

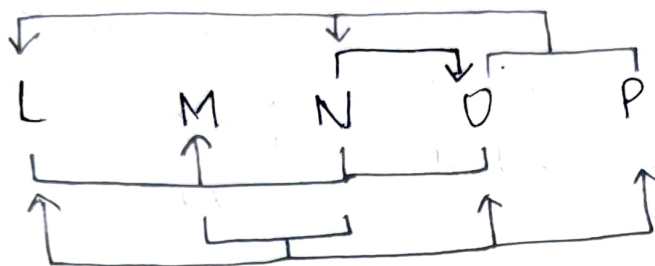
A1:-

HOMEWORK - 7

①

You have a relation $R(L, M, N, O, P, Q)$ and a set of functional dependencies $F = \{LNO \rightarrow M, MN \rightarrow LOP, N \rightarrow O, OP \rightarrow LN\}$.

Edge Diagram:-



②

a) Can we infer $NP \rightarrow LM$ from F ?

$\Rightarrow \left. \begin{matrix} N \rightarrow O \\ OP \rightarrow L \end{matrix} \right\} NP \rightarrow L$

Therefore $NP \rightarrow L$ is true.

\Rightarrow Now let's check $NP \rightarrow M$.

$NP \rightarrow L$

$NP \rightarrow N$

$NP \rightarrow P$

$NP \rightarrow O$

Therefore $NP \rightarrow NLO$

$NLO \rightarrow M$

$NP \rightarrow M$ is True

Yes, because $NP \rightarrow NPOLM$, so $NP \rightarrow LM$ is True.

b) Can we infer $NQ \rightarrow LO$ from F ?

\Rightarrow Check if $NQ \rightarrow L$

where $N \rightarrow O$

$PO \rightarrow L$

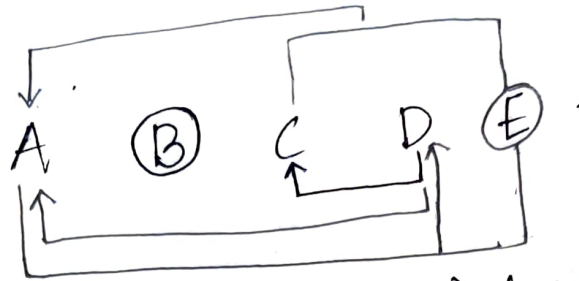
L can be derived $\left. \begin{matrix} NM \rightarrow L \\ PO \rightarrow L \end{matrix} \right\}$ But L cannot be derived using NQ

$\therefore NQ \rightarrow LO$ is not true to LO .

therefore it is not possible.

i] Find all the Candidate keys of the Relation $R(A B C D E)$ with FD's: $D \rightarrow C$, $CE \rightarrow A$, $D \rightarrow A$ and $AE \rightarrow D$. (2)

Edge Diagram:



→ The Entire relation $R(A B C D E)$ has 2 keys B and E which appear on the right hand side of functional dependencies, which should always be included on all the candidate keys.

$$\{D\}^+ \rightarrow \{D C A\}.$$

$$\{CE\}^+ \rightarrow \{C E A D\}.$$

$$\{AE\}^+ \rightarrow \{A E D C\}.$$

⇒ Let us check the right hand side of the fn dependencies.

$$\{BDE\}^+ = \{B D E C A\}$$

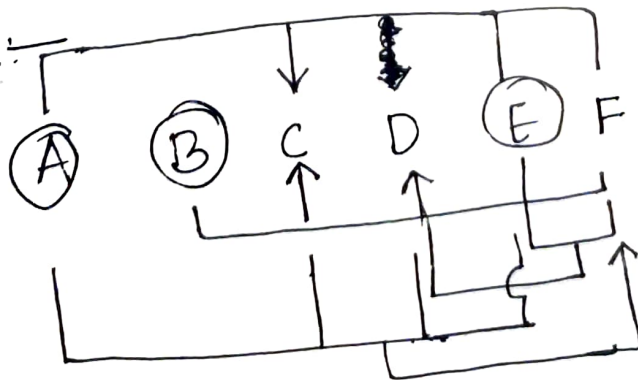
$$\{BCE\}^+ = \{B C E A D\}.$$

$$\{ABE\}^+ = \{A B E C D\}.$$

⇒ The set of attributes $\{BDE\}$, $\{BCE\}$ and $\{ABE\}$ which gives the set of all attributes of the relation R.

ii] Determine all the candidate and superkeys of the relation. $R(A B C D E F)$ with FD's: $AEF \rightarrow C$, $BF \rightarrow C$, $EF \rightarrow D$ and $ACDE \rightarrow F$.

Edge Diagram:



⇒ Let's find the closure of functional dependencies.

(3)

$$\{AEF\}^+ \rightarrow \{AEFCD\}.$$

$$\{BF\}^+ \rightarrow \{BFC\}.$$

$$\{EF\}^+ \rightarrow \{EFD\}.$$

$$\{ACDE\}^+ \rightarrow \{ACDEF\}.$$

No closure determines all the attributes of R.

⇒ Let's check the right hand side of the functional dependencies which are to be present as the part of Candidate Key A, B, E.

B to closure of $\{ABEF\}$, then $\{ABEF\}^+ \rightarrow \{ABEFC\}$.

B to closure of $\{ABCDE\}$ then $\{ABCDE\}^+ \rightarrow \{ABCDEF\}$.

for FDs $BF \rightarrow C$ and $EF \rightarrow D$, $\{BF\}^+ \rightarrow \{BFC\}$.

Add A so $\{ABDF\}^+ \rightarrow \{ABDFC\}$.

Add E so to the closure of $\{BFAD\}$ then

$$\{ABDEF\}^+ \rightarrow \{ABCDEF\}.$$

⇒ The set of attributes $\{ABEF\}$ and $\{ABCDE\}$ gives the set of all attributes of relation R.

