

Pooled Milk test

A milk bank tests pooled sample tests of 4 people at a time.

If clean, the bank stores all of them.

if Unacceptable, then all 4 samples are tested individually,

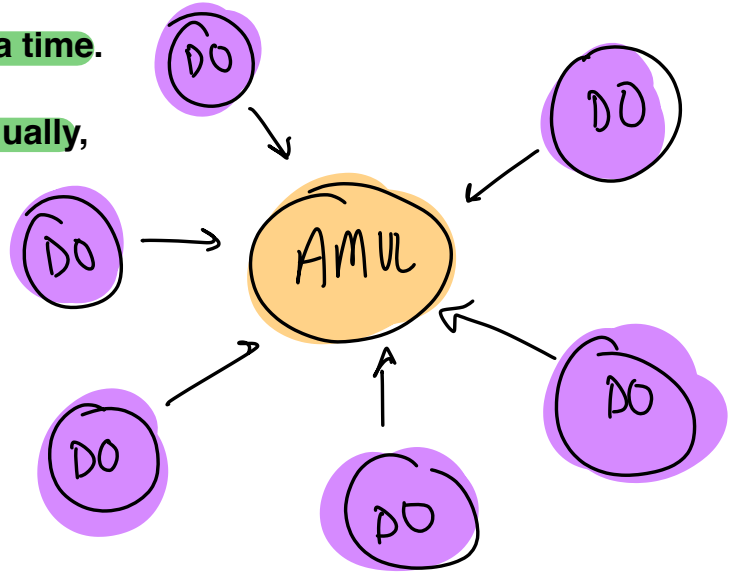
The probability of any sample being dirty is 0.1.

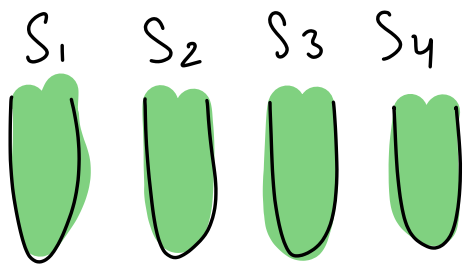
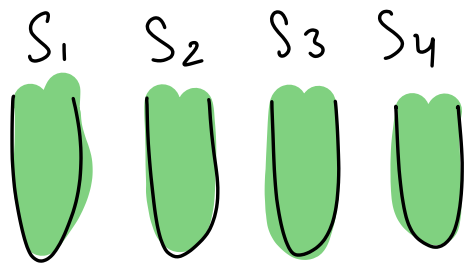
Find the expected number of tests.

Rs 1000

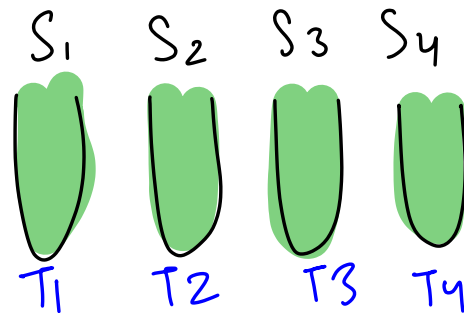
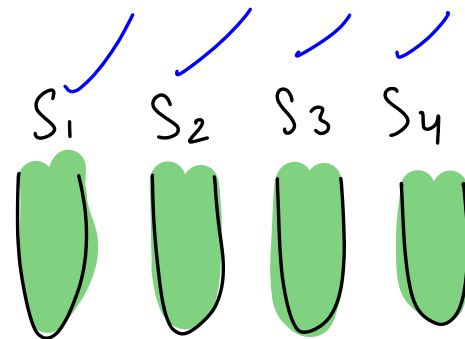
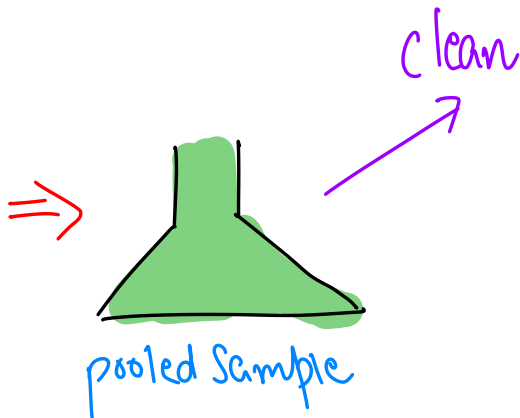
4000 DOs → 16 Samples → 40000 Samples

