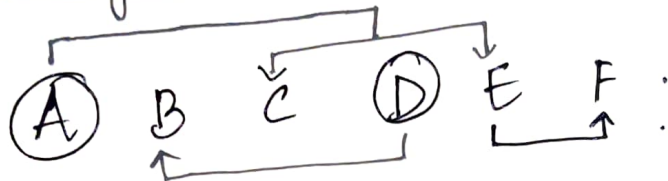


i) Given a relation $R(A, B, C, D, E, F)$ in 1NF and its functional dependency set $F = \{A \rightarrow CE, E \rightarrow F, D \rightarrow B\}$. (1)

ii) Find Candidate key of R.

iii) Decompose R into 3NF.

Sol'n Edge Diagram:-



i) Find the Candidate key of R.

$A \rightarrow CE$

$E \rightarrow F$

$D \rightarrow B$

\Rightarrow AD is the Candidate Key for R because $A \rightarrow CE$ & $D \rightarrow B$ and rest of other attributes which are not to be present on the righthand side on the Candidate key. The attributes that are functionally dependent on all other attributes to meet this criteria.

Functional Dependency & its function dependencies

ii) Decompose R into 3NF.

⇒ The transitive dependency is $A \rightarrow CE$, Thus we need to (2)
decompose R into two relations $R_1(A, B, C, D)$ & $R_2(A, E, F)$.

⇒ we can check R_1 & R_2 are in 3NF. we can see that
 $R_1(A, B, C, D)$ is in 3NF since there are no transitive dependencies.

For R_2 we can see that the only transitive dependency $A \rightarrow E$.
Thus, we decompose R_2 into two relations $R_3(A, E)$ and $R_4(A, F)$.

⇒ we can see that R_3 & R_4 are in 3NF, R_3 is in 3NF as there are
no transitive dependencies. For $R_4(A, F)$ we can see that the
only transitive dependency $A \rightarrow F$, thus we decompose $R_5(A, F)$ & $R_6(A)$.

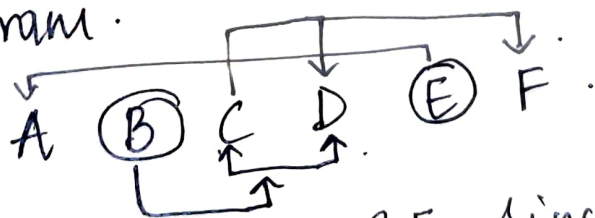
⇒ We can see both $R_5(A, F)$ & $R_6(A)$ both are having no
transitive dependencies so they are 3NF.

Thus the decomposition 3NF is $R_1(A, B, C, D)$, $R_3(A, E)$, $R_5(A, F)$ & $R_6(A)$.

Q2
Give a relation $R(A, B, C, D, E, F)$ in 1NF and its functional
dependency set $F = \{B \rightarrow CD, E \rightarrow A, C \rightarrow DF\}$.

i) Find Candidate key of R.

Edge Diagram.



$B \rightarrow CD$
 $E \rightarrow A$
 $C \rightarrow DF$

The Candidate key are B & E since the rest of the
other attributes which are not to be present are on the
right hand side. The attributes BE are ^{not} functionally dependent
on any of the other attributes to meet this criteria.

ii) The decomposition of R into BCNF is .

(3)

$R_1(B, C, D, F)$.

$R_2(E, A)$

$R_3(C, D, F)$.

The functional dependencies in each decomposed relation

$R_1: B \rightarrow CD, C \rightarrow DF$.

$R_2: E \rightarrow A$.

$R_3: C \rightarrow DF$.

\Rightarrow R where to decompose we to find the subset of attributes that contains a candidate key and all the dependent functional

\Rightarrow Since B, C, D and F are subset, which contains key B , this gives us first decomposed relation $R_1 [B \rightarrow CD, C \rightarrow DF]$.

\Rightarrow we can take attributes E & A which are in form that contains the Candidate key of all functional dependencies ($E \rightarrow A$) gives the second decomposed relation R_2 .

\Rightarrow Finally taking attribute C and its functional dependency $C \rightarrow DF$, which gives us the third decomposed relation R_3 .
The decomposed R into BCNF is .

$R_1(B, C, D, F)$

$R_2(E, A)$

$R_3(C, D, F)$.

3) Given a relational R with a function dependency $F = X \rightarrow Y$. (4)

① If X is nonprime attribute and Y is prime attribute, select the right answer.

- a. R is not in 2NF.
- b. R is in 2NF, but not 3NF
- c. R is in 3NF, but not BCNF
- d. R is in BCNF

Soln a) R is not in 2NF.

⇒ From the given functional dependency of R does not satisfy the conditions for the inclusion in 3NF and in 2NF since the given dependency $X \rightarrow Y$ do not comply with the requirement that all non-prime attributes be functionally determined by the Candidate key. The functional dependency b/w the attributes which are not tend to be prime attribute (x) and the prime attribute (y), which leads to the violation of the second normalization form, hence R is not in 2NF.

② If X is a subset of Candidate key and Y is non-prime attribute, select the right answer.

- a. R is not in 2NF
- b. R is in 2NF, but not in 3NF
- c. R is in 3NF, but not in BCNF.
- d. R is in BCNF

Soln b) R is in 2NF, but not in 3NF.

⇒ The Dependency $X \rightarrow Y$ which violates the constraint that all non-prime attributes must be functionally determined by the Candidate key. The functional dependency between the attributes that are not prime attributes violates the third normalization form.

- the right answer.
- a. R is not in 2NF
b. R is in 2NF, but not in 3NF.
c. R is in 3NF, but not BCNF.
d. R is in BCNF.

(5)

Soln (a) R is not in 2NF

⇒ The Functional dependency $F = X \rightarrow Y$ fails to meet the requirement of every non prime attribute must be functionally determined by the entire Candidate key, which indicates it does not implement factors relating to the third normalization factor either on the attributes. So the dependency which is contrary to the second normalization form of the given attribute set.

4) If X is Candidate key attribute and Y is prime attribute, select the right answer.

- a. R is not in 2NF.
b. R is in 2NF, but not in 3NF.
c. R is in 3NF, but not BCNF.
d. R is in BCNF.

Soln (b) R is in 2NF, but not in 3NF

⇒ The functional attributes of a Candidate key and the prime attributes have a reliant on the primary key of the relation is entirely functionally on the primary key which qualifies a relation to be 2NF. The relation in a way is non transitive for 3NF. where $X \rightarrow Y$ breaks the constraint that all non-prime attributes must be functionally dependent on the Candidate Key