

# Seminar 7

## ML, MAP and MMSE estimation

### DEDP

1. We want to estimate a robot's true position  $\Theta$  along a linear road.

We have one imprecise position sensor (e.g. GPS-like) which provides values affected by Gaussian noise  $\mathcal{N}(0, \sigma^2 = 2)$ .

We take one position reading from the sensor, and we obtain a position value  $r_1 = 40$  meters.

From previous measurements, we know that the robot is located somewhere around position 35 meters, the position having a Gaussian distribution  $\mathcal{N}(35, \sigma^2 = 2)$  (prior distribution).

- a. Estimate the true position using ML estimation
  - b. Estimate the true position using MAP estimation
  - c. Estimate the true position using MMSE estimators
2. Repeat Exercise 1, but instead of taking one position reading from the sensor, assume we take three separate readings, yielding positions  $r_1 = 40$ ,  $r_2 = 38.1$  and  $r_3 = 39.2$ 
    - a. Estimate again the true position using ML, MAP, MMSE estimation
    - b. Does the prior distribution have a stronger or a weaker influence now?

Another example, identical to exercise 1, but with different text and values:

1. We want to estimate today's temperature accurately.

We have one thermometer which provides imprecise values, affected by Gaussian noise  $\mathcal{N}(0, \sigma^2 = 2)$  (lousy thermometer).

We take one thermometer reading, with the value  $r_1 = 0$  degrees.

From historical data, we know that this time of the year the temperature is around  $-5$  degrees, being distributed with Gaussian distribution  $\mathcal{N}(-5, \sigma^2 = 2)$ .

- a. Estimate the true temperature using ML estimation
- b. Estimate the true temperature using MAP estimation
- c. Estimate the true temperature using MMSE estimators