Per day Amul is spending $\Rightarrow 40000 \times 1000 = 40 \text{ Cr}$





$$1000 \times 4 = 4000$$



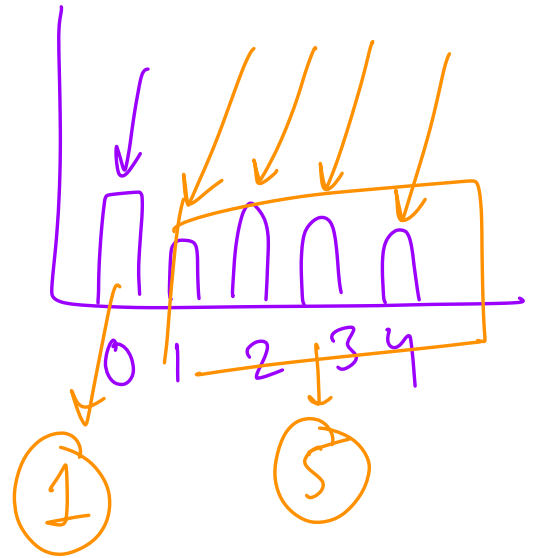
Unclean

$$\text{Binom.pmf}(n=4, k=1, p=0.1) + \text{Binom.pmf}(n=4, k=2, p=0.1) \\ + \text{Binom.pmf}(n=4, k=3, p=0.1) + \text{Binom.pmf}(n=4, k=4, p=0.1)$$

$$E[X] = \sum X P(X)$$

$$= 1 \times 0.6561 + 5 \times 0.3439$$

$$= \underline{2.3756} \quad \underline{\text{tests}} \quad \text{per } \underline{\underline{4 \text{ Samples}}}$$



4 Samples \rightarrow 4 tests \rightarrow Rs 4000

4 Samples \rightarrow 2.375 tests \rightarrow Rs 2375

<u>In one day</u>	40000 test	\rightarrow	4 Cr	}	<u><u>1.62 Cr</u></u>
	2375 test	\rightarrow	2.375 Cr		

1 year Annul is saving \Rightarrow 591 Crs per year.

Bernoulli \rightarrow $\begin{cases} \text{Success} & \text{Clean} & 0.9 \\ \text{Failure} & \text{dirty} & 0.1 \end{cases}$

X	$P(X)$
1	$\text{Binom. pmf}(n=4, k=4, p=0.9)$
5	$\text{Binom. pmf}(n=4, k=0, p=0.9) + \text{Binom. pmf}(n=4, k=1, p=0.9)$ $+ \text{Binom. pmf}(n=4, k=2, p=0.9) + \text{Binom. pmf}(n=4, k=3, p=0.9)$

$$\Rightarrow \text{Binom. cdf}(n=4, k=3, p=0.9)$$

$$\Rightarrow 1 - \text{Binom. pmf}(n=4, k=4, p=0.9)$$

Module owners of current (Fundamentals) module wants to know in the initial class that the learners have a good grasp of previous module.

6 Learners were chosen and were given P&S test. MO wants the class to score above 70 on the test for a successful module completion.

The 6 learners get the following scores : 62,92,75,68,83,95.

Can current MO have 90% C.I. that the mean score for the class on the test would be above 70?

$$H_0 : \mu = 70$$

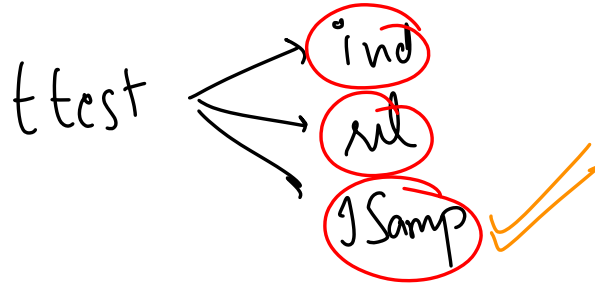
$$H_a : \mu > 70$$

$$\text{Confidence} = 90\%$$

$$\alpha = 0.1$$

$$p = 0.07$$

$$p < \alpha$$



"Right tailed test"

"Reject H_0 "

Avg. IQ of the population is 100 with std. of 15. A team of scientists want to test the new medication to see if it has either a positive or negative effect or no affect at all. A sample of 30 participants who have taken the medicines were found to have avg. IQ 140. Did the medicine affect intelligence?

