

Portfolio Management

FN 4329

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American College of Greece

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Contents

- 1 Portfolio Construction
 - Asset Allocation
 - Security Selection
 - Diversification strategy
- 2 Theory
 - Descriptive Statistics
 - Financial Metrics
- 3 Building the Portfolio
 - Naive allocation
 - Portfolio Optimization
 - Optimal Overall Portfolio

Todo

- fix contents (example: Intro, Theory, Results)
- better resolution on images

Questionnaire

1/30/2020

Vanguard - Investor Questionnaire

PERSONAL INVESTORS



Investor questionnaire

1. I plan to begin taking money from my investments in ...

- ☐ 1 year or less
- ☐ 1 - 2 years
- ☐ 3 - 5 years
- ☐ 6 - 10 years
- ☐ 11 - 15 years
- ☒ More than 15 years

2. As I withdraw money from these investments, I plan to spend it over a period of ...

- ☒ 2 years or less
- ☐ 3 - 5 years
- ☐ 6 - 10 years
- ☐ 11 - 15 years
- ☐ More than 15 years

3. When making a long-term investment, I plan to keep the money invested for ...

- ☐ 1 - 2 years
- ☐ 3 - 4 years
- ☐ 5 - 6 years
- ☐ 7 - 8 years
- ☒ More than 8 years

4. From September 2008 through November 2008, stocks lost more than 21%. If I owned a stock investment that lost about 21% in 3 months, I would ... (If you owned stocks or stock funds during this period, select the answer that corresponds to your actual behavior.)

- ☐ Sell all of the remaining investment.
- ☐ Sell a portion of the remaining investment.
- ☒ Hold onto the investment and sell nothing.
- ☐ Buy more of the investment.

5. Generally, I prefer investments with little or no fluctuation in value, and I'm willing to accept the lower return associated with these investments.

- ☐ Strongly disagree
- ☒ Disagree
- ☐ Somewhat agree
- ☐ Agree
- ☐ Strongly agree

6. During market declines, I tend to sell portions of my riskier assets and invest the money in safer assets.

- ☒ Strongly disagree
- ☐ Disagree
- ☐ Somewhat agree
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- ☐ Strongly agree

7. I would invest in a mutual fund or ETF (exchange-traded fund) based solely on a brief conversation with a friend, co-worker, or relative.

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- ☐ Disagree
- ☒ Somewhat agree
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8. From September 2008 through October 2008, bonds lost nearly 4%. If I owned a bond investment that lost almost 4% in 2 months, I would ... (If you owned bonds or bond funds during this period, select the answer that corresponds to your actual behavior.)

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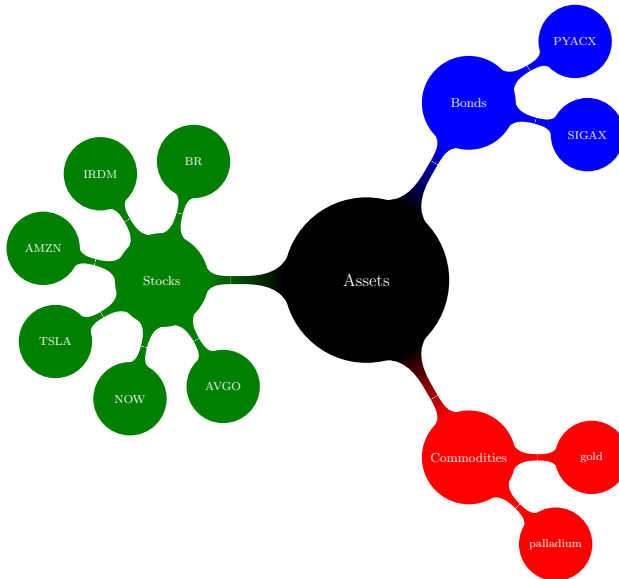
<https://personal.vanguard.com/us/FundInvQuestionnaire>

1/2

Asset Allocation

- 70% Stocks
- 20% Bonds
- 10% Commodities

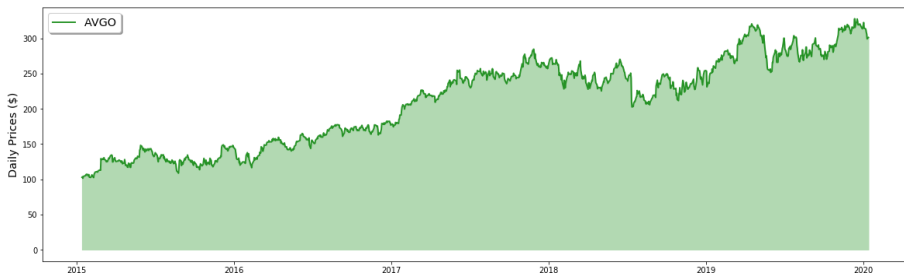
Security Selection



Stocks

AVGO - Broadcom Inc

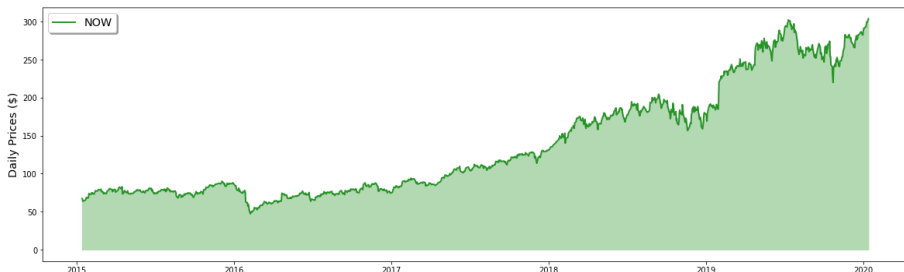
- Large/High-Dividend
- Wireless chips and semiconductor manufacturer
- Announced 15\$ billion deal with Apple Inc. in January 2020
- Potential for gains with 5G deployment



Stocks

NOW - ServiceNow Inc.

