

# Laboratory Test

DSP 2020-2021

## Information

- The test will last for 1 hour
- You will upload the Matlab files on Moodle (or send by email)
- General Matlab stuff you need to know is listed in the **Syllabus** section. This is not an exhaustive list. There may be things I forgot to put in the list, but the basics are there.
- Template subjects (i.e. exercises extracted from the labs) are in **Template Subjects** section
- The test will be roughly based on these templates, with modifications

## Syllabus (not exhaustive)

- Define scalars, vectors, matrices
  - Generate constant vectors (zeros, ones, some value)
  - Generate sin and cos signals of a certain length, with various amplitude, frequencies and initial phase
  - Generate random numbers, vectors and matrices
  - Generate linearly spaced values between a start value and a stop value (e.g. `linspace()`)
- Concatenate vectors and matrices. Build longer signals from more parts.
- Access elements from vectors/matrices. Select rows or columns from matrices.
- Do basic mathematical operations with scalars, vectors, matrices
- Display a text message (`disp()` or `fprintf()`)

- Use simple instructions (if, for, while)
- Make plots
  - Plot a vector
  - Plot multiple signals on the same figure
  - Use subplots
- Operate with audio files (`.wav`, `.mp3`)
  - load a file
  - load only a certain part of a file (e.g. the first 5 seconds)
  - extract a single channel
  - play with the data, e.g. swap channels
- Operate with images
  - Create a simple grayscale or color image and display it
  - Load and display an image file. Also do simple adjustments (convert to grayscale, divide to 255).
  - Apply a simple filter to an image (e.g. a  $3 \times 3$  matrix with coefficients)
- Create and display a video based on a simple animation of an image (e.g. scrolling the image, change luminosity)
- Create and use Matlab functions
- Implement a system in a Matlab function, based on the equation
  - the function takes  $\mathbf{x}$  as input and outputs the result vector  $\mathbf{y}$
- Pass a function as argument to another function and use it inside
- Do convolutions of vectors with `conv()`
- Compute Fourier transform (DFT) of a vector, compute and display the modulus and the phase of the Fourier transform
- Implement a system in Simulink based on the equation
  - Also apply some input, visualize the output
  - Apply an impulse and visualize the impulse response
- Test linearity and time-invariance of systems in Simulink
- Design a low-pass/high-pass etc filter with `fdatool` and implement it in Simulink (Lab 11)
- Design an oscillator with a prescribed frequency, and implement it in Simulink (Lab 11)

# Template Subjects

## Lab 2

1. Plot on the same figure the signals  $\sin(2\pi ft + \frac{\pi}{4})$  and  $\cos(2\pi ft + \frac{\pi}{8})$  , with  $f = 0.3$  and  $t \in [0, 10]$ .
2. Load the audio file ‘Kalimba.mp3’ in the Matlab workspace. Only load samples between 1 and 200000 (to avoid out of memory error)
  - a. Play it through the computer’s audio device
  - b. Change the sampling frequency to half the correct value, and play again. How will the sound be changed?
  - c. Amplify the sound by multiplying the data by 4. Play the sound and observe the difference.
  - d. Swap the left and right channels (it’s a stereo file) and play the sound again.

## Lab 3 version 1

3. Create a color image representing the Romanian flag (3 stripes of blue, yellow, red). Create the image using the following steps: Create three matrices for the R, G, B components of the image Concatenate the three matrices across third dimension, into a 3D tensor

**Variant:** Make another simple flag or figure, color or grayscale, and show it

## Lab 3 version 2

1. Load the **Lena** image (use `imread()`), convert it to double, convert it to grayscale, scale the values to the  $[0, 1]$  range, and display the image (use `imshow()`).
2. Construct a new image based on the **Lena**, but in which each pixel value is set as a linear combination of the original pixels around it, as in the following equation:

$$\begin{aligned} y[i, j] = & \frac{1}{9}x[i-1, j-1] + \frac{1}{9}x[i-1, j] + \frac{1}{9}x[i-1, j+1] \\ & + \frac{1}{9}x[i, j-1] + \frac{1}{9}x[i, j] + \frac{1}{9}x[i, j+1] \\ & + \frac{1}{9}x[i+1, j-1] + \frac{1}{9}x[i+1, j] + \frac{1}{9}x[i+1, j+1] \end{aligned}$$

Ignore the first and last row/column, if needed.

Display the resulting image in a new window. How did it change?

## Lab 4

1. Load the **Lena** image (use `imread()`), convert it to a grayscale image, convert it to `double` type, adapt the values to the  $[0, 1]$  range, and display it (use `imshow()`).
2. Create a video sequence by scrolling the Lena image circularly to the right, by 3 pixels at every frame. Display the video at 25fps.

