Intro to R Programming

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What is a program?

- Translation of an algorithm into a language that computer understands
- An algorithm takes input, perform some operations and gives output
 - Executes in finite time
 - E.g. sorting, searching, reading, copying!
- Complexity of a Program
 - Time and space!
 - E.g. Fibonacci series!
- Programming Paradigms
 - Iterative vs Recursive
 - Procedural vs Object Oriented
- Good Program
 - Re-readable, organized and modular

Typical Programing Errors

- Syntactical (spelling mistake)
 - Will get caught very easily! Just run the program.
- Semantic Errors (meaningless operations)
 - For e.g. "nikhil"+32
 - Exceptions: like divide by 0.
 - Note that R catches this exception and returns Inf
 - May get caught. A warning will be thrown nonetheless.
- Logical Errors (Unintentional)
 - Program will crash, run forever or give a wrong answer!
 - Debugging requires some skill and experience.

Getting Help in R

From Console

- Just type: ? followed by function name without parenthesis
- E.g. ?mean; ?sum; ?length;
- Clarify:
 - ?mean help for the function "mean" in the available libraries
 - Same as help(mean)
 - ??mean will perform a keyword search over the entire database
 - Same as help.search("mean")
 - mean() call the function mean
 - mean print the definition of the function "mean"

From Web sources

- Most reliable and easy to incorporate is <u>www.stackoverflow.com</u>.
- www.r-bloggers.com is also quite helpful.
- You can use https://cran.r-project.org for any resource on R
- Even typing your question in google will get you good results!
 - 99% of your questions are already answered! You just need to find them!

R Input and Output

- Simple assignment
 - X = 1; (or X < -1;)
 - Assignment is always right to left
 - Read 1 goes into X
 - We aren't comparing X with 1 here
 - The semi-colon isn't necessary in R, but it's a good practice to use it
 - X = ; is incomplete
 - # (prefix) is used as a comment. Use it for helpful comments.
 - Use Ctrl-Shift-C for multi-line comments
- Value of X can be seen by
 - X;

Vectors

• A sequence of numbers. Many ways to input!

```
Y = c(1,7,-3,41); # concatenate arbitrary numbers
Y = 1:10; # natural numbers
Y = seq(1,100,9); # skip by 9
Y = rep(2, 3); # repeat 3 times
Y = rep(1:2, 3); # repeat the vector
Y = rep(1:2, each = 3); # repeat each element 3 times
Y = c(); # empty vector
Execute this: c(1:3, rep(c(5,7), each = 2), rep(9, 4), 7);
```

- Length of vector: length(Y);
- Accessing ith element of vector: Y[i]; # square brackets
 - i should be between 1 and length(Y)
 - Printing the entire vector is as before: Y;

Objects in R

- 5 basic (atomic) types of objects
 - character strings
 - numeric real numbers. Also called double.
 - integer natural numbers. Default data type for numeric vectors.
 - typeof(1:10)
 - complex complex numbers. We won't use them now!
 - logical True/False (binary)
- Most basic collection of objects is a vector (also called an array)
 - Can only contain objects of same class (i.e. character or integer; not both)
 - "list" is a special type of object and can contain heterogeneous objects
 - Any Combination of vector, matrix, atomic types etc.
 - It can even contain another list as an object. E.g. linked-lists!
 - Due to its generality its very slow and hence rarely used with large datasets unless situation demands it

Numbers

- Default type of any number is numeric (i.e. real). typeof(1)
- R can differentiate between corner cases:

```
1/0 is Inf -- is.infinite();
0/0 is NaN -- is.nan();
Missing data is NA -- is.na();
```

Check what's Inf-Inf?

- Arithmetic Operations
 - * multiplies
 - / divides
 - ^ takes exponent
 - %% is the modulo (remainder) operator. Try: 7 %% 2;

Coercion

- Mixing Objects
 - Automatically coerced to the same class.
 - Try: c(1:7, "a"); c(T, 2); c("a", FALSE);
 - Implicit coercion!
 - Never use unless you know what you're doing!