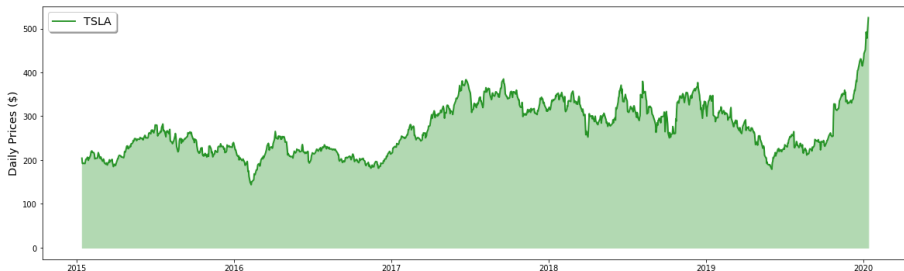
- Large/Growth
- Cloud-based solutions provider to global enterprises
- Software as a Service (SaaS) business model
- IT, Customer Support, HR and Security services



Stocks

TSLA - Tesla Inc.

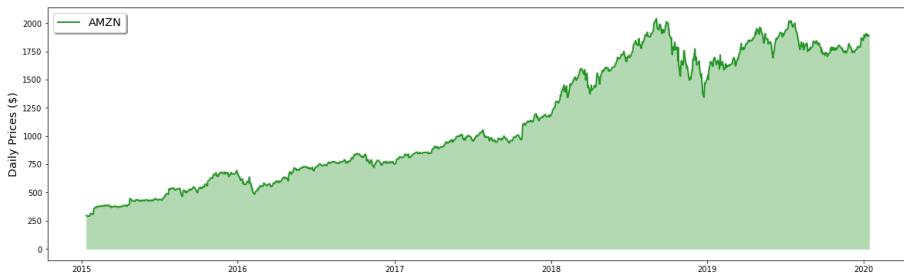
- Large/Growth
- Leader in next-generation electric vehicles
- Advancements in battery technology will allow for increased autonomy
- 4th Gigafactory in Berlin to begin operations by July 2021



Stocks

AMZN - Amazon Inc.

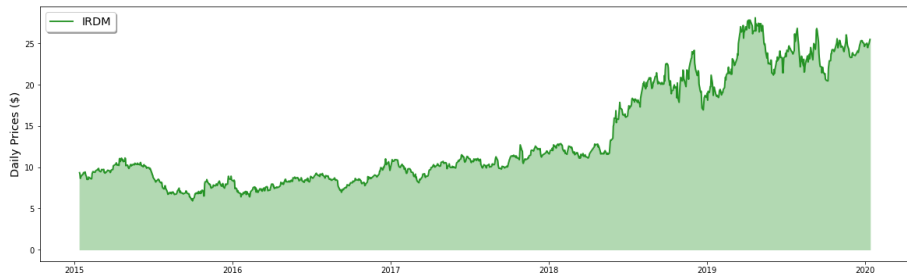
- Large/Growth
- Biggest online retailer
- Online product and digital media sales
- AWS offers solutions for Machine Learning, Big Data, IoT and Cloud-Computing



Stocks

IRDM - Iridium Communications Inc.

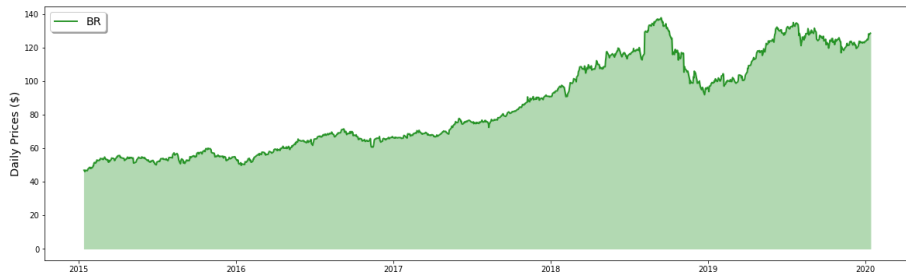
- Small/Growth
- Lead provider of satellite communications, with over 70 satellites in orbit
- Announced partnership with AWS for future applications in 2018
- Wide commercial end base, from maritime and aviation to oil & gas suppliers



Stocks

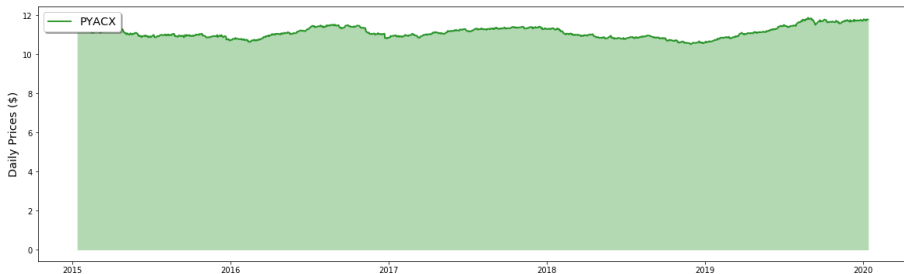
BR - Broadridge Financial Solutions Inc.

