext())
      return tok.nextToken("\n");
    return null;
  }
  int nextInt() {
    return Integer.parseInt(next());
  }
}


/* Compile: javac %
 * Run: java [Class name] */
import java.util.*;
import java.lang.*;
import java.math.*;

class Main {
    public static void main (String[] args) {
        System.out.print(1);
        System.out.print(2);
        System.out.println("Hello World");
        System.out.printf("%.2f", 0.12345);

        Scanner sc = new Scanner(System.in);
        System.out.println(sc.nextLine()); //gets()
        System.out.println(sc.next()); //scanf("%s")
        System.out.println(sc.nextInt());
        System.out.println(sc.nextDouble());
        while(sc.hasNext()) { //EOF
            int a = sc.nextInt();
            System.out.println(a);
        }

        int[] a = {1,2,3};
        int[][] b = {{1,2},{3,4,5}};
        double[] c = new double[90];
        System.out.print(b[0][1]);
        System.out.print(b[1][2]);

        int[] d = {5,2,1,3,4};
        Integer[] e = {6,3,4,1,2};
        Arrays.sort(d);
        Arrays.sort(e, new MyCom());
        for(int i=0; i<d.length; i++) {
            System.out.print(d[i]);
        }
        for(int i=0; i<e.length; i++) {
            System.out.print(e[i]);
        }

        Set<String> s = new HashSet<String>(); //or TreeSet
        s.add("123");
        s.add("234");
        System.out.println(s);
        System.out.println(s.contains("123"));
        Map<String, Integer> m = new TreeMap<String, Integer>();
        m.put("haha", 123);
        m.put("hehe", 234);
        System.out.println(m);

        BigInteger b1 = new BigInteger("-1231237182379123712");
        BigInteger b2 = BigInteger.valueOf(234);

        System.out.println(b1.add(b2));
        System.out.println(b1.mod(b2));

        int z = Integer.parseInt("-123");
        System.out.println(z);

        System.out.println(Math.PI);
        System.out.println(Math.sin(1));
    }

    static class MyCom implements Comparator<Integer> {
        public int compare(Integer i1, Integer i2) {
            return i2 - i1;
        }
    }
}
```

2 Math

2.1 Math Basic

```
vector<pii> primeFac(int n) {
  vector<pii> ret;
  for(int i=2; n>1; ++i){
    if( n%i != 0 ) continue;
    int e = 0;
    while( n%i == 0 ) ++e , n/=i;
    ret.push_back({i, e});
  }
  return ret;
}
long long fastPow(long long x, int n, long long m){
  long long ans = 1LL;
  while( n ){
    if( n&1 ) ans = ans * x % m;
    x = x*x % m;
    n >>= 1;
  }
  return ans;
}
long long modInv(long long x, long long p){
  return fastPow(x, p-2, p);
}
long long modInv_euler(long long x, long long m){
  // must be gcd(x,m)==1
  // phi is euler function: O(sqrt(x))
  return fastPow(x, phi(m)-1, m);
}
long long gt(long long a, long long b) {
  // smallest integer greater than a/b
  long long ret = a/b;
  if( ret>0 || a%b==0 ) ++ret;
  return ret;
}
```

2.2 Euler Function

```
int phi(int n){
  // euler function: in [0,n], # of coprime(i, n)
  vector<pii> fac = primeFac(n);
  int num = 1 , m = 1;
  for(auto &p : fac)
    num *= (p.first-1) , m *= p.first;
  return n/m * num;
}
```

2.3 Extended Euclidean

```
pll recur(long long n, long long m) {
  // solve one integer solution of
  // x*n + y*m = gcd(n,m)
  if( n%m == 0 )
    return {0LL, 1LL};
  pll res = recur(m, n%m);
  pll ret = {res.second, res.first - res.second * (n/m)};
  return ret;
}
```

2.4 China Remain Theorm

```
bool china_solvable(vector<pii> &rule) {
  for(int i=0; i<rule.size(); ++i)
  for(int j=1; j<rule.size(); ++j) {
    int gcd = __gcd(rule[i].second, rule[j].second);
    if( rule[i].first%gcd != rule[j].first%gcd )
      return false;
  }
  return true;
}
long long china(const vector<pii> &rule, int nlt=0){
  // solve x = ai (mod mi)
  // rule should solvable
  long long MM = 1LL;
  for(auto &r : rule)
    MM = lcm(MM, r.second);
  long long x = 0LL;
  for(auto &r : rule){
    long long ai = r.first;
    long long mi = r.second;
    long long Mi = MM / r.second;
    long long Mv = modInv_euler(Mi%mi, mi);
    long long tmp = ai*Mi%MM *Mv %MM;
    x = (x+tmp) % MM;
  }
  if( x>=nlt ) return x;
  long long n = ceil((nlt-x)*1.0/MM);
  return x + n*MM;
}
```

2.5 Counting

```
const int MaxNum = 1000004;
const int modNum = 1000000009;
long long fac  [MaxNum];
long long facIv[MaxNum];
void initFac(){
  fac[0] = facIv[0] = 1LL;
  for(int i=1; i<MaxNum; ++i) {
    fac  [i] = fac[i-1]*i % modNum;
    facIv[i] = modInv(fac[i], modNum);
  }
}
long long Cnm(int n, int m){
  if( m==0 || n==m ) return 1LL;
  return fac[n]*facIv[m] % modNum *facIv[n-m] % modNum;
}
long long nBlock_kColor(int n,int k){
  // n different blocks; k different colors
  // use inclusion-exclusion principle
  long long ans = fastPow(k, n, modNum);
  bool del = true;
  for(int i=k-1; i>0; --i, del=!del){
    long long now = Cnm(k, i)*fastPow(i, n, modNum) %modNum;
    if( del ) ans = (ans+modNum-now) % modNum;
    else ans = (ans+now) % modNum;
  }
  return ans;
}
```

2.6 Miller Rabin

```
#include <climits>
typedef unsigned long long int ull;

ull bases[20] = { 2ULL, 3ULL,5ULL,7ULL,11ULL,13ULL,17ULL,19ULL,23
    ULL,29ULL,31ULL,37ULL };

ull fake_mul(ull n, ull m, ull x);
ull fast_pow(ull n, ull p, ull x);

bool is_prime(ull n)
{
  if (n < 2ULL) return false;

  for (int tt = 0; tt < 12; tt++) {
    ull a;
    a = bases[tt] % n;

    if (a == 0 || a == 1 || a == n - 1) {
      continue;
    }

    int t = 0;
    ull u = n - 1ULL;
    while ((u & 1ULL) == 0ULL) u >>= 1, t++;

    ull x = fast_pow(a, u, n);   // x = a ^ u % n;
    if (x == 1ULL || x == (n - 1)) continue;
    for (int i = 0; i < t - 1; i++)
    {
      if (ULLONG_MAX / x < x) {
        x = fake_mul(x, x, n);
      }
      else {
        x = x*x%n;
      }
      if (x == 1) return false;
      if (x == n - 1) break;
    }
    if (x == n - 1) continue;
    return false;
  }
  return true;
}

ull fake_mul(ull n, ull m, ull x)
{
  ull re = 0ULL;
  while (m != 0ULL) {
    if ((m & 1ULL) != 0ULL) {
      if (ULLONG_MAX - re < n) {
```

```
        ull temp = ULLONG_MAX%x;

        temp += (n - (ULLONG_MAX - re)) % x;
        re = temp%x;
      }
      else {
        re = (re + n) % x;
      }
    }

    if (ULLONG_MAX - n < n) {
      ull temp = ULLONG_MAX%x;

      temp += (n - (ULLONG_MAX - n)) % x;
      n = temp%x;
    }
    else {
      n = n + n%x;
    }

    m >>= 1;
  }
  return re;
}

ull fast_pow(ull n, ull p, ull x)
{
  ull re = 1ULL;

  while (p != 0ULL) {
    if ((p & 1ULL) != 0ULL) {
      if (ULLONG_MAX / re < n) {
        re = fake_mul(n, re, x);
      }
      else {
        re = (re*n) % x;
      }
    }

    if (ULLONG_MAX / n < n) {
      n = fake_mul(n, n, x);
    }
    else {
      n = (n*n) % x;
    }
    p >>= 1;
  }
  return re;
}