Code template for creating a video sequence in Matlab:

```
height = ...; % desired height
width  = ...; % desired width
NoF    = ...; % desired number of frames
% an array of size height x width x 1 x NoF:
video  = zeros(height, width, 1, NoF);
for i = 1:NoF
    video(:,:,i) = ... the frame number i ... ;
end

% Play the sequence
implay(video);
```

**Variant:** do another thing instead of scrolling, like change luminosity etc.

## Lab 5

1. Create a function `mysys1()` that implements the following system  $H_1$ :

$$y[n] = H_1\{x[n]\} = \frac{1}{4}x[n] - \frac{1}{2}x[n-1] + \frac{1}{4}x[n-2]$$

- the function takes 1 input argument **x** and outputs 1 result vector **y**
2. In a separate script, test the linearity of this system in the following way:
    - generate two random vectors **x** and **y** and two random numbers **a** and **b**
    - apply the function `mysys1()` to **a\*x**, **b\*y**, and **a\*x + b\*y**, and check if the results verify the linearity equation
    - display a message indicating if the system is linear or not linear

## Lab 6

1. Create a Simulink model to implement the following system  $H_1$ :

$$y[n] = H_1\{x[n]\} = \frac{1}{4}(x[n] + x[n-1] + x[n-2] + x[n-3])$$

- the system should be implemented as a Subsystem block with one input and one output signal
2. Visualize the impulse response of the system
    - add a unit impulse as the input (hint: can be created from two unit ramp blocks, delayed)
    - add a Scope at the output to visualize the data

## Lab 7 Variant 1

1. Create a Simulink model to implement the following system  $H_1$ :

$$y[n] = H_1\{x[n]\} = 0.8y[n-1] + 0.25x[n] + 0.1x[n-1]$$

- the system should be implemented as a Subsystem block with one input and one output signal
2. Test linearity of this system as follows:
    - create three copies of the system inside the model (copy/paste)
    - use two random input vectors  $\mathbf{x}$  and  $\mathbf{y}$  (use two *Random* blocks)
    - apply input signals  $\mathbf{x}$ ,  $\mathbf{y}$  and  $\mathbf{x}+\mathbf{y}$  to the three copies of the system
    - add the outputs of the systems which have  $\mathbf{x}$  and  $\mathbf{y}$  as inputs, then subtract the output of the system which has  $\mathbf{x} + \mathbf{y}$  as input
    - show the resulting signal. Is the system linear?

## Lab 7 Variant 2

Same thing, but test time invariance instead of linearity (Ex. 5):

- the system will be applied to an input vector  $\mathbf{x}$ , and to  $\mathbf{x}$  prepended with a variable number of zeros (i.e. time delayed)
- the outputs shall be checked if they verify the time invariance equation

## Lab 8

1. Load an audio signal and extract an 10 seconds long sequence of it.
  - a. Convolve the sequence with the impulse response  $\{1/6, 1/6, 1/6, 1/6, 1/6, 1/6\}$ . Play the resulting sequence.
  - b. Load another impulse response from the file “Scala Milan Opera Hall.wav” (use `audioread()`). Call the resulting vector **h**. Convolve the original audio signal with **h** and play the result.
  - c. Convolve the result from b) with another impulse response from the pack. Play the resulting signal.
  - d. Compute and display the equivalent impulse response of the complete system in points b) and c).

## Lab 9

1. Generate a 100 samples long signal **x** defined as  $x[n] = 0.7 \cos(2\pi f_1 n) + 1.2 \sin(2\pi f_2 n)$ , with  $f_1 = 0.05$  and  $f_2 = 0.1$ .
  - a. Plot the signal in the top third of a figure (use `subplot()`).
  - b. Compute the Fourier series coefficients with `fft()` and plot their magnitude in the middle third, and their phase in the lower third.
  - c. Repeat the plot but do the FFT in N=1000 points (use `fft(x, N)`). What changes?

## Lab 11 Variant 1

1. Use the Filter Design tool in Matlab (`fdatool`) to design a IIR high-pass filter with order 3, with cutoff frequency 0.07. Implement the filter in Simulink and then apply at the input the signal  $x[n] = \cos(2\pi 0.03n) + \cos(2\pi 0.18n)$  and visualize the output  $y[n]$ . Compare with the input signal.

## Lab 11 Variant 2

2. Use the Filter Design tool in Matlab (`fdatool`) to design an oscillator with frequency 0.05. Implement it in Simulink, visualize & play the output signal.

Use the following steps to design the oscillator:

1. design a system of order 2 with 2 conjugate poles placed **on the unit circle** at the correct frequency, and 2 zeros at low & high frequencies
2. implement the system in Simulink, **omitting the input signal** (not necessary)
3. set a non-zero initial condition in the system, to start-up the oscillator