- Mid/Aggressive Growth
- Fintech company that provides solutions for investors, banks, brokerage offices and mutual funds
- Products include communication platforms, securities processing and financial data analytics



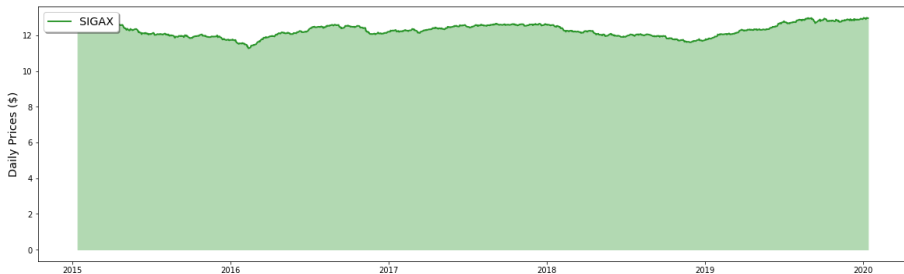
Bonds

PYACX - Payden Corporate Bond Mutual Fund



Bonds

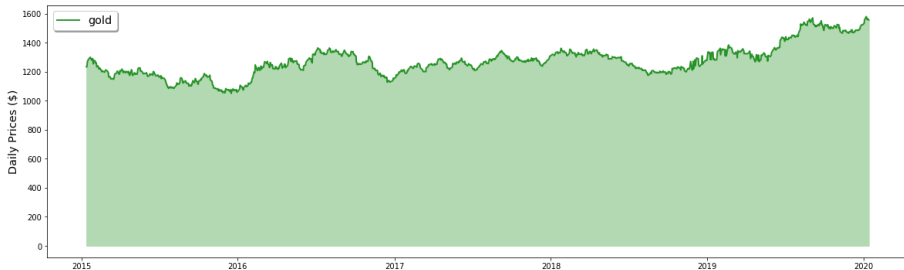
SIGAX - Western Asset Corporate Bond Mutual Fund



Commodities

gold

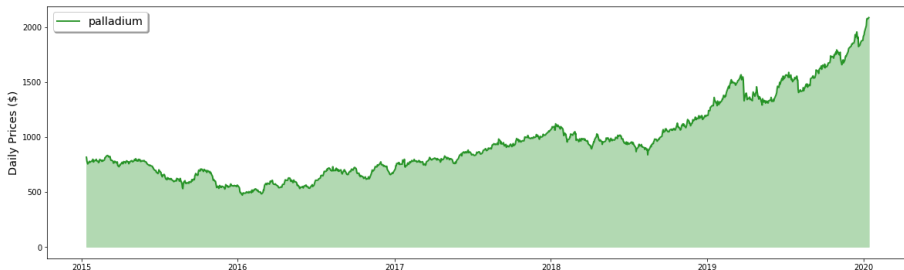
- Traditionally safe investment during rough economic times and hedge against inflation
- Recently preferred over government bonds, as the latter presented negative inflation-adjusted returns in 2019
- Does not generate return and has no holding costs



Commodities

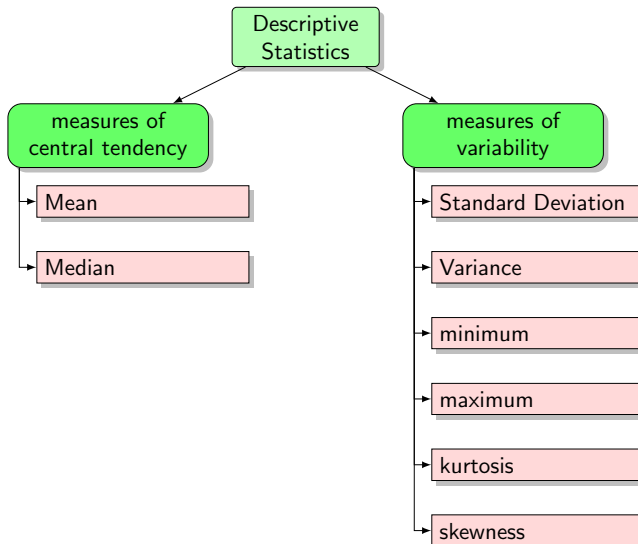
palladium

- Metal that is used in catalytic converters, turning toxic gas emissions into less harmful ones
- Secondary product from mining operations of other metals
- As miners have less control over the extracted quantities, demand outstrips supply
- Price has doubled over the last year



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Descriptive statistics Taxonomy



Measures of central tendency

Mean

Mean

$$\bar{x} = \frac{1}{n} \left(\sum_{i=1}^n x_i \right) = \frac{x_1 + x_2 + \cdots + x_n}{n}$$

Measures of central tendency

Median

- i.e. the middle value

Measures of central tendency

Median

- i.e. the middle value
- Why?

