Chapter-4 Multiple Correlation and Regression

Multiple Correlation: - In multiple correlation we study about the association (or relation) between three or more than three variables.

Let x_1, x_2 and x_3 be three variables where x_3 is dependent variable and x_2 of x_3 are independent variable. The correlation coefficient between dependent variable x_1 and joint effect of independent variable x_2 and x_3 is called x_4 multiple correlation coefficient between x_4 and x_5 is called x_4 and x_5 and it is denoted by x_4 .

Also denoted by R2.13 -> If x2 is dependent variable and x fix3 are independent variables.

R3.12 > If x3 18 dependent variable and x1 4x2 are independent variables.

Multiple Correlation 48 given by $R_{1.23} = \sqrt{\frac{\gamma_1^2 + \gamma_3^2 - 2\gamma_2\gamma_3}{1 - \gamma_{23}^2}} = \sqrt{\frac{\gamma_1^2 + \gamma_3^2 - 2\gamma_2\gamma_3}{1 - \gamma_{23}^2}}$

Similarly for R2.13 and R3.12.

For two variables

Correlation coefficient $Y = n\Xi XY - \Xi X \cdot \Xi Y$ $\sqrt{n\Xi X^2 - \Xi X}^2 \sqrt{n\Xi Y^2 - (\Xi Y)^2}$

Properties of multiple Correlation Coefficient:

1) Multiple correlation coefficient lies between 0 to 1

vies 0 \le R_{1.23} \le 1

· O \le R_{2.13} \le 1

O \le R_{3.12} \le 1

99) Here, $R_{1.23} = R_{1.32}$ $R_{2.13} = R_{2.31}$ $R_{3.12} = R_{3.21}$

(i.e., Correlation between x andy 48 stmiler) to correlation between y and x

Coefficient of Multiple determination: Coefficient of multiple determination 48 the square of coefficient of multiple correlation so, R223, R2.13 and R312 are the coefficients of multiple determination. het R1.23=0.9 then, coefficient of multiple determination (R1.23) = (0.9) Interpretation of (R223) - This means total variation on dependent variable of 18 81% that is explained by independ variables x2 and x3 and remaining (100-81) =19% variation on depending variable is due to the effect of other independent variables other than x and x3. Numerical Problems: Q1. If M2 = 0.6, r13=0.4, r23=0.35 then, 1 Find the multiple correlation coefficient between is and joint effect of x2 and x3. (P) Find the multiple correlation coefficient between x and joint effect of x and x3. Solution Given, 712 = 0.6 Y13=0.4 Y23=0.35 1 Here, Multiple correlation coefficient between a and joint effect of x2 and 23 48 R1.23 = \[\frac{72}{52} + \frac{72}{13} - 2\tau_{12} \gamma_{13} \frac{72}{23} $= \sqrt{\frac{(0.6)^2 + (0.4)^2 - 2 \times 0.6 \times 0.4 \times 0.35}{1 - (0.35)^2}}$ = 0.63@ Multiple correlation coefficient between x and goint effect of $2c_1$ and $2c_3$ +8 R_2 , $13 = \sqrt{\frac{2}{12} + 7_{23}^2 - 2r_{12}r_{23}r_{13}}$ $\frac{1 - 7_{13}^2}{1 - 7_{13}^2}$ $= (0.6)^2 + (0.35)^2 - 2 \times 0.6 \times 0.4$ =0.003

1-(0.4)2

Nate: If (R1.23 OR R2.13 OR R3.12) > 1 then Traing and no are inconsistent. 92. A sample of 10 values of three variables x1, x2 and x3 were $\leq x_2 x_3 = 64$, $\leq x_1^2 = 20$, $\leq x_2^2 = 68$, $\leq x_3^2 = 170$. 1) Find the partial correlation coefficient between x and x3 eliminating for Find the multiple correlation coefficient of & with x and x3. Solution, Here, $r_{12} = \frac{n \leq x_1 x_2 - \leq x_1 \leq x_2}{n \leq x_1 - (\leq x_1)^2} \sqrt{n \leq x_2 - (\leq x_2)^2}$ = 10×10-10×20 10x20-100 10x68-400 = -0.5913 = n & 23 23 - Ex. & 23 \n\x\2-(\x\x\)^2\n\x\x\2-(\x\x\)^2 $= \frac{10 \times 15 - 10 \times 30}{\sqrt{10 \times 20 - (10)^2} \sqrt{10 \times 170 - (30)^2}}$ -0.53 723= n を 323- を 32を 3 n Ex2 (Ex)2 / n Ex32 (Ex32) $= 10 \times 64 - 20 \times 30$ $\sqrt{10\times68-(20)^2}\sqrt{10\times170-(30)^2}$ = 0.085 of Partial correlation coefficient between x and x2 eliminating the effect of x2 98 73.2 = 713-722732 1-72 1-72 $= (-0.53) - (0.598) \times 0.085$ 11-(-0.598)2 11-(0.085)2

