

```

#fuzzy sets operations
'''
Implement Union, Intersection, Complement and Difference operations on fuzzy sets.
product of any two fuzzy sets and perform max-min composition on any two fuzzy rel
'''

#Here we define two sets young(x) and middleAged(x)

def student(x):
    if x<=20:
        return 1
    elif 20<x<=30:
        return (30-x)/(30-20)
    elif x>30:
        return 0

def doJob(x):
    if x>30:
        return 1
    elif x<=20:
        return 0
    elif 20<x<=30:
        return (x-20)/(10)

class Fuzzy:
    def __init__(self,item,membership):
        self.val = item
        self.membership = membership

    def return_membership(self):
        return self.membership

import random

x1 = random.sample(range(15, 40), 20)
x2 = x1

set1 = [] #student
set2 = [] #doJob

print(x1)
print(x2)

[15, 25, 26, 39, 30, 21, 37, 32, 38, 17, 16, 36, 28, 20, 27, 31, 29, 35, 19,
 [15, 25, 26, 39, 30, 21, 37, 32, 38, 17, 16, 36, 28, 20, 27, 31, 29, 35, 19,
for member in x1:

```

```

for member in x1:
    val = student(member)
    obj = Fuzzy(member,val)
    set1.append(obj)

for member in x2:
    val = doJob(member)
    obj = Fuzzy(member,val)
    set2.append(obj)

for obj in set1:
    print(obj.val,':',obj.membership)

print('=====')

for obj in set2:
    print(obj.val,':',obj.membership)

```

```

15 : 1
25 : 0.5
26 : 0.4
39 : 0
30 : 0.0
21 : 0.9
37 : 0
32 : 0
38 : 0
17 : 1
16 : 1
36 : 0
28 : 0.2
20 : 1
27 : 0.3
31 : 0
29 : 0.1
35 : 0
19 : 1
22 : 0.8
=====
15 : 0
25 : 0.5
26 : 0.6
39 : 1
30 : 1.0
21 : 0.1
37 : 1
32 : 1
38 : 1
17 : 0
16 : 0
36 : 1
28 : 0.8
20 : 0
27 : 0.7

```

```

31 : 1
29 : 0.9
35 : 1
19 : 0
22 : 0.2

```

```

student_x = []
student_y = []
for obj in set1:
    student_x.append(obj.val)
    student_y.append(obj.membership)
job_x=[]
job_y=[]
for obj in set2:
    job_x.append(obj.val)
    job_y.append(obj.membership)

print(student_x,student_y,job_x,job_y)

```

```

[15, 25, 26, 39, 30, 21, 37, 32, 38, 17, 16, 36, 28, 20, 27, 31, 29, 35, 19,

```



```

import numpy as np
import matplotlib.pyplot as plt

from scipy.interpolate import interp1d

x=np.array(student_x)
y=np.array(student_y)

x_new = np.linspace(x.min(), x.max(),500)

f = interp1d(x, y, kind='quadratic')
y_smooth=f(x_new)

#=====

x1=np.array(job_x)
y1=np.array(job_y)

x_new1 = np.linspace(x1.min(), x1.max(),500)

f1 = interp1d(x1, y1, kind='quadratic')
y_smooth1=f1(x_new1)

```

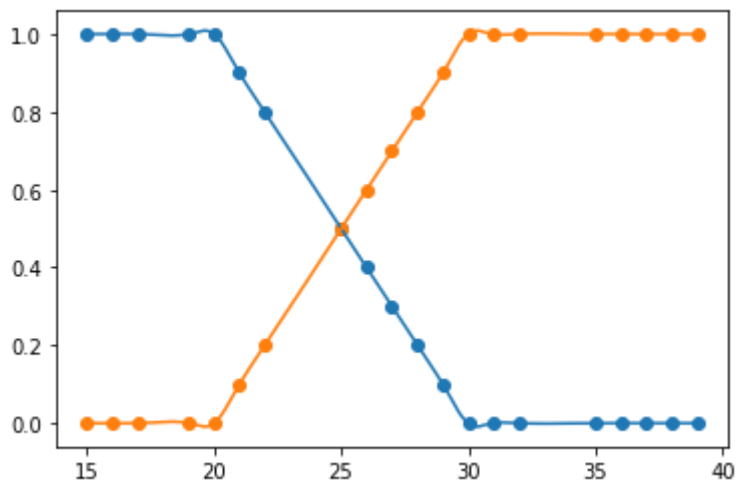
```

plt.plot (x_new,y_smooth)
plt.scatter (x, y)
plt.plot (x_new1,y_smooth1)
plt.scatter (x1, y1)

