

→ Z-test

→ t-test



$n < 30$

no pop S.D

use-case

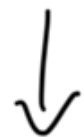


compare categorical

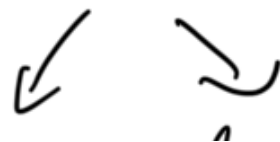
vs numeric data.

A		B	
1	✓	2	✓
2	✓	3	✓
3	✓	4	✓
<hr/> M ₁		<hr/> M ₁	

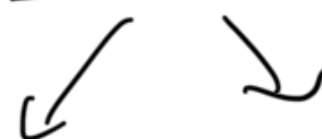
categorical vs categorical [Chi-squared test]



India



Sachin



century

no-century

win loss

continuity

DoF (Degree of Freedom)

Salary	S_1	S_2	S_3	S_4
	40	30	40	?
				↓
				50

$$\boxed{\text{avg} = 40}$$

How many known salaries
required to find the missing salary values
given we know μ salary.

n

Dof : $(n-1)$

5 {

H	W
73	85
68	73 ✓
74	96
71	82
✓ 62	70
(71)	(81)
n_1	n_2

$$\text{DoF} : (n_1 - 1) + (n_2 - 1)$$

$$=$$

win

Sachin
Century

	F	T ✓
F	x	$314 - x$ └───┘
T ✓	$176 - x$ └───┘	└───┘

314 ✓

(46) ✓

$\boxed{176 \quad 184} \mid 360$

✓

✓

①

4-1

	A	B	C	D	
X	p ✓	r	t	✓	349
Y	q ✓	s	u	✓	151
Z	✓	✓	✓	✓	150
	150 ✓	150 ✓	200 ✓	150 ✓	650

① ③

⑥ //

④

DoF:

1 2 3

$$C1 \rightarrow 3$$

$$(3-1) \times (4-1)$$

$$C2 \rightarrow 4$$

$$= 6$$

$$\underline{(n-1) \times (m-1)}$$

Chi-Squared (Goodness of Fit)