- Explicit Coercion
 - as.character(1:5);
 - as.numeric("iimb"); # warning!
 - as.logical(seq(-2,2,1));

List

Can carry different types of data together

```
L = list(1, FALSE, 3.14, "iimb", "c", 4-3i);
Print list: L;
L is in fact a list of lists. Check: typeof(L); typeof(L[4]); typeof(L[4]);
```

- Single square brackets [i] access the ith list embedded in the list L
- Double square brackets [[i]] access the ith element
- Can append elements in list: L = append(L, "7th");
- unlist(L); will coerce all elements into a single type and return a vector
- Delete an element from a list:
 - I don't know how to do that!
 - Let's google: "delete element from list in R"
 - Open the answer on www.stackoverflow.com

Matrices

- Generalization of vectors
 - 2 dimensions instead on one!
 - N x K matrix means a matrix having N rows and K columns. Total of NK elements.
 - \bullet M = matrix(nrow = 2, ncol = 3);
 - Dimensions: dim(M);
 - Can think of M as
 - 3 columns vectors each of length 2, or
 - 2 row vectors each of length 3
 - Populate matrix: M = rbind(1:3, 4:6);
 - Alternatively populate as: M = cbind(1:2, 3:4, 5:6);

Matrices (cont.)

- Indexing a matrix
 - M[i,j] gives the element at ith row and jth column
 - M[i,] gives the entire ith row (a vector)
 - M[,j] gives the entire jth column (a vector)

- Matrix multiplication
 - * just does an element wise multiplication, i.e. $(M*N)_{ij}=M_{ij}*N_{ij}$
 - %*% performs the usual matrix multiplication. Try: M %*% N
 - Dimensions must match
 - Try t(M) %*% M;
 - t(M) takes transpose of a matrix!

Matrices (cont.)

- Identity matrix: diag(3)
- Diagonal Matrix: diag(c(1,5,7)); diag(1:7);
- Diagonal of a matrix: diag(M)
- Trace of a matrix: sum(diag(M))
- Inverse of a matrix:
 - Must be a square matrix: M = matrix(1:9, nrow = 3, ncol = 3);
 - Another way to create a matrix. Data is entered column-wise.
 - Determinant must be non-zero: det(M); M[3,3] = 19; det(M);
 - Inverse: solve(M);

Reading Data

- Download some stock data from NSE
 - https://www.nseindia.com/products/content/equities/indices/historical_index_data.htm
 - Save the CSV file as data.csv
- From CSV (most common)
 - setwd("C:/Users/nikhil/data.csv"); nifty = read.csv("data.csv");
 - Alternatively: nifty = read.csv(" C:/Users/nikhil/data.csv");
- From Excel
 - Search it yourself! It is not recommended btw.
- From clipboard
 - read.table("clipboard");
 - This is quick fix for small data transfer between R and excel. Use read.csv()
 as your primary method for data reading!

Reading Data (cont.)

Viewing data

```
View(nifty);
```

Date

```
nifty$Date = as.Date(nifty$Date, format = "%d-%b-%Y");
n = nrow(nifty);
d = nifty$Date[1];
format(d, format = "%D"); # 04/02/18
format(d, format = "%d-%m-%y"); # 02-04-18
format(d, format = "%d.%b.%Y"); # 02.Apr.2018
format(d, format = "%d_%B_%Y"); # 02_April_2018
```

Alternatively,

```
• read.table("data.csv", header = T, sep = ",", nrows = 5);
```

if-else

```
• if(<COND 1>) {
                             # do something!
                                                     # do something!
     # do something!
                                                 } else if(<COND 2>) {
                           } else {
                            # ...
                                                     # ...
                                                    } else {
                                                     # ...
if(nifty$Close[2] > nifty$Close[1]) {
 str = paste("Stock market closed green on", nifty$Date[2]);
} else if(nifty$Close[2] > nifty$Open[2]) {
 str = paste("Stock market closed above opening on", nifty$Date[2]);
} else {
 str = paste("Stock market was red and closed below opening on", nifty$Date[2]);
print(str);
```