Measures of central tendency

Median

- i.e. the middle value
- Why? robust w.r.t. outliers

Measures of central tendency

Median

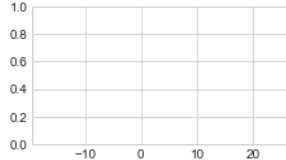
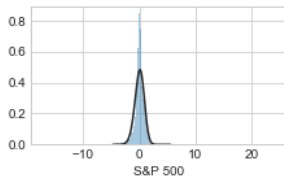
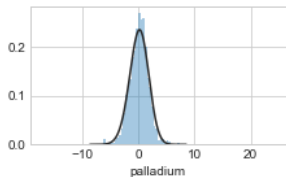
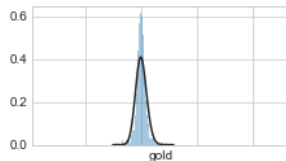
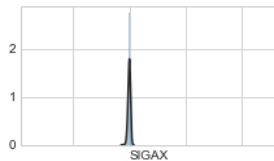
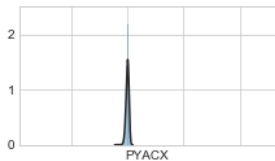
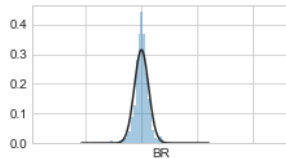
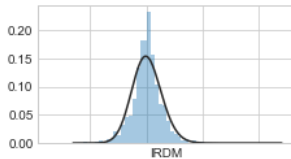
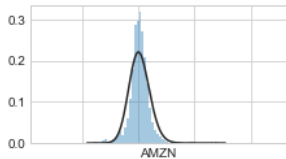
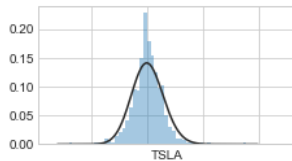
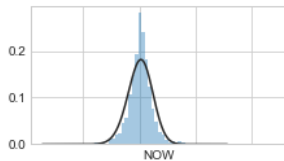
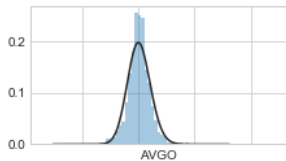
- i.e. the middle value
- Why? robust w.r.t. outliers
- indicates whether returns are positive or negative on most time instances.

Measures of Variability

Standard Deviation

$$\sigma = \sqrt{\frac{1}{N} \sum_{i=1}^N (x_i - \bar{x})^2}$$

- how "spread out" are the data around the mean
- measures confidence in statistics \implies risk in finance



Measures of Variability

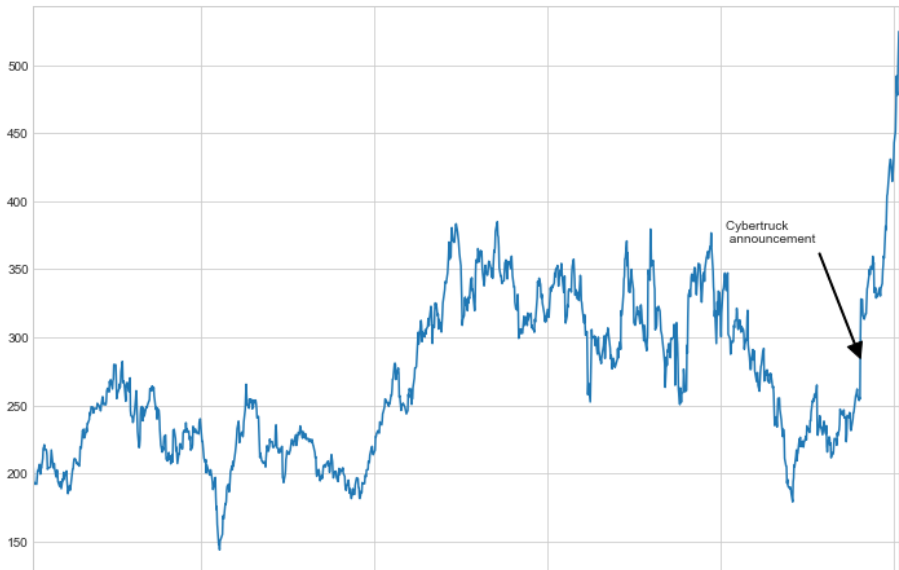
Minimum & Maximum



Figure: The minimum of the S&P500 returns would occur on the day of the economic crisis for this period.

Measures of Variability

Minimum & Maximum



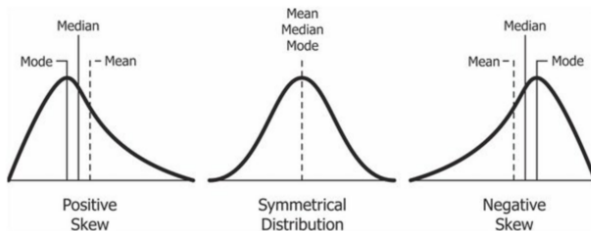
Measures of Variability

Skewness

Definition

$$\tilde{\mu}_3 = \mathbb{E} \left[\left(\frac{X - \bar{x}}{\sigma} \right)^3 \right]$$

Skewness is a measure of asymmetry that indicates if the tail of the distribution is on the left or the right.



