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Specifying Syntax

A *language*, in computer science theory, is a set of strings, where a *string* is a finite sequence of *symbols* chosen from a given *alphabet*. Computer science theory deals in part with how to specify languages using things such as Nondeterministic Finite Automata (NFAs), Context-Free Grammars (CFGs), and Turing Machines (TMs).

A *programming language* also defines a language in the theory sense, except that the strings in a programming language are called *programs*, and the symbols are called *tokens* (which we discussed in Slide Set 0). The *syntax* of a programming language is a set of rules used to specify the programs in the language. Most programming languages use a context-free grammar (or something close to it) to specify what sequences of tokens belong to the language.

A programming language also defines the run-time behavior of a program, called its *semantics*, which we discuss at length later.

Our first step is to describe a formal way in which we can define the syntax of a programming language. We start out with two simple examples of languages that describe familiar data structures. (These are not "programs" in the usual sense of the word, but they will at least get us started with how to specify syntax.)

Backus-Naur Form (BNF)

BNF is a meta-language used to specify a context-free grammar. Almost every modern programming language uses some sort of BNF notation to define its syntax. We work first with examples of languages that define two simple data structures: lists and trees. Remember that the "alphabet" of a programming language is a set of tokens, so any definition of the syntax of a language must first specify its tokens. In Slide Set 0, we showed how to specify tokens using PLCC.

Our first example is to define a language whose "programs" are lists of numbers. Some sample "programs" in this language are:

```
(3 4 5)
( 7 11 )
()
```

Backus-Naur Form (BNF) (continued)

Here is a BNF definition of this language, using three BNF formulas:

```
<lon> ::= LPAREN <nums> RPAREN
<nums> ::= NUM <nums>
<nums> ::=
```

In these formulas, the token names LPAREN and RPAREN stand for left parenthesis '(' and right parenthesis ')', respectively. The token name NUM stands for any (unsigned) decimal number. [Think about what regular expressions would match these.] Conforming to PLCC specifications, we use all-UPPERCASE letters for our token names.

BNF: (continued)

```
<lon> ::= LPAREN <nums> RPAREN
<nums> ::= NUM <nums>
<nums> ::=
```

Every BNF formula has the form

LHS ::= RHS

The *LHS* (Left-Hand Side) of a BNF formula always has the form <nonterm-symbol> where nonterm-symbol is an identifier. PLCC requires that the first character of this identifier be a lowercase letter. A <nonterm-symbol> expression is called a *nonterminal*. In the example above, the nonterminals are <lon> and <nums>.

The *RHS* (Right-Hand Side) of a BNF formula is a (possibly empty) ordered list of token names and nonterminals.

Notes: The term *syntactic category* is sometimes used instead of the term *nonterminal*, and the term *terminal* is sometimes used instead of *token name*. Instead of using a token name such as LPAREN, some BNF formulas just use the corresponding actual character string such as '('. In the examples on slide 1.2, you can see that we have also skipped whitespace.

BNF (continued)

```
<lon> ::= LPAREN <nums> RPAREN
<nums> ::= NUM <nums>
<nums> ::=
```

BNF has some shortcuts **that we do not use** but that you may run into in your reading. These shortcuts are usually called Extended BNF, or simply EBNF. For example, instead of writing two different formulas with <nums> on the LHS, one can use *alternation* notation "|":

```
<nums> ::= NUM <nums> | \epsilon
```

Note: ' ϵ ' means the empty string.

One could also use the *Kleene star* notation to define <nums>:

```
<nums> ::= { NUM }*
```

Note: We use a variant of the Kleene star notation later.

Parsing (syntatic derivation):

```
<lon> ::= LPAREN <nums> RPAREN
<nums> ::= NUM <nums>
<nums> ::=
```

A BNF grammar defines the set of all "legal" token sequences that conform to the grammar rules. This set is the *language* of the grammar, where we use the term "language" in the sense of computational theory. In the context of programming languages, these legal token sequences are called "programs". We also use the term *syntax rules* to refer to the rules given by a BNF grammar, and we use the term *syntactically correct* to refer to token sequences that conform to the grammar rules. Finally, when there is little chance for confusion, we use the term *sentence* (in the sense of computational theory) to refer to a finite length token sequence.

If we had a set of grammar rules for the Java programming language, for example, then the set of all sentences that conform to this grammar would be the set of all syntactically correct Java programs.

In these notes, we will casually use the term *token* to refer both to the name of the abstraction (like 'NUM') used in a BNF rule and to its corresponding *lexeme* (like '23') used in a program. In most instances, you should not have difficulty understanding which meaning is intended.

Parsing (syntatic derivation):

```
<lon> ::= LPAREN <nums> RPAREN
<nums> ::= NUM <nums>
<nums> ::=
```

A grammar can be used:

- to construct syntactically correct sentences, or
- to check to see if a particular target sentence belongs to the language (*i.e.*, is syntactically correct).

A programmer's job is to construct syntactically correct programs in a programming language, illustrating the first use of a grammar. This activity is called *programming*.

A compiler's job is, in part, to check a particular sentence for syntactic correctness, illustrating the second use of a grammar. This activity is called *syntax checking* or *parsing*.

Given a grammar, we want to generate an algorithm to carry out parsing. A program [written in Java, or C, or whatever] that carries out this algorithm is called, unsuprisingly, a *parser*. In this course, all of our parsers will be Java programs.

Given a BNF grammar, we describe here an algorithm (written in English, not Java) that parses a sentence in the language using what's called a *leftmost* derivation. The algorithm returns "success" if the parse is successful, "failure" otherwise.

