

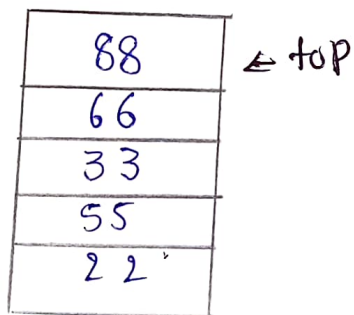
① Perform the following operations using stack. Assume the size of the stack is 5 and having a value of 22, 55, 33, 66, 88 in the stack from a position to size-1. Now perform the following operation.

1) Insert the elements in the stack, 2, POP[3,3] POP[], 3) POP[], 4) push[99], 5) push[36], 6) push[11], 7) push[88], 8) POP[], 9) POP[], draw the diagram of stack & illustrate the above operations & identify where the top is?

→ 1) Stack of the stack : 5

Elements in stack (from bottom to top): 22, 55, 33, 66, 88

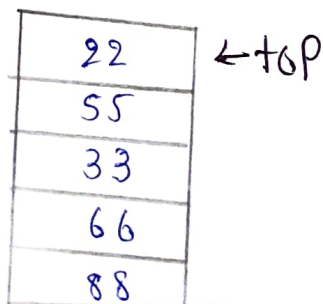
Top of stack : 88



operations:

1) Invert the elements in the stack:

- The operation will reverse the order of elements in the stack.
- After inversion, the stack will look like:



2) pop():

- Remove the top element (22).

55	← top
33	
66	
88	

3) pop():

- Remove the top element (55).

33	← top
66	
88	

4) pop():

- Remove the top element (33).

Stack after pop:

66	← top
88	

5) push(90):

- push the element 90 onto the stack
- Stack after push

90	← top
66	
88	

6) push(36):-

- push the element 36 onto the stack.
stack after push:

36	← top
90	
66	
88	

7) push(11):-

- push the element 11 onto the stack.
stack after push:

11	← top
36	
90	
66	
88	

8) push(88):-

- push the element 88 onto the stack.
stack after push.

88	← top
11	
36	
90	
66	

9) pop() :

• Remove the top element (88).

stack after pop:

11	← top
36	
90	
66	

10) pop() :

• Remove the top element (11).

stack after pop:

36	← top
90	
66	

Final stack state:-

size of stack : 5

Elements in stack (from bottom to top):

36, 90, 66

TOP of stack : 66.

66	← top
90	
36	

Develop an algorithm to detect duplicate elements in an unsorted array linear using search. Determine the time complexity & discuss how you would optimize this process.

Algorithm:

1) Initialization:

create an empty set or list to keep track of elements that have already been seen.

2) linear search:

Iterate through each element of the array:

- for each element, check if it is already in the set of seen elements
- If it is, a duplicate has been found.
- If it is found, add it to the set of seen elements.

3) Output:

Return the list of duplicates, or simply indicate that duplicates exist.

C code :-

```
#include <stdio.h>
#include <stdbool.h>
int main()
{
    int arr[] = {4, 5, 6, 7, 8, 5, 4, 9, 0};
    int size = sizeof(arr) / sizeof(arr[0]);
```

```

bool seen[1000] = {false};
for (int i=0; i<size; i++)
    if (seen[arr[i]])
        printf ("Duplicate found : %d \n", arr[i]);
    else
        seen[arr[i]] = true;
return 0;
}

```

Time complexity:

The linear search complexity:-

The time complexity for this algorithm is $O(n)$, where 'n' is the no. of elements in the array. This is because each element is checked only once, and operations (checking for membership & adding to a set) are $O(1)$ on the average.

Space Complexity:

The space complexity is $O(n)$ due to the additional space used by the 'seen' & 'duplicates' sets, which may store up to 'n' elements in the worst case.

Optimization.

hashing:

the use of a set for checking duplicates is already efficient because sets provide average $O(1)$ time complexity for membership and insertions.

sorting:

If we are allowed to modify the array, another approach is to sort the array first & then perform a linear scan to find duplicates.

sorting would take $O(n \log n)$ time, & the subsequent scan would take $O(n)$ time. this approach uses less space ($O(1)$ additional space if sorting in-place).