

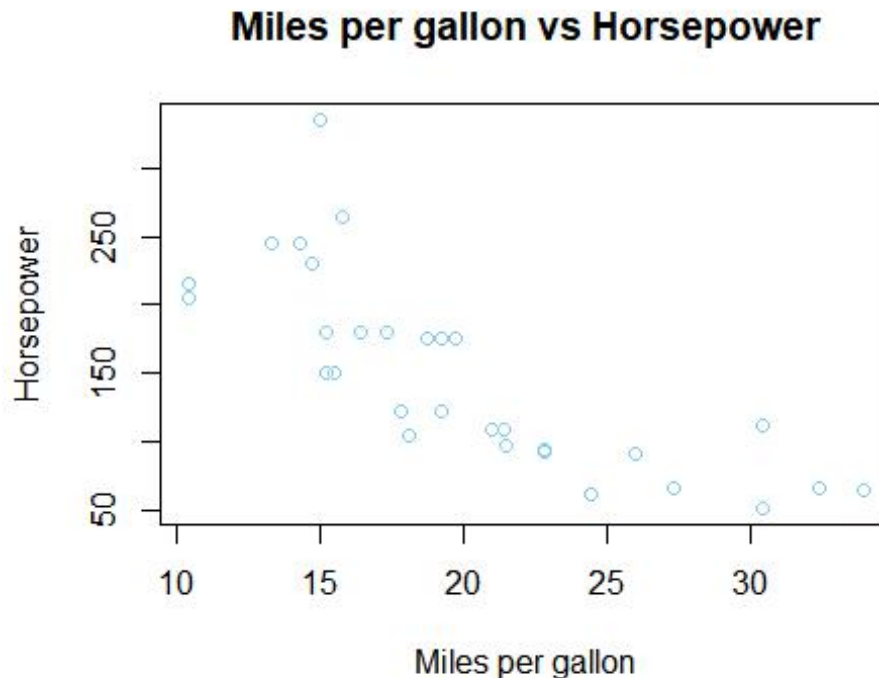
assignment-1R

2019-12-22

```
data(mtcars)
cars=mtcars
head(cars)
```

| ## | | mpg | cyl | disp | hp | drat | wt | qsec | vs | am | gear | carb |
|----|-------------------|------|-----|------|-----|------|-------|-------|----|----|------|------|
| ## | Mazda RX4 | 21.0 | 6 | 160 | 110 | 3.90 | 2.620 | 16.46 | 0 | 1 | 4 | 4 |
| ## | Mazda RX4 Wag | 21.0 | 6 | 160 | 110 | 3.90 | 2.875 | 17.02 | 0 | 1 | 4 | 4 |
| ## | Datsun 710 | 22.8 | 4 | 108 | 93 | 3.85 | 2.320 | 18.61 | 1 | 1 | 4 | 1 |
| ## | Hornet 4 Drive | 21.4 | 6 | 258 | 110 | 3.08 | 3.215 | 19.44 | 1 | 0 | 3 | 1 |
| ## | Hornet Sportabout | 18.7 | 8 | 360 | 175 | 3.15 | 3.440 | 17.02 | 0 | 0 | 3 | 2 |
| ## | Valiant | 18.1 | 6 | 225 | 105 | 2.76 | 3.460 | 20.22 | 1 | 0 | 3 | 1 |

```
plot(cars$mpg,cars$hp,type="p",col="skyblue",xlab="Miles per gallon",ylab="Horsepower",
     ,main="Miles per gallon vs Horsepower")
```



```
#Simple linear model
relation=lm(cars$mpg~cars$hp)
print(relation)
```

```