// Below is non-extreme version
ull fake_mul(ull n, ull m, ull x) {
  ull re = 0ULL;
  n %= x, m %= x;
  while( m ) {
    if( m&1ULL )
      re = (re+n) % x;
    n = (n+n) % x;
    m >>= 1;
  }
  return re;
}
ull fast_pow(ull n, ull p, ull x) {
  ull re = 1ULL;
  while( p ) {
    if( p&1ULL )
      re = fake_mul(re,n,x);
    n = fake_mul(n,n,x);
    p >>= 1;
  }
  return re;
}
bool is_prime(ull n) {
  static const int bNum = 12;
  static const ull bases[bNum] = {
    2ULL,3ULL,5ULL,7ULL,11ULL,13ULL,17ULL,19ULL,23ULL,29ULL,31ULL
     ,37ULL
  };
  if( n<=2ULL ) return n==2ULL;
  if( !(n&1ULL) ) return false;

  ull u = n-1;
  while( !(u&1ULL) )
    u >>= 1;
  for(int i=0; i<bNum; i++) {
    if( bases[i]%n == 0 ) continue;
    ull t = u;
    ull a = fast_pow(bases[i], t, n);
    if( a==1 || a==n-1 ) continue;
    while( t!=n-1 && a!=1 && a!=n-1 ) {
      a = fake_mul(a,a,n);
      t <<= 1;
    }
    if( t==n-1 && a==1 ) continue;
    if( a!=n-1 ) return false;
  }
  return true;
}
```

2.7 Pollard rho

```
// need fack_mul, is_prime
ull gcd(ull a, ull b) {
  return (a%b==0)? b : gcd(b, a%b);
}
ull dif(ull a, ull b) {
  return a>b? a-b : b-a;
}
void pollard_rho(ull n, map<ull,int> &facs) {
  while( !(n&1ull) ) {
    // must extract factor 2
    int cnt = 0;
    while( !(n&1ull) )
      ++cnt, n>>=1;
    facs[2] = cnt;
  }
  if( n==1ull ) return;
  if( is_prime(n) ) {
    facs[n]++;
    return;
  }
  ull x = rand()%n;
  ull y = x;
  ull a = rand()%(n-1) + 1;
  ull g = 1ull;
  while( g==1ull ) {
    x = (fake_mul(x,x,n) + a) %n;
    y = (fake_mul(y,y,n) + a) %n;
    y = (fake_mul(y,y,n) + a) %n;
    if( x==y ) {
      g = n;
      break;
    }
    g = gcd(dif(x,y), n);
  }
  if( g==n ) // unluck try again
    pollard_rho(n, facs);
  else if( g>1ull ) { // luck, found g
    pollard_rho(g, facs);
    pollard_rho(n/g, facs);
  }
}
```

2.8 Linear Algebra

```
#ifndef _MATRIX_H_
#define _MATRIX_H_

#include <iostream>
#include <vector>
using namespace std;

template <class T>
class Matrix{
public:
  int rSize, cSize;
  vector< vector<T> > mat;

  Matrix(int r = 0, int c = 0) :rSize(r), cSize(c), mat(rSize,
     vector<T>(cSize)){}
  vector<T>& operator[](int i) {
    return mat[i];
  }
  void print();
};

template <class T>
void Matrix<T>::print() {
  cout << "Matrix elements:" << endl;
  for (int i = 0; i < rSize; i++) {
    cout << "[";
    for (int j = 0; j < cSize; j++) {
      cout << "\t" << mat[i][j];
      if (j != cSize - 1)cout << ",";
    }
    cout << " ]" << endl;
  }
}
```

```
#endif

#include "Matrix.h"

template <class T>
Matrix<T> matMul(Matrix<T> matA, Matrix<T> matB){
  Matrix<T> matRe(matA.rSize, matB.cSize);

  for (int i = 0; i < matRe.rSize; i++) {
    for (int j = 0; j < matRe.cSize; j++) {
      matRe[i][j] = 0;
      for (int k = 0; k < matA.cSize; k++) {
        matRe[i][j] += matA[i][k] * matB[k][j];
      }
    }
  }
  return matRe;
}
```

2.9 FFT

```
#include <complex>
#include <vector>
using namespace std;

const double PI = 3.141592654;
typedef complex<double> Complex;

void _fft(vector<Complex>& buf, vector<Complex>& out,
  int st, int step, bool isInv) {

  if (step >= buf.size()) return;

  _fft(out, buf, st, step * 2, isInv);
  _fft(out, buf, st + step, step * 2, isInv);

  int n = buf.size();
  double c = isInv ? 1.0 : -1.0;
  for (int i = 0; i < n; i += 2 * step) {
    Complex t = polar(1.0, c * 2 * PI * i / n) * out[i + step +
     st];
    buf[i / 2 + st] = out[i + st] + t;
    buf[(i + n) / 2 + st] = out[i + st] - t;
  }
}

void fft(vector<Complex> &x, bool isInv) {
  int n = x.size(), nxt2 = 0;
  for (int i = 0, mask = 1; i < 31; i++, mask <<= 1)
    nxt2 = (n&mask) ? (n != mask) ? 1 << (i + 1) : 1 << i : nxt2;
  n = nxt2;
  while (x.size() < n)
    x.push_back(0);

  vector<Complex> out = x;
  _fft(x, out, 0, 1, isInv);
  for (int i = 0; isInv && i < x.size(); i++)
    x[i] /= n;
}
```

2.10 Hash

```
#include <iostream>
#include <cstdio>
#include <cstring>
#include <algorithm>
using namespace std;
const int hashRange = 131072;
int hashtable[4][256], shuffleArr[hashRange], ref[hashRange];
void buildHashTable() {
  memset(ref, -1, sizeof(ref));
  for(int i = 0; i < hashRange; i++)
    shuffleArr[i] = i;
  for(int i = 0; i < 4; i++) {
    random_shuffle(shuffleArr, shuffleArr + hashRange);
    for(int j = 0; j < 256; j++)
      hashtable[i][j] = shuffleArr[j];
  }
}
int myhash(int input) {
  int x[4];
  for(int i = 0; i < 4; i++)
    x[i] = hashtable[i][(input >> (i*8)) & (0xff)];
  int k = x[0] ^ x[1] ^ x[2] ^ x[3];
  if(ref[k] != input)
    for(int i = k; ; i = (i+1)%hashRange)
      if(ref[i] == -1 || ref[i] == input) {
        ref[i] = input;
        return i;
      }
  return k;
}
```

3 String

3.1 KMP

```
class kmp{
  private:
    int  prefix[maxLen];
    char pat[maxLen];
  public:
    void setPattern(const char *str){
      strcpy(pat, str);
      prefix[0] = -1;
      int i=1 , j=0;
      for( ; str[i]!='\0' ; ++i , ++j ){
        if( str[i]==str[j] )
          prefix[i] = prefix[j];
        else
          prefix[i] = j;
        while( j>=0 && str[j]!=str[i] )
          j = prefix[j];
      }
      prefix[i] = j;
    }
    int search(const char *str){
      // return index of str match pattern
      int i=0 , j=0;
      for( ; str[i]!='\0' && pat[j]!='\0' ; ++i,++j){
        while( j>=0 && pat[j]!=str[i] )
          j = prefix[j];
      }
      if( pat[j]=='\0' )
        return i-j;
      return -1;
    }
    int countMatched(const char *str){
      // return # of pattern in str
      int cnt = 0;
      int i=0 , j=0;
      while( true ){
        if( pat[j]=='\0' ) ++cnt;
        if( str[i]=='\0' ) break;
        while( j>=0 && pat[j]!=str[i] )
          j = prefix[j];
        ++i , ++j;
      }
      return cnt;
    }
};
```

3.2 LPS

