Package 'PGAS'

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Description

Implementation of Particle Gibbs with Ancestor Sampling ([1]) and the Particle Marginal Metropolis-Hastings ([2]) algorithms. See (http://www.it.uu.se/katalog/freli660/software) for implementation in 'MATLAB'.

2 conditionalParticleFilter

Details

This package offeres a inverse gamma prior based solution for the PGAS and PMMH algorithms. In future, more generalized priors are planned to be supported. We refer to [1] for theoretical details of PGAS, [2] for details on PMMH algorithm and [3] for implementation details of PGAS and PMMH in MATLAB.

References

- [1] Lindsten, Fredrik, Michael I. Jordan, and Thomas B. Schön. "Particle Gibbs with ancestor sampling." The Journal of Machine Learning Research 15.1 (2014): 2145-2184.
- [2] C. Andrieu, A. Doucet and R. Holenstein, "Particle Markov chain Monte Carlo methods" Journal of the Royal Statistical Society: Series B, 2010, 72, 269-342.
- [3] Lindsten, Fredrik, http://www.it.uu.se/katalog/freli660/software

conditionalParticleFilter

An implementation of conditional particle filter with ancestor sampling

Description

An implementation of conditional particle filter with ancestor sampling

Usage

```
conditionalParticleFilter(param, y, x0, X, N = 100, resamplingMethod = "multi")
```

Arguments

param	state parameters
У	measurements
x0	initial state

X conditioned particles
N number of particles

resamplingMethod

resampling methods: 'multi' multinomial and 'systematic' systematic resampling methods are currently supported.

Value

particles particles
logLikelihood log likelihood
normalisedWeights
normalised weights

conditionalParticleFilter 3

Author(s)

Niharika Gauraha

See Also

```
PGAS, PMMH, particleFilter
```

```
generateData <- function(param, x0, T)</pre>
 #Initialize the state parameters
 f <- param$f # state transition function</pre>
 g <- param$g # tranfer function</pre>
 Q <- param$Q # process noise variance
 R <- param$R # measurement noise variance</pre>
 x = rep(0, T)
 y = rep(0, T)
 x[1] = x0 # Initial state
 for(t in 1:T)
   if(t < T)
     x[t+1] = stateTransFunc(x[t],t) + sqrt(Q)*rnorm(1)
   y[t] = transferFunc(x[t]) + sqrt(R)*rnorm(1)
 return(list(x = x, y = y))
}
stateTransFunc = function(xt, t) 0.5*xt + 25*xt/(1+xt^2) + 8*cos(1.2*t)
transferFunc = function(x) x^2/20
 # Set up some parameters
 T = 100
                         # Length of data record
 # Generate data
 Q = 0.1 # True process noise variance
 R = 1 # True measurement noise variance
 param <- list(f = stateTransFunc, g = transferFunc, Q = Q, R = R)</pre>
 res = generateData(param = param, x0 = 0, T = T)
 x <- res$x
 y <- res$y
 cat("First plot true states and observed states ")
 \#p \leftarrow plot_ly(x = c(1:T), y = x,
               name = 'Real States', type = 'scatter', mode = 'lines+markers')
 \#add_lines(p, x = c(1:T), y = y,
             name = 'Observed States', type = 'scatter', mode = 'lines+markers')
```

4 particleFilter

particleFilter

An implementation of particle filter

Description

An implementation of particle filter

Usage

```
particleFilter(param, y, x0, N = 100, resamplingMethod = "multi")
```

Arguments

param state parameters
y measurements
x0 initial state

N number of particles

 ${\tt resamplingMethod}$

resampling methods: 'multi' multinomial and 'systematic' systematic resampling methods are currently supported.