H_0 : Not effect
 H_a : Affect Intelligence

Z test

$$Z = \frac{140 - 100}{15/\sqrt{30}} = \underline{\underline{14.6}}$$

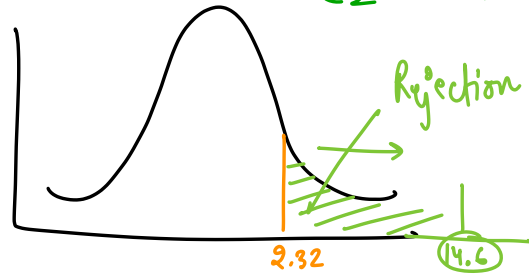
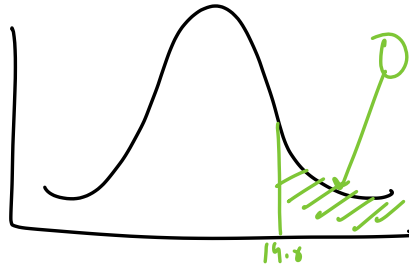
"Right tailed"

pvalue = 0

"Reject H_0 "

$\mu = 100$
 $\sigma = 15$
 $n = 30$
 $\bar{x} = 140$

$\alpha = 0.01$
 $CI = 99\%$



Amazon Fulfillment centre

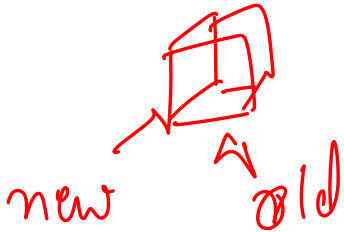
Amazon is trying to experiment 2 different machines that will pack the deliveries. It is supposed that the new machine will package on an average quicker in comparison to the old one. To test the hypothesis, the time it takes to pack the deliveries are recorded. Do the data provide sufficient evidence to conclude that, on average the new machine is better than the old one?

```
new_machine = np.array([42.1, 41, 41.3, 41.8, 42.4, 42.8, 43.2, 42.3, 41.8, 42.7])  
old_machine = np.array([42.7, 43.6, 43.8, 43.3, 42.5, 43.5, 43.1, 41.7, 44, 44.1])
```

H_0 new machine = old machine	$\mu_N = \mu_0$	TEST ttest_ind.
H_a new > old	$\mu_N < \mu_0$	

CI = 99%

$\alpha = 0.01$



pvalue = 0.006

pvalue < $\alpha \Rightarrow$ "Reject H_0 "

A gym is claiming to help you lose weight and they take help from an independent consultant to prove their claim. The consultant takes in sample of 15 people, weighing each of them before the gym begins and 3 months later. Test their Claim.

$$H_0 : \mu_A = \mu_B$$

$$H_a : \mu_A < \mu_B$$

$$\text{Confidence} = 95\%$$

$$\alpha = 0.05$$

Valid

ttest - rel (After , Before , alternative = " less ")

$$p\text{value} < \alpha$$

"Reject H_0 "

A study claims that children learn most effectively with a constant background sound in comparison to unpredictable sound or no sound at all. Scientists divided 24 children into groups of 8 each. All the children are asked to learn a passage for 3 days under 3 conditions. After 3 days, they were asked to take a test and their scores are calculated.

$$H_0: \mu_1 = \mu_2 = \mu_3$$

$$H_a: \mu_1 \neq \mu_2 \neq \mu_3 \text{ (At least one of them is different)}$$

$$p = 0.04 \quad \alpha = 0.05$$

$$p < 0.05 \rightarrow \text{"Rejected"}$$

A random sample of 500 Adult Indians are questioned about their opinions and affiliations to political parties on the new bill passed in Rajya Sabha. We need to test whether their affiliation and their opinion are dependant at 5% Alpha.

	Favour	Indifferent	Opposed	Total
BJP	138	83	64	285
INC	64	67	84	215
Total	200	150	148	500

H_0 : Independent
 H_a : dependent

$$\alpha = 0.05$$

$$p\text{value} = 1.54 \times 10^{-5}$$

$$p < \alpha \rightarrow \text{"Rejcd } H_0"$$

dependent.