- 1. Find the *start symbol* of the grammar. (For all of the grammars we define in these notes, the start symbol will be the first LHS nonterminal in the set of grammar rules.) This nonterminal becomes the initial *sentential form* of the derivation. (A "sentential form" is a sentence-like thing that is a sequence of nonterminals, token names, and lexemes. A "sentence" only has lexemes. Once all of the nonterminal symbols have been removed and the token names have been replaced by lexemes using the steps given below, the result is a sentence.) Set the *unmatched* sentence to the target sentence.
- 2. Repeat Step 3 (see the next page) until the sentential form is a sentence -i.e., consists only of lexemes (no nonterminals, no token names).

- 3. (a) If the leftmost unmatched term in the sentential form is a **token name**, match it with the leftmost string in the unmatched sentence. [Here, *match* means that the token name in the sentential form describes exactly the leftmost string to be matched. For example, the token name LPAREN matches the string '(' and NUM matches the string '42'.] If there is no match, return failure. If there is a match, replace the leftmost token name in the sentential form with its matching string from the unmatched sentence and remove the matched string from the unmatched sentence.
 - (b) If the leftmost unmatched term in the sentential form is a **nonterminal**, choose a rule from the grammar with this nonterminal as its LHS and *replace* the nonterminal with the (possibly empty) RHS of the chosen rule. [Which rule to choose depends on finding a rule that is most likely to complete the derivation. For some grammars, there is only one choice: these grammars are said to be *predictive*. All of the grammars we use in this course are predictive.] If no rule can apply, return failure.
- 4. If the unmatched sentence is empty, return success: the target sentence has been successfully parsed. Otherwise, return failure.

It is possible, for some grammars, that Step 3 loops indefinitely. However, for all of the grammars that we encounter in this course, this step exits in a finite number of iterations.

```
<lon> ::= LPAREN <nums> RPAREN
<nums> ::= NUM <nums>
<nums> ::=
```

We perform a *leftmost derivation* of the target string (14 6). Always start with the first nonterminal in the grammar (the *start symbol* – in this case it's <lon>) as the sentential form:

sentential form	unmatched sentence	algorithm step taken
<lon></lon>	(14 6)	1
\Rightarrow LPAREN < nums > RPAREN	(14 6)	3b
\Rightarrow (<nums> RPAREN</nums>	14 6)	3a
\Rightarrow (<u>NUM < nums></u> RPAREN	14 6)	3b
\Rightarrow (<u>14</u> <nums> RPAREN</nums>	6)	3a
\Rightarrow (14 NUM < nums> RPAREN	6)	3b
\Rightarrow (14 <u>6</u> <nums> RPAREN</nums>)	3a
\Rightarrow (14 6 $_$ RPAREN)	$3b (< nums > \Rightarrow empty)$
\Rightarrow (14 6 <u>)</u>		3a
\Rightarrow success!		4

In the above derivation, the leftmost unmatched token name or nonterminal is shown in **boldface**. The underlined parts are the matched lexemes for the unmatched token name as described in rule 3a, or the chosen substitutions for the LHS nonterminals as described in rule 3b.

A derivation ends successfully when there are no token names or nonterminals in the sentential form and no unmatched lexemes.

```
<lon> ::= LPAREN <nums> RPAREN
<nums> ::= NUM <nums>
<nums> ::=
```

Next we attempt a parse of '(14 (6)' using this grammar. As before, we start with the first nonterminal <10n> as the sentential form:

```
      sentential form
      unmatched sentence

      <lo>>
      ( 14 ( 6 )

      ⇒ LPAREN 
      ( 14 ( 6 )

      ⇒ ( nums> RPAREN
      14 ( 6 )

      ⇒ ( NUM < nums> RPAREN
      14 ( 6 )

      ⇒ ( 14 < nums> RPAREN
      ( 6 ) - try first < nums> rule ...

      ⇒ ( 14 NUM < nums> RPAREN
      ?? NUM doesn't match " ("

      ⇒ ( 14 RPAREN
      ( 6 ) - try second < nums> rule ...

      ⇒ ( 14 RPAREN
      ?? RPAREN doesn't match " ("
```

We can conclude that the string '(14 (6)' does not conform to the grammar specifications, so it is *not* a "list of numbers".

A tree is another data type that can be specified in BNF form:

```
<tree> ::= NUM
<tree> ::= LPAREN SYMBOL <tree> <tree> RPAREN
```

Here, SYMBOL is a token name that represents a string of alphanumeric characters starting with a letter. [Think of how to specify this using a regular expression.] The NUM, LPAREN and RPAREN token names are as before.

Here are some examples of trees that you can check for syntactic correctness using the parsing algorithm given above.

```
3
( bar 1 ( foo 1 2 ) )
( bar ( biz 3 4 ) ( foo 1 2 ) )
```

BNF (continued)

```
<tree> ::= NUM
<tree> ::= LPAREN SYMBOL <tree> <tree> RPAREN
```

In a given sentential form, the nonterminal <tree> can be replaced by the right-hand side of either rule having <tree> as its left-hand side. For example, parsing the string '(bar 1 (foo 1 2))' gives this:

```
<tree>
⇒ LPAREN SYMBOL <tree> <tree> RPAREN
⇒ ( bar <tree> <tree> RPAREN [*see below...]
⇒ ( bar NUM <tree> RPAREN
⇒ ( bar 1 <tree> RPAREN
⇒ ( bar 1 LPAREN SYMBOL <tree> <tree> RPAREN
⇒ ...
```

*Note: this line collapses two match steps into one:

```
LPAREN \Rightarrow '('
SYMBOL \Rightarrow bar
```

Parsers 1.14

Recall our grammar for a list of numbers (directory LON):

```
<lon> ::= LPAREN <nums> RPAREN
<nums> ::= NUM <nums>
<nums> ::=
```

We have seen how to take a sentence in this language and use a leftmost derivation to parse it. What can we do to automate this algorithm?

