Exercises Week 4

Information Theory

- 1. For the first two exercises of last week, also compute the equivocation H(X|Y), the mutual information I(X,Y), and draw the geometrical representation.
- 2. A communication process has the following joint probability matrix:

$$P(x_i \cap y_j) = \begin{bmatrix} \frac{1}{2} & \frac{1}{4} \\ \frac{1}{8} & \frac{1}{8} \end{bmatrix}$$

- a. Find the channel matrix P(Y|X) and the equivocation matrix P(X|Y)
- b. Compute the average information obtained on the input X when output symbol y_2 is received
- c. Compute the uncertainty remaining over the input X when output symbol y_2 is received
- 3. At the input of a binary symmetric channel with the following channel matrix

$$P(y_j|x_i) = \begin{bmatrix} \frac{2}{3} & \frac{1}{3} \\ \frac{1}{3} & \frac{2}{3} \end{bmatrix}$$

we apply two inputs x_1 and x_2 with probabilities $p(x_1) = \frac{3}{4}$ and $p(x_2) = \frac{1}{4}$.

- a. Draw the graph of the channel
- b. Find H(X), H(Y) and I(X,Y)