##
## Call:
## lm(formula = cars$mpg ~ cars$hp)
##
## Coefficients:
## (Intercept)      cars$hp
##      30.09886      -0.06823

print(summary(relation,correlation=TRUE,symbolic.cor=TRUE))

##
## Call:
## lm(formula = cars$mpg ~ cars$hp)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -5.7121 -2.1122 -0.8854  1.5819  8.2360
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  30.09886    1.63392   18.421  < 2e-16 ***
## cars$hp      -0.06823    0.01012   -6.742 1.79e-07 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.863 on 30 degrees of freedom
## Multiple R-squared:  0.6024, Adjusted R-squared:  0.5892
## F-statistic: 45.46 on 1 and 30 DF, p-value: 1.788e-07
##
## Correlation of Coefficients:
##
## (Intercept) 1
## cars$hp      * 1
## attr(,"legend")
## [1] 0 ' ' 0.3 '.' 0.6 ',' 0.8 '+' 0.9 '*' 0.95 'B' 1

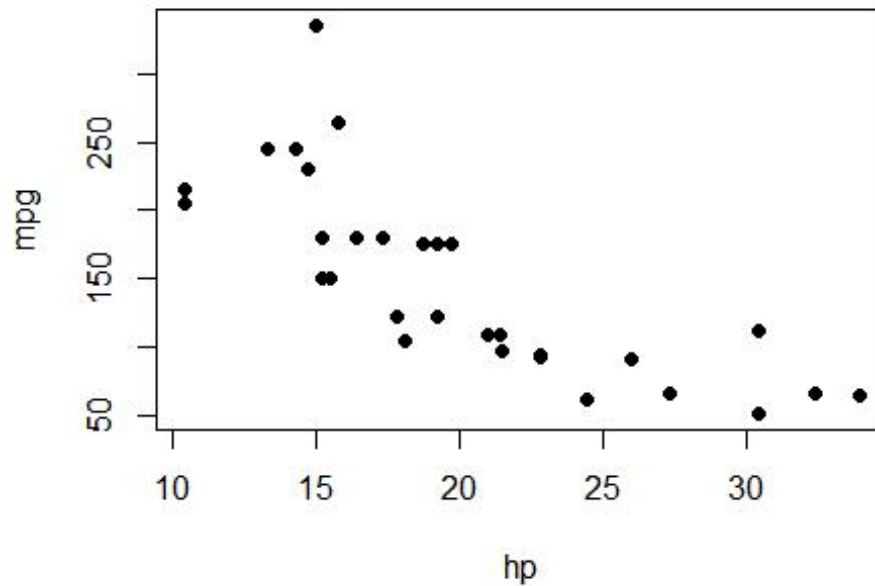
confint(relation)

##              2.5 %      97.5 %
## (Intercept) 26.76194879 33.4357723
## cars$hp      -0.08889465 -0.0475619

#Intercept:30.09886
#slope: -0.06823
#Confidence interval:97.5%

plot(cars$mpg,cars$hp,xlab="hp",ylab="mpg",pch=16,main="Linear Regression wit
h mpg~hp")
```