```

```
plt.scatter (x1, y1,
```

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```
#complement
#on set 1
import numpy as np
import matplotlib.pyplot as plt

from scipy.interpolate import interp1d

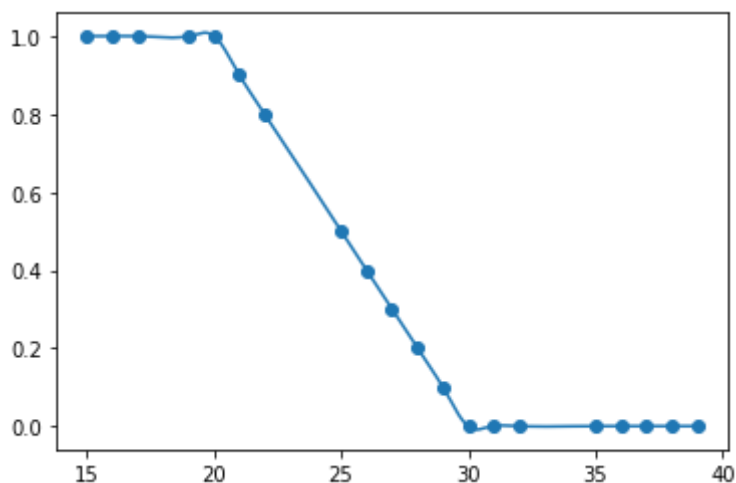
x=np.array(student_x)
y=np.array(student_y)

x_new = np.linspace(x.min(), x.max(),500)

f = interp1d(x, y, kind='quadratic')
y_smooth=f(x_new)

plt.plot (x_new,y_smooth)
plt.scatter (x, y)
```

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```
NOTset1 = []
for obj in set1:
```

```

for obj in SET1:
    new_obj = Fuzzy(obj.val,1- obj.membership)
    NOTset1.append(new_obj)

```

```

student_x1 = []
student_y1 = []
for obj in NOTset1:
    student_x1.append(obj.val)
    student_y1.append(obj.membership)

```

```

x_compli=np.array(student_x1)
y_compli=np.array(student_y1)

```

```

x_new_compli = np.linspace(x_compli.min(), x_compli.max(),500)

```

```

f2 = interp1d(x_compli, y_compli, kind='quadratic')
y_smooth_compli=f2(x_new_compli)

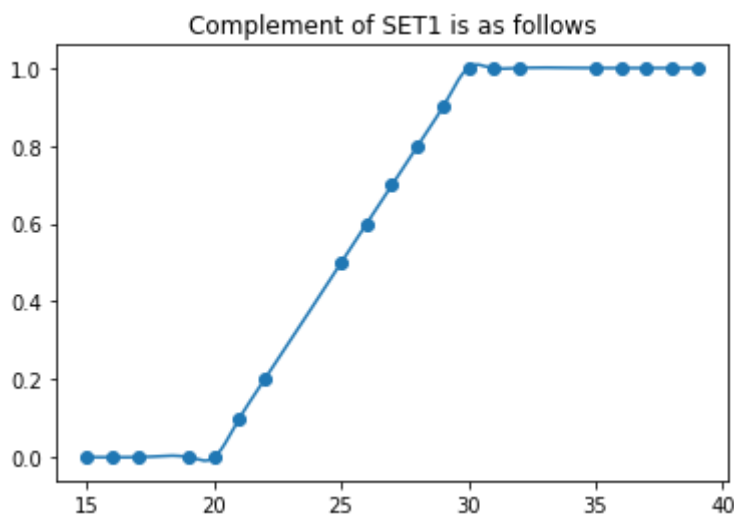
```

```

plt.plot (x_new_compli,y_smooth_compli)
plt.title('Complement of SET1 is as follows')
plt.scatter (x_compli, y_compli)

