

Classification

When we have Balanced Dataset  $\rightarrow$  Go for Accuracy  
else  $\rightarrow$  Precision, Recall or F1 score !!!

For Binary Classification

## (1) Confusion Matrix

$$\text{FP rate} := \frac{FP}{FP + TN}$$

$$\text{FN rate} := \frac{FN}{FN + TN}$$

I	O
TP	FP
FN	TN

Type I error  
Type II error

$$\text{FN rate} := \frac{FN}{FN + TP}$$

Now Since we have a balanced dataset,

$$\text{Accuracy} := \frac{TP + TN}{TP + TN + FP + FN}$$

Consider that we have an unbalanced dataset as following

$\{ A : 90\% \}$  +  $\{ B : 10\% \}$  Now let's assume the model classify everything into class A, then by default it'll have a 90% accuracy.

## (2) Precision &amp; (Sensitivity)

## Recall (Specificity)

$$\text{Precision} := \frac{TP}{TP + FP}$$

I	O
TP	FP
FN	TN

Precision

$$\text{Recall} := \frac{TP}{TP + FN}$$

The choice of Precision or Recall depends on your problem statement.

Eg: Spam Detection: Need Precision

FP is very bad in this case

Corona Detection: Need Recall

False Negative could be lethal in this.

$$F_{Beta} = \frac{(1 + \beta^2)(P \times R)}{\beta^2 \times (P + R)}$$

$$\beta = 1, H = \frac{2PR}{P+R} \Rightarrow \frac{1}{\frac{1}{P} + \frac{1}{R}}$$

(When both false positive & false negatives are important)

if false negative impact is high, increase  $\beta$  if false positive impact is high decrease  $\beta$

$$\beta \uparrow \quad \beta \downarrow$$

## (3) AUC &amp; ROC

$$y \quad \hat{y}_{prob} \quad \Delta(\hat{y})_{\Delta=0} \quad \Delta(\hat{y})_{\Delta=0.2} \quad \Delta(\hat{y})_{\Delta=0.3}$$