A *parser* is a program that takes as input a sentence in a language and that carries out a parse of the sentence, producing either success or failure. Building a parser from the BNF specification of a language is conceptually simple: we only need to write a program to carry out the steps of the parsing algorithm. The difficulty is the algorithm's essential *nondeterminism*: given a nonterminal in a sentiential form, how do we replace this nonterminal with the right-hand side of the "correct" grammar rule having this nonterminal as its left-hand side? (For some grammars, there may even be more than one "correct" rule that leads to a successful parse – such grammars are said to be *ambiguous*.)

```
<lon> ::= LPAREN <nums> RPAREN
<nums> ::= NUM <nums>
<nums> ::=
```

There are several tool sets that can be used to convert a BNF-like grammar specification into a parser. Many of these tool sets use C or C++ as the target language: input to such a tool set is a grammar specification, and the output is a set of target language programs that, when compiled, produces a parser. Learning how to use some of these tool sets can be a daunting task, and the generated parsers can be obscure. Furthermore, most of these tool sets are split into two separate parts: a lexical analysis (scanning) part and a syntax analysis (parsing) part.

The PLCC tool set is designed to make it easy to build a scanner and parser for a large collection of programming languages. While it is not "industrial strength" like many of the standard tool sets, it is easy to learn. The target language for PLCC is Java, so all of the source code that PLCC generates consists of self-contained Java programs. To use PLCC, you only need to be comfortable reading and writing programs in Java.

To say that a parser returns only success or failure is cold comfort, since in most cases you will want to "run" a program once it parses successfully. So a parser generally does one of two things: it "runs" the program as it carries out the parse algorithm (which is called interpretation on the fly), or it produces some form of output that can later be used to run the program once the parse is complete. PLCC uses the latter approach, since generating a parser is simpler if it is divorced from any attempts to carry out run-time behavior during the parse.

The input to a PLCC parser is a token stream – specifically, the tokens produced by an instance of the Scan class (see Slide Set 0). The output of a PLCC parser is a *parse tree* of a program: more specifically, it is a Java object that is the root of the parse tree.

The following diagram shows how the output of a scanner (a program that implements lexical analysis) becomes input to a parser (a program that implements syntax analysis). The output of a parser is a *parse tree* – which we will describe in more detail later.

Lexical analysis (scanning) Syntax analysis (parsing)



For a particular language whose PLCC grammar file specifies the language tokens and BNF grammar, the placemk program generates and compiles Java source files that implement a scanner and parser directly from the grammar file.

We will start with the list-of-numbers (LON) example to show how this works.

```
<lon> ::= LPAREN <nums> RPAREN
<nums> ::= NUM <nums>
<nums> ::=
```

From each BNF grammar rule for a language, PLCC generates Java class. A rule such as

```
<lon> ::= LPAREN <nums> RPAREN
```

generates the Java class Lon. PLCC gets the name Lon from the LHS nonterminal <1on> of this grammar rule by converting the first letter of this nonterminal name to uppercase.

PLCC determines the *fields* of a Java class generated from a BNF grammar rule from the RHS terms of the rule – specifically, the terms that are enclosed in angle brackets < . . . >. The RHS of the lon grammar rule given above has one term in angle brackets: <nums>. The corresponding field name in the Lon class is nums (Java field names always begin with a lowercase letter). The *type* of this field is Nums, because Nums is the name of the Java class corresponding to the nonterminal <nums>.

Since <nums> appears as the LHS nonterminal on the second and third grammar rules for this language, PLCC generates a corresponding Nums class.

```
<lon> ::= LPAREN <nums> RPAREN
<nums> ::= NUM <nums>
<nums> ::=
```

However, there are two grammar rules with <nums> as the LHS nonterminal. PLCC generates the class name Nums automatically (by converting the first character of the LHS nonterminal name to uppercase), but PLCC must generate a *unique* Java class name for each grammar rule. We accomplish this by annotating the LHS nonterminal on each of these lines with a Java class name that is different from Nums and that distinguishes one from the other. We modify these grammar rules with annotations as follows:

```
<nums>:NumsNode ::= NUM <nums>
<nums>:NumsNull ::=
```

(Any Java class names are OK for these annotations, but good naming conventions should prevail, and the names must be unique among the Java class names that PLCC generates.) A colon is used to separate the nonterminal from its annotated Java class name. The RHS entries of these grammar rules are unchanged.

With these modifications, PLCC generates two new classes, NumsNode and NumsNull. Both of these classes are declared to extend the Nums class, so an instance of a NumsNode class, for example, is also automatically an instance of its parent Nums class.

Here is a complete text file representation of the LON language, including its lexical specification and grammar rules, suitable for processing by plccmk. Notice that we have included the annotations for the two <nums> rules as described on the previous slide:

```
# Language specification for a list of numbers
# Lexical spec
skip WHITESPACE '\s+'
NUM '\d+'
LPAREN '\(')
RPAREN '\(')')
%
# BNF rules
<lon> ::= LPAREN <nums> RPAREN
<nums>:NumsNode ::= NUM <nums>
<nums>:NumsNull ::=
%
```

```
# Language specification for a list of numbers
# Lexical spec
skip WHITESPACE '\s+'
NUM '\d+'
LPAREN '\(')
RPAREN '\(')')
%
# BNF rules
<lon> ::= LPAREN <nums> RPAREN
<nums>:NumsNode ::= NUM <nums>
<nums>:NumsNull ::=
%
```

To summarize, the top lines of the file, up to the first percent (%) line, constitute the *lexical specification* of the language. For this language, these lines say that whitespace (including spaces, tabs, and newlines) should be skipped, that a NUM is a string of one or more decimal digits, and that LPAREN and RPAREN match the characters '(' and ')', respectively.

The remaining lines of the file constitute the *syntax specification* of the language, given in BNF form. PLCC takes this file as input and generates a collection of Java source files in a Java subdirectory that implement a scanner and parser for the language.