Measures of Variability

Kurtosis

Definition

$$\text{Kurt}(X) = \tilde{\mu}_4 = \mathbb{E} \left[\left(\frac{X - \bar{x}}{\sigma} \right)^4 \right]$$

Kurtosis measures whether the distribution is heavy- or light-tailed relative to a normal distribution

- high kurtosis \rightarrow heavy tails (**outliers**)
- low kurtosis \rightarrow no outliers

Measures of Variability

An overview

Moments from an investor's perspective

- $\tilde{\mu}_2$ standard deviation σ
- $\tilde{\mu}_3$ skewness
- $\tilde{\mu}_4$ kurtosis

TODO

add what each moments means to understanding security performance

Descriptive Statistics

For our assets

	mean%	median%	std%	var%	min%	max%	kurtosis	skewness
AVGO	0.11	0.11	2.04	4.17	-13.74	14.71	5.31	0.23
NOW	0.15	0.21	2.23	4.96	-15.66	14.07	6.50	-0.33
TSLA	0.12	0.06	2.85	8.13	-13.90	17.67	5.06	0.30
AMZN	0.17	0.14	1.85	3.42	-7.82	14.13	9.83	1.01
IRDM	0.12	0.12	2.63	6.94	-11.13	22.24	6.47	0.62
BR	0.09	0.09	1.27	1.61	-9.70	11.16	9.29	-0.19
PYACX	0.00	0.00	0.27	0.07	-2.08	0.77	3.40	-0.71
SIGAX	0.00	0.00	0.23	0.05	-1.29	0.67	1.28	-0.43
gold	0.02	0.00	0.99	0.98	-4.32	5.10	4.56	0.33
palladium	0.09	0.15	1.71	2.92	-7.40	7.28	1.49	-0.15
S&P 500	0.04	0.05	0.84	0.71	-4.10	4.96	3.87	-0.47

Covariance Definition

Let X and Y be two random variables. Then the covariance is a measure of the joint variability of these two random variables:

$$\text{cov}(X, Y) = \mathbb{E}[(X - \bar{x})(Y - \bar{y})]$$

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- not so helpful!

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- not so helpful! \rightarrow correlation

Correlation

Definition

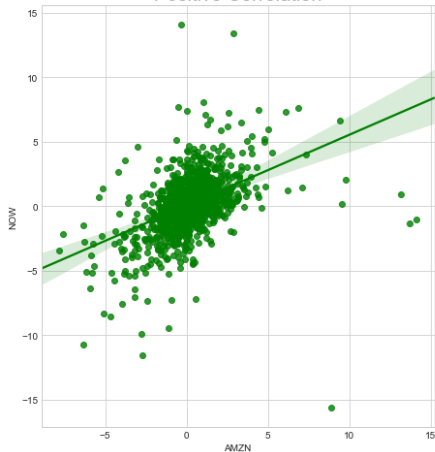
The correlation is the normalization of the covariance.

$$\rho_{X,Y} = \frac{\text{cov}(X,Y)}{\sigma_X \cdot \sigma_Y}$$

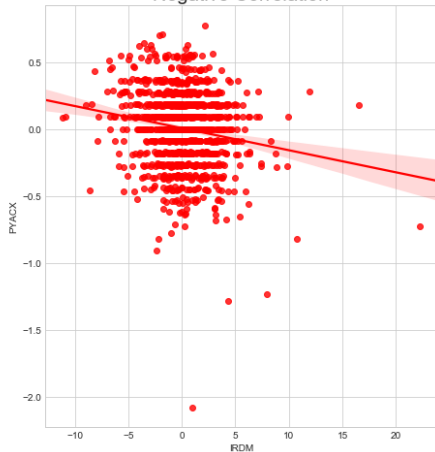
$$\rho_{X,Y} \begin{cases} = -1, & \text{perfect decreasing (inverse) linear relationship} \\ \in (-1, 1), & \text{indicating the degree of linear dependence} \\ = 1, & \text{perfect (increasing) linear relationship} \end{cases}$$

A closer look at correlation

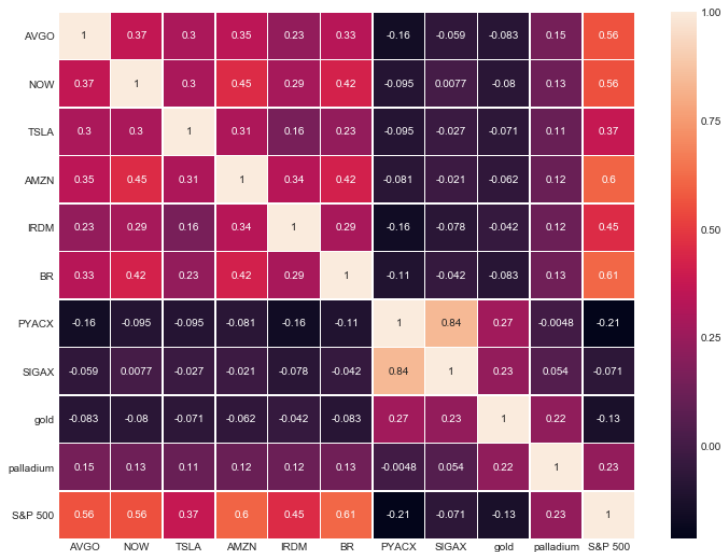
Positive Correlation



Negative Correlation



Correlation Matrix



Definition

The beta coefficient measures the systematic risk of an individual stock compared to the market risk, also called unsystematic risk.

