

## WINTER-2019

### UNIT-1

**Q.1 a)** Show the following equivalences (7)

1.  $A \rightarrow (P \vee C) \Leftrightarrow (A \wedge \neg P) \rightarrow C$

2.  $(P \rightarrow C) \wedge (Q \rightarrow C) \Leftrightarrow (P \vee Q) \rightarrow C$

**b)** Show that the following implication without constructing truth table. (7)

1.  $(P \rightarrow Q) \Rightarrow (P \rightarrow (P \wedge Q))$

2.  $((P \rightarrow Q) \rightarrow Q) \Rightarrow (P \vee Q)$

**Q.2 a)** Obtain principle disjunctive normal form (7)

1.  $P \rightarrow ((P \rightarrow Q) \wedge \neg(\neg Q \vee \neg P))$

2.  $\neg(P \vee Q) \Leftrightarrow (P \wedge Q)$

**b)** Obtain principle conjunctive normal form. (7)

1.  $(\neg P \rightarrow R) \wedge (Q \Leftrightarrow P)$

2.  $(P \wedge Q) \vee (\neg P \wedge R)$

### UNIT-2

**Q.3 a)** Determine whether the conclusion C follows logically from premises given.

1.  $H_1 : \neg Q, H_2 : P \rightarrow Q, C : \neg P.$

2.  $H_1 : \neg P, H_2 : P \vee Q, C : Q$

3.  $H_1 : P \rightarrow Q, H_2 : P, C : Q$  (7)

**b)** Show that  $R \wedge (P \vee Q)$  is a valid conclusion from the premises  $P \vee Q, Q \rightarrow R, P \rightarrow M, \& \neg M.$  (6)

**Q.4)** Show that following set of premises are inconsistent.

1.  $P \rightarrow Q, P \rightarrow R, Q \rightarrow \neg R, P$

2.  $A \rightarrow (B \rightarrow C), D \rightarrow (B \wedge \neg C), A \wedge D$  (7)

**b)** Use indirect proof method to show  $\neg (P \wedge Q)$  follows from  $\neg P \wedge \neg Q.$  (6)

### UNIT-3

**Q.5 a)** Given the relation matrices  $M_R$  &  $M_S$  (7)

Find  $M_{R \circ S}$ ,  $M_{\overline{R}}$ ,  $M_{\overline{S}}$ ,  $M_{\overline{R \circ S}}$   $M_{\overline{S \circ R}}$

$$M_R = \begin{bmatrix} 1 & 0 & 1 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix} \quad M_S = \begin{bmatrix} 1 & 0 & 0 & 1 & 0 \\ 1 & 0 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 0 \end{bmatrix}$$

**b)** Let the compatibility relation onset  $\{x_1, x_2, \dots, x_6\}$  be given by the matrix (6)

$x_2$	1				
$x_3$	1	1			
$x_4$	0	0	1		
$x_5$	0	0	1	1	
$x_6$	1	0	1	0	1
	$x_1$	$x_2$	$x_3$	$x_4$	$x_5$

Draw the graph and find maximal compatibility blocks of the relation.

**Q.6 a)** Let  $R = \{\langle 1,2 \rangle \quad \langle 3,4 \rangle \quad \langle 2,2 \rangle\}$  and  $S = \{\langle 4,2 \rangle \quad \langle 2,5 \rangle \quad \langle 3,1 \rangle \quad \langle 1,3 \rangle\}$

Find  $R \circ S$ ,  $S \circ R$ ,  $R \circ (S \circ R)$ ,  $((R \circ S) \circ R)$   $R \circ R \circ R$ ,  $S \circ S$ . (6)

**b)** Given  $S = \{S, a, \{3\}, 4\}$   $R = \{\{a\}, 3, 4, 1\}$

Indicate whether following are true or false.

1.  $\{a\} \in S$
2.  $\{a\} \in R$
3.  $\{a, 4 \{3\}, 4\} \subseteq S$
4.  $\{\{a\}, 1, 3, 4\} \subset R$
5.  $R = S$
6.  $\{a\} \subseteq S$
7.  $\{a\} \subseteq R$
8.  $\phi \in R$

(7)

## UNIT-4

**Q.7 a)** Define the following terms. (6)

- 1) Sub Algebra
- 2) Semigroup
- 3) Monoid
- 4) Group.

**b)** Let  $\langle G, * \rangle$  be a group in which  $G = \{e, a\}$  and  $\langle \langle G, * \rangle$  is defined as. (7)

*	e	a
e	e	a
a	a	e

Find out  $\langle G \times G, 0 \rangle$  direct product of G with itself.

**Q.8 a)** Write down the composition table for  $\langle Z_6^*, +_6 \rangle$  and  $\langle Z_6, *_6 \rangle$  where,  $Z_6^* = Z_6 - [0]$ . (7)

**b)** Show that every element in a group is its own inverse then the group must be abelian group. (6)

## UNIT-5

**Q.9 a)** Obtain the sum of product expression of each of the following using k map

1.  $f(a, b, c, d) = \Sigma 2, 4, 5, 6, 7, 9, 11, 12, 13, 14, 15.$

2.  $f(a, b, c, d) = \Sigma 0, 5, 7, 8, 10, 12.$  (7)

**b)** Simplify following Boolean expression. (7)

1.  $(a * b)' = (a + b)'$

2.  $(a' * b * c) + (a * b' * c) + (a * b' * c')$

3.  $(a + b') * (b + c') * (c + a')$

**Q.10 a)** prove the following Boolean identities. (7)

1.  $a + (a' * b) = a + b.$

2.  $a * (a' + b) = a * b.$

3.  $(a * b) + (a * b') = a$

4.  $(a * b * c) + (a * b) = (a * b)$

**b)** Let  $X = \{2, 3, 6, 12, 24, 36\}$  then relation  $\leq$  i.e.,  $x < y$  if  $x$  divides  $y$  draw Hasse diagram.  $\langle x, \leq \rangle$  and Determine it is lattice or not. (7)

## UNIT-6

**Q.11 a)** Define the terms.

1) Strongly connected graph

2) Weakly connected graph.

3) Null graph

4) Simple graph. (7)

**b)** Give the Warshall's Algorithm for path matrix with example. (6)

**Q.12 a)** Show that in a complete binary tree, the total number of edges is given by  $2(n_t - 1)$  where  $n_t$  is total number of terminal nodes. (6)

**b)** Traverse the following tree with in-order, pre-order. (7)

