

Summary of Last Lecture

Functional Dependency :

- Direct
- Indirect (logically derived)
 - Reflexivity, Augmentation ,Transitivity ,
 - Additivity, Projectivity , Pseudotransitivity

Functional dependency closure (F^+)

Closure of Functional Dependency

The set of functional dependencies and all logically implied functional dependencies form a closure of F.

Denoted by F^+

Eg – $R=(A,B,C,D)$ and $F = \{A \rightarrow B, A \rightarrow C, BC \rightarrow D\}$

$$F \models \{A \rightarrow BC, A \rightarrow D\}$$

$$F^+ = \{A \rightarrow B, A \rightarrow C, BC \rightarrow D, A \rightarrow BC, A \rightarrow D\}$$

Closure of Functional Dependency

Eg. $R = (A, B, C, D, E)$ and $F = \{A \rightarrow BC, CD \rightarrow E, B \rightarrow D, E \rightarrow A\}$

FIND F_+ ?

Eg. $R = (A, B, C)$ and $F = \{A \rightarrow B, B \rightarrow C\}$

FIND F_+ ?

Closure of Attribute Set

It is a set of all attributes that are dependent on X and derived using the FDs in F .

Denoted by X_+

Algorithm to compute X_+

$X_+ = X$ (where X is candidate key)

while (changes to X_+) do

for each FD $w \rightarrow z$ in F do

begin

if $w \subseteq X_+$ then

$X_+ = X_+ \cup z$

end

Closure of Attribute Set

Eg. Compute X^+ of $X = BCD$ for $R = (ABCDEH)$

$F = \{A \rightarrow BC, CD \rightarrow E, E \rightarrow C, D \rightarrow AEH, ABH \rightarrow BD, DH \rightarrow BC\}$

Algorithm to compute X^+

$X^+ = X$ (where X is candidate key)

while (changes to X^+) do

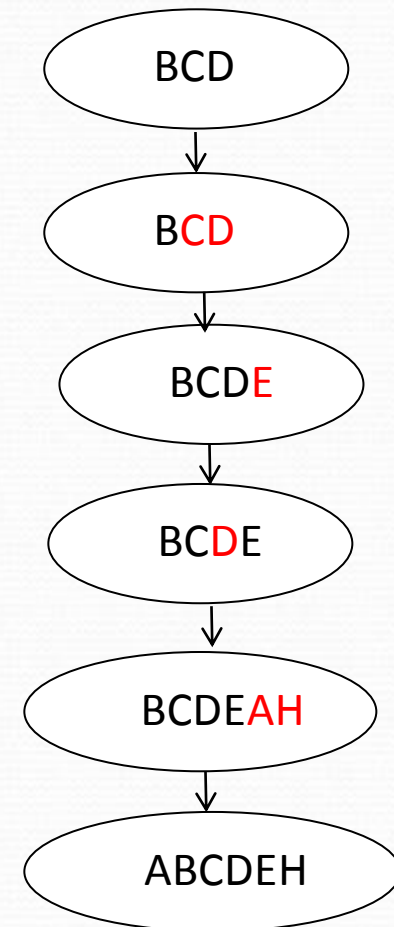
for each FD $w \rightarrow z$ in F do

begin

if $w \subseteq X^+$ then

$X^+ = X^+ \cup z$

end



Closure of Attribute Set

Eg. $R = (ABCDE)$ and $F = \{AB \rightarrow E, AD \rightarrow B, B \rightarrow C, C \rightarrow D\}$

Find X^+ if $X = AC$

Ans : AC is a candidate key

Eg. $R = (ABCDEH)$ and $F = \{A \rightarrow BC, CD \rightarrow E, E \rightarrow C, AH \rightarrow D\}$

Find candidate key and compute X^+

Ans : AH is a candidate key

Eg. $R = (ABCDE)$ and $F = \{A \rightarrow B, BC \rightarrow E, ED \rightarrow A\}$

Find candidate key and compute X^+

Ans : ACD , BCD , CDE are candidate key

Closure of Attribute Set

Eg. $R=(ABCDE)$ and $F=\{A \rightarrow BC, CD \rightarrow E, B \rightarrow D, E \rightarrow A\}$

Find candidate key and compute X_+

Ans : A, E, CD are candidate keys

Eg. $R = (ABCDEH)$ and $F=\{A \rightarrow BC, CD \rightarrow E, E \rightarrow C,$
 $D \rightarrow AEH, ABH \rightarrow BD, DH \rightarrow BC\}$

Find candidate key and computer X_+

Ans : CD, D, ABH, DH, AH are candidate keys