THEORY OF FINANCE

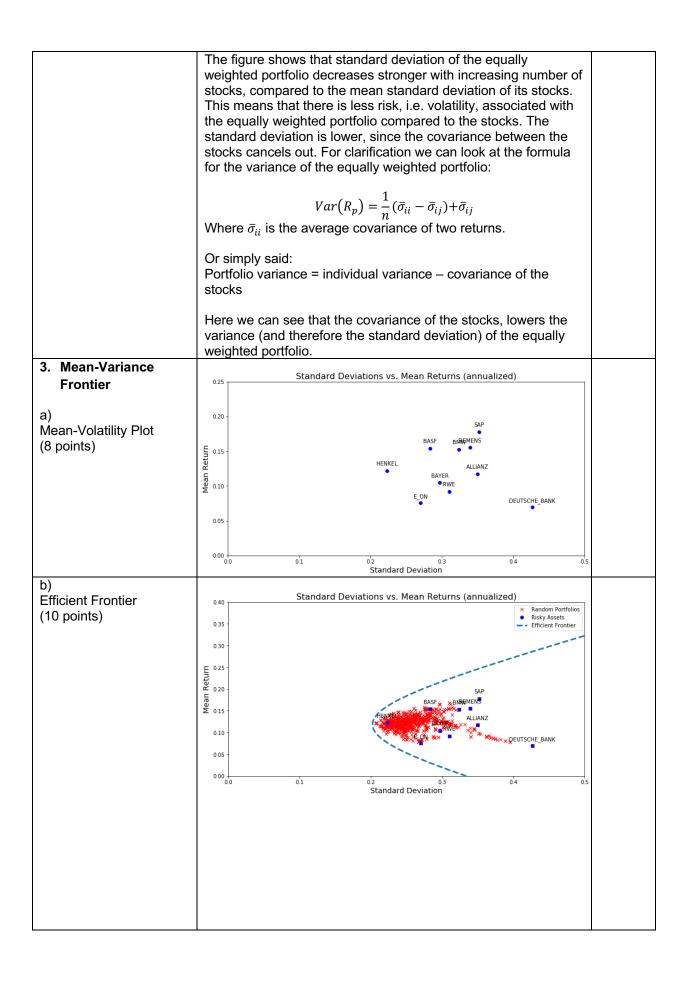
Solution Sheet on Problem Set 1

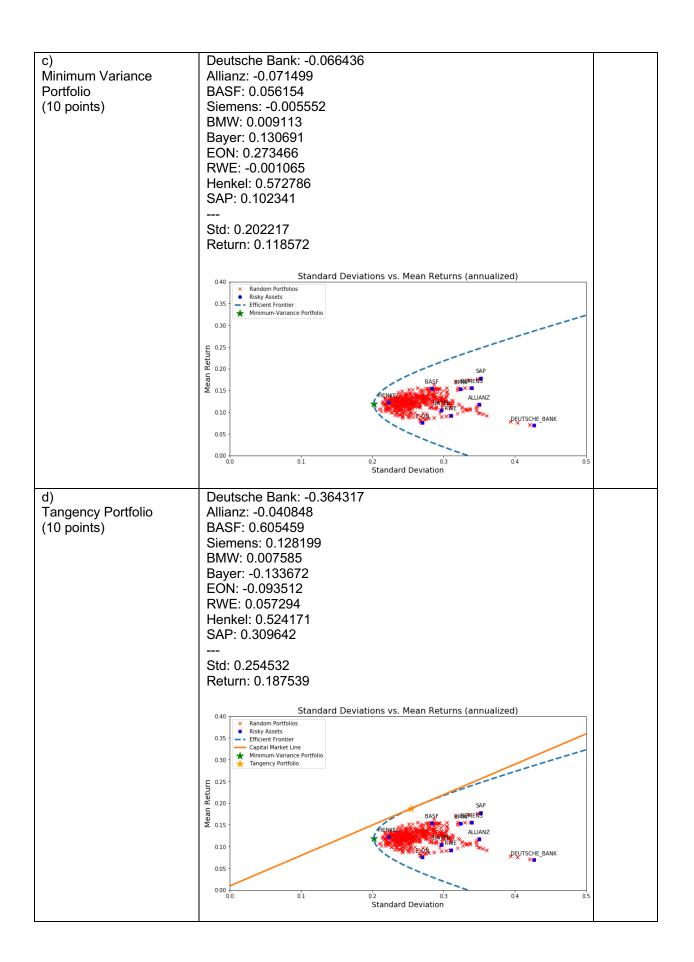
Return Calculations, Portfolio Choice and Mean-Variance Frontier Deadline: 19.10.2021