50 trials

H_0 : fair coin ✓✓

H_a : not a fair coin

contingency matrix
cross-table

→ ✓✓ expected

	H	T
✓	25 ✓	25 ✓
✓		

50 ✓✓

\rightarrow Actual
 $(O - E)^2$

(28) ✓	(22) ✓	(50) ✓
9	9	DoF ✓✓
$(3)^2$	$(3)^2$	(1) ✓✓

observed - expected = $+ (3)$
 $- 3$

total error
 $= 3^2 + 3^2$
 $= (18)$ ✓✓

$(O - E)^2 \rightarrow$ total error

\checkmark 1 cr ✓

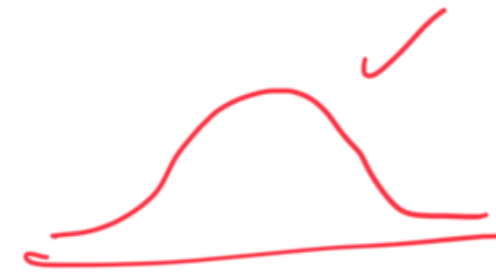
100 cr ✓
 12

A
Ro 10

10
30 ch

$$\text{Error} = \frac{(O - E)^2}{E}$$

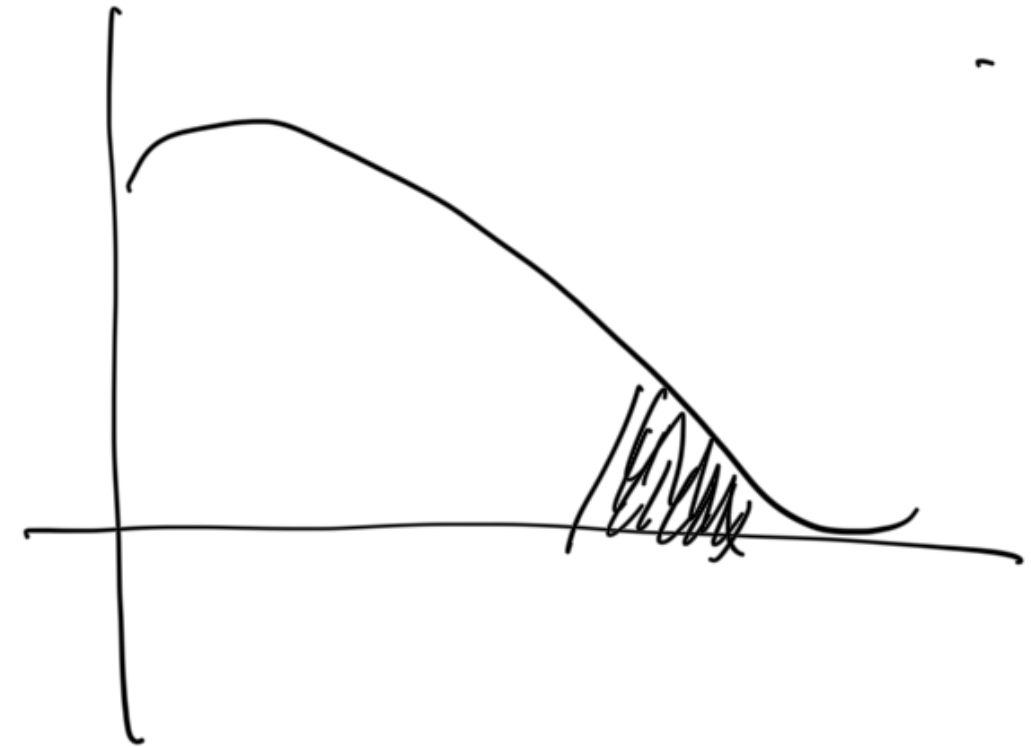
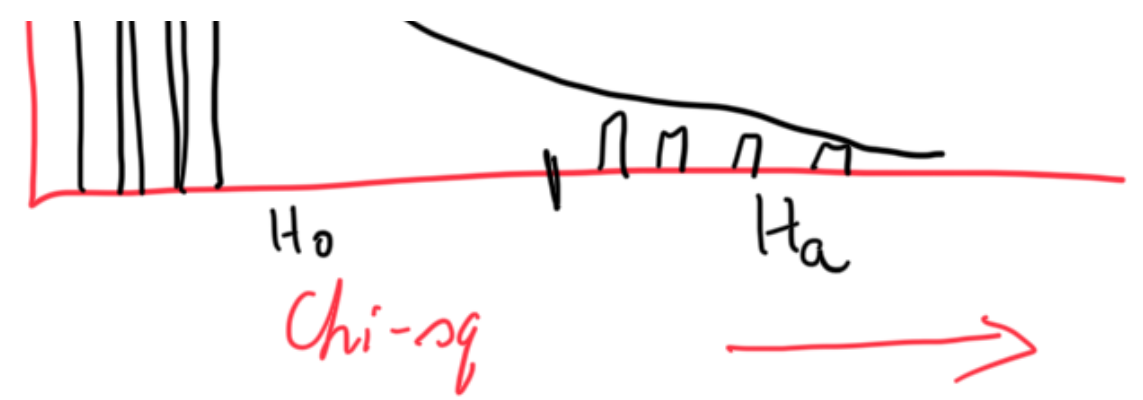
Chi-sq statistic
 χ^2



Distribution
of χ^2 test.



Coin is fair



Test of Independence.