1.22

Parsers (continued)

```
# Language specification for a list of numbers
# Lexical spec
skip WHITESPACE '\s+'
NUM '\d+'
LPAREN '\(')
RPAREN '\(')
%
# BNF rules
<lon> ::= LPAREN <nums> RPAREN
<nums>:NumsNode ::= NUM <nums>
<nums>:NumsNull ::=
%
```

Observe that the LPAREN and RPAREN token specifications use regular expressions having a backslash '\'. This is because parentheses have a special meaning in regular expressions, and the backslash voids this special meaning. So, for example, the regular expression '\' (' really matches the left parenthesis symbol. (You should take this opportunity to review how to write and interpret regular expressions in the Java Pattern class.)

To complete this example, assume that you have created a directory named LON, and that in this directory you have created a file named grammar that contains lines appearing above. In your LON directory, run the placemk script as follows:

plccmk

Your script output should appear as follows:

```
Nonterminals (* indicates start symbol):
    *<lon>
        <nums>
Abstract classes:
        Nums
Source files created:
        NumsNode.java
        ...
```

```
<lon> ::= LPAREN <nums> RPAREN
<nums>:NumsNode ::= NUM <nums>
<nums>:NumsNull ::=
```

(The above text shows just the grammar rules section of the grammar file we have been examining.) In your LON directory, change to the subdirectory named Java. The plccmk command creates this subdirectory and populates it with Java source code generated by plcc.py. In this subdirectory you will find (among other things) the following Java source files:

```
Lon.java
Nums.java
NumsNode.java
NumsNull.java
```

Each of these corresponds to one or more of the grammar rule lines. For example, the line beginning with <lon> results in the file Lon.java being created in the Java subdirectory. As you can see from looking at the Java code in the Java subdirectory for the NumsNode and NumsNull classes, both of these classes extend the Nums abstract class. This is because the <nums> nonterminal appears as the LHS of two grammar rules.

For every grammar rule, PLCC creates a Java class uniquely associated with the rule. For grammar rules that have the same nonterminal appearing on the LHS of multiple rules, PLCC creates an abstract class based on the nonterminal name, and the annotated class names become derived classes of this abstract class.

The first nonterminal in the grammar file is the *start symbol* for the language. Given a program in the language, the parser produces an instance of the class of the start symbol, which is the root of the parse tree for the program.

In the case of the LON language, the start symbol is <lon>, and the corresponding class name is Lon. Given a program in the LON language, the output of the parser is an instance of the Lon class. We will see shortly how to interpret this instance as the root of a tree.

```
<lon> ::= LPAREN <nums> RPAREN
<nums>:NumsNode ::= NUM <nums>
<nums>:NumsNull ::=
```

PLCC generates a stand-alone parser with class name Parser that uses the Java classes created from processing the lexical and grammar specification sections. To run this parser, change to the Java subdirectory (of the LON directory, in this case) and run the Parser class file with command-line arguments consisting of strings (in quotes) that you want to parse. For example:

```
java Parser "(14 6)" "(14 (6)" "(42)" "()"
```

The output produced looks something like this:

```
(14 6) -> Lon@15db9742
(14 (6) -> java.lang.RuntimeException: Nums cannot begin with (
(42) -> Lon@7852e922
() -> Lon@6d06d69c
```

For each command-line argument, the parser prints a copy of the argument, then a string '->', and finally a string of the form Lon@....

The Lon@... strings are simply the toString() values of the instances of the Lon class that are created for each **successful** parse. For any grammar, an instance of the class associated with the *start symbol* of the language is always the root of the parse tree generated by the parser. If the parse fails for a particular command-line string, the parser prints an error message giving the nature of the error.

```
<lon> ::= LPAREN <nums> RPAREN
<nums>:NumsNode ::= NUM <nums>
<nums>:NumsNull ::=
```

When invoked without any command-line arguments, the Parser program reads a single "program" from standard input (without a prompt) and prints its result in the same way as if the program had been given (in quotes) on the command line.

Here is a sample interaction with the Parser program using this grammar, with the same programs as before, except from standard input instead of from the command line:

```
$ java Parser
(14 6)
Lon@15db9742
$ java Parser
(14 (6)
java.lang.RuntimeException: Nums cannot begin with (
$ java Parser
(42)
Lon@6d06d69c
$ java Parser
()
Lon@7852e922
```

```
<lon> ::= LPAREN <nums> RPAREN
<nums>:NumsNode ::= NUM <nums>
<nums>:NumsNull ::=
```

PLCC also generates an interactive parser called Rep that resides in the Java sub-directory along with the Parser program. Rep executes a "read-eval-print" loop that displays a prompt, *Reads* program input from the keyboard, *Evaluates* (parses) the program, and *Prints* the result: a human-readable representation of the root of the program's parse tree, in exactly the same way as the Parser program does.

The Rep program prints only the Java object that represents the root of each program's parse tree. To see how the objects in the parse tree are being constructed as the parse proceeds, you can use the '-t' switch when invoking Rep. The '-t' stands for trace. The next slide shows the output using this feature.

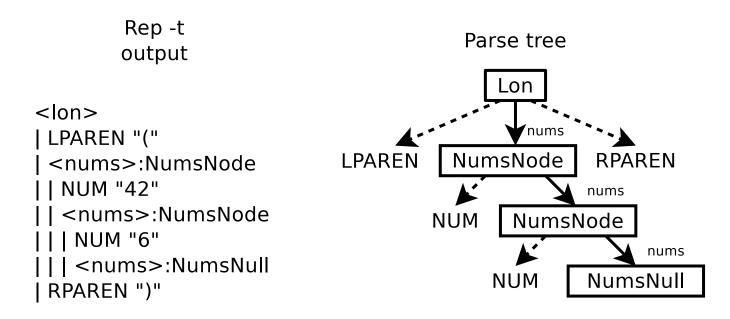
```
<lon> ::= LPAREN <nums> RPAREN
<nums>:NumsNode ::= NUM <nums>
<nums>:NumsNull ::=
```

Here's a sample interaction using this trace feature, with the output edited for the sake of readability:

```
$ java Rep -t
--> (14 6)
<lon>
| LPAREN "("
| <nums>:NumsNode
| NUM "42"
| | <nums>:NumsNode
| | NUM "6"
| | | <nums>:NumsNode
| | RPAREN ")"
```

In this example, the root of the parse tree is a Lon object whose nums field is an instance of NumsNode. This instance in turn has a nums field that is also an instance of NumsNode. And finally, this instance has a nums field that is an instance of NumsNull. A NumsNull object has no fields. The trace also shows how each token is matched by the parser, along with the lexeme from the input program that matched the token.

