

**WINTER-2014****UNIT 1**

**Q1. a)** What is statement formula? What are the rules for generating well-formed formula? (6)

**b)** Explain with the example:

i. Conditional and Bi-conditional statements      ii. Tautology and contradiction (6)

**Q2. a)** Show the following equivalences without truth table

**i.**  $A \rightarrow (P \vee C) \Leftrightarrow (A \wedge \neg P) \rightarrow C$       **ii.**  $(P \vee Q) \rightarrow C \Leftrightarrow (P \rightarrow C) \wedge (Q \rightarrow C)$  (8)

**b)** Obtain Principle Conjunctive Normal form of  $(\neg P \rightarrow R) \vee (Q \Leftrightarrow P)$  (5)

**UNIT 2**

**Q3. a)** Symbolize the following statements

i. All cats are animals

ii. Rosses are red and violets are blue (6)

**b)** Show that  $S \vee R$  is tautological implied by  $(P \vee Q) \wedge (P \rightarrow R) \wedge (Q \rightarrow S)$ . (7)

**Q4. a)** Show that, (5)

$(x) (P(x) \rightarrow Q(x)) \wedge (x) (Q(x) \rightarrow R(x)) \Rightarrow (x) (P(x) \rightarrow R(x))$

**b)** Determine whether the conclusion C follows logically from the premises  $H_1$  and  $H_2$ :

i. $H_1: P \rightarrow Q$	$H_2: \neg P$	$C: Q$	
ii. $H_1: P \rightarrow Q$	$H_2: \neg(P \wedge Q)$	$C: \neg P$	(8)

**UNIT 3**

**Q5. a)** Define:      i. Intersection      ii. Union  
                          iii. Relative Complement      iv. Disjoint Sets (6)

**b)** Draw Venn diagram of

i.  $A \cap B = A \cap C$  but  $B \neq C$       ii.  $A \cup B = A \cup C$  but  $B \neq C$

iii.  $A \cap B = A \cap C$  but B is not subset of C. (7)

**Q6. a)** Given the relation matrices  $M_R$  and  $M_S$  find  $M_{R \circ S}$ ,  $M_{\bar{R}}$ ,  $M_{\bar{S}}$ ,  $M_{R \circ \bar{S}}$ . Show that  $M_{R \circ \bar{S}} = M_{\bar{S} \circ \bar{R}}$  (7)

$$M_R = \begin{bmatrix} 1 & 0 & 1 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix} \quad M_S = \begin{bmatrix} 1 & 0 & 0 & 1 & 0 \\ 1 & 0 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 0 \end{bmatrix}$$

**b)** Let  $P = \{<1, 2>, <2, 4>, <3, 3>\}$  and  $Q = \{<1, 3>, <2, 4>, <4, 2>\}$ . Find  $P \cup Q$ ,  $P \cap Q$ ,  $D(P)$ ,  $D(Q)$ ,  $R(P)$ ,  $R(Q)$ ,  $D(P \cup Q)$  and  $R(P \cap Q)$ .

Show that  $D(P \cup Q) = D(P) \cup D(Q)$  and  $R(P \cap Q) \subseteq R(P) \cap R(Q)$ . (6)

### UNIT 4

**Q7. a)** Write down the composition tables for

i.  $\langle Z_6, t_6 \rangle$  ii.  $\langle Z_6, X_6 \rangle$  (6)

**b)** Define: i. Group ii. Subgroup (7)

**Q8. a)** What is coset? Find coset of  $\{[0], [4]\}$  in the group  $\langle Z_7, +_7 \rangle$ . (7)

**b)** Convert the following infix expressions to their prefix and postfix form,

i.  $A * B + C / D$  ii.  $A + B * C - D / F$  (6)

### UNIT 5

**Q9. a)** For the following function:  $f = x + y + z$ , Give,

i. Circuit diagram representation ii. Truth Table representation

iii. K-map representation. (8)

**b)** Write the following Boolean expressions in an equivalent sum of product canonical form: i.  $x_1 * x_2$  ii.  $x_1 + (x_2 * x_3')$  (6)

**Q10. a)** Use K-map representation to find minimal sum of product expressions for:

i.  $f(a, b, c) = \Sigma(0, 1, 4, 6)$  ii.  $f(a, b, c, d) = \Sigma(0, 5, 7, 8, 12, 14)$  (8)

**b)** Prove the following Boolean identities,

$$\text{i. } a + (a' * b) = a + b$$

$$\text{ii. } a * (a' + b) = a * b. \quad (6)$$

## UNIT 6

**Q11. a)** Explain with examples

i. Adjacency matrix

ii. Path matrix

iii. Tree

(6)

**b)** Show that the sum of indegrees of all the nodes of a simple digraph is equal to the sum of out degree of all its nodes and that this sum is equal to the number of edges of the graph. (7)

**Q12. a)** Give the directed tree representation of the following formula

$$(P \vee (\neg P \wedge Q)) \wedge ((\neg P \vee Q) \wedge \neg R) \quad (6)$$

**b)** Give three different elementary paths from node  $u_1$  to  $u_3$  for the digraph given in the following figure. What is the shortest distance between  $u_1$  and  $u_3$ ? Is there any cycle in the graph? (7)