$$\beta = \frac{\text{cov}(R_e, R_m)}{\text{var}(R_m)}$$

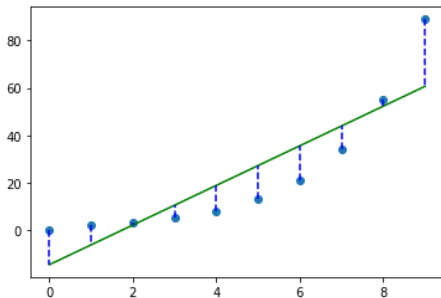
Definition

Alpha is the difference between the realised returns and the expected returns:

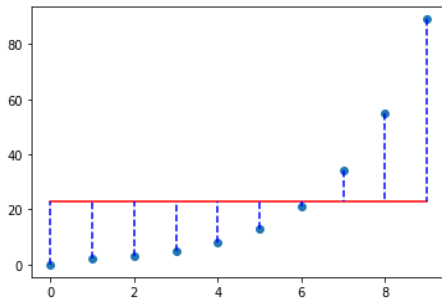
$$\alpha = \bar{R} - \mathbb{E}(R)$$
$$\stackrel{\text{CAPM}}{\implies} \alpha = \bar{R} - \left\{ R_f + \beta(\mathbb{E}(R_m) - R_f) \right\}$$

R-squared

$$R^2 = 1 - \frac{\text{Explained Variation}}{\text{Total Variation}}$$



(a) Explained Variation



(b) Total Variation

Sharpe Ratio

$$\text{Sharpe Ratio} = \frac{R_p - R_f}{\sigma_p}$$

where

- R_p = return of mutual fund
- R_f = risk-free rate
- σ_p = standard variation of the portfolio's excess return

Financial Metrics

For our assets

	alpha	beta	R-squared
AVGO	0.14213	1.35333	0.31393
NOW	0.24718	1.46614	0.30955
TSLA	0.17711	1.26445	0.14046
AMZN	0.32815	1.32199	0.36539
IRDM	0.15867	1.41795	0.20698
BR	0.13206	0.92064	0.37655
PYACX	-0.00576	-0.06792	0.04613
SIGAX	-0.01215	-0.01911	0.00501
gold	0.05087	-0.15174	0.01684
palladium	0.17817	0.47398	0.05493

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Risk and return

Return

$$R_p = \vec{w}^\top \cdot \mathbb{E}(\mathcal{R})$$

Risk

$$\sigma_p = \sqrt{\vec{w}^\top K \vec{w}}$$

$$\begin{aligned} &= \sqrt{\begin{bmatrix} w_1 & w_2 & \dots & w_n \end{bmatrix} \begin{bmatrix} \sigma_1^2 & \text{COV}_{1,2} & \dots & \text{COV}_{1,n} \\ \text{COV}_{2,1} & \sigma_2^2 & \dots & \text{COV}_{2,n} \\ \vdots & \vdots & \ddots & \vdots \\ \text{COV}_{n,1} & \text{COV}_{n,2} & \dots & \sigma_n^2 \end{bmatrix} \begin{bmatrix} w_1 \\ w_2 \\ \vdots \\ w_n \end{bmatrix}} \\ &= \sqrt{\sum_{i=1}^n w_i^2 \sigma_i^2 + \sum_{i=1}^n \sum_{j=1}^n w_i w_j \text{COV}_{ij}} \end{aligned}$$

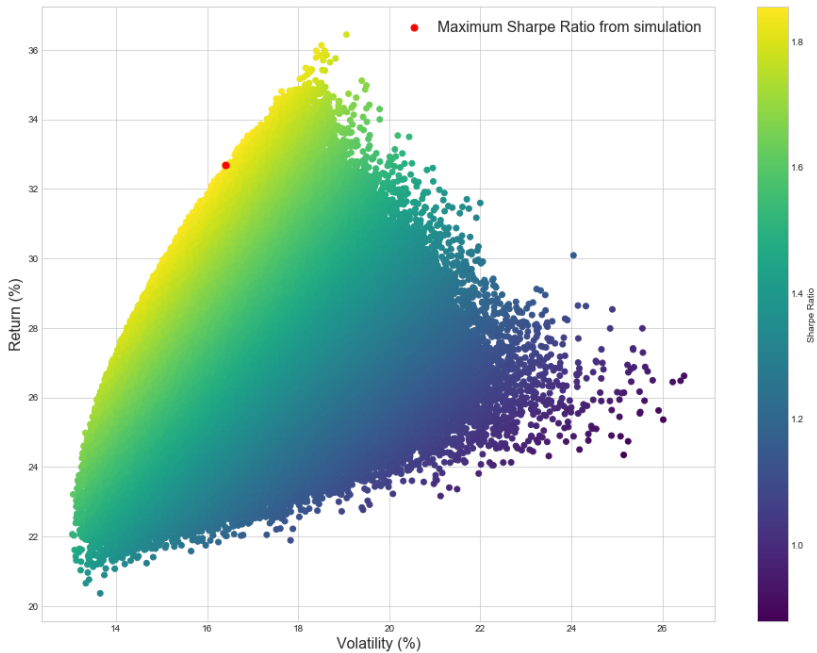
Naive weight allocation

Remember!

