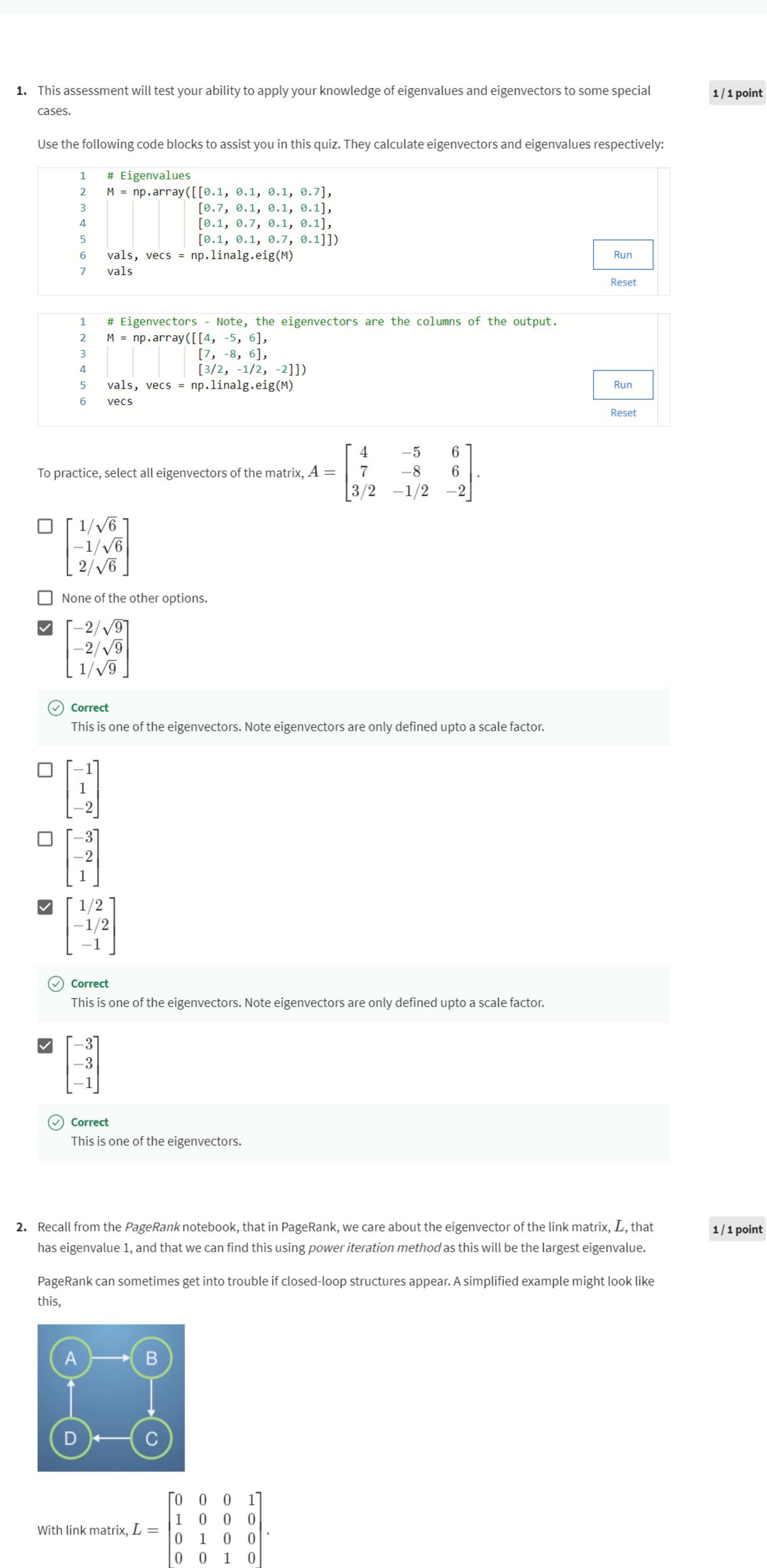
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What might be going wrong? Select all that apply. 
Other eigenvalues are not small compared to 1, and so do not decay away with each power iteration. 
Other eigenvalues are not small compared to 1, and so do not decay away with each power iteration. 
The other eigenvectors have the same size as 1 (they are -1, i, -i)

Some of the eigenvectors are complex.

▼ The other eigenvalues get smaller.

It makes the eigenvalue we want bigger.

None of the other options.

Correct

The system has zero determinant.

None of the other options.

Correct

 $\bigcirc \lambda^2 + 2\lambda + \frac{1}{4}$ 

 $A = \begin{bmatrix} 3/2 & -1 \\ -1/2 & 1/2 \end{bmatrix}.$ 

 $\lambda_1 = 1 - \frac{\sqrt{3}}{2}, \lambda_2 = 1 + \frac{\sqrt{3}}{2}$ 

eigenvalues of A.