$$1 \quad .8 \quad 1 \quad 1 \quad 1$$

$$0 \quad .96 \quad 1 \quad 1 \quad 1$$

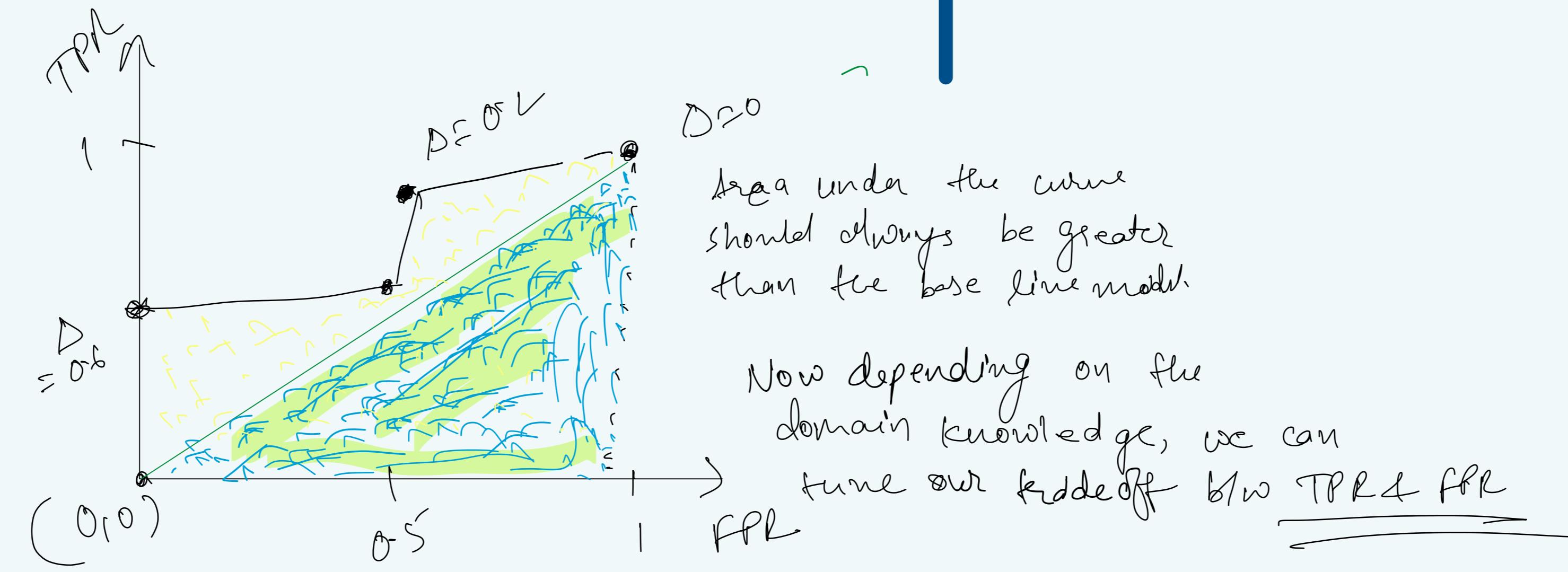
$$1 \quad .04 \quad 1 \quad 1 \quad 1$$

$$1 \quad .03 \quad 1 \quad 1 \quad 1$$

$$0 \quad .02 \quad 1 \quad 0 \quad 1$$

$$1 \quad .01 \quad 1 \quad 1 \quad 1$$

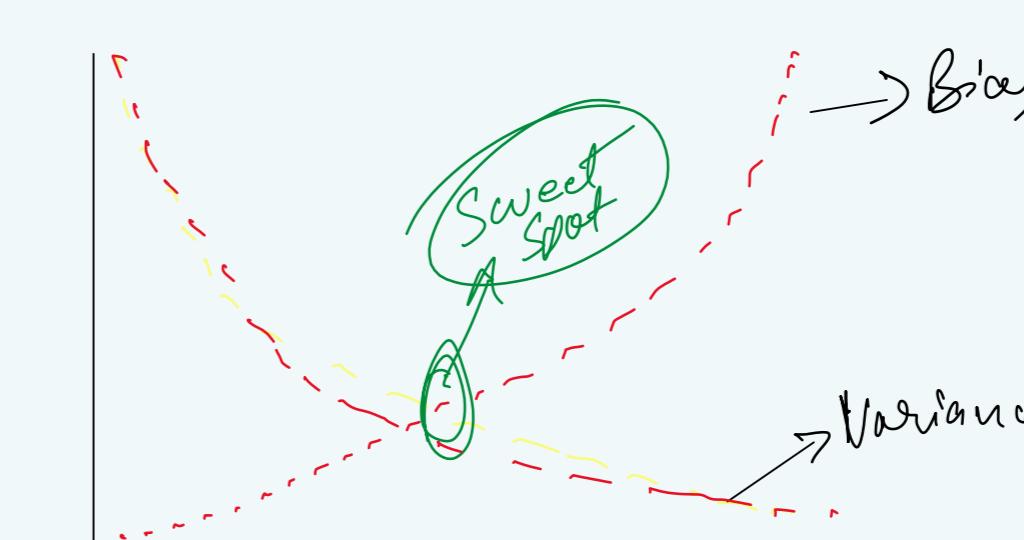
$$\left\{ \begin{array}{l} TPR = \frac{TP}{TP + FN} \\ FPR = \frac{FP}{FP + TN} \end{array} \right\}$$