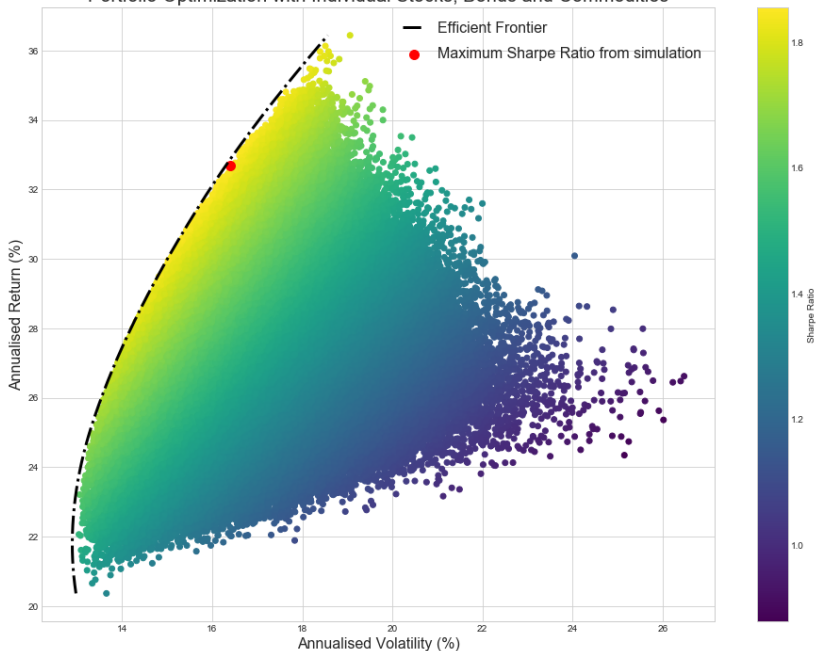
- 70% Stocks
- 20% Bonds
- 10% Commodities

What about \vec{w} ?

- 70% for 6 Stocks $\rightarrow \frac{70\%}{6} = 11.67\%$ each
- 20% for 2 Bonds $\rightarrow 10\%$ each
- 10% for 2 Commodities $\rightarrow 5\%$ each



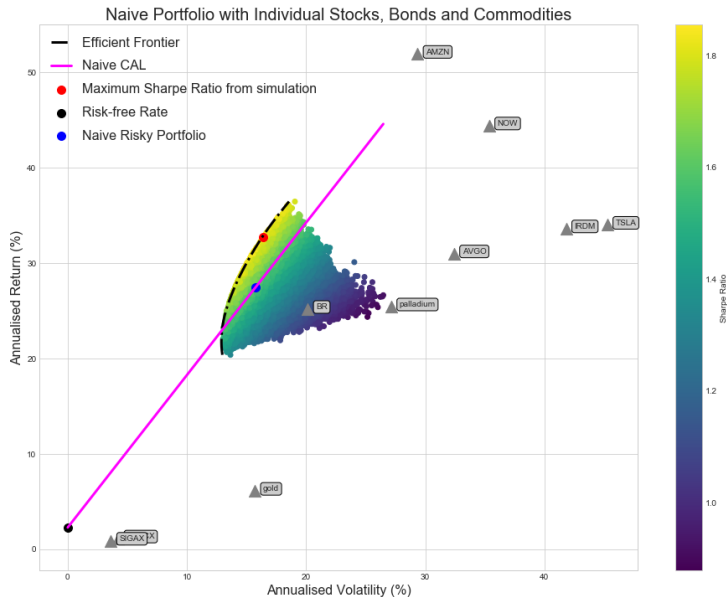
Portfolio Optimization with Individual Stocks, Bonds and Commodities



CAL construction

$$\left\{ \begin{array}{l} (0, r_f) \in \epsilon_{\text{naive}} \\ (\sigma_{\text{naive}}, r_{\text{naive}}) \in \epsilon_{\text{naive}} \end{array} \right\} \Rightarrow \epsilon_{\text{naive}} : y = \underbrace{\frac{r_{\text{naive}} - r_f}{\sigma_{\text{naive}}}}_{\text{naive Sharpe ratio}} \cdot x + r_f$$

Naive CAL



But...

We can do better!

Optimal portfolio

Optimization problem formulation

$$\begin{aligned} \max \quad & \frac{\vec{w}^\top \cdot \mathbb{E}(\mathcal{R}) - r_f}{\sqrt{\vec{w}^\top K \vec{w}}} \\ \text{s.t.} \quad & \mathbf{1}^\top \vec{w} = 1 \\ & \mathbf{1}^\top \vec{w}_S = w_s \\ & \mathbf{1}^\top \vec{w}_B = w_b \\ & \mathbf{1}^\top \vec{w}_C = w_c \\ & w_s + w_b + w_c = 1 \\ & w_i \geq 0 \quad i = 1, \dots, n \end{aligned}$$

Optimal portfolio

Optimization problem formulation

Sharpe Ratio

max

$$\frac{\vec{w}^\top \cdot \mathbb{E}(\mathcal{R}) - r_f}{\sqrt{\vec{w}^\top K \vec{w}}}$$

s.t.

$$\mathbf{1}^\top \vec{w} = 1$$

$$\mathbf{1}^\top \vec{w}_S = w_s$$

$$\mathbf{1}^\top \vec{w}_B = w_b$$

$$\mathbf{1}^\top \vec{w}_C = w_c$$

$$w_s + w_b + w_c = 1$$

$$w_i \geq 0 \quad i = 1, \dots, n$$

Optimization yields...

optimal weights

$$\vec{w} = \begin{bmatrix} w_{\text{AVGO}} \\ w_{\text{NOW}} \\ w_{\text{TSLA}} \\ w_{\text{AMZN}} \\ w_{\text{IRDM}} \\ w_{\text{BR}} \\ w_{\text{PYACX}} \\ w_{\text{SIGAX}} \\ w_{\text{gold}} \\ w_{\text{palladium}} \end{bmatrix} = \begin{bmatrix} 4.0068 \\ 8.6743 \\ 1.0266 \\ 38.2827 \\ 1.32 \\ 16.6897 \\ 20.0 \\ 0.0 \\ 0.0 \\ 10.0 \end{bmatrix} \%$$

Optimization yields...