```
int lps(const char *str){
  // return len of longest palindrom substring
  static char emptyChar = '@';
  static char tmp[maxLen*2];
  static int lprb[maxLen*2];
  // [i-lprb[i], i+lprb[i]] is the lps when mid is i
  for(int i=0, j=-1; true; ++i){
    if( str[i]=='\0' ){
      tmp[++j] = emptyChar;
      tmp[++j] = '\0';
      break;
    }
    tmp[++j] = emptyChar;
    tmp[++j] = str[i];
  }
  lprb[0] = 0;
  int rightBorder = 0 , midId = 0;
  for(int i=1; tmp[i]!='\0'; ++i){
    if( i>rightBorder ){
      rightBorder = i;
      midId = i;
      lprb[i] = 0;
    }
    int mirId = midId - (i-midId);
    if( i+lprb[mirId] > rightBorder )
      lprb[i] = rightBorder - i;
    else if( i+lprb[mirId] < rightBorder )
      lprb[i] = lprb[mirId];
    else{
      int j=lprb[mirId];
      while( tmp[i+j]!='\0' && i-j>=0 && tmp[i+j]==tmp[i-j])
        ++j;
      rightBorder = i+j-1;
      midId = i;
      lprb[i] = j-1;
    }
  }
  int ans = 1;
  for(int i=0 ; tmp[i]!='\0' ; ++i)
    if( lprb[i]>ans )
      ans = lprb[i];
  return ans;
}
```

3.3 AC Automation

```
#include <queue>
#include <cstdio>
#include <cstring>
using namespace std;
struct AC_algorithm {
  struct node {
    static const int signNum = 52;  //number of kind of character
    node *ch[signNum];
    node *suffix, *dict;
    int index;
    node() {
      memset(ch, 0, sizeof(ch));
      suffix = dict = 0;
      index = -1;
    }
  };

  static const int stringNum = 100010;//number of pattern
  node *root;
  int occur[stringNum];       //string i occur occur[i] times
  int reflect[stringNum];       //string i is the same as string
     reflect[i];

  AC_algorithm() {
    root = new node();
    memset(occur, 0, sizeof(occur));
    memset(reflect, -1, sizeof(reflect));
  }

  int decode(char c) {        //decode char
    return c <= 'Z' ? (c - 'A') : (c - 'a' + 26);
  }

  void insert(char *s,int index) {  //add string to trie
    node *p = root;
    for(; *s; s++) {
      int code = decode(*s);
      if(p->ch[code] == NULL)
        p->ch[code] = new node();
      p = p->ch[code];
    }
    if(p->index == -1)
      p->index = index;
    else
      reflect[index] = p->index;
  }

  void build() {            //build machine
    queue<node*> q;
    q.push(root);
    while(!q.empty()) {
      node *p = q.front();
      for(int i = 0; i < node::signNum; i++)
        if(p->ch[i]) {
          node *tmp = p->suffix;
          while(tmp && !tmp->ch[i]) tmp = tmp->suffix;
          if(tmp)
            p->ch[i]->suffix = tmp->ch[i];
          else
            p->ch[i]->suffix = root;
          tmp = p->ch[i]->suffix;
          if(tmp->index != -1)
            p->ch[i]->dict = tmp;
          else
            p->ch[i]->dict = tmp->dict;
          q.push(p->ch[i]);
        }
      q.pop();
    }
  }

  void match(char *s) {       //match patterns with Text
    node *p = root;
    for(; *s; s++) {
      int code = decode(*s);
      while(p && !p->ch[code]) p = p->suffix;
      if(p)
        p = p->ch[code];
      else
        p = root;
```

```
      node *tmp = p;
      while(tmp) {
        if(tmp->index != -1)
          occur[tmp->index]++;
        tmp = tmp->dict;
      }
    }
  }

  ~AC_algorithm() {
    queue<node*> q;
    q.push(root);
    while(!q.empty()) {
      node *p = q.front();
      q.pop();
      for(int i = 0; i < node::signNum; i++)
        if(p->ch[i])
          q.push(p->ch[i]);
      delete p;
    }
  }
};
```

3.4 Z

```
#include <cstring>
int z[length];
void z_function(char *str) {
  int len = strlen(str), L = 0, R = 1;
  z[0] = len;
  for(int i = 1; i <len; i++)
    if(R <= i || z[i-L] >= R-i) {
      int x = max(R, i);
      while(x < len && str[x] == str[x-i])
        x++;
      z[i] = x-i;
      L = i; R = x;
      //if(i < x) {L = i; R = x;}
    } else
      z[i] = z[i-L];
}
```

3.5 Suffix Array

```
vector<int> buildSuffixArray(const vector<int> &str, int
     endOfString=-1) {
    // sa: i -> start position of str
    // O(n*lgn*lgn). probably faster than O(n*lgn) version
    int len = str.size();
    vector<int> sa(len+1), rank(len+1);
    for(int i=0; i<len; ++i) rank[sa[i] = i] = str[i];
    rank[sa.back() = len] = endOfString;
    for(int ll=1, cnt=0; cnt!=len; ll<<=1, cnt=rank[sa.back()]) {
        auto cmp = [&](const int l, const int r) {
            if( rank[l]!=rank[r] ) return rank[l] < rank[r];
            int lv = (l+ll < len) ? rank[l+ll] : 0;
            int rv = (r+ll < len) ? rank[r+ll] : 0;
            return lv < rv;
        };
        sort(sa.begin(), sa.end(), cmp);
        vector<int> tmp = rank;
        tmp[sa[0]] = 0;
        for(int i=1; i<sa.size(); ++i)
            tmp[sa[i]] = tmp[sa[i-1]] + cmp(sa[i-1], sa[i]);
        rank = tmp;
    }
    return sa;
}

vector<int> buildLcp(const vector<int> &str, const vector<int> &
     sa) {
    // lcp: longest common prefix for sa[i-1] sa[i]
    int len = sa.size();
    vector<int> lcp(len, 0), idx(len);
    for(int i=0; i<len; ++i) idx[sa[i]] = i;
    for(int i=0, l=0; i<len; ++i) {
        if( idx[i] == 0 ) {
            l = 0;
            continue;
        }
        int j = sa[idx[i]-1];
        while( i+l<len && j+l<len && str[i+l]==str[j+l] )
            ++l;
        lcp[idx[i]] = l;
        l -= l>0;
    }
    return lcp;
}
```

```
pair<int,int> longestRepeatedSubstring(const vector<int> &sa,
     const vector<int> &lcp, int k) {
    // longest repeated substring who occurs at least k times
    // return <longest length, start position>
    pair<int,int> ret = {-1, -1};
    if( k<=1 ) {
        for(int i=0; i<sa.size(); ++i)
            if( sa[i]==0 ) return {sa.size()-1, i};
    }
    if( lcp.size() < k ) return ret;
    deque<pair<int,int>> dq;
    auto maintain = [&](pair<int,int> v) {
        while( dq.size() && dq.front().second <= v.second-(k-1) )
            dq.pop_front();
        while( dq.size() && dq.back() >= v )
            dq.pop_back();
        dq.push_back(v);
    };
    for(int i=0; i<k-2; ++i) maintain({lcp[i], i});
    for(int i=k-2; i<lcp.size(); ++i) {
        maintain({lcp[i], i});
        ret = max(ret, dq.front());
    }
    return ret;
}

pair<int,int> lcs(const vector<int> &s1, const vector<int> &s2,
     int e1, int e2) {
    // Longest Common "Substring" in O(n*lgn*lgn) n = s1+s2
    vector<int> arr(s1.size()+s2.size()+2);
    int idx = -1;
    for(int i=0; i<s1.size(); ++i) arr[++idx] = s1[i];
    arr[++idx] = e1;
    for(int i=0; i<s2.size(); ++i) arr[++idx] = s2[i];
    arr[++idx] = e2;
    vector<int> sa = buildSuffixArray(arr);
    vector<int> lcp = buildLcp(arr, sa);
    pair<int,int> ret = {-1, -1};
    for(int i=1; i<lcp.size(); ++i)
        if( (sa[i]<=s1.size()) ^ (sa[i-1]<=s1.size()) )
            ret = max(ret, {lcp[i], sa[i]});
    return ret;
}
```

3.6 BWT

