

χ^2 -TEST

Hypothesis Testing Framework

H_0

H_a

- 1) Setup the Null and Alternate Hypothesis
- 2) Choose the right test statistic
- 3) Left tailed vs Right tailed vs Two-Tailed
- 4) Compute P-value
- 5) If P-value is less than alpha, then reject the null hypothesis.

t test

Numerical v/s Categories
(2 categories)
Categorical v/s Categorical

T test

Chi square test.

Degree of freedom

$$\underline{\bullet} \quad \underline{\bullet} \quad \underline{\quad} = 36$$

If I have 'n' places to fill & I know the
mean



$$\text{degree of freedom} = n - 1$$

	H	W
x_1	●	
x_2	●	●
x_3		●
x_4	●	●
	μ_H	μ_W
	n_1	n_2

$$(n_1 - 1) + (n_2 - 1)$$

$$\text{Dof} = n_1 + n_2 - 2$$

Cities

Candidate

	A	B	C	D	
X_1	x_1	100	90	x_3	350
X_2	x_2	20	20	x_4	50
X_3	80	20	50	50	200
	150	140	160	150	600

Rows = m (3)
Columns = n (4)

$$x_1 + x_2 = 70 \quad (1)$$

$$x_1 + x_3 = 160 \quad (2)$$

$$x_3 + x_4 = 100 \quad (3)$$

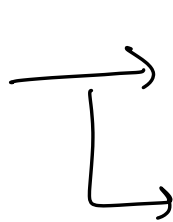
$$x_2 + x_4 = 10 \quad (4)$$

x_1, x_2, x_3, x_4

$$\underbrace{(n-1) + (m-1) + (m-1)}_{(3)}$$

$$\text{DOF} = (m-1) \times (n-1)$$

Chisquare



Goodness of fit

Test of Independence

① Coin toss

H_0 : Coin is fair

H_a : Coin is biased

50

	Heads	Tails
OBSERVATION	28	22
EXPECTATION	25	25

$$\chi^2_{stat} = \frac{(28 - 25)^2}{25} + \frac{(22 - 25)^2}{25}$$

frequencies

$$\chi^2_{stat} = \sum \left(\frac{\text{observation} - \text{Expectation}}{\text{Expectation}} \right)^2$$

(S1) $\chi^2_{stat} = 0.72$

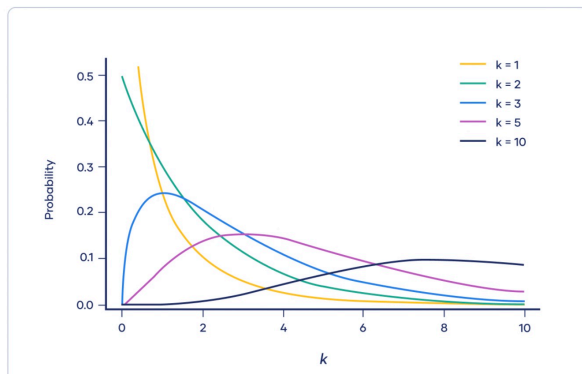
Coin
is
fair

H_0

(S2) $\chi^2_{stat} = 32$

Coin
is
not
fair

H_a

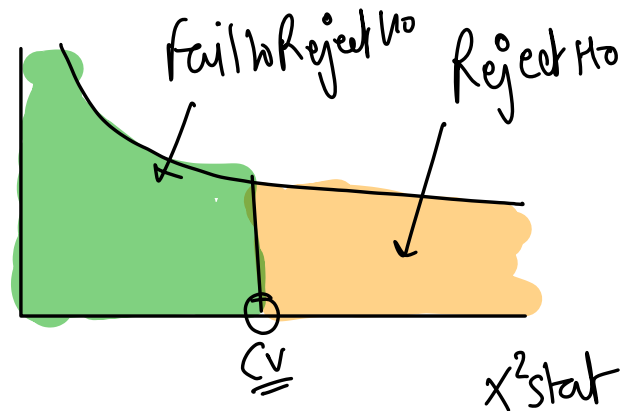


(S1)

	Heads	Tails
OBSERVATION	28	22
EXPECTATION	25	25

(S2)

	Heads	Tails
OBSERVATION	45	5
EXPECTATION	25	25



χ^2 tests are always Right Tailed.

Profit 110600

Profit - 111800

Bulb manufacturer.

	10	20	30	100	50	60	80	
	B1	B2	B3	B4	B5	B6	B7	
Expectations	50	20	30	10	40	30	20	200
OBSERVATIONS	60	10	10	30	50	20	20	
No. of bulbs	100	100	100	100	100	100	100	
Revenue	1000	2000	3000	10000	5000	6000	8000	
no. of defective	50	20	30	10	40	30	20	
Refund	500	400	900	1000	2000	1800	1600	
Refund .9400	60	10	10	30	50	20	20	
	600	200	300	3000	2500	1200	1600	

20,000

no. of defective

8200

Refund

TEST OF INDEPENDANCE

Amazon

observation

	F	M	
offline	527	72	599
Online	206	102	308
	733	174	907

Expected freq -

	F	M	
offline	484	115	599
Online	249	59	308
	733	174	907

H_0 Gender doesn't affect buying pattern (independant)

H_a Gender affect buying pattern (dependant)

If we know that 66% of Total people prefer offline shopping, how many females will prefer to buy offline -

observed

597	72	0
206	102	0
0	0	1

expected

