

$$E \rightarrow E + T$$

for the given grammar  
↓

$$\Sigma = \{id, +, *, (, )\}$$

$$E \rightarrow T$$

$$T \rightarrow T * F$$

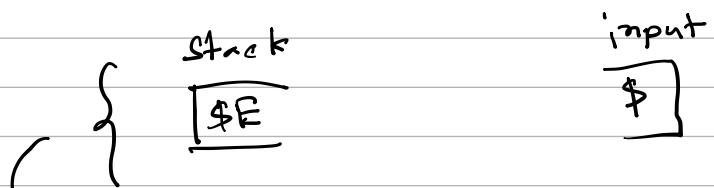
$$T \rightarrow F$$

$$F \rightarrow id$$

$$F \rightarrow (E)$$

we say a LR parser accepts a program when the stack has

the starting starting symbol and remaining input is empty.



Step 1

this configuration says that the program is accepted grammatically accurate.

But what if:



since we can only see the topmost element of stack

To avoid the scenario we add a new non-terminal and appoint it as the new start symbol. If  $E'$  will not be in <sup>any</sup> other production rule.

$$E' \rightarrow E \rightarrow E + T \rightarrow \text{augmentation of}$$

$$E \rightarrow T$$

$$T \rightarrow T * F$$

$$T \rightarrow F$$

$$F \rightarrow id$$

$$F \rightarrow (E)$$

the grammar

## Step 2: Constructing automaton $\rightarrow$ LR(0)

↳ automata is plural  
of automaton

what is a state in the automaton?

→ In DFA state means how much string we have consumed.  
since DFA is deterministic

But for CFG:

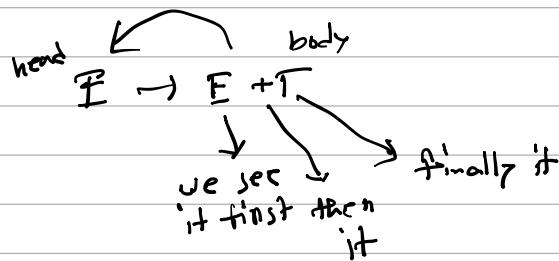
we have many options through the grammar.

(what we have seen so far) + (what we expect to see next  
or in the future (not only the immediate next))

came  $\downarrow$   
on DFA

$\downarrow$   
meaning of state  
in automaton

\* hence the bottom up approach, we see the body then  
transition to head.



we can also write in this manner:

$E \rightarrow \bullet E + T$

we can only shift  $\leftarrow$   
it works like a cursor. } this at first means  
How much of th's production } we havent seen  
we have seen so far. } anything so far.

⇒ these are called LR(0) items.

*only shift*     $\Leftarrow E \rightarrow E_0 + T$

↓

I have seen  $E$  in the body and hoping  
to see ' $+$ ' in future.

*we are ready to reduce to reduce*     $\Leftarrow E \rightarrow E + T_0$

↓

I have seen the whole of a body and  
now I expect to reduce the body into  
the head.

∴ A state of the automaton is the set of production  
parts we think we have seen partially or whole.

\* strings are consist of terminals (tokens).

$(id + id) * id$

where is  $E$  here?

$E \rightarrow E_0 + T$

↳ I have seen part of the input  
that I reduced to  $E$  condition.

to ensure end we also include the  $\$$  in the sigma.

$$\Sigma = \{id, +, *, (,), \$\}$$

if we have

$A \rightarrow \alpha \cdot B \beta$  in a state

and  $B \rightarrow \gamma_1$

$B \rightarrow \gamma_2$

⋮

$B \rightarrow \gamma_m$

are  $B$ 's productions

we have to add all  
items:  $B \rightarrow \gamma_1$ ,  
 $B \rightarrow \gamma_2$ ,  
 $B \rightarrow \gamma_m$   
in the state.

