Seminar 11

DEDP

1. Consider the ML estimation of a signal with the form

$$s_{\Theta}(t) = a \cdot t^2 + b \cdot t$$

with two unknowns $\Theta = [a, b]$, from 4 samples $\mathbf{r} = [0, 2.5, -3, 2]$ taken at time moments $\mathbf{t} = [0, 1, 2, 3]$. The noise is AWGN.

Perform 1 iteration of the Gradient Descent algorithm to estimate a and b, starting from the initial values $a_0 = 1$, $b_0 = 0.1$, with $\mu = 0.1$.

- 2. Consider the k-NN algorithm with the following training set, composed of 5 vectors of class A and another 5 vectors from class B:
 - Class A:

$$\mathbf{v}_1 = \begin{bmatrix} 2 \\ -4 \end{bmatrix} \ \mathbf{v}_2 = \begin{bmatrix} 1 \\ -5 \end{bmatrix} \ \mathbf{v}_3 = \begin{bmatrix} -2 \\ 6 \end{bmatrix} \ \mathbf{v}_4 = \begin{bmatrix} -3 \\ 4 \end{bmatrix} \ \mathbf{v}_5 = \begin{bmatrix} 2 \\ -5 \end{bmatrix}$$

• Class B:

$$\mathbf{v}_6 = \begin{bmatrix} 3\\1 \end{bmatrix} \ \mathbf{v}_7 = \begin{bmatrix} -1\\1 \end{bmatrix} \ \mathbf{v}_8 = \begin{bmatrix} -4\\-3 \end{bmatrix} \ \mathbf{v}_9 = \begin{bmatrix} -3\\0 \end{bmatrix} \ \mathbf{v}_{10} = \begin{bmatrix} -2\\3 \end{bmatrix}$$

Compute the class of the vector $\mathbf{x} = \begin{bmatrix} -2 \\ 5 \end{bmatrix}$ using the k-NN algorithm, with k=1, k=3, k=5, k=7 and k=9

3. Consider the following data

$$\mathbf{v} = \{v_i\} = [1.1, 0.9, 5.5, 0.6, 5, 6, 1.3, 4.8, 6, 0.8]$$

Use the k-Means algorithm to find the two centroids \mathbf{c}_1 and \mathbf{c}_2 , starting from two random values $\mathbf{c}_1 = 0.95$ and $\mathbf{c}_2 = 0.96$. Perform 5 iterations of the algorithm.

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