The Bias - Variance Tradeoff

(Bias)  $\downarrow$  (Variance)  $\uparrow$

(Bias)  $\uparrow$  (Variance)  $\downarrow$

But we need Bias  $\downarrow$ , Variance  $\downarrow$



Bias: Error from making assumptions of the algorithm

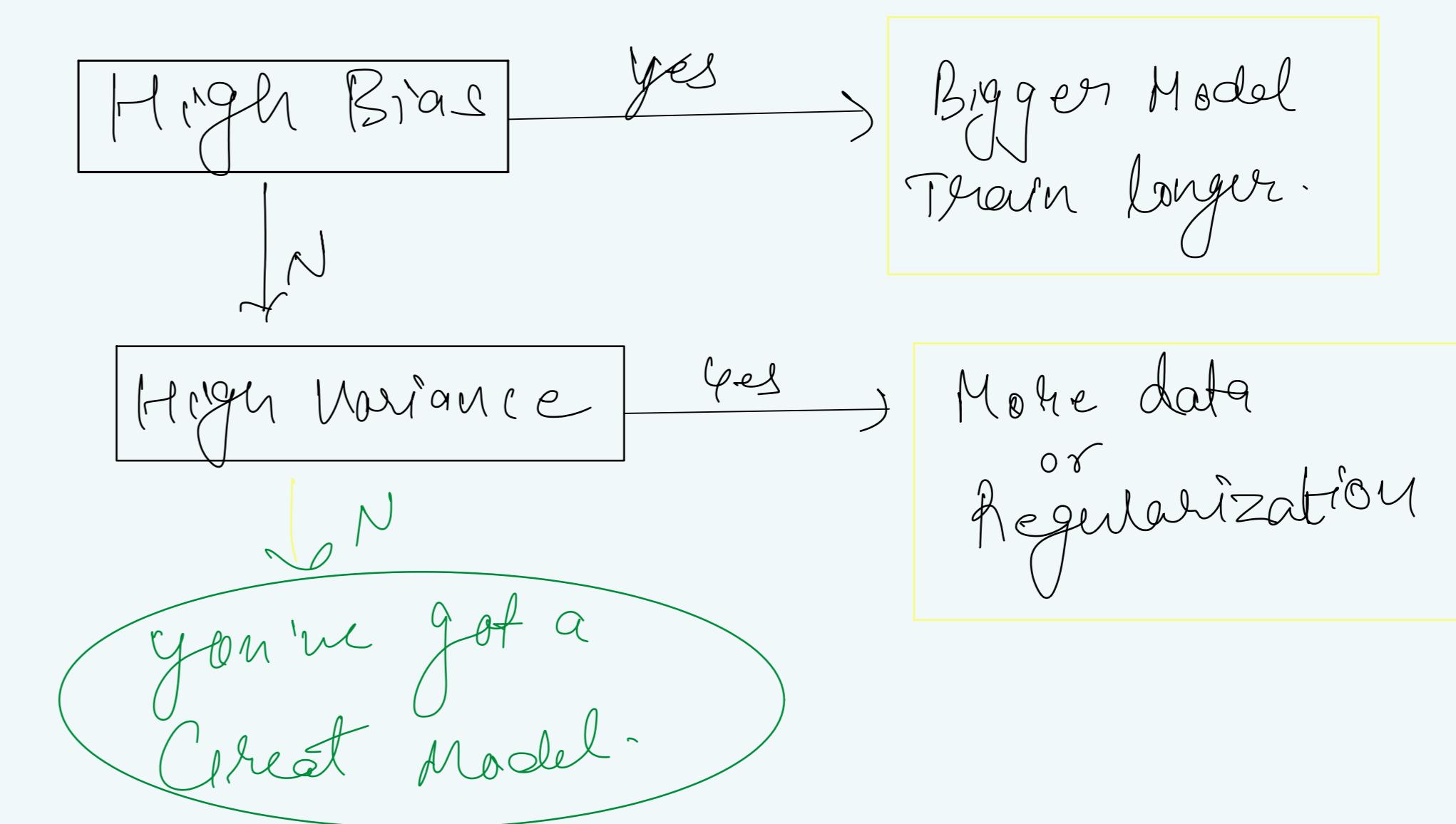
High Bias can make the model miss the relevant relationship b/w the feature and the target resulting in Underfitting.

Variance: Variance is an error that occurs from the sensitivity of the model.  
High sensitivity give rise to a condition where model learns everything called overfitting.

Train Set Error := 1% Test set error := 11%  $\rightarrow$  High Variance

Train Set Error's  $\rightarrow$  1% Test set error @ 1%  $\rightarrow$  High Bias

Train set error  $\oplus$  Test set error @ 18%  $\oplus$  30%  $\rightarrow$  Apodize

Regularization:

$$L_1 \Rightarrow \frac{1}{2m} \|w\| \quad \text{where } \|w\| = \|w_1 + w_2 + w_3 + \dots\|$$

$$L_2 \Rightarrow \frac{1}{2m} \|w\|^2 \quad \text{where } \|w\|^2 = (w_1^2 + w_2^2 + w_3^2 + \dots)^2$$

While you do gradient descent,

$$\text{Loss} = y \log \hat{y} + (1-y) \log(1-\hat{y})$$

$$(Loss)_{L_1} := \text{Loss} + \frac{1}{2m} * \|w\| \text{ norm}$$

$$(Loss)_{L_2} := \text{Loss} + \frac{1}{2m} \|w\|^2$$

Now depending on the domain knowledge, we can tune our tradeoff b/w TPR & FPR