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Task		Points
a) Discrete vs. Log- Returns: mean, st.dev. and annualized (6 points)	See return variations in code section "Problem 1 – Return Comparison – a)"	Earned
b) Discrete vs. Log-Returns: Plot and interpretation (8 points)	Log- vs. Discrete Returns DEUTSCHE_BANK Log- vs. Discrete Returns E_ON Log- vs. Discrete Returns E_ON We are using log returns which have a normalizing effect on the data, and therefore the differences in the plot are rather small. Nonetheless, it can be seen that the curvature in the DB plot is slightly more pronounced because there we have the larger maximal difference in discrete and log return. Moreover, there is an upwards curvature in both plots which is because discrete returns are always larger than the corresponding log return.	
c) Usage of return type (6 points)	Usually, the discrete return is used for calculating the return of a portfolio (i.e. multiple assets) and when choosing the different weights of assets in a portfolio.	

	Log returns are used when returns are aggregated across time and when comparing investment horizons for the same asset.																	
d) Investment value (6 points)		At end the of July 2021 the investment would be worth EUR 814.91.																
2. Diversification Effect	impl	When looking purely for diversification (regardless of any implies on return) the idea is to reduce the portfolio variance. Given the portfolio variance in this case is defined by																
a) Diversification using two stocks		$Var(R_P) = \omega_1^2 \sigma_{11} + \omega_2^2 \sigma_{22} + 2\omega_1 2\omega_2 \sigma_{12}$																
(6 points)	of they dive stoo give effectively	the diversification benefit increases with decreasing covariance of the two assets. Therefore, to get the highest diversification benefit an investor should choose stocks Henkel and E_ON as they have the lowest covariance out of the 10 stocks. The worst diversification benefit is achieved by only investing in a single stock (as this would result in the highest covariance). However, given two stocks need to be picked, the worst diversification effect is achieved with investing into RWE and Henkel given they have the highest covariance.																
b) Diversification and portfolio volatility (12 points)	DEUTS SAP ALLIA SIEME BMW RWE BAYER BASF E_ON HENKE	Stocks based on return standard deviation from high to low: DEUTSCHE_BANK																
	Nr Of st oc	1	2	3	4	5	6	7	8	9	10							
	k M ea n St D	0. 12 3	0. 11 2	0. 10 8	0. 10 5	0. 10 3	0. 10 1	0. 09 8	0. 09 6	0. 09 4	0. 09 1							
	P F St D ev	0. 12 3	0. 09 4	0. 09 0	0. 08 7	0. 08 3	0. 07 7	0. 07 5	0. 07 4	0. 07 1	0. 06 9							
c) Visualization and interpretation of b) (12 points)	Portfolio Standard Deviation	0.12 - 0.120 - 0.110 Page 10 0.10 - 0.110 Page 10 0.09 - 0.100 Page 10 0.09 - 0.005 Page 10 0.00 - 0.005 Page 10 0																





e)	Optimal allocation for portfolio in ETF and risk-free asset:	
Portfolio Choice		
(6 points)	Weight in ETF: 36.84%	
	Weight in risk-free asset: 63.16%	