Twenty-five men between the ages of 25 and 30, who were participating in a well-known heart study carried out in Framingham, Massachusetts, were randomly selected. Of these, 11 were smokers and 14 were not. The following data refer to readings of their systolic blood pressure. Use these data to test the hypothesis that the mean blood pressures of smokers and nonsmokers are the same.

```
: non_smokers= [130, 122, 128, 129, 118, 122, 116, 127, 135, 120, 122, 120, 124, 134, 136, 125, 133, 127, 135, 131, 133, 125, 118]
```

$$H_0: \mu_S = \mu_{NS}$$

2 tailed test

$$H_a: \mu_S \neq \mu_{NS}$$

T-test-ind.

$$p = 0.018$$
$$p < \alpha$$

$\alpha = 0.05$
"Reject H_0 " →

In a test of the ability of a certain polymer to remove toxic wastes from water, experiments were conducted at three different temperatures. The data below give the percentages of the impurities that were removed by the polymer in 21 independent attempts.

```
low_temp=[42,41,37,29,35,40,32]  
mid_temp=[36,35,32,38,39,42,34]  
high_temp=[33,44,40,36,44,37,45]
```

$$H_0 : \mu_1 = \mu_2 = \mu_3$$

$$H_a : \mu_1 \neq \mu_2 \neq \mu_3 \quad (\text{At least one of them is diff.})$$

Q) Recommender System

When a customer buys a T-Shirt, a recommender algorithm suggests a few related items. The recommender system in production(legacy) that has a success rate of 10%. You and your team have developed a new DL algorithm for recommendation. It is tested before deploying. Of the next 500 customers, 72 bought items recommended by the new model. Is the improvement brought by the new model is statistically significant at 95% confidence?

$$H_0: \text{old} = \text{new}$$

$$H_a: \text{old} < \text{new}$$

"Right"

Binomial

$$n$$

$$500$$

$$k$$

$$72$$

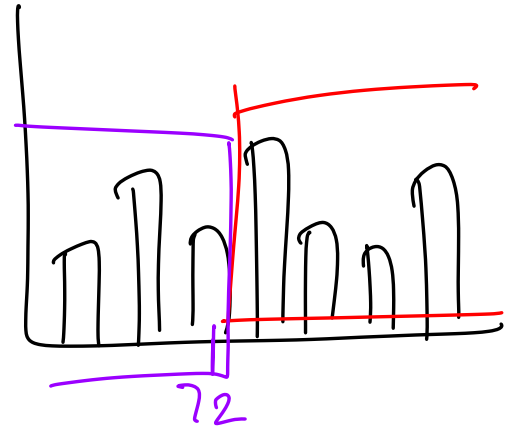
$$p$$

$$0.1$$

Bernoulli \rightarrow $\begin{matrix} S & (0.1) \\ f & (0.9) \end{matrix}$

$$P[X \geq 72] \text{ pvalue}$$

$$1 - \text{binom. cdf}(n=500, k=71, p=0.1)$$



Q) A sample of 300 cars having cellular phones and 400 cars without phones were tracked for 1 year. The following table gives the number of these cars involved in accidents over that year.

Use the above to test the hypothesis that having a cellular phone in your car and being involved in an accident are independent. Use the 5 percent level of significance.

	Accident	No accident
Cellular phone	22	278
No phone	26	374

H_0 Ind

H_a : dep

$$\alpha = 0.05$$

$$p = 0.77$$

"fail to reject H_0 "

Numerical \rightarrow 2 Categories \rightarrow tTest $\begin{cases} \rightarrow \text{rel} \\ \rightarrow \text{ind} \\ \rightarrow \text{1samp} \end{cases}$