```
vector<int> btwEncode(const vector<int> &src) {
    // O(n*lgn*lgn). probably faster than O(n*lgn) version
    int len = src.size();
    vector<int> sa(len), rank(len);
    for(int i=0; i<len; ++i) rank[sa[i] = i] = src[i];
    for(int ll=1, cnt=0; cnt!=len; ll<<=1, cnt=rank[sa.back()]+1)
      {
        auto cmp = [&](const int l, const int r) {
            if( rank[l]!=rank[r] ) return rank[l] < rank[r];
            return rank[(l+ll)%len] < rank[(r+ll)%len];
        };
        sort(sa.begin(), sa.end(), cmp);
        vector<int> tmp = rank;
        tmp[sa[0]] = 0;
        for(int i=1; i<sa.size(); ++i)
            tmp[sa[i]] = tmp[sa[i-1]] + cmp(sa[i-1], sa[i]);
        rank = tmp;
    }
    vector<int> rst(len);
    for(int i=0; i<len; ++i) rst[i] = src[(sa[i]+len-1)%len];
    return rst;
}

vector<int> btwDecode(const vector<int> &rst) {
    int len = rst.size();
    vector<pair<int,int> > pre(len);
    for(int i=0; i<len; ++i) pre[i] = {rst[i], i};
    sort(pre.begin(), pre.end());
    vector<int> table(len);
    for(int i=0; i<len; ++i) table[pre[i].second] = i;
    vector<int> src(len);
    for(int i=rst.size()-1, idx=0; i>=0; --i, idx=table[idx])
        src[i] = rst[table[idx]];
    return src;
}
```

4 Tree

4.1 Tree Min Vertex Cover

```
class TreeMinVertexCover {
private:
  static const int maxNum = 100004;
  vector<int> G[maxNum];
  int in[maxNum];
public:
  bool pick[maxNum];
  int MVC; // min vertext cover
  void init() {
    for(int i=0; i<maxNum; ++i)
      G[i].clear();
    memset(in, 0, sizeof(in));
  }
  void addEdge(int u, int v) {
    G[u].emplace_back(v);
    G[v].emplace_back(u);
    ++in[u];
    ++in[v];
  }
  int treeMinVertexCover() {
    memset(pick, 0, sizeof(pick));
    MVC = 0;
    queue<int> myQ;
    for(int i=1; i<=maxNum; ++i)
      if( in[i]==1 ) myQ.push(i);
    while( myQ.size() ) {
      int nowAt = myQ.front();
      myQ.pop();
      if( in[nowAt]==0 ) continue;
      ++MVC;
      int id;
      for(int i=0; i<G[nowAt].size(); ++i)
        if( in[G[nowAt][i]] ) {
          id = G[nowAt][i];
          break;
        }
      for(int i=0; i<G[id].size(); ++i)
        if( in[G[id][i]] ) {
          --in[G[id][i]];
          --in[id];
          if( in[G[id][i]]==1 )
            myQ.push(G[id][i]);
        }
    }
    return MVC;
  }
};
```

4.2 Treap ordered

```
struct node {
  int v , p , sz ;
  node *l , *r ;
  node() { l = r = NULL ;}
  node(int v_):v(v_),p(rand()),sz(1) {l = r = 0;}
  int size() {
    return this!=NULL ? this->sz : 0 ;
  }
  void maintain() {
    sz = l->size() + r->size() + 1 ;
  }
} ;
void splite_v(node *t,node* &a,node* &b,int v) {
  if(!t)
    a = b = NULL ;
  else if(v >= t->v) {
    a = t ;
    splite_v(t->r,a->r,b,v) ;
    a->maintain() ;
  } else if(v < t->v) {
    b = t ;
    splite_v(t->l,a,b->l,v) ;
    b->maintain() ;
  }
}
node* merge(node *a,node *b) {
  if(a==NULL || b==NULL)
    return a!=NULL ? a : b;
  if(a->p > b->p) {
    a->r = merge(a->r,b) ;
    a->maintain() ;
    return a ;
  } else if(a->p <= b->p) {
    b->l = merge(a,b->l) ;
    b->maintain() ;
    return b ;
  }
}
int kth(node *t,int k) {
  if(k<=t->l->size())
    return kth(t->l,k) ;
  else if(k>t->l->size()+1)
    return kth(t->r,k-t->l->size()-1) ;
  return t->v ;
}
void release(node *t) {
  if(t) {
    release(t->l) ;
    release(t->r) ;
    delete t ;
  }
}
```

4.3 Treap unordered

```
#include <iostream>
#include <cstdio>
#include <stdlib.h>
#include <cstring>
using namespace std;
const int oo = 1e9 ;
struct node {
  int v , p , sz ;
  int sum , presum , sufsum , maxsum , flag , set ;
  node *l , *r ;
  node(){ }
  node(int v_):p(rand()),sz(1),l(NULL),r(NULL) {
    v = sum = presum = sufsum = maxsum = v_ ;
    flag = 0 ;
    set = oo ;
  }
  int size() { return this ? sz : 0 ; }
  int Sum() { return this ? sum : 0 ; }
  int Presum() { return this ? (!flag ? presum : sufsum) : -oo ;
    }
  int Sufsum() { return this ? (!flag ? sufsum : presum) : -oo ;
    }
  int Maxsum() { return this ? maxsum : -oo ; }
  int max(int a,int b) { return a > b ? a : b ; }
  int max(int a,int b,int c) { return max(a,max(b,c)) ; }
  void makesame(int st) {
    if(this) {
      set = st ;
      sum = st*sz ;
      presum = sufsum = maxsum = (st <= 0 ? st : sum) ;
    }
  }
  void pushdown() {
    if(flag) {
      if(l) l->flag = !l->flag ;
      if(r) r->flag = !r->flag ;
      swap(l,r) ;
      swap(presum,sufsum) ;
      flag = 0 ;
    }
    if(set!=oo) {
      v = set ;
      l->makesame(set) ;
      r->makesame(set) ;
      set = oo ;
    }
  }
  void maintain() {
    presum = max(l->Presum(), l->Sum() + v, l->Sum() + v + r->
     Presum()) ;
    sufsum = max(r->Sufsum(), r->Sum() + v, r->Sum() + v + l->
     Sufsum()) ;
    int maxsum1 = max(l->Maxsum(), r->Maxsum(), v) ;
    int maxsum2 = max(l->Sufsum() + v, r->Presum() + v, l->Sufsum
     () + v + r->Presum()) ;
    maxsum = max(maxsum1, maxsum2) ;
    sum = l->Sum() + r->Sum() + v ;
    sz = 1 + l->size() + r->size() ;
  }
} ;
void splite(node *t,node* &a,node* &b,int k) {
  if(t == NULL) {
    a = b = NULL ;
    return ;
  }
  t->pushdown() ;
  if(t->l->size()+1 <= k) {
    a = t ;
```