```

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```

x=np.array(student_x)
y=np.array(student_y)

```

```

x_new = np.linspace(x.min(), x.max(),500)

```

```

f = interp1d(x, y, kind='quadratic')
y_smooth=f(x_new)

```

```

plt.plot (x_new,y_smooth)
plt.scatter (x, y)

```

```

x_compli=np.array(student_x1)
y_compli=np.array(student_y1)

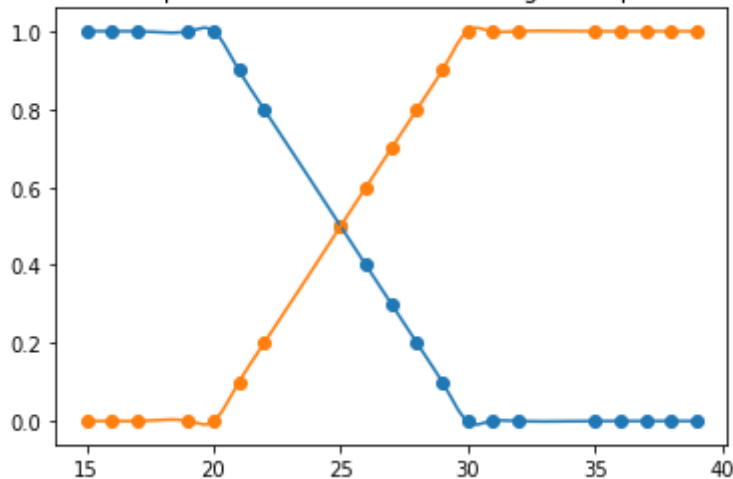
x_new_compli = np.linspace(x_compli.min(), x_compli.max(),500)

f2 = interp1d(x_compli, y_compli, kind='quadratic')
y_smooth_compli=f2(x_new_compli)
plt.title('Set and its Complement : blue: set1 and orange: complement of set1')
plt.plot (x_new_compli,y_smooth_compli)
plt.scatter (x_compli, y_compli)

```

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Set and its Complement : blue: set1 and orange: complement of set1



```

#union
import math
union = []
for obj1,obj2 in zip(set1,set2):
    new_obj = Fuzzy(obj1.val,max(obj1.membership,obj2.membership))
    union.append(new_obj)

```

```

Ux = []
Uy = []
for obj in union:
    Ux.append(obj.val)
    Uy.append(obj.membership)

```

```

x=np.array(Ux)
y=np.array(Uy)

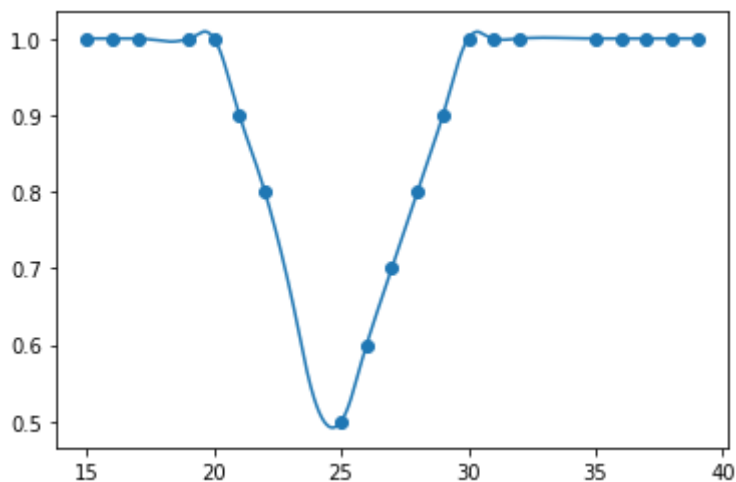
x_new = np.linspace(x.min(), x.max(),500)

f = interp1d(x, y, kind='quadratic')
y_smooth=f(x_new)

```

```
plt.plot (x_new,y_smooth)
plt.scatter (x, y)
```

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```
#intersection
intersection = []
for obj1,obj2 in zip(set1,set2):
    new_obj = Fuzzy(obj1.val,min(obj1.membership,obj2.membership))
    intersection.append(new_obj)
```

```
Ix = []
Iy = []
for obj in intersection:
    Ix.append(obj.val)
    Iy.append(obj.membership)
```

