Spectral estimation methods

Lab 11, SDP

Objective

Students should use some well-known spectral estimation methods and one of its applications.

Theoretical notions

Exercises

1. Find the average value and the autocorrelation function of the signal x[n] obtained as the output of an ARMA(1,1) random process with the following difference equation:

$$x[n] = \frac{1}{2}x[n-1] + w[n] + w[n-1],$$

where w[n] is white noise with variance σ_w^2 and average value 0.

2. The autocorrelation function of an AR random process x[n] is:

$$\gamma_{xx}[m] = \frac{1}{4}^{|m|}.$$

Find the difference equation of the random process x[n]. Is this unique? If not, find more than one possible solution.

3. In Matlab, create a signal of length N = 1000 defined as follows:

$$x[n] = \cos(2\pi f_1 n) + 0.5 \cdot \cos(2\pi f_2 n) + A \cdot noise$$

where $f_1 = 1000/44100$ and $f_2 = 1800/44100$, and the noise is random white gaussian noise (randn()).

Try different values of A (e.g. 0.1, 0.3).

- 4. Estimate the power spectral density of the signal x:
 - 1. Compute the Fourier transform X(f) (with fft()), and display $|X(f)|^2$
 - 2. Use the function periodogram()
 - 3. Split the signal in semnalul in 2, 4, or 10 segments of equal lengths, compute the periodogram of each one, and then average them. What are the differences?
 - 4. Use the Yule Walker method (pyulear).

Pay attention to:

- are the frequency peaks correctly located at f_1 and f_2 ?
- are the frequency peaks wide or narrow?
- is the noise spectrum flat or not?
- 5. In Matlab, create a script file which implements a live spectrum analyzer.
 - a. Load the signal music.wav with the function audioread().
 - b. Use the function buffer() to split the signal into windows of length 30ms.
 - c. Use periodogram() to estimate and plot, successively, the spectrum of each window signal.
 - d. Optional: localize and plot the dominant frequency from the spectrum of each window. Convert the frequency to the corresponding musical note and output it.

Final questions

1. TBD