= 0.729

i) Multiple correlation coefficient of x with x 2 and x 18,

$$R_{1.23} = \sqrt{\frac{\gamma_{12}^{2} + \gamma_{13}^{2} - 2\gamma_{13}\gamma_{23}}{1 - \gamma_{23}^{2}}}$$

$$= \sqrt{\frac{(-0.598)^{2} + (-0.53)^{2} - 2 \times (-0.598) \times (-0.53) \times 0.085}{1 - (0.085)^{2}}}$$

$$= 0.767$$

Partial Correlation Coefficient:

Let x_1, x_2 and x_3 are three variables then partial correlation coefficient between x_1 and x_2 when x_3 is taken as constant is given denoted by $R_{12,3}$ and given as:

$$\gamma_{12.3} = \frac{\gamma_{12} - \gamma_{13}, \gamma_{23}}{\sqrt{1 - \gamma_{13}^2} \sqrt{1 - \gamma_{23}^2}}$$

Similarly for 13.2 and 723.1

Properties:

is Partial correlation coefficient lies between -1 to +1. i.e., $-1 \le r_{12,3} \le +1$ $-1 \le r_{12,3} \le +1$

$$-1 \le r_{13,2} \le +1$$

 $-1 \le r_{23,1} \le +1$

ii) Here, $\gamma_{21.3} = \gamma_{12.3}$ $\gamma_{31.2} = \gamma_{13.2}$

732.1 = 723.1

Coefficient of partial determination: Coefficient of partial determination 18 the square of coefficient of partial correlation. So, 7,2,3,72,3 and 7,23,1 are the coefficient of partial determination.

Interpretation > Let coefficient of partial correlation (Tis.2) = 0.8

Then coefficient of partial determination is (Tis.2) = (0.8)² = 0.64

This means the total variation on dependent variable is 64% that is explained by independent variable is when the independent variable is a constant and remaining 36% variation on its due to the effect of other independent variation.

93. From the data given below find 72.3, R1.23, 723.1 and R2.13 \(\mathbb{x}_1 \mathbb{x}_2 = 40, \(\mathbb{Z}_1 \mathbb{x}_3 = 55, \mathbb{Z}_2 \mathbb{x}_2 = 35\) $\leq x_1^2 = 90, \leq x_2^2 = 60, \leq x_3^2 = 50$ where on, on and on are variables measured from Solution Given, \(\zexix_2 = 40\), \(\zexix_3 = 55\), \(\zexix_3 = 35\). \(\mathbb{Z}\mathbb{X}^2 = 90, \mathbb{Z}\mathbb{X}^2 = 60, \mathbb{Z}\mathbb{X}^2_3 = 50 Rough Since, x1, x2 and x3 are measured from their we know that

So,
$$Y_{12} = \frac{2}{\sqrt{2}} \frac{x_1 x_2}{\sqrt{2}}$$

$$= \frac{40}{\sqrt{90}\sqrt{60}}$$

$$= 0.54$$

Now,
$$\gamma_{12.3} = \frac{\gamma_{12} - \gamma_{13}\gamma_{23}}{\sqrt{1 - \gamma_{13}^2}}$$

$$= \frac{0.54 - 0.639 \times 0.819}{\sqrt{1 - (0.639)^2} \sqrt{1 - (0.819)^2}}$$

$$= \frac{0.038}{\sqrt{1 - (0.639)^2} \sqrt{1 - (0.819)^2}}$$

T= Cov(X,Y) ox ox $=\frac{1}{n} \leq (x-\overline{x}) (Y-\overline{Y})$ 清を(x-X)2 まを(Y-Y)2 = E(x-x)(Y-V) Z(X-X)2 Z(Y-Y)2 = Zxy 2 /2x2 /2y2

Check the answers ornor maybe in ans while using calculator consider them as normal errors and correct yourself.