• if(<COND 1>) {

• if(<COND 1>) {

for loop

Looping is used to perform similar set of tasks repetitively

```
for(i in n:1) {
    print(nifty$Date[i]);
}
n:1; is same as seq(n,1,1); i.e. backwards counting!
Alternatively, you can execute: rev(nifty$Date); or nifty$Date[n:1];
```

- Try avoiding loops if you can!
 - Increasing all dates by a week: nifty\$Date + 7
 - Finding Daily growth: nifty\$Close[-1] / nifty\$Close[-n]
 - Daily diff. b/w high and low prices: nifty\$High nifty\$Low
 - Question: find % growth in daily volatility
 - Volatility is defined as: $Vol_t = (High_t Low_t)/Open_t$
 - Percentage Growth is defined as: $%G = \frac{(Value_{t+1} Value_t)}{Value_t} * 100$
- Loops and if-else can be used in conjunction!

Jumping

- Till now all our commands executed sequentially
- There may be circumstances when we need to jump
- Next and Break
 - next is used to skip an iteration, while break exits the loop entirely.

```
• for(i in 1:10) {
    if(i <= 3) {
        next;
    }
    if(i > 6) {
        break;
    }
    print(i);
}
i;
```

return() is used to exit a function with a value.

Function

- Organize often-used set of instructions separately in a "function"
- Calling a function will execute all the commands in the body of function
- We have used many functions till now
 - They end with parenthesis: ()
 - E.g. sum(); rbind(); vector(); format(); read.csv(); etc
 - Note that curly braces {} are used for if-else and for loops, square braces [] for vector/matrix indexing and parenthesis () for grouping, if-else & for conditions and functions.

A function has

- A name by which we call them, e.g. sum
- A set of inputs to be put within parenthesis like numbers 1:10 in sum()
- Return value which is the output of the function like the sum of numbers in sum()

Function Example

```
my_mean = function(x) {
    n = length(x);
    mean = sum(x) / n;
    return(mean);
}
```

- Name of the function is: my mean
- Input is: x
- Output is: mean
 - Note that the mean here is just a name, we could well have used any other name without changing anything about our function

Function (Example) Cont.

Alternate ways to write the same function

```
my_mean = function(x) {
    return( sum(x) / length(x) );
}
No need to store sum and length. We can directly divide them!
my_mean = function(x) {
    sum(x) / length(x);
}
```

- No need for an explicit return. The last statement is returned by default.
- Try various value with my_mean() and the inbuilt mean(). See that the answers are exactly the same.
- Write a function for variance where $Var(x) = mean([x mean(x)]^2)$
 - Compare it with the inbuilt var() function?

Multiple conditions & which() function

• The arguments to if() and which() and the output of is.xx() family of functions is a logical object, i.e. either TRUE or FALSE.

- A valid combination of logical objects is also a logical object. E.g.
 - Logical AND: TRUE & FALSE is FALSE
 - Logical OR: TRUE FALSE is TRUE
 - Logical NOT: ! FALSE is TRUE

- De Morgan's Law
 - !(A | B) = (!A) & (!B)
 - !(A & B) = (!A) | (!B)

The below two indexes are one and same (by De Morgan Law),

```
day = as.numeric( substr(nifty$Date, 9, 10) );
OR day = as.numeric( format(df[,1], format = "%d") );
idx = which(nifty$Close > nifty$Open & (day < 5));</li>
idx = which(!(nifty$Close < nifty$Open | (day >= 5)) );
```

 which() gives the indexes matching the criterion. E.g. out of 101:200 which numbers are multiples of 2,3 and 5?

```
count = 101:200;
which( count %% 2 == 0 & count %% 3 == 0 & count %% 5 == 0 );
count[count %% 2 == 0 & count %% 3 == 0 & count %% 5 == 0];
```