Q: is gender related to online vs offline behaviour

shopping

observed values

	M	F	
	206 249	102	308
online	1 mill		
offline	527	72	599
	484	115	
	733	174	907

34%

$\frac{599}{907} \approx 66\%$

66% of 733 =

$$\frac{(206 - 249)^2}{249} +$$

no relation b/w gender and shopping style

H_0 : no relationship

H_a : there is a relationship

	A	B	C
1			
2			
3			

$$(n-1) \times (m-1)$$

$$2 \times 2 = \underline{\underline{4}}$$

A ✓

B ✓

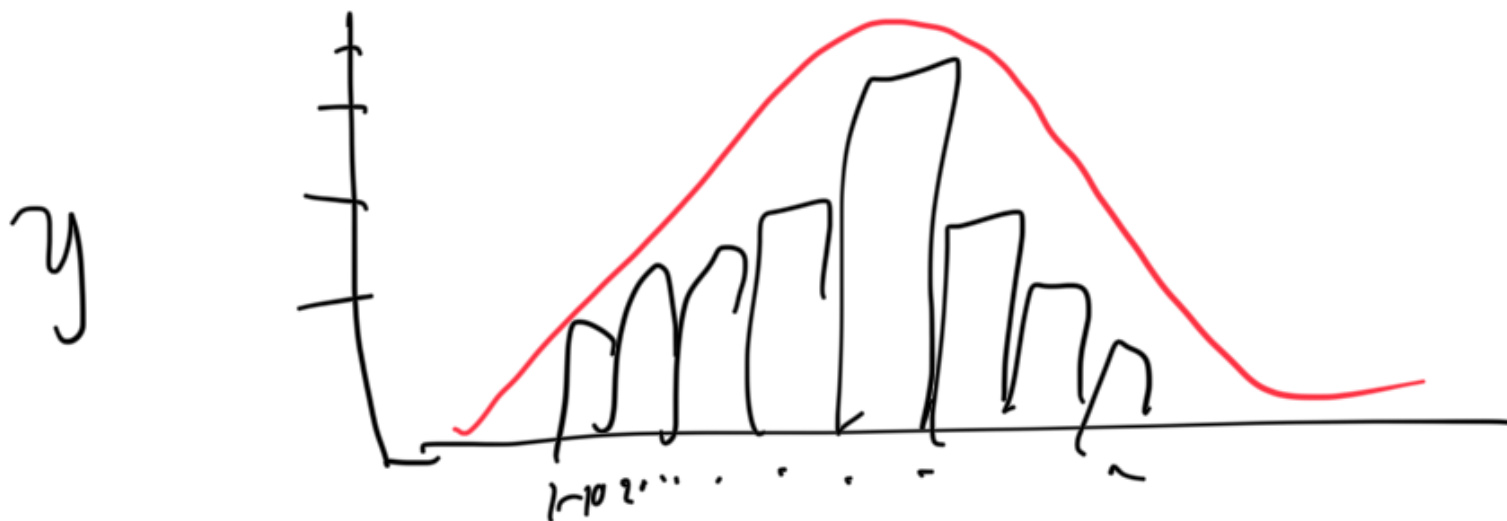
C ✓

$$3 - 1 = \underline{2}$$

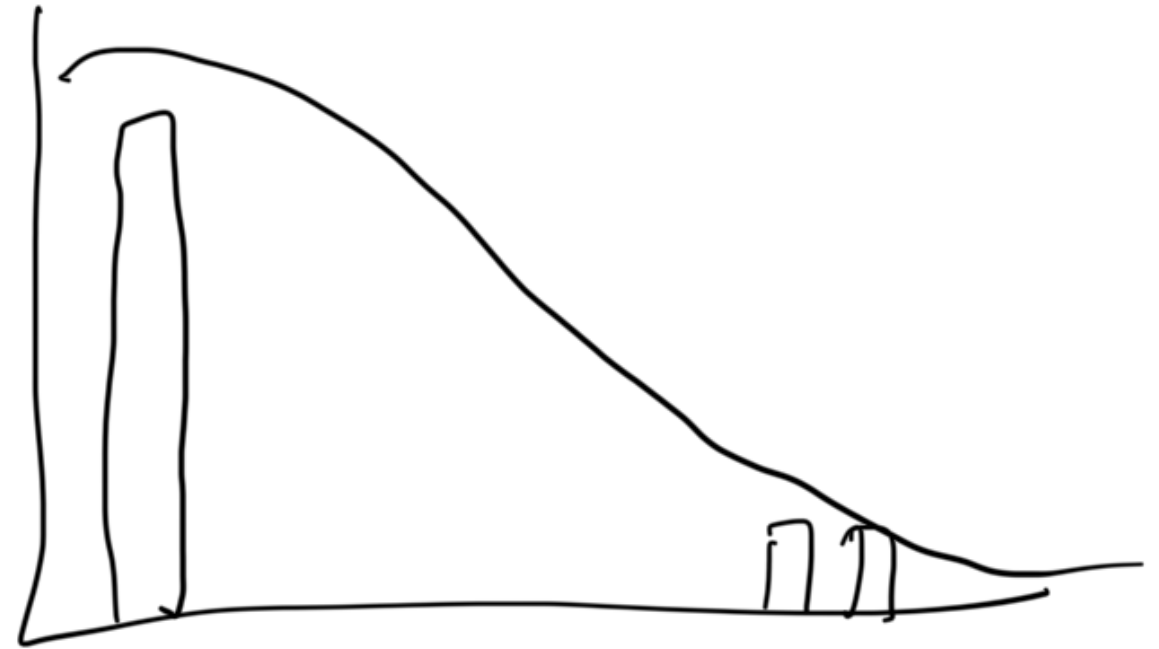
observed
expected

A			
70	80	50	200
60 ✓	80 ✓	60 ✓	200

GOF: for a categorical var
if obs and expected match or not.



age



Chi-