$$R_{1.23} = \sqrt{\frac{\gamma_{12}^2 + \gamma_{13}^2 - 2\gamma_{12}\gamma_{13}\gamma_{23}}{1 - \gamma_{23}^2}}$$

$$= \sqrt{\frac{(0.54)^2 + (0.639)^2 - 2\times 0.54\times 0.639\times 0.819}{1 - (0.819)^2}}$$

$$= 0.64$$

$$\gamma_{23,1} = \gamma_{23} - \gamma_{12} \cdot \gamma_{13}
= 0.819 - 0.54 \times 0.639
\sqrt{1 - (0.54)^2} \sqrt{1 - (0.639)^2}
= 0.73$$

$$R_{2.13} = \sqrt{\gamma_{12}^2 + \gamma_{23}^2 - 2\gamma_{12} \cdot \gamma_{23} \cdot \gamma_{13}}
- \sqrt{1 - (0.54)^2 + (0.819)^2 - 2 \times 0.54 \times 0.819 \times 0.639}
= \sqrt{(0.54)^2 + (0.819)^2 - 2 \times 0.54 \times 0.819 \times 0.639}
1 - (0.639)^2$$

94 From the information given below calculate 1,2.3, 1,3.2 and 1,2.3.1

24	6	8	9	111	12	14	
x_2	14	16	17	18	20	23	
23	21	22	27	29 1	31	32	

Soln

= 0.82

24	\propto_2	203	u=x=1			u2	1/22	W2	luv	luw	vw
6	14	21	-3	-3	$\frac{7}{-8} = \frac{2}{3} = \frac{29}{3}$	9	9	64	9	24	24
8	16	22	-1	-1		1					
9	17	27	0	0	-7	1	1	49	1	7	7
11	18	29	2	1	-2 0	0	0	4	0	0	0
12	20	31	3	3		4	1	0	2	0	0
14		-0			2	9	9	4	9	6	6
		32	5	6	3	25	36	9	30	15	18
			≤u=6	€10=6	≤w=12	242= 48	2v2=	Zw2	ZUV	=52	ZVW

Now,

$$Y_{12.3} = Y_{12} - Y_{13} \cdot Y_{23}$$

 $\sqrt{1 - Y_{13}^2} \sqrt{1 - Y_{23}^2}$
 $= \frac{0.98 - 0.95 \times 0.92}{\sqrt{1 - (0.95)^2} \sqrt{1 - (0.92)^2}}$
 $= 0.87$

$$\gamma_{13.2} = \gamma_{13} - \gamma_{12} \gamma_{23}$$

$$\sqrt{1 - \gamma_{12}^{2}} \sqrt{1 - \gamma_{23}^{2}}$$

$$= 0.95 - 0.98 \times 0.92$$

$$\sqrt{1 - (0.98)^{2}} \sqrt{1 - (0.92)^{2}}$$

$$= 0.65$$

$$\gamma_{23.1} = \gamma_{23} - \gamma_{12} \cdot \gamma_{13} \\
\sqrt{1 - \gamma_{12}^2} \sqrt{1 - \gamma_{13}^2} \\
= \frac{0.92 - 0.98 \times 0.95}{\sqrt{1 - (0.98)^2} \sqrt{1 - (0.95)^2}} \\
= 0.45$$

= -0.18

= -0.16

3.5. Are the following data consistent;

Y23 = 0.8, Y31 = -0.5, Y12 = 0.6.

For testing it is consistency we need to find multiple

correlation coefficient R1.23. (We take R1.23, also we can take R2.13 or R3.12)

for testing

Now,
$$R_{1.23} = \sqrt{\frac{\gamma_{12}^2 + \gamma_{13}^2 - 2\gamma_{12} \cdot \gamma_{13} \cdot \gamma_{23}}{1 - \gamma_{23}^2}}$$

$$= \sqrt{\frac{(0.6)^2 + (-0.5)^2 - 2 \times 0.6 \times (-0.5) \times 0.8}{1 - (0.8)^2}}$$

= 1.118

Since R1.23 ± 1.118 > 1. (Not in the range of 0 to 1). So, the data are inconsistent.