Financial Metrics

	Optimal Risky Portfolio
Return (%)	32.7164
Risk (%)	16.3185
Sharpe Ratio	1.8658
Beta (β)	0.9067

Capital Allocation Line

$$\left\{ \begin{array}{l} (0, r_f) \in \epsilon_{\text{CAL}} \\ (\sigma_{\text{OPT}}, r_{\text{OPT}}) \in \epsilon_{\text{CAL}} \end{array} \right\}$$

Capital Allocation Line

$$\left\{ \begin{array}{l} (0, r_f) \in \epsilon_{\text{CAL}} \\ (\sigma_{\text{OPT}}, r_{\text{OPT}}) \in \epsilon_{\text{CAL}} \end{array} \right\} \Rightarrow \epsilon_{\text{CAL}} : y = \underbrace{\frac{r_{\text{OPT}} - r_f}{\sigma_{\text{OPT}}}}_{\text{max Sharpe ratio}} \cdot x + r_f$$

Optimal Overall Portfolio

Which portfolio is the overall optimal?

- i.e. which portfolio along the CAL is the best

Optimal Overall Portfolio

Which portfolio is the overall optimal?

- i.e. which portfolio along the CAL is the best **for us**?

Optimal Overall Portfolio

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- i.e. which portfolio along the CAL is the best **for us**?

Utility maximization

$$\text{Utility} = U = r_f + z \cdot (r_{\text{opt}} - r_f) - 0.05 \cdot A \cdot \sigma_{\text{opt}}^2 \cdot z^2$$

Optimal Overall Portfolio

Which portfolio is the overall optimal?

- i.e. which portfolio along the CAL is the best **for us**?

Utility maximization

$$\text{Utility} = U = r_f + z \cdot (r_{\text{opt}} - r_f) - 0.05 \cdot A \cdot \sigma_{\text{opt}}^2 \cdot z^2$$

Maximize w.r.t. z :

Optimal Overall Portfolio

Which portfolio is the overall optimal?

- i.e. which portfolio along the CAL is the best **for us**?

Utility maximization

$$\text{Utility} = U = r_f + z \cdot (r_{\text{opt}} - r_f) - 0.05 \cdot A \cdot \sigma_{\text{opt}}^2 \cdot z^2$$

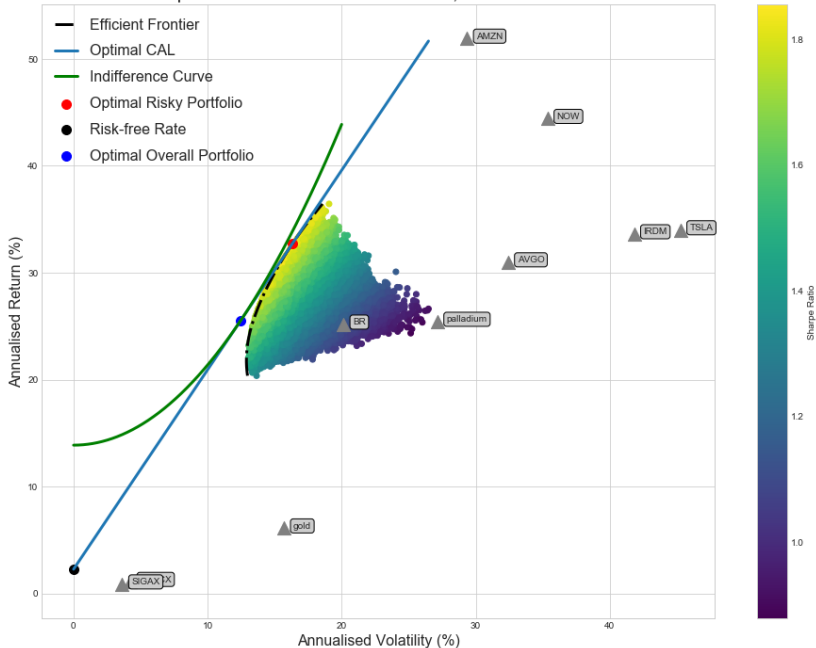
Maximize w.r.t. z :

$$\frac{\partial U}{\partial z} = 0$$

$$\implies r_{\text{opt}} - r_f - 0.1 \cdot A \cdot \sigma_{\text{opt}}^2 \cdot z = 0$$

$$\implies z^* = \frac{r_{\text{opt}} - r_f}{0.1 \cdot A \cdot \sigma_{\text{opt}}^2}$$

Portfolio Optimization with Individual Stocks, Bonds and Commodities



Past Performance

(1/13/2015 - 1/13/2020)

	Optimal Overall Portfolio	S&P 500
Return (%)	25.4769	11.3118
Risk (%)	12.4384	13.4138
Sharpe Ratio	1.8658	0.6741
Beta (β)	0.6911	1.0
Alpha (α) (%)	16.9584	0.0

References



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The end!