 $\mathbf{v_1} = \begin{bmatrix} -1 - \sqrt{5} \\ 1 \end{bmatrix}, \mathbf{v_2} = \begin{bmatrix} -1 + \sqrt{5} \\ 1 \end{bmatrix}$ 

 $O \quad \mathbf{v_1} = \begin{bmatrix} 1 - \sqrt{5} \\ 1 \end{bmatrix}, \mathbf{v_2} = \begin{bmatrix} 1 + \sqrt{5} \\ 1 \end{bmatrix}$ 

There are two loops of size 2. (A  $\rightleftarrows$  B) and (C  $\rightleftarrows$  D)

Correct

Use the calculator in Q1 to check the eigenvalues and vectors for this system.

Because of the loop, *Procrastinating Pat*s that are browsing will go around in a cycle rather than settling on a webpage.

the system will not converge to this result by applying power iteration.

None of the other options.

The system is too small.

1/1 point

If all sites started out populated equally, then the incoming pats would equal the outgoing, but in general

3. The loop in the previous question is a situation that can be remedied by damping.

There is now a probability to move to any website.
 Correct
 This helps the power iteration settle down as it will spread out the distribution of Pats

If we replace the link matrix with the damped,  $L'=\begin{bmatrix}0.7 & 0.1 & 0.1 & 0.1\\0.1 & 0.7 & 0.1 & 0.1\end{bmatrix}$  , how does this help?

So their eigenvectors will decay away on power iteration.

4. Another issue that may come up, is if there are disconnected parts to the internet. Take this example,

with link matrix,  $L = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}$ . This form is known as block diagonal, as it can be split into square blocks along the main diagonal, i.e.,  $L = \begin{bmatrix} A & 0 \\ 0 & B \end{bmatrix}$ , with  $A = B = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$  in this case. What is happening in this system?

■ None of the other options.
 ✓ There are two eigenvalues of 1.
 ✓ Correct

The eigensystem is degenerate. Any linear combination of eigenvectors with the same eigenvalue is also an eigenvector.

There isn't a unique PageRank.

Correct

By similarly applying damping to the link matrix from the previous question. What happens now?
The system settles into a single loop.
There becomes two eigenvalues of 1.

The power iteration algorithm could settle to multiple values, depending on its starting conditions.

power iteration method.

Damping does not help this system.

The negative eigenvalues disappear.

There is now only one eigenvalue of 1, and PageRank will settle to it's eigenvector through repeating the

6. Given the matrix  $A=\begin{bmatrix} 3/2 & -1 \\ -1/2 & 1/2 \end{bmatrix}$  , calculate its characteristic polynomial.

Well done - this is indeed the characteristic polynomial of A.

O  $\lambda_1 = -1 - \frac{\sqrt{5}}{2}, \lambda_2 = -1 + \frac{\sqrt{5}}{2}$ O  $\lambda_1 = -1 - \frac{\sqrt{3}}{2}, \lambda_2 = -1 + \frac{\sqrt{3}}{2}$ O  $\lambda_1 = 1 - \frac{\sqrt{5}}{2}, \lambda_2 = 1 + \frac{\sqrt{5}}{2}$ 

7. By solving the characteristic polynomial above or otherwise, calculate the eigenvalues of the matrix

8. Select the two eigenvectors of the matrix  $A=\begin{bmatrix} 3/2 & -1 \\ -1/2 & 1/2 \end{bmatrix}$  .

Well done! These are the roots of the above characteristic polynomial, and hence these are the

 $\mathbf{v_1} = \begin{bmatrix} 1 - \sqrt{3} \\ 1 \end{bmatrix}, \mathbf{v_2} = \begin{bmatrix} 1 + \sqrt{3} \\ 1 \end{bmatrix}$   $\mathbf{v_1} = \begin{bmatrix} -1 - \sqrt{3} \\ 1 \end{bmatrix}, \mathbf{v_2} = \begin{bmatrix} -1 + \sqrt{3} \\ 1 \end{bmatrix}$   $\mathbf{v_2} = \begin{bmatrix} -1 + \sqrt{3} \\ 1 \end{bmatrix}$   $\mathbf{v_3} = \begin{bmatrix} -1 + \sqrt{3} \\ 1 \end{bmatrix}$   $\mathbf{v_4} = \begin{bmatrix} -1 + \sqrt{3} \\ 1 \end{bmatrix}$   $\mathbf{v_5} = \begin{bmatrix} -1 + \sqrt{3} \\ 1 \end{bmatrix}$   $\mathbf{v_6} = \mathbf{v_6} = \mathbf{v_6}$ 

By calculating  $D=C^{-1}AC$  or by using another method, find the diagonal matrix D.

9. Form the matrix C whose left column is the vector  $\mathbf{v_1}$  and whose right column is  $\mathbf{v_2}$  from immediately above.

**10.** By using the diagonalisation above or otherwise, calculate  $A^2$ .

 $\bigcap$   $\lceil -11/4$  2  $\rceil$ 

 $\oslash$  Correct Well done! In this particular case, calculating  $A^2$  directly is probably easier - so always try to look for the method which solves the question with the least amount of pain possible!

1/1 point