

Source Coding Algorithms

Information Theory Exercises

1. We perform Shannon coding on an information source with $H(S) = 20\text{b}$.
 - a. What are the possible values for the efficiency of the code?
 - b. What are the possible values for the redundancy of the code?
 - c. What is the minimum number of messages the source may possibly have?
2. A discrete memoryless source has the following distribution:

$$S : \begin{pmatrix} s_1 & s_2 & s_3 & s_4 & s_5 \\ 0.05 & 0.4 & 0.1 & 0.25 & 0.2 \end{pmatrix}$$

- a. Encode the source with Shannon, Shannon-Fano coding and Huffman coding and compute the average length in every case.
 - b. Find the efficiency and redundancy of the Huffman code
 - c. Compute the probabilities of the symbols 0 and 1, for the Huffman code
3. For the following source, perform Huffman coding and obtain three different codes with same average length, but different individual codeword length.

$$S : \begin{pmatrix} s_1 & s_2 & s_3 & s_4 & s_5 & s_6 \\ 0.05 & 0.05 & 0.15 & 0.25 & 0.25 & 0.25 \end{pmatrix}$$

- a. Compute the average length in all three cases and show it is the same
4. A discrete memoryless source has the following distribution:

$$S : \begin{pmatrix} s_1 & s_2 & s_3 \\ 0.1 & 0.7 & 0.2 \end{pmatrix}$$

- a. Find the average code length obtained with Huffman coding on the original source and on its second order extension.
 - b. Encode the sequence $s_7s_7s_3s_7s_7s_7s_1s_3s_7s_7$ with both codes.
5. A discrete memoryless source has the following distribution

$$S : \begin{pmatrix} s_1 & s_2 & s_3 & s_4 & s_5 & s_6 & s_7 & s_8 \\ 0.4 & 0.3 & 0.2 & 0.04 & 0.03 & 0.02 & 0.009 & 0.001 \end{pmatrix}$$

Find the Huffman code for a code with 4 symbols, x_1 , x_2 , x_3 and x_4 , and encode the sequence

$$s_1 s_7 s_8 s_3 s_3 s_1$$