```
    splite(t->r, a->r, b, k-(t->l->size()+1)) ;
    a->maintain() ;
  } else {
    b = t ;
    splite(t->l,a,b->l,k) ;
    b->maintain() ;
  }
}
node* merge(node *a,node *b) {
  if(!a || !b)
    return a ? a : b ;
  if(a->p > b->p) {
    a->pushdown() ;
    a->r = merge(a->r,b) ;
    a->maintain() ;
    return a ;
  } else {
    b->pushdown() ;
    b->l = merge(a,b->l) ;
    b->maintain() ;
    return b ;
  }
}
void Delete(node *t) {
  if(!t) return ;
  Delete(t->l) ;
  Delete(t->r) ;
  delete t ;
}
void INSERT(node* &root) {
  int p , k , v ;
  node *t=0 , *L, *R;
  scanf("%d%d",&p,&k) ;
  for(int i=0 ; i<k ; i++) {
    scanf("%d",&v) ;
    t = merge(t,new node(v)) ;
  }
  splite(root, L, R, p) ;
  root = merge(L, merge(t, R)) ;
}
void DELETE(node* &root) {
  int p , k ;
  scanf("%d%d",&p,&k) ;
  node *L, *M, *R;
  splite(root, L, R, p-1) ;
  splite(R, M, R, k) ;
  Delete(M) ;
  root = merge(L, R) ;
}
void MAKE_SAME(node* &root) {
  int p , k , l ;
  scanf("%d%d%d",&p,&k,&l) ;
  node *L, *M, *R ;
  splite(root, L, R, p-1) ;
  splite(R, M, R, k) ;
  M->makesame(l) ;
  root = merge(L, merge(M, R)) ;
}
void REVERSE(node* &root) {
  int p , k ;
  scanf("%d%d",&p,&k) ;
  node *L, *M, *R ;
  splite(root, L, R, p-1) ;
  splite(R, M, R, k) ;
  M->flag = !M->flag ;
  root = merge(L, merge(M, R)) ;
}
int GET_SUM(node* &root) {
  int p , k , v ;
  scanf("%d%d",&p,&k) ;
  node *L, *M, *R ;
  splite(root, L, R, p-1) ;
  splite(R, M, R, k) ;
  v = M->Sum() ;
  root = merge(L, merge(M, R)) ;
  return v ;
}
int MAX_SUM(node* &root) {
  return root->Maxsum() ;
}
int main () {
  int n, m ;
  srand(860514) ;
  while(scanf("%d%d",&n,&m)==2) {
    node *root=0 ;
    for(int i=0,v ; i<n ; i++) {
      scanf("%d",&v) ;
      root = merge(root,new node(v)) ;
    }
    while(m--) {
      char s[10] ;
      scanf("%s",s) ;
      if(strcmp(s,"INSERT")==0) {
        INSERT(root) ;
        continue ;
      }
      if(strcmp(s,"DELETE")==0) {
        DELETE(root) ;
        continue ;
      }
      if(strcmp(s,"MAKE-SAME")==0) {
        MAKE_SAME(root) ;
        continue ;
      }
      if(strcmp(s,"REVERSE")==0) {
        REVERSE(root) ;
        continue ;
      }
      if(strcmp(s,"GET-SUM")==0) {
        printf("%d\n",GET_SUM(root)) ;
        continue ;
      }
      if(strcmp(s,"MAX-SUM")==0) {
        printf("%d\n",MAX_SUM(root)) ;
        continue ;
      }
    }
  }
}
```

4.4 Tree Heavy Light Decomposition

```
#include <iostream>
#include <cstdio>
#include <vector>
#include <string.h>
#define N 50000
using namespace std;

vector<int> G[N];
int ind[N], f[N], d[N], head[N], son[N], pn, n;

int dfs(int u,int parent) {
  int i, v, x, w = 0, sum = 1;
  f[u] = parent;
  son[u] = -1;
  for(i = 0; i < G[u].size(); i++) {
    v = G[u][i];
    if(v != parent) {
      d[v] = d[u] + 1;
      x = dfs(v,u);
      sum += x;
      if(x > w) {
        son[u] = v;
        w = x;
      }
    }
  }
  return sum;
}
void chain(int u) {
  int i , v;
  ind[u] = pn++;
  if(f[u] == -1 || son[f[u]] != u)
    head[u] = u;
  else
    head[u] = head[f[u]];
  if(son[u]!=-1)
    chain(son[u]);
  for(i=0; i<G[u].size(); i++) {
    v = G[u][i] ;
    if(v != f[u] && v != son[u])
      chain(v);
  }
}
void modify(int u, int v, ...) {
  while(head[u] != head[v])
    if(d[head[u]] > d[head[v]]) {
      //do something in rang(ind[head[u]], ind[u]);
      u = f[head[u]];
    } else {
      //do something in rang(ind[head[v]], ind[v]);
      v = f[head[v]];
    }
  if(d[u] > d[v])
    //do something in rang(ind[head[u]], ind[u]);
  else
    //do something in rang(ind[head[v]], ind[v]);
}
```

```
int getLca(int u, int v) {
  while(head[u] != head[v])
    if(d[head[u]] > d[head[v]])
      u = f[head[u]];
    else
      v = f[head[v]];
  if(d[u] > d[v])
    return v;
  else
    return u;
}
void build() {
  pn = 1;
  d[0] = 0; //set depth of root to 0
  dfs(0,-1);
  chain(0); //relabel node
}
```

5 Graph

5.1 Biconnected Components

```
#include <iostream>
#include <cstdio>
#include <cstring>
#include <stack>
#include <vector>
using namespace std;
//Biconnected Components
struct BCC {
  static const int maxNum = 1010;
  vector<int> G[maxNum], bccGroup[maxNum];
  int Node;
  int bcc_cnt;
  int timeStamp;
  int low[maxNum];
  int visit[maxNum];
  int bcc[maxNum];
  bool is_ap[maxNum];
  stack< pair<int,int> > S;
  BCC(int Node) {
    for(int i = 0; i < maxNum; i++) {
      G[i].clear();
      bccGroup[i].clear();
      low[i] = visit[i] = bcc[i] = -1;
      is_ap[i] = false;
    }
    this->Node = Node;
    bcc_cnt = 0;
  }
  void DFS(int u,int parent) {
    int children = 0;
    low[u] = visit[u] = timeStamp++;
    for(int i = 0; i < G[u].size(); i++) {
      int v = G[u][i];
      if(visit[v] == -1) {
        S.push(make_pair(u, v));
        children++;
        DFS(v, u);
        low[u] = min(low[u], low[v]);
        if(low[v] >= visit[u]) {
          is_ap[u] = true;
          pair<int,int> e;
          do {
            e = S.top();
            if(bcc[e.first] != bcc_cnt) {
              bccGroup[bcc_cnt].push_back(e.first);
              bcc[e.first] = bcc_cnt;
            }
            if(bcc[e.second] != bcc_cnt) {
              bccGroup[bcc_cnt].push_back(e.second);
              bcc[e.second] = bcc_cnt;
            }
            S.pop();
          }while(e.first!=u || e.second!=v);
          bcc_cnt++;
        }
      } else if(v != parent) {
        S.push(make_pair(u, v));
        low[u] = min(low[u], visit[v]);
      }
    }
    if(u == parent) // u is root
      is_ap[u] = (children >= 2);
  }
  void articulation_vertex() {
    timeStamp = 0;
    for(int i = 0; i < Node; i++)
      if(low[i] == -1)
        DFS(i, i);
  }
};
```

5.2 Strong Connected Components

```
class SCC {
private:
    static const int maxN = 10004;
    vector<int> G[maxN];
    vector<int> invG[maxN];
    vector<int> stk;
    bool visited[maxN];
    void dfs_1(int nowAt) {
        visited[nowAt] = true;
        for(auto v : G[nowAt])
            if( !visited[v] )
```

```
                dfs_1(v);
        stk.emplace_back(nowAt);
    }
    void dfs_2(int nowAt, const int id) {
        sccID[nowAt] = id;
        for(auto v : invG[nowAt])
            if( sccID[v]==-1 )
                dfs_2(v, id);
    }
public:
    int sccNum;
    int sccID[maxN];

    void init() {
        for(int i=0; i<maxN; ++i) {
            G   [i].clear();
            invG[i].clear();
        }
    }
    void addEdge(int u, int v) {
        G   [u].emplace_back(v);
        invG[v].emplace_back(u);
    }
    vector<vector<int>> findAllSCC(int base, int n) {
        memset(visited, 0, sizeof(visited));
        stk.clear();
        for(int i=base; i<=n; ++i)
            if( !visited[i] )
                dfs_1(i);

        sccNum = 0;
        memset(sccID, -1, sizeof(sccID));
        for(int i=stk.size()-1; i>=0; --i)
            if( sccID[stk[i]]==-1 ) {
                dfs_2(stk[i], sccNum);
                ++sccNum;
            }