⇒ Hence, the Candidate keys of the relation $R(ABCDEF)$ are $\{ABEF\}$ and $\{ABCDE\}$.

⇒ The Super keys of the relation $R(ABCDEF)$ are $\{ABDEF\}$, $\{ABCEF\}$ and $\{ABCDEF\}$.

(4)

Q3:- Minimal Cover:-

Find all minimum covers for the following set F of functional dependencies $X \rightarrow Z, XY \rightarrow Z, Z \rightarrow UT, ZU \rightarrow T, ZW \rightarrow XY, WT \rightarrow Z$.

Given set Functional dependencies.

$X \rightarrow Z, XY \rightarrow Z, Z \rightarrow UT, ZU \rightarrow T, ZW \rightarrow XY, WT \rightarrow Z$

⇒ The minimal cover of F functional dependencies

→ Every single Attribute on the Right hand Side must have a dependency in F .

⇒ $Z \rightarrow UT$

⇒ $[Z \rightarrow U, Z \rightarrow T]$

→ Removing all extraneous attributes such as $\alpha \rightarrow \beta$ and $\alpha\gamma \rightarrow \beta$ then γ is an extraneous attributes.

→ $X \rightarrow Z$ and $XY \rightarrow Z$ then Y is extraneous so removing it becomes $[X \rightarrow Z]$.

→ Removing redundant functional dependencies of F . such as $\alpha \rightarrow \beta, \alpha \rightarrow \beta$ (removing one of similar one. $\alpha \rightarrow \beta$)

In the above given F functional dependencies.

a) Convert Right Hand Side Attribute into single.

→ $Z \rightarrow U$

$Z \rightarrow T$

$ZW \rightarrow X$

$ZW \rightarrow Y$

b) Remove extraneous attribute dependencies.

→ $X \rightarrow Z$

$XY \rightarrow Z$

$X \rightarrow Z$

→ $Z \rightarrow T$

$ZU \rightarrow T$

$Z \rightarrow T$

c) Removing all the redundant functional dependencies of F. (5)

$$\rightarrow X \rightarrow Z$$

$$X \rightarrow Z$$

$$Z \rightarrow U$$

$$Z \rightarrow T$$

$$Z \rightarrow T$$

$$ZW \rightarrow X$$

$$ZW \rightarrow Y$$

$$WT \rightarrow Z$$

The Minimal Cover of the given F of functional dependencies are
 $\Rightarrow X \rightarrow Z, Z \rightarrow U, Z \rightarrow T, ZW \rightarrow X, ZW \rightarrow Y, WT \rightarrow Z$.

A4

Consider the following set of F.D.s. Determine if FD1 is equivalent to FD2 or to FD3. (6)

FD1:
 $\{BC \rightarrow D, ACD \rightarrow B, CG \rightarrow B, CG \rightarrow D, AB \rightarrow C, C \rightarrow AD \rightarrow E, BE \rightarrow C, D \rightarrow G, CE \rightarrow A, CE \rightarrow G\}$

FD2:
 $\{AB \rightarrow C, C \rightarrow A, BC \rightarrow D, CD \rightarrow B, D \rightarrow E, D \rightarrow G, BE \rightarrow C, CG \rightarrow D\}$

FD3:
 $\{AB \rightarrow C, C \rightarrow A, D \rightarrow G, BE \rightarrow C, CG \rightarrow D, CE \rightarrow G, BC \rightarrow D, CD \rightarrow B, D \rightarrow E\}$

You must show closure of each LHS attributes on the left hand side of each FD- i where $i = \{1, 2, 3\}$ via going through the other FD set.

\Rightarrow If all the Equivalent Conditions are FD1 covers FD2 and FD2 covers FD1.

The equivalent with FD2 :-
 lets check if FD2 covers FD1:

FD1: $BC \rightarrow D$

$AB \rightarrow C$

$C \rightarrow A$

$D \rightarrow E$

$BE \rightarrow C$

$D \rightarrow G$

$ACD \rightarrow B$

$CG \rightarrow B$

$CG \rightarrow D$

\Rightarrow The rest of the relations in FD1:

$ACD \rightarrow ACDEG$ so, $ACD \rightarrow B$

$CG \rightarrow CGABEG$ so $CG \rightarrow B, CG \rightarrow D$

$CE \rightarrow CEA$, so $CE \rightarrow A$ but $CE \rightarrow G$ in FD1 is not covered by FD2.

Finally FD1 & FD2 are similar and are not equivalent

⇒ Equivalent Conditions of FD1 covers FD3 and FD3 covers FD1.
equivalent with FD3: \textcircled{f}

The relations of FD1:

$BC \rightarrow D$

$CG \rightarrow D$

$AB \rightarrow C$

$C \rightarrow A$

$D \rightarrow E$

$BE \rightarrow C$

$D \rightarrow G$.

$CE \rightarrow G$ are already in FD3.

⇒ The rest of the relations in FD1:

$ACD \rightarrow ACDGEB$ so $ACD \rightarrow B$

$CG \rightarrow CGDEAB$ so, $CG \rightarrow B$.

$CE \rightarrow CEGADB$ so $CE \rightarrow A$.

As a result FD3 covers FD1.

Similarly let's check if FD1 covers FD3:

$AB \rightarrow C$.

$C \rightarrow A$

$D \rightarrow G$

$BE \rightarrow C$

$CG \rightarrow D$

$CE \rightarrow G$

$BC \rightarrow D$

$D \rightarrow E$ are not in FD1.

$CD \rightarrow CDAEGB$ so $CD \rightarrow B$.

As a result FD1 covers FD3, therefore they are equivalent.