

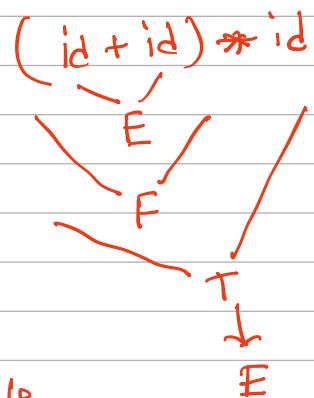
Lecture 4

9-11-2024

* For the same string, if there is different syntax tree then the grammar is ambiguous.

$$\begin{array}{l} E \rightarrow E + T \mid E - T \mid T \\ T \rightarrow T * F \mid T / F \mid F \\ F \rightarrow id \mid \text{number} \mid (E) \end{array} \quad \left. \begin{array}{l} \text{Thus it removes the ambiguity} \\ \text{of order of operations.} \\ \text{mul must be done before} \\ \text{addition} \end{array} \right\}$$

(ensuring addition before multiplication)



* we need PDA to verify whether a string belongs to CFG.

* $E \rightarrow E + T \mid T$
 $T \rightarrow T * F \mid F$
 $F \rightarrow id \mid (E)$

input string : id + id * id \$

① + id * id \$

② + id * id \$

③ + id * id \$

④ + id * id \$

⑤ id * id \$

⑥ id \$

⑦ " , ⑧ "

⑨ id \$

⑩ \$

⑪ \$ ⑫ \$ ⑬ \$

stack
\$ ← nothing in the stack

① # id > reverse order derivation
② \$ F ↑ > reverse order derivation

③ \$ T we are not pushing + sign since according to grammar we can only use + sign in E.

④ \$ E

⑤ \$ E +

⑥ \$ E + id

⑦ \$ E + F

⑧ \$ E + T → we can convert it to E but we will not since * will not work then.