        // returned zero base scc dag
        vector<vector<int>> sccDAG(sccNum);
        vector<unordered_set<int>> have(sccNum);
        for(int u=base; u<=n; ++u) {
            int sccU = sccID[u];
            for(auto v : G[u]) {
                int sccV = sccID[v];
                if( sccU==sccV ) continue;
                if( have[sccU].find(sccV) == have[sccU].end() ) {
                    have  [sccU].insert      (sccV);
                    sccDAG[sccU].emplace_back(sccV);
                }
            }
        }

        return sccDAG;
    }
};
```

5.3 2 SAT

```
class TwoSAT {
private:
  static const int maxN = 100004;
  static const int size = 2*maxN + 4;
  bool        pick[size];
  vector<int> G   [size];

  int id(int i, int T) { return (i<<1) + T; }
  int alter(int i) { return i^1; }
  bool dfsTry(int nowAt, vector<int> &stk) {
    if( pick[alter(nowAt)] )
      return false;
    stk.emplace_back(nowAt);
    pick[nowAt] = true;
    for(auto v : G[nowAt]) {
      if( !pick[v] && !dfsTry(v, stk) )
        return false;
    }
    return true;
  }
public:
  void init() {
    memset(pick, 0, sizeof(pick));
    for(int i=0; i<size; ++i)
      G[i].clear();
  }
  void addClause(bool TA, int A, bool TB, int B) {
    // Add clause (TA + TB)
    // When TA not true, TB must true. vise versa.
    G[id(A, !TA)].emplace_back(id(B, TB));
    G[id(B, !TB)].emplace_back(id(A, TA));
  }
  bool solve() {
    // O(n) solve
    memset(pick, 0, sizeof(pick));
    for(int i=0; i<maxN; ++i) {
      if( pick[id(i, 0)] || pick[id(i, 1)] )
        continue;
      vector<int> stk;
      if( dfsTry(id(i, 0), stk) )
        continue;
      for(auto v : stk)
        pick[v] = false;
      if( !dfsTry(id(i, 1), stk) )
        return false;
    }
    return true;
  }
  bool T(int i) {
    // should solve() first
    return pick[id(i, 1)];
  }
};
```

5.4 System of Difference Constraints

```
class System_of_DifConstrain {
private:
  static const int maxN = 504;
  static const int maxM = 3004;
  struct Edge {
    int s, t;
    long long cost;
  };
  Edge es[maxM];
  int eSize;
public:
  bool solvable;
  long long x[maxN]; // one solution
  void init() {
    eSize = -1;
  }
  void addConstrain(int xI, int xJ, long long c) {
    // add xi - xj <= c
    es[++eSize] = {xJ, xI, c};
  }
  bool solve(int n=maxN) {
    // n is max # of node of CC
    memset(x, 0, sizeof(x));
    for(int i=0; i<n; ++i)
    for(int j=0; j<=eSize; ++j)
      if( x[es[j].s] + es[j].cost < x[es[j].t] )
        x[es[j].t] = x[es[j].s] + es[j].cost;
    for(int j=0; j<=eSize; ++j)
      if( x[es[j].s] + es[j].cost < x[es[j].t] )
        return solvable = false;
    return solvable = true;
  }
};
```

5.5 Bipartite: MaxMatch, MinVer-Cover, MaxIndSet

```
class Bipartite {
private:
  static const int MaxNum = 1004;
  vector<int> g[MaxNum];
  bool visited [MaxNum];

  bool bipart(int nowAt, int nowSide) {
    visited[nowAt] = true;
    side[nowAt] = nowSide;
    for(auto &id : g[nowAt])
      if( !visited[id] )
        bipart(id , !nowSide);
      else if( side[id]==nowSide )
        return false;
    return true;
  }
  bool maxMatch(int nowAt) {
    visited[nowAt] = true;
    for(auto &id : g[nowAt])
      if( cp[id]==-1
        || (!visited[cp[id]] && maxMatch(cp[id])) ){
        cp[id]    = nowAt;
        cp[nowAt] = id;
        return true;
```

```
      }
    return false;
  }
  void minVertexCover(int nowAt) {
    MVC[nowAt] = 1;
    for(auto &id : g[nowAt])
      if( !MVC[id] ) {
        MVC[id] = 1;
        minVertexCover(cp[id]);
      }
  }
  void maxIndependentSet(int nowAt) {
    MIS[nowAt] = 1;
    for(auto &id : g[nowAt])
      if( !MIS[cp[id]] )
        maxIndependentSet(cp[id]);
  }
public:
  int  matchNum;     // max match num
  int  cp  [MaxNum]; // id and cp[id] is couple
  bool side[MaxNum]; // left/right side
  bool MVC [MaxNum]; // min vertex cover
  bool MIS [MaxNum]; // max indepent set
  void addEdge(int u, int v) {
    g[u].emplace_back(v);
    g[v].emplace_back(u);
  }
  void init() {
    for(int i=0; i<MaxNum; ++i)
      g[i].clear();
  }
  bool countAll() {
    // if graph is not bipartite return false

    // bipartite
    memset(side, 0, sizeof(side));
    memset(visited , 0 , sizeof(visited));
    for(int i=0 ; i<MaxNum ; ++i)
      if( !visited[i] && !bipart(i, 0) )
        return false;


    // maximum match
    // O(VE), this code can be more optimized
    // alternative: dinic O(V^0.5*E)
    matchNum = 0;
    memset(cp , -1 , sizeof(cp));
    for(int i=0 ; i<MaxNum ; ++i){
      if( cp[i]!=-1 ) continue;
      memset(visited , 0 , sizeof(visited));
      if( maxMatch(i) )
        ++matchNum;
    }

    // min vertex cover
    memset(MVC, 0, sizeof(MVC));
    for(int i=0; i<MaxNum; ++i)
      if( side[i]==1 && cp[i]==-1 )
        minVertexCover(i);
    for(int i=0; i<MaxNum; ++i)
      if( side[i]==1 )
        MVC[i] = !MVC[i];

    // max independent set
    memset(MIS, 0, sizeof(MIS));
    for(int i=0; i<MaxNum; ++i)
      if( cp[i]==-1 )
        maxIndependentSet(i);
    for(int i=0; i<MaxNum; ++i)
      if( side[i]==1 && cp[i]!=-1
        && !MIS[i] && !MIS[cp[i]] )
        MIS[i] = 1;

    return true;
  }
};
```

5.6 Bipartite: KM

```
#include <cstring>
#include <iostream>
using namespace std;
struct KM {
  static const int N = 105, big_value = 100000000;
  int G[N][N] , visx[N] , visy[N];
  int n , labelx[N] , labely[N] , matchx[N] , matchy[N] ;

  KM(int n_):n(n_) {} ;

  bool DFS(int x) {
    visx[x] = true ;
    int y ;
    for(y=0 ; y<n ; y++)
      if(!visy[y] && labelx[x]+labely[y]==G[x][y]) {
        visy[y] = true ;
        if(matchy[y]==-1 || DFS(matchy[y])) {
          matchx[x] = y ;
          matchy[y] = x ;
          return true ;
        }
      }
    return false ;
  }

  int max_match() {   //Maximum Weight Perfect Bipartite Matching
    memset(labelx,0,sizeof(labelx)) ;
    memset(labely,0,sizeof(labely)) ;
    memset(matchx,-1,sizeof(matchx)) ;
    memset(matchy,-1,sizeof(matchy)) ;
    int i , x , y ;
    for(x=0 ; x<n ; x++)
      for(y=0 ; y<n ; y++)
        labelx[x] = max(labelx[x],G[x][y]) ;
    for(i=0 ; i<n ; i++)
      while(true) {
        memset(visx,0,sizeof(visx)) ;
        memset(visy,0,sizeof(visy)) ;
        if(DFS(i)) break ;
        int d=big_value ;
        for(x=0 ; x<n ; x++) if(visx[x])
          for(y=0 ; y<n ; y++) if(!visy[y])
            d = min(d,labelx[x]+labely[y]-G[x][y]) ;
        if(d==big_value) return -1 ;  //faile to exist perfect
     matching
        for(int j=0 ; j<n ; j++) {
          if(visx[j]) labelx[j] -= d ;
          if(visy[j]) labely[j] += d ;
        }
      }
    int total=0 ;
    for(i=0 ; i<n ; i++)          //must be perfect!!!
      total += G[i][matchx[i]] ;
    return total ;
  }
} ;
```

5.7 Min Vertex Cover