Multiple Regression: Multiple Regression 48 the functional relationship

Non mighles where one variable between three or more than three variables where one variable is dependent and remaining are independent variable. By the use of regression model we can be able to estimate the value of dependent variable with the last of dependent variables. of dependent variable with the help of independent variable. dependent and X_2 and X_3 are three variables, of X_1 18 represent and X_2 and X_3 are independent then, the multiple regression equation es, $_{7}X_{1} = a + b_{1}X_{2} + b_{2}X_{3}$ also we carface)
take y in place) where, a -> ×1 Intercept b_+regression coeff. of x1 on X2 when X3 is taken as constant. b2+ regression coeff. of x3 on x3 when X3 is taken as constant. For finding the values of a, b, and b, we have, By using least square method the normal equations are $\leq x_1 = na + b_1 \leq x_2 + b_2 \leq x_3 - m$ On Multiplying both sides by X2 of egn® = X1X2 = a = X2 + b1 = X2 + b2 = X2X3 - (1) On multiplying both sides by X3 of egn @ ZX1X3=aZX3+b1ZX2X3+b2ZX3-10.

solving these three equations (P), (P) and (P) we get the value of a, b, & b, Finally substituting values of a, b, & b, m eqn (P) we get the solution.

9.N6 The table shows the corresponding values of the three, variables X1, X2 and X3.
X1: 5 7 8 6 10 9

X2: 12 20 30 40 33 25

X3: 51 55 58 60 70 66

Find the regression equation of X1 on X2 and X3. Estimate,

X1 when X2=50 and X3=100. Where X1 represents pull length,

X2 represents wire length and X3 represents die height.

Since X1 depends upon X2 & X3 so, the multiple regression equation 48; also we can write to in place of a X1 = a+b1X2+b2X3—P

For finding the value of a, b, and b, we have the following normal equations,

 $\Xi X_1 = na + b_1 \Xi X_2 + b_2 \Xi X_3 - P$ $\Xi X_1 X_2 = a \Xi X_2 + b_1 \Xi X_2^2 + b_2 \Xi X_2 X_3 - P$ $\Xi X_1 X_3 = a \Xi X_3 + b_1 \Xi X_2 X_3 + b_2 \Xi X_3^2 - P$

for the calculation of ZX1, ZX2, ZX3, ZX2, ZX3, ZX3, ZX2, ZX3, ZX1X3, ZX1X3, We proceed as following table.

1	X1	X2	X3	X2	X32	X_1X_2	X1X3	X2X3
	5	12	51	144	2601	60	255	612
-	7	20	55	400	3025	140	385	1100
	8	30'	58	900	3364	240	464	1740
	6	40	60	1600	3600	240.	360	2400
-	10	33	70	1089	4900	330	700	2310
	9	25	66	625	4356	225	594	1650
NA L	EX1=45	£X2=160	£X3=360	£X2=4758	2X3=21846	2×1×2=1235	£ X4X3=2758	£X ₂ X ₃ =9812

Now, we put the values of \$\(X_1, \)\(X_2, \)\(X_3, \)\(X_2^2, \)\(X_3^2, \)\(X_3^2, \)\(X_4^2, \) \$\times_1 \times_2 \times_3, \times_1 \times_3 \tand n and n an an an and m 6a + 160 b + 360 b = 45 - 0. 160a + 4758b1+9812b2 = 1235 - VP 360a +9812b2+21846b2 = 2758 - (18). Using Cramer's Rule (OR, we can find a , b2 , b2 by directly solving equations). Coefficient of a coefficient of b1 coefficient of b2 constant

6
160
4758
9812
1035 360 9812 21846 2758 Now, $D = \begin{vmatrix} 6 & 160 & 360 \\ 160 & 4758 & 9812 \\ 360 & 9812 & 21846 \end{vmatrix}$ =6(103943268-96275344)-160(3495360-3532320) + 360 (1569920-1712880) Similarly $D_1 = \begin{vmatrix} 45 & 160 & 360 \\ 1235 & 4758 & 9812 \\ 2758 & 9812 & 21846 \end{vmatrix}$ = 45(103943268-96275344)-160(26979810-27081496) +360(12117820-13122564) = -3581500 $D_2 = \begin{vmatrix} 6 & 45 & 360 \\ 160 & 1235 & 9812 \\ 360 & 2758 & 21846 \end{vmatrix}$ = 6 (26979810-27061496)-45(3495360-3532320) +360(441280-444600)

=-22116

$$\mathcal{D}_3 = \begin{vmatrix} 6 & 160 & 45 \\ 160 & 4758 & 1235 \\ 360 & 9812 & 2758 \end{vmatrix}$$