⑨ \$ E + T *

⑩ \$ E + T * id

⑪ \$ E + T * F

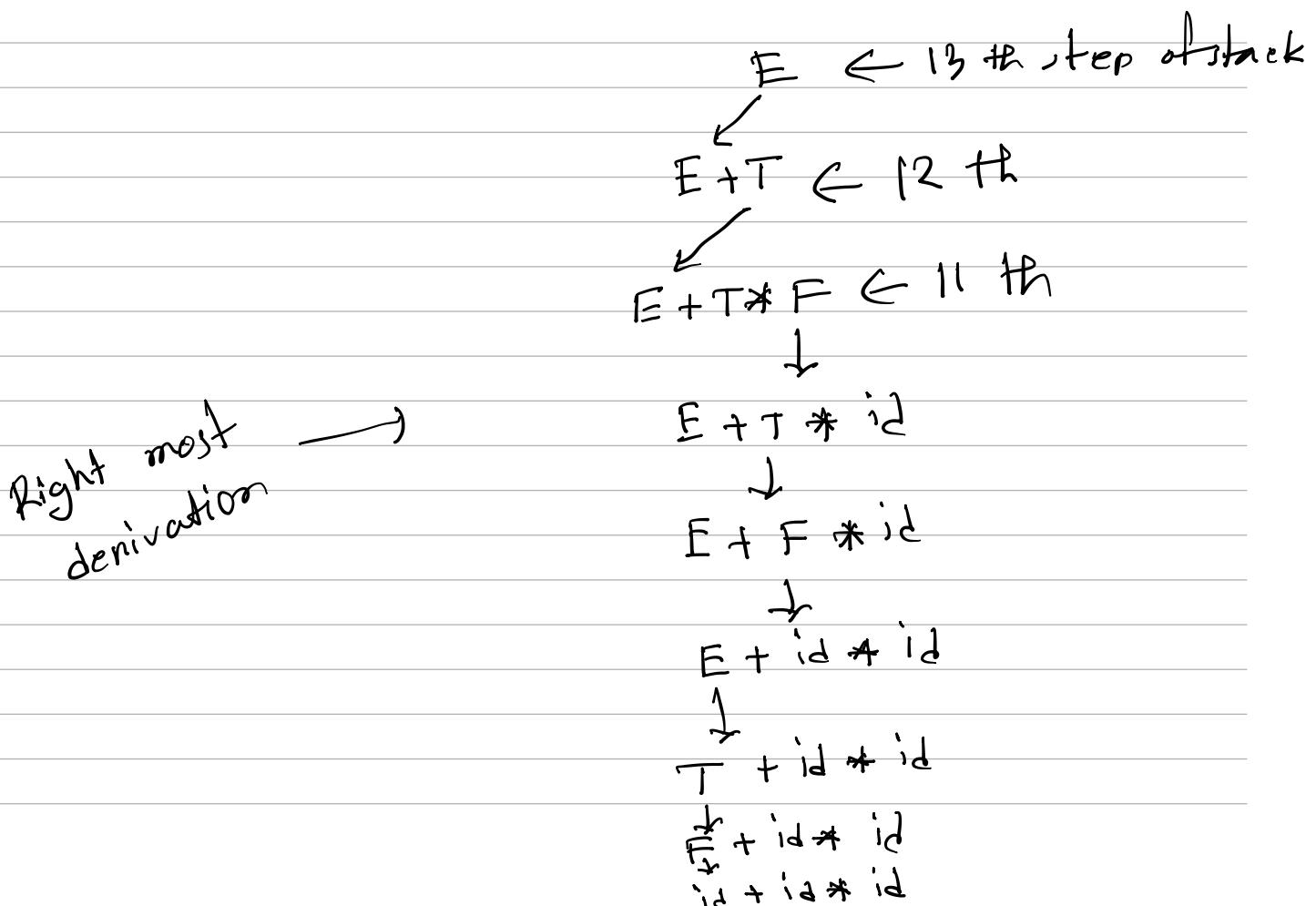
⑫ \$ E + T

⑬ \$ E

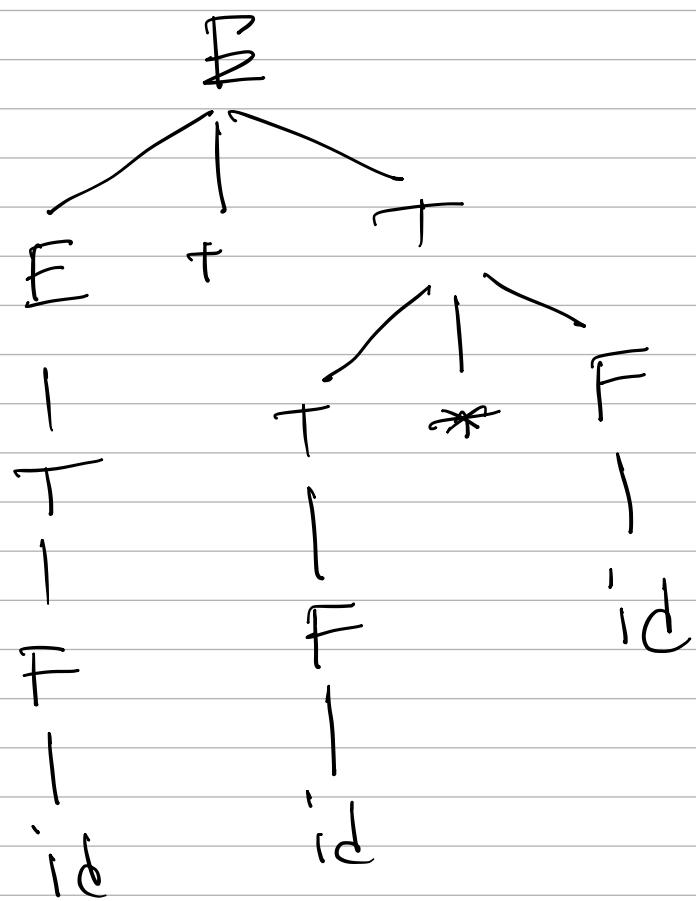
~ indicating the End

← Bottom-up approach

we ended up with empty input string & stack has only the start symbol of the grammar.



Syntax tree



* Syntax analyzzen we create

are called Bottom-up parsing)

Syntax analyzzen,

* the input is readen from leftmost
and the derivation is done from
right most,

∴ LR parser.

left-right
scanning

right most
derivation

→ it generates the rightmost
derivation in reverse orden.

* Bottom-up parsers are also called LR parser.

* Top down is a small subset of Bottom up. That's why we use Bottom up.

* In the stack we either:

① push some token inside \leftarrow Shift operation

② Converted a production body into the head of the production. \leftarrow Reduce

$$E \xrightarrow{\text{Head}} E + T \xrightarrow{\text{Body}}$$

Head to Body \rightarrow derivation/expansion

Body to Head \rightarrow reverse derivation/reduce

* Bottom-up parser is also called Shift-reduce parser.

* making the right choice between shift & reduce is a critical decision. We need an algorithm to do the task. At 8th step we shifted rather than reducing. To take the decision we looked into the remaining input string. We restrict the numbers of " " " " to investigate since otherwise it will take too much time. So in the LR parser we give the number of future tokens the syntax analyzer checks to make its decision, inside a parenthesis.

LR(1) parser

4 checks 1 future token

LR(2) parser

↳ checks 2

The complexity increases exponentially.

* we will learn simple LR(1) parser



Simple LR parser



LL parser

* In lab we will use LALR parser,



look ahead LR parser.

Steps to construct LR syntax analyzer:

- ① You augment the grammar with a new start symbol.
- ② You create an LR(0) automaton diagram from the augmented grammar.
- ③ Compute two functions First and Follows of non terminals.
- ④ Construct a two parts parsing table from information from step ② & ③.