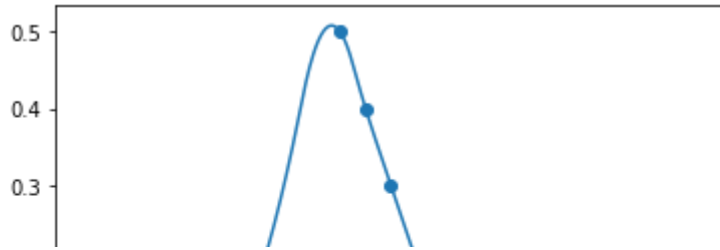
```
x=np.array(Ix)
y=np.array(Iy)
```

```
x_new = np.linspace(x.min(), x.max(),500)
```

```
f = interp1d(x, y, kind='quadratic')
y_smooth=f(x_new)
```

```
plt.plot (x_new,y_smooth)
plt.scatter (x, y)
```

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#difference

#difference of 2 sets F1 and F2 is

$F1 - F2 = F1 \text{ intersect } | - F2|$

set2 complement

NOTset2 = []

for obj in set2:

new_obj = Fuzzy(obj.val, 1- obj.membership)

NOTset2.append(new_obj)

intersection1 = []

for obj1,obj2 in zip(set1,NOTset2):

new_obj = Fuzzy(obj1.val, min(obj1.membership, obj2.membership))

intersection1.append(new_obj)

Ix1 = []

Iy1 = []

for obj in intersection1:

Ix1.append(obj.val)

Iy1.append(obj.membership)

x=np.array(Ix1)

y=np.array(Iy1)

x_new = np.linspace(x.min(), x.max(), 500)

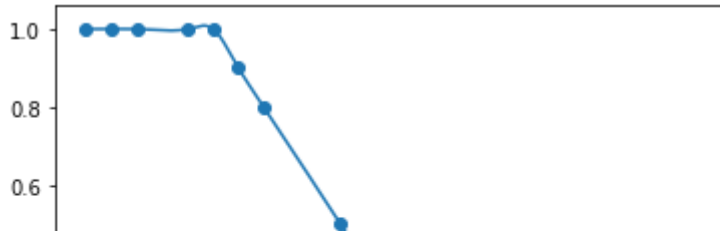
f = interp1d(x, y, kind='quadratic')

y_smooth=f(x_new)

plt.plot (x_new,y_smooth)

plt.scatter (x, y)

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MIN-MAX composition of 2 fuzzy relatons

'''

Let 2 relations be R and S and given as follows

'''

```
R = [
    [0.62,0.45,0.4],
    [0.12,0.1,0.34],
    [0.43,0.27,0.9]
]
```

```
S = [
    [0.11,0.33,0.98],
    [0.23,0.37,0.74],
    [0.6,0.5,0.19]
]
```

#min-max composition will be N*N matrix where N is dimension of both R and S

N = 3

min_max = []

```
for i in range(N):
    List = []
    for j in range(N):
        #ith row and jth column
        I = R[i]
        new = []
        for k in range(N):
            new.append(min(I[k],S[k][j]))
        List.append(max(new))
    min_max.append(List)
```

```
print('R : ')
for i in range(N):
    for j in range(N):
        print(R[i][j], ' ',end='')
    print()
```

```
print('=====')
```

```
print('S:')
for i in range(N):
```

```
    for j in range(N):
        print(S[i][j], ' ', end= ' ')
    print()

print('=====MIN-MAX COMPOSITION IS: =====')
for i in range(N):
    for j in range(N):
        print(min_max[i][j], ' ', end= '')
    print()
```

```
R :
0.62  0.45  0.4
0.12  0.1   0
0.43  0.27  0.9
=====
S:
0.11   0.33   0.98
0.23   0.37   0.74
0.6    0.5    0.19
=====MIN-MAX COMPOSITION IS: =====
0.4   0.4   0.62
0.11  0.12  0.12
0.6   0.5   0.43
```