```
struct MinVertexCover {
private:
  static const int MaxNum = 54;
  vector<int> G[MaxNum];
  int in[MaxNum];

  int undo(vector<int> &record) {
    for(int i=0; i<record.size(); ++i)
      ++in[record[i]];
    record.clear();
  }
  int delNode(int u, vector<int> &record) {
    for(int i=0; i<G[u].size(); ++i)
      if( in[G[u][i]] ) {
        --in[G[u][i]];
        --in[u];
        record.push_back(G[u][i]);
        record.push_back(u);
      }
  }

  int cnt(int from, int *visited, bool type) {
    if( visited[from] ) return 0;
    if( type==1 ) visited[from] = 1;
    for(int i=0; i<G[from].size(); ++i)
    if( in[G[from][i]] && !visited[G[from][i]] )
      return type+cnt(G[from][i], visited, !type);
    return type;
  }
  int cnt(int *visited) {
    int ret = 0;
    for(int i=0; i<MaxNum; ++i)
      if( in[i]==1 && !visited[i] )
        ret += cnt(i, visited, 0);
    for(int i=0; i<MaxNum; ++i)
      if( in[i]==2 && !visited[i] )
        ret += cnt(i, visited, 0);
    return ret;
  }
```

```
public:
  int MVCPick[MaxNum];
  int MVC; // min vertex cover
  void init() {
    for(int i=0; i<MaxNum; ++i)
      G[i].clear();
    memset(in, 0, sizeof(in));
  }
  void addEdge(int u, int v) {
    G[u].push_back(v);
    G[v].push_back(u);
    ++in[u];
    ++in[v];
  }
  void minVertexCover(int nowMVC=0, const int *lastPick=NULL) {
    // O(n^2 * 1.38^n)
    int nowPick[MaxNum] = {};
    if( nowMVC==0 ) {
      MVC = MaxNum;
      memset(MVCPick, 0, sizeof(MVCPick));
    }
    else memcpy(nowPick, lastPick, sizeof(nowPick));

    int maxid = 0;
    for(int i=0; i<MaxNum; ++i)
      if( in[i]>in[maxid] )
        maxid = i;
    if( in[maxid]<=2 ) {
      nowMVC += cnt(nowPick);
      if( nowMVC<MVC ) {
        MVC = nowMVC;
        memcpy(MVCPick, nowPick, sizeof(nowPick));
      }
      return;
    }

    vector<int> record;

    delNode(maxid, record);
    nowPick[maxid] = 1;
    minVertexCover(nowMVC+1, nowPick);
    nowPick[maxid] = 0;
    undo(record);

    int cnt = 0;
    for(int i=0; i<G[maxid].size(); ++i)
      if( in[G[maxid][i]] ) {
        ++cnt;
        delNode(G[maxid][i], record);
        nowPick[G[maxid][i]] = 1;
      }
    minVertexCover(nowMVC+cnt, nowPick);
    undo(record);
  }
};
```

5.8 Kirchhoff's theorem

```
D = Degree matrix (diagonal entries are node's degree)
A = Adjacency matrix (01 matrix)
Q = Laplacian matrix = D - A
Q* = deleting any row and any column from Q
Number of spanning tree = det(Q*)
```

5.9 Popular matching

```
N applicant M position
Each applicant have his own perference list (not required
     containing all position)
Target: find a matching s.t. not existing another matching have
     more applicant prefer. This matching called popular matching
A applicant u prefer another matching which imply that
    "This matching doesn't have u but the other does"
    or
    "The other matching give u the position that he more prefer"

Define hot position: the position is any applicant's first choice

Solve: Whethere there is a popular matching
(1) Each applicant build and edge with "his first choice" and "
     his first choice except all hot position" (if not exist,
     build a dummy position)
(3) Return whether all applicant can have a position

Solve: Maximum popular matching
(1) If popular matching not exist return No
(2) Use the result above
(3) Remove all dummy position
(4) Find augmenting path for all unmatch applicant
(5) For all unmatch hot position, rob an applicant(all it's
     applicant choice non hot position)
(6) return the matching
```

6 Flow

6.1 Dinic Maxflow Mincut

```
class Dinic{
private:
    typedef pair<int,int> pii;
    static const int maxN = 504;
    static const int infF = 1023456789;
    int cap [maxN][maxN];
    int pipe[maxN][maxN];
    vector<int> g[maxN];
    int level[maxN], visited[maxN];

    bool bfsLabeling(int s, int t){
        memset(level , 0 , sizeof(level));
        queue<int> myQ;
        myQ.push( s );
        level[s] = 1;
        while( !myQ.empty() ){
            int nowAt = myQ.front();
            myQ.pop();
            for(int i=0;i<g[nowAt].size();++i)
                if( !level[g[nowAt][i]] && pipe[nowAt][g[nowAt][i
    ]] ){
                    level[g[nowAt][i]] = level[nowAt] + 1;
                    myQ.push( g[nowAt][i] );
                }
        }
        return level[t];
    }
    int dfsFindRoute(int nowAt, int t, int maxC) {
        visited[nowAt] = true;
        if( nowAt==t ){
            maxFlow += maxC;
            return maxC;
        }
        for(int i=0; i<g[nowAt].size(); ++i) {
            int next = g[nowAt][i];
            if( visited[next] ) continue;
            if( level[next] != level[nowAt]+1 ) continue;
            if( !pipe[nowAt][next] ) continue;
            int nowOut = dfsFindRoute(next ,t ,min(maxC , pipe[
    nowAt][next]));
            if( nowOut==0 )
                continue;
            pipe[nowAt][next] -= nowOut;
            pipe[next][nowAt] += nowOut;
            return nowOut;
        }
        return 0;
    }
    void dfsFindMinCut(int nowAt) {
        sside[nowAt] = 1;
        for(auto v : g[nowAt])
            if( !sside[v] && pipe[nowAt][v] )
                dfsFindMinCut(v);
    }

public:
    int maxFlow;
    bool sside[maxN];
    vector<pii> minCut;

    void init() {
        memset(cap  , 0, sizeof(cap));
        memset(pipe , 0, sizeof(pipe));
        memset(sside, 0, sizeof(sside));
        for(int i=0;i<maxN;++i)
            g[i].clear();
        maxFlow = 0;
        minCut.clear();
    }
    void addEdge(int u, int v, int c) {
        if( u==v ) return;
        if( !cap[u][v] && !cap[v][u] ) {
            g[u].emplace_back(v);
            g[v].emplace_back(u);
        }
        cap[u][v] += c;
    }
    void coculAll(int s, int t) {
        memcpy(pipe, cap, sizeof(pipe));

        // max flow
        while( bfsLabeling(s,t) ) {
            memset(visited, 0, sizeof(visited));
            while( dfsFindRoute(s,t,infF) )
                ;
        }

        // min cut
        dfsFindMinCut(s);
        for(int u=0; u<maxN; ++u)
        if( sside[u] )
            for(auto v : g[u])
            if( !sside[v] )
                minCut.push_back({u, v});
    }
};
```

7 Geometry

7.1 Geometry basic

```
struct Point{
  double x,y;
  Point(double xi=0.0,double yi=0.0){
    x = xi , y = yi;
  }
  Point operator - (const Point &r)const{
    return Point(x-r.x , y-r.y);
  }
};
typedef Point Vector;

double angle(const Vector &v,const Vector &u){
  // return rad [0, pi] of two vector
  return acos( dot(v,u)/len(v)/len(u) );
}
Vector rotate(const Vector &v,double rad){
  return Vector(
    v.x*cos(rad) - v.y*sin(rad),
    v.x*sin(rad) + v.y*cos(rad)
  );
}
double pointSegLen(const Point &A,const Point &B,const Point &Q){
  if(A==B) return len(Q-A);
  if( dot(B-A , Q-A)<0 ) return len(Q-A);
  if( dot(B-A , Q-B)>0 ) return len(Q-B);
  return fabs( cross(B-A , Q-A) ) / len(B-A);
}
bool pointOnSeg(const Point &A,const Point &B,const Point &Q){
  return fabs( len(Q-B)+len(Q-A)-len(A-B) ) < 1e-9;
}

struct Line{
  Point P0;
  Vector v;
  Line(const Point &pi,const Vector &vi):p0(pi) , v(vi) {}
};

double pointLineLen(const Line &L,const Point &Q){
  return fabs( cross(L.v , Q-L.P0) ) / len(L.v);
}
Point projectToLine(const Line &L,const Point &Q){
  double t = dot(Q-L.P0 , L.v) / dot(L.v , L.v);
  return L.P0 + L.v * t;
}