↓  
now F can be reduced to E

same for T

that's why we add all possible  
rules of E.

first state

$$E' \rightarrow \cdot E$$

↳ E has 2 more production rules  
we have to add them as well

$E \xrightarrow{\cdot} E + T$  we have already considered E & set doesn't  
contain duplicate

$E \rightarrow \cdot T$  ↳ T has 2 more ∴ add

$T \rightarrow \cdot T * F$

$T \rightarrow \cdot F$  ↳ same for F

$F \rightarrow \cdot id$

$F \rightarrow \cdot (E)$

I<sub>0</sub>

$$E' \rightarrow \cdot E$$

$$E \xrightarrow{\cdot} E + T$$

$$E \rightarrow \cdot T$$

$$T \rightarrow \cdot T * F$$

$$T \rightarrow \cdot F$$

$$F \rightarrow \cdot id$$

$$F \rightarrow \cdot (E)$$

→ we don't know which E? so we have to increment both

E E?

$$\boxed{E' \rightarrow E \cdot}$$

$$E \rightarrow E \cdot + T$$

↓  
accept

I<sub>1</sub>

$$E \rightarrow E + \cdot T$$

$$T \rightarrow \cdot T * F$$

$$T \rightarrow \cdot F$$

$$F \rightarrow \cdot id$$

$$F \rightarrow \cdot (E)$$

T

F

I<sub>2</sub>

→ this type of  
state asks  
to expand/shift  
more

will expand  
more

I<sub>3</sub>

$$\boxed{E \rightarrow T \cdot}$$

$$T \rightarrow T \cdot * F$$

$$T \rightarrow T * \cdot F$$

$$F \rightarrow \cdot id$$

$$F \rightarrow \cdot (E)$$

$$T \rightarrow T * \cdot F$$

$$F \rightarrow \cdot id$$

$$F \rightarrow \cdot (E)$$

I<sub>4</sub>

id

I<sub>5</sub>

id

I<sub>6</sub>

id

I<sub>7</sub>

id

I<sub>8</sub>

id

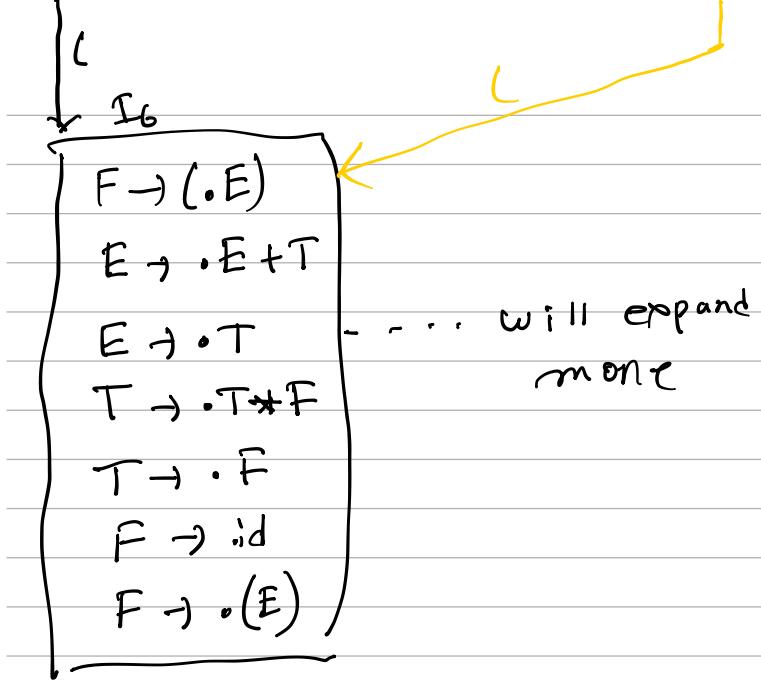
I<sub>8</sub>

T → T \* F.

↳ this type of states

indicates we can

reduce



automaton

CLR can have exponentially more states than SLR for same grammar. LALR concises the numbers of states of CLR.