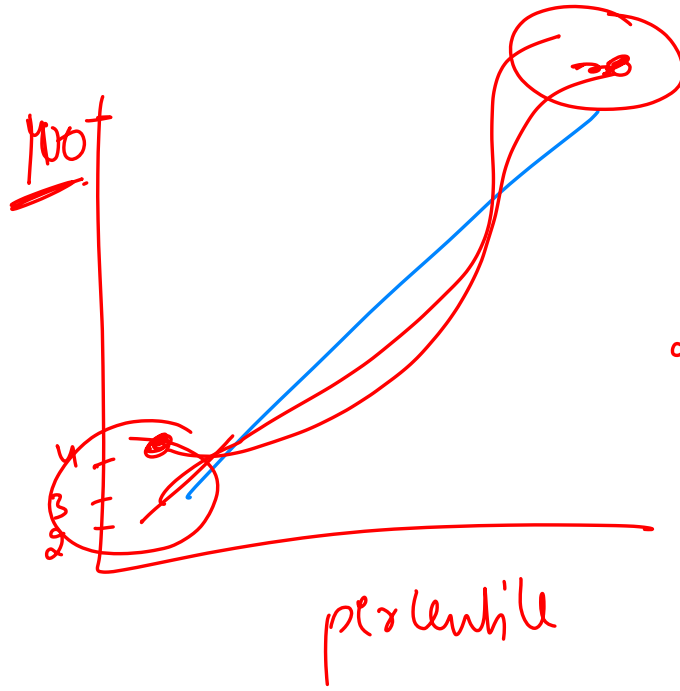
Numerical - Numerical \rightarrow Correlation

Categorical - Categorical \rightarrow Chi'square

\hookrightarrow Goodness of fit

dependent
Independent

2 Categorical \rightarrow Test of Independence -



$$\begin{array}{r} 2, 4, 3, 100 \\ \hline 100 \end{array}$$

~~25~~

25 th	50 th	75 th	100
2	3	4	100

Ttest Ind

② Numerical 2 Categories } Non Smoker
Numerical values } μ_1, μ_2 } Smoker.

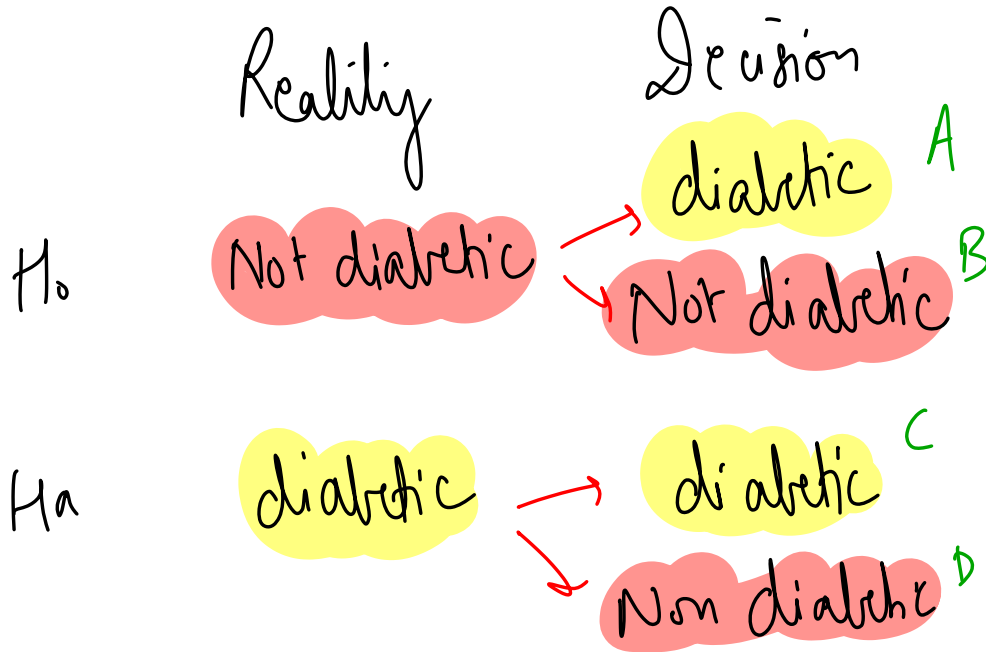
Chi square Test
of Independence

② Categorical Column mentioning

freq

Numerical	Categorical
Mean	Mode
Median	"Unknown" —
-1 ✓ 0 ✓	"Other" —

① Diabetic (+ve)
Non diabetic (-ve)



(α) Type I error

FALSE POSITIVE

TRUE NEGATIVE

TRUE POSITIVE

FALSE NEGATIVE

(β)

Type II error.