Using the trace feature, we can construct the parse tree whose root is an object of type Lon. The diagram below shows the trace on the left and the resulting parse tree on the right. Nodes in the tree are represented by boxes. The dashed lines point to tokens that are part of the conceptual parse tree but that do *not* correspond to fields in the node. (Normally this is the case when the BNF entries on its RHS are tokens that are fixed – such as LPAREN.)



In order to make the connection clear between a grammar rule and its PLCC-generated Java class, we often display the grammar rules in the following way:

The item in the box following a grammar rule is the *Java signature of the Java class constructor* corresponding to the class PLCC generates from the grammar rule. So the box

```
Lon(Nums nums)
```

means that the constructor for the PLCC-generated class Lon has a single parameter nums of type Nums.

There is a one-to-one correspondence between the types and formal parameters in the constructor and the types and field names in the class. More specifically, when the constructor is invoked, the constructor body simply copies the values of its parameters into the corresponding field names of the instance being constructed.

As you can see from above, the NumsNull constructor takes no parameters, and the NumsNull class has no fields.

```
<lon> ::= LPAREN <nums> RPAREN
<nums>:NumsNode ::= NUM <nums>
<nums>:NumsNull ::=
```

The parse tree for a program in this language accurately represents the length of the list of numbers given as input – count the number of instances of NUM in the parse trace given on Slide 1.30 above – but the actual values of the NUM tokens are not preserved in the parse tree. The problem is that the parse tree instances of NumsNode objects do not have fields corresponding to their token values.

To remedy this situation, we want to define a field in the NumsNode class that captures the value of the NUM token. We use angle brackets for all nonterminals on the RHS of grammar rules, and these nonterminals automatically become fields in the Java class. To capture values of the *tokens* on the RHS, we use angle brackets for these token names as well. This means that the NumsNode line now looks like this:

```
<nums>:NumsNode ::= <NUM> <nums>
```

The '<NUM>' entry creates a field named num (which is the token name 'NUM' converted to lowercase) of type Token (since NUM is the name of a token in the grammar file).

Observe that it's unnecessary to capture tokens that always have the same string representation, like LPAREN: every instance of the LPAREN token looks like every other instance, so there's no need to distinguish among them. This is not so with tokens that can take on multiple string values, such as NUM. Indeed, for a list of numbers, knowing exactly *what* numbers are in the list can be essential – for example, if you want to find the sum of the numbers in the list. If these items do not appear as fields in the PLCC-generated classes, their values do not appear in the parse tree, and so their values are not retrievable after the parse.

The revised grammar now looks like this:

```
<lon> ::= LPAREN <nums> RPAREN
<nums>:NumsNode ::= <NUM> <nums>
<nums>:NumsNull ::=
```

Since we now have two fields in the NumsNode class, we need to modify the signature of the NumsNode constructor, as shown here (compare with slide 1.31):

```
<lon>
    ::= LPAREN <nums> RPAREN

    Lon(Nums nums)

<nums>:NumsNode
    ::= <NUM> <nums>
    NumsNode(Token num, Nums nums)

<nums>:NumsNull
    ::=
    NumsNull()
```

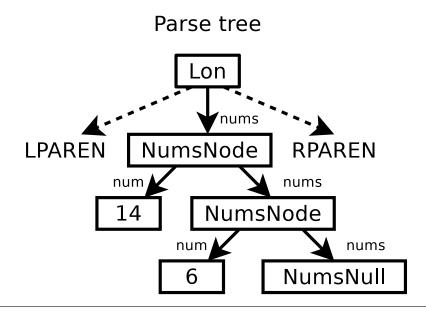
```
<lon> ::= LPAREN <nums> RPAREN
<nums>:NumsNode ::= <NUM> <nums>
<nums>:NumsNull ::=
```

We now have two fields in the NumsNode class: num (of type Token) and nums (of type Nums). When the parser generates a NumsNode object, it fills in its num field with the value of the Token object. The toString() method applied to this object retrieves the lexeme of the scanned token, which will be a string of decimal digits. The rest of the NumsNode object is the same as before.

The following diagram shows the parse tree for the string

```
(146)
```

using this revised grammar. Notice that each NumsNode object now has a num field (a Token) containing decimal digits.



Let's return to our tree example (directory TREE). Here is a modified grammar for a tree as originally given on slide 1.12 that takes into account the PLCC requirements for unique class names and the introduction of fields for the NUM and SYMBOL tokens: The Java signatures for the constructors are also given.

But there is a problem with the Interior constructor signature. Java does not allow multiple field names or constructor formal parameters with the same name: specifically, in this case, there cannot be two field names with the name tree. Here is what PLCC has to say about this when given the above grammar (the line has been folded for clarity):

```
duplicate field name tree in rule
RHS LPAREN <SYMBOL> <tree> <tree> RPAREN
```

The solution is to use different identifiers for these field names and to their corresponding constructor formal parameters. PLCC allows duplicate RHS fields (in angle brackets) to be annotated – much like we have seen for duplicate LHS nonterminal names – with alternate names that avoid this conflict.