Value

particles particles
logLikelihood log likelihood
normalisedWeights
normalised weights

Author(s)

Niharika Gauraha

See Also

PGAS, particleFilter, conditionalParticleFilter

particleFilter 5

```
generateData <- function(param, x0, T)</pre>
 #Initialize the state parameters
 f <- param$f # state transition function</pre>
 g <- param$g # tranfer function</pre>
 Q <- param$Q # process noise variance
 R <- param$R # measurement noise variance
 x = rep(0, T)
 y = rep(0, T)
 x[1] = x0 # Initial state
 for(t in 1:T)
 {
    if(t < T)
      x[t+1] = stateTransFunc(x[t],t) + sqrt(Q)*rnorm(1)
   y[t] = transferFunc(x[t]) + sqrt(R)*rnorm(1)
 return(list(x = x, y = y))
}
stateTransFunc = function(xt, t) 0.5*xt + 25*xt/(1+xt^2) + 8*cos(1.2*t)
transferFunc = function(x) x^2/20
 # Set up some parameters
 T = 100
                         # Length of data record
 # Generate data
 Q = 0.1 # True process noise variance
 R = 1 # True measurement noise variance
 param <- list(f = stateTransFunc, g = transferFunc, Q = Q, R = R)</pre>
 res = generateData(param = param, x0 = 0, T = T)
 x <- res$x
 y <- res$y
 #cat("First plot true states and observed states ")
 \#p \leftarrow plot_ly(x = c(1:T), y = x,
               name = 'Real States', type = 'scatter', mode = 'lines+markers')
 \#add_lines(p, x = c(1:T), y = y,
             name = 'Observed States', type = 'scatter', mode = 'lines+markers')
 # Run the particle filter
 cat("Running particle filter ")
 param <- list(f = stateTransFunc, g = transferFunc, Q = Q, R = R)</pre>
 res = particleFilter(param = param, y = y, x0 = 0, N = 100)
 \#p < -plot_ly(x = c(1:T), y = x,
               name = 'Real States', type = 'scatter', mode = 'lines+markers')
 #J <- which(runif(1) < cumsum(res$w[,T]))[1]</pre>
 \#add\_lines(p, x = c(1:T), y = res*particles[J,],
```

6 PGAS

```
# name = 'Filtered States', type = 'scatter', mode = 'lines+markers')
```

PGAS

An Implementation of Particle Gibbs with ancestor sampling

Description

An Implementation of Particle Gibbs with ancestor sampling using inverse gamma priors on noise variables.

Usage

```
PGAS(param, y, x0, prior, M = 1000, N = 100, resamplingMethod = "multi")
```

Arguments

param	state parameters
у	measurements
x0	initial state

prior hyperparameters for the inverse gamma priors (uninformative)

M number of MCMC runs
N number of particles

resamplingMethod

resampling methods: 'multi' multinomial and 'systematic' systematic resampling methods are currently supported.

Value

q sample path of the process noise Q
r sample path of the measurement noise R
x sample path of the states

Author(s)

Niharika Gauraha

References

[1] Lindsten, Fredrik, Michael I. Jordan, and Thomas B. Schön. "Particle Gibbs with ancestor sampling." The Journal of Machine Learning Research 15.1 (2014): 2145-2184.

See Also

```
PMMH, particleFilter, conditionalParticleFilter
```

PGAS 7

```
generateData <- function(param, x0, T)</pre>
 #Initialize the state parameters
 f <- param$f # state transition function</pre>
 g <- param$g # tranfer function</pre>
 Q <- param$Q # process noise variance
 R <- param$R # measurement noise variance
 x = rep(0, T)
 y = rep(0, T)
 x[1] = x0 # Initial state
 for(t in 1:T)
 {
   if(t < T)
      x[t+1] = stateTransFunc(x[t],t) + sqrt(Q)*rnorm(1)
   y[t] = transferFunc(x[t]) + sqrt(R)*rnorm(1)
 return(list(x = x, y = y))
}
 stateTransFunc = function(xt, t) 0.5*xt + 25*xt/(1+xt^2) + 8*cos(1.2*t)
 transferFunc = function(x) x^2/20
 # Set up some parameters
 N1 = 5
                         # Number of particles used in PGAS
 N2 = 500
                         # Number of particles used in PMMH
 T = 100
                         # Length of data record
                        # Number of iterations in the MCMC samplers
 numMCMC = 3000
                         # Number of interations to burn
 burnin = 300
 # Generate data
 Q = 0.1 # True process noise variance
 R = 1 # True measurement noise variance
 param <- list(f = stateTransFunc, g = transferFunc, Q = Q, R = R)
 res = generateData(param = param, x0 = 0, T = T)
 x <- res$x
 y <- res$y
 # Hyperparameters for the inverse gamma priors (uninformative)
 prior = c(0.01, 0.01)
 cat("First plot true states and observed states ")
 \#p \leftarrow plot_ly(x = c(1:T), y = x,
              name = 'Real States', type = 'scatter', mode = 'lines+markers')
 \#add_lines(p, x = c(1:T), y = y,
             name = 'Observed States', type = 'scatter', mode = 'lines+markers')
 cat("Running PGAS : ")
```

8 PMMH

PMMH

An Implementation of the Particle Marginal Metropolis-Hastings algorithm.

