## Lecture Notes for "The Neuroscience of Decision Making" IrBO26 Summer Camp

- Slide 5
  - A more conservative strategy is called for when a large loss is associated with a false alarm, and a more lax strategy when a large loss is associated with a miss. The overall loss size for false alarms is determined by the loss value associated with a single false alarm times the probability of a false alarm. Therefore the appropriate criterion depends on the relative cost of the errors and the prior probability of encountering the signal.
- Slide 9
  - This equation is also termed Bayes's Theorem despite the fact that it follows from simple laws of probability.
- Slide 10
  - As can be seen from the equation, d' can increase by either increasing the separation of the means or reducing the distributions' variance.
- Slide 11
  - Note that the power and size are both functions of some threshold.
- Slide 13
  - Here, the minimum threshold value is assumed to be 0 since we are discussing signal detection in the context of neural firing rates, and negative firing rates are physically impossible.
- Slide 16
  - The term  $r_{\text{ave}}$  in the second equation is the average of the two Gaussians' means  $\left(\frac{r_{+}+r_{-}}{2}\right)$  and  $\sigma_{r}$  is the standard deviation of the Gaussians.
- Slide 18
  - Sections 3.1 and 3.2
- Slide 22
  - Read the figure from left to right
- Slide 24
  - Task difficulty can also be increased by making the directions of motion more similar, but decreasing the coherence is a more convenient option.
- Slide 25
  - You can find this video here.
- Slide 26
  - Make sure to notice that the x-axis is not linear and that  $\mathbb{P}(\text{correct}) = \frac{1}{2}$  at 0% coherence.
- Slide 27
  - Area MT is also called V5 or visual area 5.
- Slide 30
  - We cannot initially posit direct inhibitory connections between our two excitatory populations due to Dale's Law: neurons, and therefore populations of homogeneous neurons cannot project both excitatory

and inhibitory connections.

- Slide 31
  - We call an input unbiased if  $mean(I_1) = mean(I_2)$ .
- Slide 32
  - The gain function  $g_{\sigma}(I)$  relates the current at neuronal population  $\sigma$  to its firing rate A.
  - The equation describing h is Ohm's law convolved by  $e^{-t}$ . Think of it as resistance R times the sum of all currents ever injected into this population weighted by  $e^{t-s}$ , where s is how far away this time point is in the past.
- Slide 33
  - Assumption 1 means that the dynamics of the inhibitory population is instantaneous, and its potential is always at the fixed point  $h_{\rm I} = w_{\rm IE} \left[ g_{\rm E}(h_{\rm E,1}) + g_{\rm E}(h_{\rm E,2}) \right]$ .
  - Since the gain function has a positive slope (higher input currents lead to higher firing rates),  $\gamma$  is a positive constant.
- Slide 34
  - These dynamics also hold for small unbiased inputs.
- Slide 35
  - A saddle point is an *unstable* equilibrium point.
- Slide 39
  - The stimulated neurons add a small amount of evidence for rightward motion, so they only change the total signal the brain uses to make its decision by a small amount. This is why microstimulation has a larger observable effect in near-zero motion strengths.
- Slide 41
  - Note that decisions that take longer are more accurate given some constant motion strength. If we allow the motion strength to vary, longer decision times will be associated with weaker motion strengths and will therefore be less accurate.
- Slide 42
  - The dotted circles are response fields.
- Slide 42
  - This figure charts firing rate vs. time only for neurons with a response field to the right (dotted circles) and only when the monkey makes a correct choice.
- Slide 50
  - The normalization factor  $\frac{1}{\mathbb{P}(x_1,x_2)}$  has been left out since we can normalize at the final stage.
  - The prior  $\mathbb{P}(s)$  has been left out in the graph since it's a uniform distribution.
- Slide 51
  - Refer to Ma (2021) problem 3.3 for a guide to deriving the product of two Gaussians.
- Slide 54

- Remember that the posterior variance is guaranteed to shrink *only if* the measurements are conditionally independent.
- Slide 57
  - In this setup a LR >1 or  $\log LR>0$  is evidence in favor of green.