We can do multi-way match using %in%

```
mult_17 = seq(17,300,17);
which(count %in% mult_17);
which(mult_17 %in% count);
which(!(count %in% mult_17));
which(!(mult_17 %in% count));
```

Correlation

- Difference between Independence and Correlation
 - $X \sim N(0,1), Y = X^2$. Are X and Y correlated?
 - Let's check in R

```
• X = rnorm(1000, 0, 1);
Y = X^2;
cor(X,Y);
```

- However, cor(X, X^3) != 0.
- Let $Y \sim N(0,1)$ independent of X. Then is cor(X,Y) = 0? What about $cor(X^q,Y)$?

```
• Y = rnorm(1000,0,1);
• cor_q = rep(NA, 10);
  for(q in 1:10) {
      cor_q[q] = cor(X^q, Y);
  }
  cor_q;
```

Independence implies NO correlation of any functional form.

Regression

• Let, $Y = \beta_0 + \beta_1 \cdot X + u$ be the true model. By regressing Y on X, we hope to recover an unbiased estimate of β_1 and see how much of the variation in Y is explained by variation in X unrelated to variation in u.

```
n = 1000;

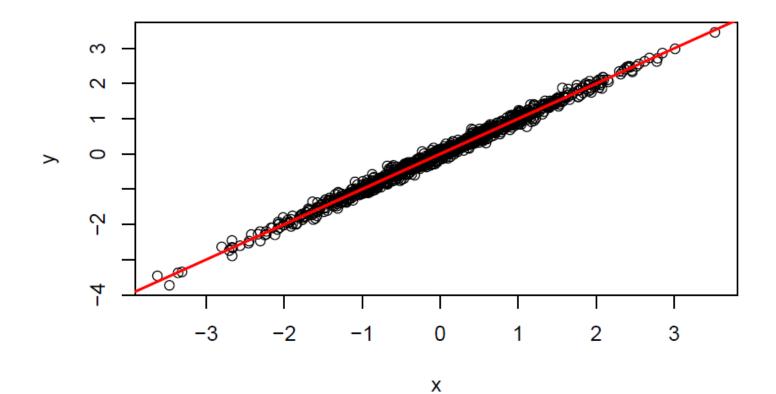
x = rnorm(n, 0, 1);

u = rnorm(n, 0, 0.1);

y = u + x;

plot(x,y);
```

```
fit = lm(y ~ x);
summary(fit);
stargazer(fit, type = "html", out = "fit.html");
# Regression Line
abline(fit$coefficients, col = "red", lwd = 2);
```



```
7
u = rnorm(n, 0, 0.5);
y = u + x;
                                                  Х
plot(x,y);
fit = lm(y \sim x);
summary(fit);
# Regression Line
abline(fit$coefficients, col = "red", lwd = 2);
```

```
u = rnorm(n, 0, 5);
y = u + x;
plot(x,y);
fit = lm(y \sim x);
summary(fit);
# Regression Line
abline(fit$coefficients, col = "red", lwd = 2);
```

Some Useful functions

cumprod() using only cumsum() ?

```
• unique(), duplicated()
• list.files()

    Pattern matching using regex

   All files starting from "s": "^s"
   All files starting with "b" or "d": "^(b|d)"
   All CSV files: ".*.csv"
• order()

    Sort data/dataframes

    It gives the sequence of ordered indexes NOT the ordered numbers

    Can do 2-way and 3-way sorts

• union(), intersect()
cumsum(), cumprod()
```

Merging

- Combining two datasets is a very routine and important task
- Merging is akin to Joining (in relational database, SQL etc)