In the case we are considering, we can resolve this issue in the RHS of the <tree>:Interior grammar rule by using the identifier left for the first <tree> field and the identifier right for the second <tree> field, as shown here:

```
<tree>:Interior ::= LPAREN <SYMBOL> <tree>left <tree>right RPAREN

Interior(Token symbol, Tree left, Tree right)
```

In summary, this grammar rule creates:

- a class Interior
- that extends the abstract class Tree and
- that has a field symbol of type Token,
- a field left of type Tree, and
- a field right of type Tree.

As a result, the following grammar is acceptable to PLCC:

When processed by PLCC, we get the following interaction using the Rep parser loop:

```
$ java Rep
--> 3
Leaf@15db9742
--> (foo 5 8)
Interior@6d06d69c
--> (foo (bar 13 23) 8)
Interior@7852e922
--> (goo blah 99) % blah is the culprit here
java.lang.RuntimeException: Tree cannot begin with SYMBOL
-->
```

Examine the Java code for the Interior class. You will see the following fields:

```
public Token symbol;
public Tree left;
public Tree right;
```

Let's return to the list-of-numbers example.

```
<lon> ::= LPAREN <nums> RPAREN
<nums>:NumsNode ::= <NUM> <nums>
<nums>:NumsNull ::=
```

The Nums abstract class is extended by both NumsNode and NumsNull classes.

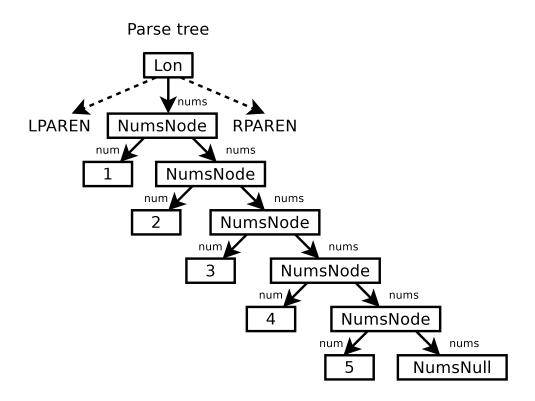
```
<nums>:NumsNode ::= <NUM> <nums>
<nums>:NumsNull ::=
```

Clearly, when parsing the <nums> grammar rules, you get zero or more NumsNode instances but just one final NumsNull instance. Since the the RHS of the first <nums> rule has <nums> as its last entry (which means that this rule is *right recursive*), this rule results in a parsing loop, ending only when there are no more NUM tokens in the program.

The parse tree for the following list-of-numbers

(12345)

is shown here:



Because of this right-recursive looping, the nodes in the parse tree drift to the right as the number of elements in the list grows. Clearly a list of numbers with 100 entries would have 100 NumsNode nodes in the tree, weighted significantly to the right. How can we structure our tree nodes to avoid this?

This sort of looping occurs frequently in programming language specifications, and PLCC has a way to encode this. Instead of having two <nums> rules, with the first being right-recursive and the second having an empty RHS, we can re-write these rules using a special '**=' notation:

```
<nums> **= <NUM>
Nums(List<Token> numList)
```

The parser accumulates all of the NUM tokens into a single numList field. The numList field name is obtained from the NUM token name by converting all of its characters to lowercase and appending the string List.

Note: The use of '**' in the notation we have just introduced should suggest the *Kleene star* repetition notation used in EBNF as well as in regular expressions.

The modified list-of-numbers grammar is as follows:

```
<lon> ::= LPAREN <nums> RPAREN
<nums> **= <NUM>
```

```
<lon> ::= LPAREN <nums> RPAREN
<nums> **= <NUM>
```

Here is an (edited) example of a parse trace for the list of numbers (3 5 8 13):

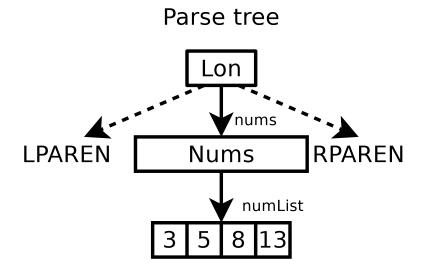
```
--> (3 5 8 13)
<lon>
| LPAREN "("
| <nums>
| NUM "3"
| NUM "5"
| NUM "5"
| NUM "13"
| RPAREN ")"
```

Compare this with the parse trace using the previous grammar that does not use the **= construct. The previous parse trace drifts to the right as additional NUM entries are encountered. Using the **= construct, the parse trace becomes flat.

PLCC grammar rules that use this construct are called *repeating grammar rules*. Repeating rules are useful in specifying most of our languages.

```
<lon> ::= LPAREN <nums> RPAREN
<nums> **= <NUM>
```

The parse tree for the list of numbers (3 5 8 13) is shown here, using a box with compartments to represent a Java List structure:



This parse tree has fewer nodes, and the individual NUM token values are all packaged together into a single structure.

```
<lon> ::= LPAREN <nums> RPAREN
<nums> **= <NUM>
```

How exactly can we access the values of the NUM fields from the parse tree? The Rep program first parses the program, yielding an instance of the start symbol class – an instance of Lon, in this case. It then prints the toString() value of this instance, which as we have seen defaults to something like 'Lon@...'.

But a Lon object has a nums field of type Nums, and a Nums object has a numList field of type List<Token>, so perhaps we can redefine the toString() method in the Lon class to print the values in this list.

To do this, we need to modify the Lon.java file to incorporate this new toString() behavior. We can do this directly by editing the file (once it has been created by PLCC). But every change we make to the grammar file involves re-running the placmk script, which will clobber any edits we may have made to the previous version.