Description

An Implementation of the Particle Marginal Metropolis-Hastings algorithm using inverse gamma priors on noise variables, and Gaussian random walk proposals.

Usage

```
PMMH(param, y, x0, prior, prop, M = 1000, N = 100, resamplingMethod = "multi")
```

Arguments

param	state parameters
у	measurements
x0	initial state

prior hyperparameters for the inverse gamma priors (uninformative)

prop proposal for PMMH (Gaussian random walk)

M number of MCMC runs
N number of particles

resamplingMethod

resampling methods: 'multi' multinomial and 'systematic' systematic resampling methods are currently supported.

Value

q	sample path of the process noise Q
r	sample path of the measurement noise R

x sample path of the states

PMMH 9

Author(s)

Niharika Gauraha

References

[1] C. Andrieu, A. Doucet and R. Holenstein, "Particle Markov chain Monte Carlo methods" Journal of the Royal Statistical Society: Series B, 2010, 72, 269-342.

See Also

PGAS, particleFilter, conditionalParticleFilter

```
generateData <- function(param, x0, T)</pre>
{
 #Initialize the state parameters
 f <- param$f # state transition function</pre>
 g <- param$g # tranfer function</pre>
 Q <- param$Q # process noise variance
 R <- param$R # measurement noise variance
 x = rep(0, T)
 y = rep(0, T)
 x[1] = x0 # Initial state
 for(t in 1:T)
 {
   if(t < T)
   {
     x[t+1] = stateTransFunc(x[t],t) + sqrt(Q)*rnorm(1)
   y[t] = transferFunc(x[t]) + sqrt(R)*rnorm(1)
 return(list(x = x, y = y))
stateTransFunc = function(xt, t) 0.5*xt + 25*xt/(1+xt^2) + 8*cos(1.2*t)
transferFunc = function(x) x^2/20
 # Set up some parameters
                        # Number of particles used in PGAS
 N1 = 5
 N2 = 500
                       # Number of particles used in PMMH
 T = 100
                       # Length of data record
                       # Number of iterations in the MCMC samplers
 numMCMC = 3000
                         # Number of interations to burn
 burnin = 300
 # Generate data
 Q = 0.1 # True process noise variance
 R = 1 # True measurement noise variance
 param <- list(f = stateTransFunc, g = transferFunc, Q = Q, R = R)</pre>
 res = generateData(param = param, x0 = 0, T = T)
```

10 PMMH

```
x <- res$x
y <- res$y
# Hyperparameters for the inverse gamma priors (uninformative)
prior = c(0.01, 0.01)
cat("First plot true states and observed states ")
\#p \leftarrow plot_ly(x = c(1:T), y = x,
            name = 'Real States', type = 'scatter', mode = 'lines+markers')
\#add_lines(p, x = c(1:T), y = y,
           name = 'Observed States', type = 'scatter', mode = 'lines+markers')
cat("Running PMMH : ")
# Proposal for PMMH (Gaussian random walk)
prop = c(.1, .1)
param <- list(f = stateTransFunc, g = transferFunc, Q = .1, R = 1)</pre>
res = PMMH(param, y, x0 = 0, prior, prop, N = N2, M = numMCMC)
\# p <-plot_ly(x = c(1:T), y = x,
            name = 'Real States', type = 'scatter', mode = 'lines +markers')
# add_lines(p, x = c(1:T), y = res$x[N2,],
           name = 'PMMH States', type = 'scatter', mode = 'lines+markers')
#plot histrograms of the process noise variance and the measurement variance
#hist(res$q[burnin:numMCMC], main = "Distribution of the process noise variance",
#freq = FALSE)
#hist(res$r[burnin:numMCMC], main = "Distribution of the measurement noise variance",
#freq = FALSE)
```

Index

```
conditionalParticleFilter, 2, 4, 6, 9 particleFilter, 3, 4, 4, 6, 9 PGAS, 3, 4, 6, 9 PGAS-package, 1 PMMH, 3, 6, 8
```