■ Summary:

s=	attr1	attr3
	b	s2
	С	s3
	d	s4

$r \bowtie s$					
attr1 attr2 attr3					
b	r2	s2			
С	r3	s3			

$r \bowtie s$				
attr1	attr2	attr3		
а	r1	null		
b	r2	s2		
С	r3	s3		

attr1	attr2	attr3	
b	r2	s2	
С	r3	s3	
d	null	s4	

 $r \bowtie s$

attr1	attr2	attr3
а	r1	null
b	r2	s2
С	r3	s3
d	null	s4

 $r \propto s$

Merging Example

- Taken from <u>Stackoverflow webpage</u>
- Create two datasets:

```
• df1 = data.frame(cust_id = c(1:6), Product =
  c(rep("Toaster", 3), rep("Radio", 3)));
```

- df2 = data.frame(cust_id = c(2, 4, 6), State =
 c(rep("Alabama", 2), rep("Ohio", 1)));
- The data looks like:
- We will need to use a new package dplyr
 - install.packages("dplyr");

<u>df1</u>		<u>df2</u>		
cust id	Product	cust id	<u>State</u>	
1	Toaster	2	Alabama	
2	Toaster	4	Alabama	
3	Toaster	6	Ohio	
4	Radio			
5	Radio			
6	Radio			

Inner Join

Full Join

• dplyr::inner_join(df1, df2);

cust id	Product	<u>State</u>
2	Toaster	Alabama
4	Radio	Alabama
6	Radio	Ohio

• dplyr::full_join(df1, df2);

cust id	Product State		
1	Toaster NA		
2	Toaster	Alabama	
3	Toaster	NA	
4	Radio	Alabama	
5	Radio	NA	
6	Radio	Ohio	

Left Join

Right Join

• dplyr::left_join(df1, df2);

cust id	Product	<u>State</u>
1	Toaster	NA
2	Toaster	Alabama
3	Toaster	NA
4	Radio	Alabama
5	Radio	NA
6	Radio	Ohio

- dplyr::right_join(df1, df2);
 - The above is identical to, dplyr::left_join(df2, df1);

cust id	Product	State
2	Toaster	Alabama
4	Radio	Alabama
6	Radio	Ohio

Cartesian Product

- Every row of df1 multiplied with every row of df2
- cart_prd = merge(df1, df2, by = NULL);

S.No.	cust id.x	<u>Product</u>	cust id.y	<u>State</u>
1	1	Toaster	2	Alabama
2	2	Toaster	2	Alabama
3	3	Toaster	2	Alabama
4	4	Radio	2	Alabama
5	5	Radio	2	Alabama
6	6	Radio	2	Alabama
7	1	Toaster	4	Alabama
8	2	Toaster	4	Alabama
9	3	Toaster	4	Alabama

S.No.	cust id.x	Product	cust id.y	<u>State</u>
10	4	Radio	4	Alabama
11	5	Radio	4	Alabama
12	6	Radio	4	Alabama
13	1	Toaster	6	Ohio
14	2	Toaster	6	Ohio
15	3	Toaster	6	Ohio
16	4	Radio	6	Ohio
17	5	Radio	6	Ohio
18	6	Radio	6	Ohio

- Cartesian products are extremely slow. Never do that even on a decent sized (> 1000 rows) dataset. Your computer will probably hang.
- Although there is no use of Cartesian products, it encapsulates all types of merges. Meaning we can extract any type of merge from a Cartesian product.
- Inner join can be extracted via

```
idx = which(cart_prd$cust_id.x == cart_prd$cust_id.y);cart prd[idx,];
```