Fortunately, PLCC allows us to add methods to PLCC-generated source files by including the added methods in the grammar file. Every time placmk is run, these added methods are incorporated into the Java source files automatically.

```
<lon> ::= LPAREN <nums> RPAREN
<nums> **= <NUM>
```

For example, if we want to add a toString() method to the Lon. java source file, we put the following lines into the grammar file in the section following the BNF section. This section is separated from the BNF section by a line containing a single '%'.

```
Lon
%%%

public String toString() {
...
}
%%%
```

The Lon line tells PLCC that we are adding a method to the Lon. java file, and the lines containing %%% bracket the Java code to be added. This technique can be used to add Java code to any PLCC-generated Java file arising from the BNF grammar lines. The added code appears at the end of the class definition in the Java code generated automatically by PLCC for the class.

```
<lon> ::= LPAREN <nums> RPAREN
<nums> **= <NUM>
```

We want to redefine the toString() method in the Lon class so it prints the values of the tokens in the numList field. This field, an object of type List<Token>, is accessible from the Lon class as follows:

```
nums.numList
```

So we can get the NUM entries by iterating over this list, accumulating the corresponding (String) values of the tokens, and returning the resulting string. Here is the completed version of the PLCC specification that adds the modified toString() method to the Lon.java file. This code also adds back the parentheses to make the output look "pretty".

```
Lon
%%%

public String toString() {
    String ret = "(";
    for (Token tok: nums.numList) {
        ret += tok + " ";
    }
    return ret + ")";
}
```

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Parsers (continued)

Here is the complete grammar file in code directory LON2 with these changes:

```
# Lexical specification
skip WHITESPACE '\s+'
NUM '\d+'
LPAREN '\('
RPAREN '\)'
# Grammar
<lon> ::= LPAREN <nums> RPAREN
<nums> ** = <NUM>
Lon
응응응
    public String toString() {
        String ret = "(";
        for (Token tok: nums.numList) {
            ret += tok + " ";
        return ret + ")";
응응응
```

Continuing with our list-of-numbers example, suppose we want our parser to require that the numbers in our list are separated by commas, like this:

```
(5, 8, 13, 21)
```

How can we devise a grammar that accommodates these separators?

PLCC provides a way to specify a token that serves as a separator between items in a repeating grammar rule. The separator name must appear at the end of the rule, preceded by a '+' character. So if we want to separate the items in our lists by a comma (with token name COMMA), here is what the specification looks like:

```
skip WHITESPACE '\s+'
NUM '\d+'
LPAREN '\('
RPAREN '\)'
COMMA ','
%
<lon> ::= LPAREN <nums> RPAREN
<nums> **= <NUM> +COMMA
%
```

While this grammar requires comma separators between NUM items, the parser generates *exactly the same parse trees* for this language as for the previous specification.

Slide set 1a provides a summary of PLCC features. You should familiarize yourself with this section in preparation for material in subsequent parts of this course.

Static Properties of Variables

A *variable* in a program is a symbol that has an associated value at run-time. One of the principal issues in determining the behavior of a program is determining *how* to find the value of a variable at run-time. At any instance in time, the value associated with a variable is called a *binding* of the variable to the value.

An *expression* is a language construct that has a value at run-time. A variable, by itself, is therefore an expression, but other language constructs can also have values: for example x+y is an expression if x and y are numeric-valued variables.

A programming language that is designed solely for the purpose of evaluating expressions is called an *expression-based language*. Many of the languages we construct in these notes are expression-based, especially early on. Scheme, ML, and Haskell are examples of expression-based languages used in practice. Expression-based languages do their looping principally using recursion.

A programming language whose language constructs are designed to "do something" (such as assigning the value of an expression to a variable or printing the value of an expression to standard output) is called an *imperative language*. In an imperative language, a language construct that "does somthing" is called a *statement*; Imperative languages are therefore often called *statement-based*. C, Java, and Python are examples of imperative languages used in practice. Imperative languages do their looping principally using a form of "goto".

Expression-based languages get their power from defining and applying *functions*, so another term describing such languages is *functional*.

Determing the value of an expression at run-time is at the heart of executing a program, particularly so in expression-based languages. Since most expressions involve variables, evaluating an expression requires determining the values of its constituent variables – in other words, finding the values bound to these variables.

At run-time, how can you find the value bound to a variable? There are two basic approaches:

- if the location of the value bound to a variable can be determined by *where* that variable appears *in the text of a program*, we call it *static binding*.
- if the location of the value bound to a varible can only be determined by when the variable is accessed *during program execution*, we call it *dynamic binding*.

Almost all programming languages commonly in use today use static bindings, principally because it is easier to reason (or prove things) about programs that use static bindings. You will have the opportunity to explore dynamic binding in your homework.

We consider only static bindings for now, so the program text will tell us how to determine variable bindings.

For a given variable, the *scope* of the variable is the region of code in which that variable's binding can be determined. Consider the following Java program:

```
public class Foo {
   public static int y;
   public int z;
   public static void main(String [] args) {
      // args is local to main
      Foo f = new Foo(); // f is local to main
      int x = 1; // x is local in main
      Foo.y = 2; // y is static throughout in Foo
      f.z = 3; // z is known only within instances of Foo
   }
}
```

In the above code, the scope of y is *global*, from its declaration as a public static variable to the end of the class. The scope of z is *instance-global*, known only within (and throughout) instances of the class Foo. The scopes of f and x are *local*, from their declarations to the end of the main method body. The scope of args is also local, from the beginning of the method body to the end.

It is possible for one symbol to have multiple bindings depending on where it occurs in the program. Consider:

```
public class Bar {
  public static int x;
  public static void main(String [] args) {
    x = 3;
    System.out.println(x);
    { // beginning of block
       int x = 4;
       System.out.println(x);
    } // end of block
    System.out.println(x);
}
```

When this program is run, the output will be

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This is because the "int x = 4;" line defines a new variable x bound to the value 4 whose scope is from its point of declaration to the end of the *block* in which it is defined, as shown in the program comments. In this case, we say that the definition of x in the block *shadows* the global int x, and that the block definition *punches a hole in the scope* of the global definition.