Linear Regression with mpg~hp



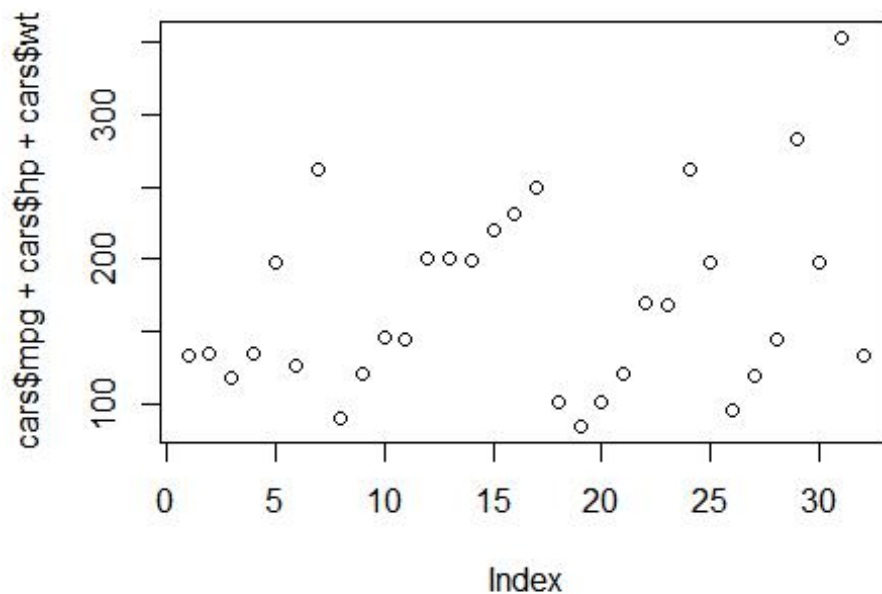
```
new=c(126,167,189,211,272,312)
new1=as.data.frame(new)
#Predict mileage
predict(relation,new1,interval="confidence")

## Warning: 'newdata' had 6 rows but variables found have 32 rows

##           fit      lwr      upr
## 1 22.593750 21.006344 24.18116
## 2 22.593750 21.006344 24.18116
## 3 23.753631 21.971485 25.53578
## 4 22.593750 21.006344 24.18116
## 5 18.158912 16.646511 19.67131
## 6 22.934891 21.295615 24.57417
## 7 13.382932 10.918575 15.84729
## 8 25.868707 23.630821 28.10659
## 9 23.617174 21.860464 25.37388
## 10 21.706782 20.228730 23.18483
## 11 21.706782 20.228730 23.18483
## 12 17.817770 16.262471 19.37307
## 13 17.817770 16.262471 19.37307
## 14 17.817770 16.262471 19.37307
## 15 16.112064 14.268892 17.95523
## 16 15.429781 13.445318 17.41424
## 17 14.406357 12.190623 16.62209
## 18 25.595794 23.421947 27.76964
## 19 26.550990 24.148024 28.95396
```

```
## 20 25.664022 23.474282 27.85376
## 21 23.480718 21.748829 25.21261
## 22 19.864619 18.468309 21.26093
## 23 19.864619 18.468309 21.26093
## 24 13.382932 10.918575 15.84729
## 25 18.158912 16.646511 19.67131
## 26 25.595794 23.421947 27.76964
## 27 23.890087 22.081920 25.69825
## 28 22.389065 20.830320 23.94781
## 29 12.086595 9.289663 14.88353
## 30 18.158912 16.646511 19.67131
## 31 7.242387 3.108308 11.37647
## 32 22.661978 21.064598 24.25936
```

```
#HP versus mpg,wt
plot(cars$mpg+cars$hp+cars$wt,type="p")
```



```
car.fit=lm(cars$mpg~cars$hp+cars$wt,data=cars)
print(car.fit)

##
## Call:
## lm(formula = cars$mpg ~ cars$hp + cars$wt, data = cars)
##
## Coefficients:
## (Intercept)      cars$hp      cars$wt
##    37.22727    -0.03177    -3.87783
```

```
summary(car.fit,correlation=TRUE,symbolic.cor=TRUE)
```

```
##
## Call:
## lm(formula = cars$mpg ~ cars$hp + cars$wt, data = cars)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3.941 -1.600 -0.182  1.050  5.854
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  37.22727    1.59879   23.285  < 2e-16 ***
## cars$hp      -0.03177    0.00903   -3.519  0.00145 **
## cars$wt      -3.87783    0.63273   -6.129  1.12e-06 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.593 on 29 degrees of freedom
## Multiple R-squared:  0.8268, Adjusted R-squared:  0.8148
## F-statistic: 69.21 on 2 and 29 DF,  p-value: 9.109e-12
##
## Correlation of Coefficients:
##
## (Intercept) 1
## cars$hp      1
## cars$wt      , , 1
## attr(,"legend")
## [1] 0 ' ' 0.3 '.' 0.6 ', ' 0.8 '+' 0.9 '*' 0.95 'B' 1
```

#Returns:

#The weighted residuals, the usual residuals rescaled by the square root of the weights specified in the call to lm.

#p x 4 matrix with columns for the estimated coefficient, its standard error, t-statistic and corresponding (two-sided) p-value.