Point innerCircle(point &p1, point &p2, point &p3){
  // p1,p2,p3 should not on same line
  double a1 = (-2*p1.x + 2*p2.x);
  double b1 = (-2*p1.y + 2*p2.y);
  double c1 = (p2.x*p2.x + p2.y*p2.y - p1.x*p1.x - p1.y*p1.y);
  double a2 = (-2*p1.x + 2*p3.x);
  double b2 = (-2*p1.y + 2*p3.y);
  double c2 = (p3.x*p3.x + p3.y*p3.y - p1.x*p1.x - p1.y*p1.y);
  double cx = (c1*b2-c2*b1) / (a1*b2-a2*b1);
  double cy = (a1*c2-a2*c1) / (a1*b2-a2*b1);
  return Point(cx, cy);
}
Point outerCircle(point &p1, point &p2, point &p3) {
  // p1,p2,p3 should not on same line
  double x1 = (p1.x+p2.x)/2.0;
  double y1 = (p1.y+p2.y)/2.0;
  double x2 = (p2.x+p3.x)/2.0;
  double y2 = (p2.y+p3.y)/2.0;
  double vx = p2.x-p1.x;
  double vy = p2.y-p1.y;
  double ux = p3.x-p2.x;
  double uy = p3.y-p2.y;
  double A  = vx*x1 + vy*y1;
  double B  = ux*x2 + uy*y2;
  double cx = (uy*A - vy*B) / (uy*vx - ux*vy);
  double cy = (ux*A - vx*B) / (ux*vy - uy*vx);
  return Point(cx, cy);
}
```

7.2 Minimal Enclose Disk

```
struct Circle {
  Point c;
  double R2; // square of radius
  Circle() {}
  Circle(const Point &p1, const Point &p2) {
    c.x = (p1.x+p2.x)/2.0;
    c.y = (p1.y+p2.y)/2.0;
    R2 = dot(p1-p2, p1-p2)/4.0;
  }
  Circle(const Point &p1, const Point &p2, const Point &p3) {
    // p1, p2, p3 should not on same line
    c = outerCircle(p1, p2, p3);
    double dx = p1.x - c.x;
    double dy = p1.y - c.y;
    R2 = dx*dx + dy*dy;
  }
  bool contain(const Point &p) const {
    double dx = c.x - p.x;
    double dy = c.y - p.y;
    return fdif(dx*dx + dy*dy - R2)<=0;
  }
};

Circle minEncloseDisk(vector<Point> &ps) {
  // Find minimal circal enclose all point
  // worst case O(n^3), expected O(n)
  Circle D;
  if( ps.size()==0 ) return D;
  if( ps.size()==1 ) {
    D.c  = ps[0];
    D.R2 = 0.0;
    return D;
  }

  random_shuffle(ps.begin(), ps.end());
  D = Circle(ps[0], ps[1]);
  for(int i=2; i<ps.size(); ++i) {
    if( D.contain(ps[i]) )
      continue;
    D = Circle(ps[i], ps[0]);
    for(int j=1; j<i; ++j) {
      if( D.contain(ps[j]) )
        continue;
      D = Circle(ps[i], ps[j]);
      for(int k=0; k<j; ++k) {
        if( D.contain(ps[k]) )
          continue;
        D = Circle(ps[i], ps[j], ps[k]);
      }
    }
  }
}
```

7.3 2D Convex Hull

```
bool turnLeft(const Vector &v1, const Vector &v2) {
  return fdif(cross(v1, v2)) > 0LL;
}
vector<Point> convexHull(vector<Point> &ps) {
  // return convex hull without redundant point
  sort(ps.begin(), ps.end());

  vector<Point> up;
  for(int i=0; i<ps.size(); ++i) {
    while( up.size()>1
      && !turnLeft(up.back()-up[up.size()-2],
        ps[i]-up.back()) )
      up.pop_back();
    up.emplace_back(ps[i]);
  }

  vector<Point> btn;
  for(int i=ps.size()-1; i>=0; --i) {
    while( btn.size()>1
      && !turnLeft(btn.back()-btn[btn.size()-2],
        ps[i]-btn.back()) )
      btn.pop_back();
    btn.emplace_back(ps[i]);
  }

  vector<Point> res(up);
  res.insert(res.end(), btn.begin()+1, btn.end());
  res.pop_back();
  return res;
}
```

7.4 Closest Point

```
#include <iostream>
#include <cstdio>
#include <algorithm>
#include <cstring>
#include <cmath>
#define N 10010
#define INFINITY__ 1e10
using namespace std;
```

```
int diff(double f) {
  if(fabs(f) < 1e-9)
    return 0;
  return f < 0 ? -1 : 1;
}
struct point {
  double x, y;
  bool operator < (const point &p) const {
    return diff(x - p.x) < 0;
  }
};
point pt[N], tmp[N];
double dis(point a,point b) {
  return sqrt((a.x - b.x)*(a.x - b.x) + (a.y - b.y)*(a.y - b.y));
}
double closestpoint(int L,int R) {
  if(R - L + 1 == 1) return INFINITY__;
  int M = (L+R)/2;
  double middle = pt[M].x;
  double Ldis = closestpoint(L, M);
  double Rdis = closestpoint(M+1, R);
  double radi = min(Ldis, Rdis);
  int cntpt = 0;
  merge(pt+L, pt+M+1, pt+M+1, pt+R+1, tmp+L, [](point a,point b)
     {
    return diff(a.y - b.y) < 0;
  });
  copy(tmp + L,tmp + R + 1, pt + L);
  for(int i = L; i <= R; i++)
    if(diff(fabs(pt[i].x - middle) - radi) < 0)
      tmp[cntpt++] = pt[i];
  for(int i = 0; i < cntpt; i++)
    for(int j = 1; i + j < cntpt && j < 8; j++)
      radi = min(radi, dis(tmp[i], tmp[i+j]));
  return radi;
}
```

7.5 Min Max Triangle

```
pair<double,double> findMinMaxTri(vector<Point> &ps) {
  static const double PI = acos(-1.0);
  struct Seg {
    double rad; // [0.5pi, 1.5pi]
    int s1, s2;
  };

  const int n = ps.size();
  sort(ps.begin(), ps.end(), [](const Point &l, const Point &r) {
    if( fdif(l.x - r.x) == 0 )
      return l.y > r.y;
    return l.x < r.x;
  });
  vector<int> id(n+4);
  for(int i=0; i<n; ++i)
    id[i] = i;

  // sort all pair of point
  vector<Seg> segs;
  for(int i=0; i<n; ++i)
  for(int j=i+1; j<n; ++j) {
    double m = atan2(ps[j].y-ps[i].y, ps[j].x-ps[i].x) + PI;
    segs.push_back({m,i,j});
  }
  sort(segs.begin(), segs.end(), [](const Seg &l, const Seg &r) {
    return fdif(l.rad - r.rad) < 0;
  });

  // find min max triangle
  pair<double,double> ret;
  ret.first = ret.second = fabs(cross(ps[0], ps[1], ps[2]));
  for(auto seg : segs) {
    swap(ps[id[seg.s1]], ps[id[seg.s2]]);
    swap(id[seg.s1], id[seg.s2]);

    const Point &p1 = ps[id[seg.s1]];
    const Point &p2 = ps[id[seg.s2]];
    int id1 = min(id[seg.s1], id[seg.s2]);
    int id2 = max(id[seg.s1], id[seg.s2]);

    // find min triangle
    if( id1-1 >= 0 ) {
      double a = fabs(cross(p1, p2, ps[id1-1]));
      if( a < ret.first )
        ret.first = a;
    }
    if( id2+1 < n ) {
      double a = fabs(cross(p1, p2, ps[id2+1]));
      if( a < ret.first )
        ret.first = a;
    }

    // fin max triangle
    if( id1 != 0 ) {
      double a = fabs(cross(p1, p2, ps[0]));
      if( a > ret.second )
        ret.second = a;
    }
    if( id2 != n-1 ) {
      double a = fabs(cross(p1, p2, ps[n-1]));
      if( a > ret.second )
        ret.second = a;
    }
  }
  ret.first  /= 2.0;
  ret.second /= 2.0;
  return ret;
}
```