Merging with more than one variable

 Most of the merging usage is with two variables: date and company name. Generate data using below:

```
date = seq.Date(as.Date("2018-01-01"), by = 1, length.out = 5);
comp = c("A", "B", "C", "D", "E");
all pairs = merge(comp, date, by = NULL);
# sales data - 15 points
idx = sample(1:nrow(all pairs), 15, replace = F);
df1 = data.frame(comp = all pairs$x[idx], date = all pairs$y[idx],
                 sales = round(runif(15, min = 1e3, max = 1e5)));
# advertising data - 12 points
idx = sample(1:nrow(all_pairs), 12, replace = F);
df2 = data.frame(comp = all_pairs$x[idx], date = all_pairs$y[idx],
                 adv = round(runif(12, min = 1e2, max = 1e4)));
```

<u>df1</u>		<u>df2</u>			
comp	<u>date</u>	<u>sales</u>	comp	<u>date</u>	<u>adv</u>
В	05-04-2018	53429	С	03-04-2018	980
Α	03-04-2018	70750	С	06-04-2018	6183
В	03-04-2018	5426	В	06-04-2018	8077
В	06-04-2018	88504	В	02-04-2018	241
Е	06-04-2018	78449	D	02-04-2018	3642
Α	04-04-2018	98954	В	04-04-2018	3878
D	04-04-2018	57618	E	02-04-2018	1501
E	04-04-2018	22011	В	03-04-2018	6727
С	02-04-2018	85976	D	06-04-2018	4259
D	02-04-2018	42842	D	03-04-2018	4434
Е	02-04-2018	94057	Α	06-04-2018	6745
Α	05-04-2018	25063	E	03-04-2018	2208
Е	05-04-2018	51320			
D	06-04-2018	99720			
Е	03-04-2018	16845			

Inner Join

• dplyr::inner_join(df1, df2);

comp	<u>date</u>	<u>sales</u>	<u>adv</u>
В	03-04-2018	5426	6727
В	06-04-2018	88504	8077
D	02-04-2018	42842	3642
E	02-04-2018	94057	1501
D	06-04-2018	99720	4259
E	03-04-2018	16845	2208

Full Join

• dplyr::full_join(df1, df2);

<u>comp</u>	<u>date</u>	<u>sales</u>	<u>adv</u>
В	05-04-2018	53429	NA
A	03-04-2018	70750	NA
В	03-04-2018	5426	6727
В	06-04-2018	88504	8077
Е	06-04-2018	78449	NA
Α	04-04-2018	98954	NA
D	04-04-2018	57618	NA
Е	04-04-2018	22011	NA
С	02-04-2018	85976	NA
D	02-04-2018	42842	3642
Е	02-04-2018	94057	1501
Α	05-04-2018	25063	NA
E	05-04-2018	51320	NA
D	06-04-2018	99720	4259
Е	03-04-2018	16845	2208
С	03-04-2018	NA	980
С	06-04-2018	NA	6183
В	02-04-2018	NA	241
В	04-04-2018	NA	3878
D	03-04-2018	NA	4434
Α	06-04-2018	NA	6745
			_

Left Join

• dplyr::left_join(df1, df2);

comp	<u>aate</u>	saies	<u>adv</u>
В	05-04-2018	53429	NA
Α	03-04-2018	70750	NA
В	03-04-2018	5426	6727
В	06-04-2018	88504	8077
E	06-04-2018	78449	NA
Α	04-04-2018	98954	NA
D	04-04-2018	57618	NA
Е	04-04-2018	22011	NA
С	02-04-2018	85976	NA
D	02-04-2018	42842	3642
Е	02-04-2018	94057	1501
Α	05-04-2018	25063	NA
Е	05-04-2018	51320	NA
D	06-04-2018	99720	4259
E	03-04-2018	16845	2208

Right Join

- dplyr::right_join(df1, df2);
 - The above is identical to, dplyr::left_join(df2, df1);

comp	<u>date</u>	<u>sales</u>	<u>adv</u>
С	03-04-2018	NA	980
С	06-04-2018	NA	6183
В	06-04-2018	88504	8077
В	02-04-2018	NA	241
D	02-04-2018	42842	3642
В	04-04-2018	NA	3878
<u>E</u>	02-04-2018	94057	<u>1501</u>
В	03-04-2018	5426	6727
D	06-04-2018	99720	4259
D	03-04-2018	NA	4434
Α	06-04-2018	NA	6745
Е	03-04-2018	16845	2208