Here is the Foo class given on the second previous slide:

```
public class Foo {
   public static int y;
   public int z;
   public static void main(String [] args) {
      Foo f = new Foo(); // f is local to main
      int x = 1; // x is local in main
      y = 2; // y is static throughout in Foo
      f.z = 3; // z is known only within instances of Foo
   }
}
```

Consider just the main procedure in this class:

```
public static void main(String [] args) {
  Foo f = new Foo(); // f is local to main
  int x = 1; // x is local in main
  y = 2; // y is static throughout in Foo
  f.z = 3; // z is known only within instances of Foo
}
```

In this method, the identifiers f and x are explicitly defined. In these cases, we say that these identifiers *occur bound* in the main procedure.

However, the variable y is not defined anywhere in the procedure main. In this case, we say that the identifier y *occurs free* in the main method, but it *occurs bound* in the enclosing class Foo.

The Lambda Calculus - OPTIONAL SECTION

The following grammar defines a formal language called "the lambda calculus". This language plays an important role in the foundations of computer science (similar to Turing Machines). The PROC token is the string proc, and the SYMBOL, LPAREN, RPAREN, LBRACE, RBRACE, and DOT tokens are straight-forward – see the examples below.

```
<exp> ::= <SYMBOL>
<exp> ::= PROC LPAREN <SYMBOL> RPAREN LBRACE <exp> RBRACE
<exp> ::= DOT <exp> LPAREN <exp> RPAREN
```

Consider the sentential form (remember what that means?) in this language obtained from the second grammar rule, where s replaces <SYMBOL>:

```
proc(s) { <exp> }
```

The occurrence of the symbol s in this expression is called a *variable declaration* that *binds* all occurrences of s that appear in $\langle exp \rangle$ unless some intervening declaration of the same symbol s occurs in $\langle exp \rangle$. We say that the expression $\langle exp \rangle$ is the *scope* of the variable declaration for s.

Occurs Free, Occurs Bound (informal definitions):

A symbol \times *occurs free* in an expression \mathbb{E} if \times appears somewhere in \mathbb{E} in a way that is not bound by any declaration of \times in \mathbb{E} . A symbol \times *occurs bound* in \mathbb{E} if \times appears in \mathbb{E} in such a way that is bound by a declaration of \times in \mathbb{E} . It is possible for the same symbol to occur both bound and free in different parts of an expression. (Note that the declaration itself is not considered free or bound.)

```
<exp> ::= <SYMBOL>
<exp> ::= PROC LPAREN <SYMBOL> RPAREN LBRACE <exp> RBRACE
<exp> ::= DOT <exp> LPAREN <exp> RPAREN
```

Formal definitions of *occurs free* and *occurs bound*:

For a Lambda Calculus expression E, a symbol x occurs free in E if

• *Rule 1*:

```
E is a <SYMBOL> and E is the same as x.

x ; x is free
```

• *Rule 2*:

```
E is of the form proc(y) {E'} where y is different from x and x occurs free in E'
proc(y) {x}; x is free
```

• *Rule 3*:

E is of the form .E1 (E2) and x occurs free in E1 or E2

```
.proc(y) {x} (y) ; x is free
.proc(y) {y} (x) ; x is free
```

```
<exp> ::= <SYMBOL>
<exp> ::= PROC LPAREN <SYMBOL> RPAREN LBRACE <exp> RBRACE
<exp> ::= DOT <exp> LPAREN <exp> RPAREN
```

For a Lambda Calculus expression E, a symbol x occurs bound in E if

• *Rule 1*:

E is of the form proc(y) {E'} where x occurs bound in E' or x and y are the same symbol and y occurs free in E'

```
proc(y) \{proc(x) \{x\}\}; x is bound proc(y) \{y\}; y is bound
```

• *Rule 2*:

E is of the form .E1 (E2) and x occurs bound in E1 or E2

```
.proc(y) {proc(x) \{x\}} (y) ; x is bound
.proc(y) \{x\} (proc(y) \{y\}) ; y is bound
```

Lexical and Grammar specification for the Lambda Calculus:

```
# Lexical specification
skip WHITESPACE '\s+'
LPAREN '\('
RPAREN '\)'
LBRACE '\{'
RBRACE '\}'
DOT '\.'
PROC 'proc'
SYM '\w+'
# Grammar
<exp>:Var ::= <SYM>
<exp>:Proc ::= PROC LPAREN <SYM> RPAREN LBRACE <exp> RBRACE
<exp>:App ::= DOT <exp>rator LPAREN <exp>rand RPAREN
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```

In the Lambda Calculus, if a symbol is bound by a declaration, we can easily determine the precise declaration that binds the variable. The Lambda Calculus is of interest theoretically, but it has no practical value as a programming language.

Most imperative programming languages are *block structured* and use *lexical binding*, another term for static scope rules. A *block* is a region of code introduced by one or more variable declarations and continuing to the end of the code where these declarations are active. In C, C++, and Java, blocks are delimited by matching pairs of braces '{ . . . }'.

In some languages, blocks may be *nested*, in which case variable bindings at outer blocks may be *shadowed* by bindings in inner blocks. Consider, for example the following C++ code fragment:

This code prints 5 and then 3.

In block structured languages, a variable in an expression is bound to the variable with the same name in the *innermost* block that defines the variable. (Note that Java does not allow the same variable to be defined both in an outer block and in an inner block.)

Let's return to our C++ example. The following picture shows the blocks of the C++ program fragment given on the previous slide:

To determine the binding of a variable in an expression, cross the boxes textually outwards (up) until a variable declaration with the same variable name is found.

When defining procedures in block structured languages, the formal parameter declarations are considered to be at the same lexical level as local variable declarations in the outermost block of the procedure. In the following C++ example, the formal parameter x is at the same lexical level as the local variable y:

```
int foo(int x) {
   int y;
   ...
}
```