= 6(13122564 - 12117820) - 160(441280 - 444600) + 45(1569920 - 1712880) = 126464

Here,
$$a = \frac{D_1}{D} = \frac{-3581500}{4.55544} = -7.862$$

$$b_1 = \frac{D_2}{D} = \frac{-22116}{4.55544} = -0.048$$

$$b_2 = \frac{D_3}{D} = \frac{126464}{4.55544} = 0.277$$

Now putting values of a, b_1 & b_2 on (3) we get regression equation of X_1 on X_2 and X_3 as;

 $X_1 = -7.862 - 0.048 \times_2 + 0.277 \times_3$

Again,
$$X_1$$
 when $X_2 = 50$ and $X_3 = 100$ 48, $X_1 = -7.862 - 0.048 \times 50 + 0.277 \times 100$ $= -7.862 - 2.4 + 27.7$ $= 27.7 - 10.262$ $= 17.438$

@ Measure of variation:

To tal variation (Total sum of square) = explained variation (sum of square due to regression) + unexplained variation (sum of square due to errors.)

or We can write

or SSR=TSS-SSE

where, $TSS = \Xi (Y - \overline{Y})^2$ $= \Xi Y^2 - n \overline{Y}^2$ $4 SSE = \Xi (Y - \widehat{Y})^2$ denived from

Y= bot bo X1+bo X2

Y= bot bo X1+bo X2

bo Z1-bo Z1X-bo Z1X

= = = 12-6=1-6=1Xy-6=2YX2

@ Coefficient of Determination:

Coefficient of determination is also determined

as
$$(R^2) = \frac{SSR}{TSS}$$

or, $R^2 = \frac{TSS - SSE}{TSS}$ (": SSR= TSS-SSE)
or, $R^2 = 1 - \frac{SSE}{TSS}$

Interpretation: - Coefficient of determination that measures the total variation on dependent variable explained by Independent variable.

€. Standard From of Estimate (S.E):

Standard error of estimate (S.E) = $\int SSE$ N-k-1where, n=n0, of observations. k=n0, of mdependent variable.

Q.N.7 From following Information of variables X1, X2 and X3 $\leq X_1 = 13$, $\leq X_2 = 11$, $\leq X_3 = 51$, $\leq X_1^2 = 63$, $\leq X_2^2 = 95$, $\leq X_1 X_3 = 77$, $\Sigma X_2 X_3 = 136$, $\Sigma X_1 X_2 = -240$, $\Sigma X_3^2 = 450$, n = 10. 1) Find the regression equation of X3 on X1 and X2 and interpret the regression coefficients. 10) Redict X3 when X1=1 and X2=4. 1817 Compute TSS, SSR and SSE. my Compute standard error of estimate. v) Compute the coefficient of multiple determination and interpret. Solution:
Given, The regression equation of X3 on X1 and X2 13 For finding bo, be dibe we need to solve the following normal equations: 51 X3 = nbo+b1 51 X1 + b2 51 X2 - 10 至X1X3=b0至X1+b1至X1+b2至X1X2一個 = X2X3 = 60 = X2+ 61 = X1X2+ 62 = X2-Now, putting the given values in egn (1), (11) and (12), $10b_0 + 13b_1 + 11b_2 = 51$ 13bo +63b1-240b2=77 £ 1160 - 24061+9562=136 Using Cramers Rule Coeff.b2 Coeff. bo Coeff. b1 Constants -240 77 -240 95 136. 10 13 11 13 63 -240 =10(5985-57600)-13(1235+2640)+11(-3120-693)

of X_3 on X_1 and X_2 as: $X_3 = 5.7 - 0.348 X_1 - 0.105 X_2$.

17) x_3 when $x_1 = 1$ and $x_2 = 4.48$; $x_3 = 5.7 - 0.348 \times 1 - 0.105 \times 4$ = 4.932 1) ((ontinue) part: Interpretation -> Since, b_=-0.348, this means the value of dependent variable 18 decreased by -0.348 as per unit change in the value of X1 and b2=-0.205, this means value of independent variable is decreased by -0.105 as per unit change in value of X2.