Loop Functions

- Writing loops in a single command. Can come very handy and compact. The function name ends with "apply".
- List of functions: lapply(), apply(), sapply(), tapply(), mapply()
- These functions work on a list of inputs, not just one input!
- E.g.
 - X = list(a = 1:10, b = rnorm(100, 0, 1), c = runif(1e3, 9, 91));
 - lappy(X, mean); # returns a list
 - sapply(X, mean); # returns a vector
- Let's say we want to find cor(X,X^i) for i in 1:10 w/o writing a loop?
 - X = rnorm(1000, 0, 1);
 - sapply(1:10, function(i) cor(X,X^i));
 - Here we have used anonymous function, i.e. a function w/o a name.

- apply() is mostly used for applying functions on rows or cols of a matrix
 - Like taking means by rows

```
M = matrix(1:50, nrow = 10, ncol = 5);
apply(M, 1, mean); # mean of each row
```

- apply(M, 2, mean); # mean of each col
- You can do the above using a loop also, but apply() is more compact.
- The faster version of above are also available:
 - rowSums(x) is equivalent to apply(x, 1, sum)
 - colMeans(x) is equivalent to apply(x, 2, mean)

tapply() is used to apply a function over a subset of vector. Lets say,

```
x = c(rnorm(100), runif(100));
f = rep(1:2, each = 100);
tapply(x, f, mean);
```

Pipe and the dplyr package

- Download the tidyverse package and load it: library(tidyverse);
 - Also load dplyr: library(dplyr);
- We will use the gapminder dataset.
 - Install gapminder package
 - df = gapminder::gapminder; df = as.data.frame(df);
- Selecting a particular column
 - df %>% select(lifeExp);
 - Performing operation on data
 - df %>% select(lifeExp) %>% mean
- Selecting some rows (based on a filtering criterion):
 - df %>% filter(year > 2000)
 - df %>% filter(year > 2000 & country == "India")

- Selecting some rows (based on a filtering criterion):
 - df %>% filter(year > 2000)
 - df %>% filter(year > 2000 & country == "India")
- Selecting and filtering together
 - df %>% select(country, year, lifeExp) %>% filter(year > 2000)
 - df %>% select(country, year, lifeExp) %>% filter(country == "India")

Grouping data

- df %>% select(country, year, lifeExp) %>% group_by(lifeExp) %>% as.data.frame %>% head
- df %>% group_by(country, gdpPercap) %>% as.data.frame %>% head
- Create new columns (mutate)
 - df %>% mutate(decade = 10*(as.integer(year/10))) %>% head
- Ordering
 - df %>% arrange(-pop) %>% head

 Performing aggregation on grouped data is the most important usage of dplyr library

Aggregation:

```
df %>% select(-c(continent)) %>% group_by(country) %>% summarise_all(mean)
df %>% select(-c(continent)) %>% group_by(country) %>% summarise_all(mean)
df %>% group_by(continent) %>% summarise_all(mean)
df %>% group_by(continent, year) %>% summarise_all(mean) %>% filter(continent == "Asia")
```

Counting and ordering in Aggregation:

- df %>% group_by(continent, year) %>% summarise(n()) %>% filter(continent == "Asia")
- df %>% group_by(continent) %>% summarise(n())
- df %>% filter(year == 2007) %>% group_by(pop) %>% arrange(-pop)
- df %>% filter(year == 2007) %>% group_by(pop) %>% arrange(-gdpPercap)
- df %>% filter(year == 2007) %>% group_by(pop) %>% mutate(GDP =
 gdpPercap*pop) %>% arrange(-GDP) %>% as.data.frame %>% select(country, GDP)
 %>% head(15)