TSS=ZIX3-nX3 $\left(: \overline{X}_3^2 = \underline{X_3^2} \right)$ $=450-10\times(8.82)^{2}$ =450-778.5467= -328.5467

> SSE = \$\frac{1}{3} - b_0 \frac{1}{2} \text{X}_3 - b_1 \frac{1}{2} \text{X}_3 \text{X}_1 - b_2 \frac{1}{2} \text{X}_3 \text{X}_2 $=450-5.66\times51+0.348\times77+0.105\times136$ = 450-288.66+26.796+14.28 = 202.416

& SSR = TSS-SSE = -328.5467 - 202.416=-530.9627

iv) Standard error of estimate (S.F) = \ \ \frac{55E}{n-k-1} $=\sqrt{\frac{202.416}{10-2-1}}$ =5.377

v> coefficient of multiple determination 48 given by, This question is from q. N.20

 $\left(R_{3,12}\right)^2 = \frac{SSR}{TSS}$ $= -\frac{530.9627}{-328.5467}$

The Question All value wrong that the grand th = 1.616 \ Interpretation > It means _ 1 of total variation on dependent variable X3 is explained by independent variable X2 dix2.

यो १ मन्दी सीनी

@ Significance lest of regression Coefficient: Florder] 9.No.8: Given the following information from a multiple regression analysis; n=20, b1=4, b2=3, Sb1=1.2, Sb2=0.8. At 0.05 level of significance, determine whether each of explanatory (dependent) variable makes a significant contribution to the regression model. Soly Given, 61=4 b2 = 3 (i.e, standard, error of b2) $Sb_1 = 1.2$ level of significance = < = 0.05. Problem to Lest: Null hypothesis (Ho); 1=0 i.e. there is no linear relationship between dependent variable Yand independent variable X1. Alternative hypothesis (H1); \$ \$ = 0 rie, there is linear relationship Test statistics: $t_{cal} = \frac{b_1}{5b_1} = \frac{4}{1.2} = 3.33$ between dependent variable Y and independent variable X1. Critical value— the tabulated value of 't' at 0.05 level of significant with n-k-1 degree of freedom 48 (to.05, 20-2-1) - value of to.05,17 $= t_{0.05}, 17$ = 2.110 from table given back of book in page no 318 Decision: Since true =3.33 > tab= 2.110 So, Ho 48 rejected ing H1 48 accepted.

Conclusion - Hence, there is linear relation between dependent variable Y of independent variable X1.

Note: - We have done for X1, Similarly we can do same for X2.

Q.N.9: In order to establish the functional relationship between anual salaries (y), years of educated high school (x1) and years of experience, with the form (22), data on these three variables were collected from a random sample of 10 persons working on a large firm. Analysis of data produces the following results. The sum of squares $\leq (y-y)^2 = 397.6.5$ um of squares due to error $\Xi(Y-\hat{Y})^{1/2} = 23.5$. Test the overall significance of regression coefficients at 5% level of significance. We have, regression model, Y=b_+b_1 X_1+b_2 X_2. $\leq (Y-\overline{Y})^2 = TSS = 397.6$ $\Xi (Y-V)^2 = SSE = 235$ So, SSR=TSS-SSE = 397.6-235 Problem to fest: = 374.1. Null hypothesis (Ho); $\beta_1 = \beta_2 = 0$. Ties there 48 no linear relationship between dependent variable Y and independent variables X_1 & X_2 . Alternative hypothesis (H1); $\beta_1 \neq \beta_2 \neq 0$. 4ie, there is linear

Test Statistics:

Feat = MSR Question III overall word 3117

The feat method at II state in the state of t

where, MSR -> Mean square due to regression.

MSE -> Mean square due to error.

and MSR = SSR

defree of freedom (d.f)

MSF = SSE

d.f

Now, we construct ANOVA table for regression analysis;

The second secon	1			
Source of Variation	degree of freedom	Sum of Square	MSS	Feal.
Regression	F=2	SSR=374,1	$MSR = \frac{SSR}{d_1f}$ $= \frac{374.1}{2}$	$F_{cal} = \frac{MSR}{MSE}$ $= 187.05$
Error	n-F-1=7	SSE= 23.5	= 187.05 $MSE = 23.5$ 7	3,35
T. 1. 1.	m-1	TSS=397. 6	=3,35	
Total	= 10-1	SSR+SSE	3 '	

Critical valve—the tabulated value of Fat 0.05 level of significance with (2,7) d.f 18 fo.05 (2,7).

= 4.74 from table given in book given in book given in book given in book given in book

Decision → Since fcal = 55.835 The Fab = 4.74 So, Ho 18 rejected.

4.8 H1 18 accepted.

Equalsto or smaller

3117 accept 506

Conclusion -> Hence we can conclude that there is linear relationship between Yand independent variables.