#the square root of the estimated variance of the random error

#R^2, the 'fraction of variance explained by the model',

#R^2 = 1 - Sum(R[i]^2) / Sum((y[i]- y)^2),*

#where y is the mean of y[i] if there is an intercept and zero otherwise.*

#Other correlation coefficients

```
confint(car.fit)
```

```
##              2.5 %      97.5 %
## (Intercept) 33.95738245 40.49715778
## cars$hp     -0.05024078 -0.01330512
## cars$wt     -5.17191604 -2.58374544
```

#Intercept:37.22727

#cars\$hp:-0.03177

#cars\$wt:-3.87783

```
pred1=predict(car.fit)
pred1
```

```
##          Mazda RX4          Mazda RX4 Wag          Datsun 710          Hornet 4
Drive
##          23.572329          22.583483          25.275819          21.2
65020
##  Hornet Sportabout          Valiant          Duster 360          Merc
240D
##          18.327267          20.473816          15.599042          22.8
87067
##          Merc 230          Merc 280          Merc 280C          Merc
450SE
##          21.993673          19.979460          19.979460          15.7
25369
##          Merc 450SL          Merc 450SLC          Cadillac Fleetwood          Lincoln Contin
ental
##          17.043831          16.849939          10.355205          9.3
62733
##  Chrysler Imperial          Fiat 128          Honda Civic          Toyota Co
rolla
##          9.192487          26.599028          29.312380          28.0
46209
##          Toyota Corona          Dodge Challenger          AMC Javelin          Camar
o Z28
##          24.586441          18.811364          19.140979          14.5
52028
##          Pontiac Firebird          Fiat X1-9          Porsche 914-2          Lotus E
uropa
##          16.756745          27.626653          26.037374          27.7
69769
##          Ford Pantera L          Ferrari Dino          Maserati Bora          Volvo
142E
##          16.546489          20.925413          12.739477          22.9
83649
```

```
car.fit1=lm(cars$mpg~cars$hp+cars$wt+cars$hp*cars$wt)
print(car.fit1)
```

```
##
## Call:
## lm(formula = cars$mpg ~ cars$hp + cars$wt + cars$hp * cars$wt)
##
## Coefficients:
##          (Intercept)          cars$hp          cars$wt  cars$hp:cars$wt
##          49.80842          -0.12010          -8.21662           0.02785
```

```
confint(car.fit1)
```

```
##          2.5 %          97.5 %
## (Intercept)  42.42359654  57.19325031
```

```

## cars$hp          -0.17069436 -0.06950982
## cars$wt          -10.81750352 -5.61574508
## cars$hp:cars$wt   0.01264983  0.04304647

#Intercept:49.8042
#Slope:-0.12010
#Returns:
#The weighted residuals, the usual residuals rescaled by the square root of the weights specified in the call to lm.
#p x 4 matrix with columns for the estimated coefficient, its standard error, t-statistic and corresponding (two-sided) p-value.
#the square root of the estimated variance of the random error
#R^2, the 'fraction of variance explained by the model',
#R^2 = 1 - Sum(R[i]^2) / Sum((y[i]- y*)^2),
#where y* is the mean of y[i] if there is an intercept and zero otherwise.
#Other correlation coefficients
summary(car.fit1,correlation=TRUE,symbolic.cor=TRUE)

##
## Call:
## lm(formula = cars$mpg ~ cars$hp + cars$wt + cars$hp * cars$wt)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3.0632 -1.6491 -0.7362  1.4211  4.5513
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    49.80842     3.60516   13.816 5.01e-14 ***
## cars$hp        -0.12010     0.02470    -4.863 4.04e-05 ***
## cars$wt       -8.21662     1.26971    -6.471 5.20e-07 ***
## cars$hp:cars$wt  0.02785     0.00742     3.753 0.000811 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.153 on 28 degrees of freedom
## Multiple R-squared:  0.8848, Adjusted R-squared:  0.8724
## F-statistic: 71.66 on 3 and 28 DF,  p-value: 2.981e-13
##
## Correlation of Coefficients:
##
## (Intercept)      1
## cars$hp          + 1
## cars$wt          B , 1
## cars$hp:cars$wt * B * 1
## attr(,"legend")
## [1] 0 ' ' 0.3 '.' 0.6 ', ' 0.8 '+' 0.9 '*' 0.95 'B' 1

pred2=predict(car.fit1)
pred2

```

```
##          1          2          3          4          5          6          7          8
## 23.09547 21.78138 25.58488 20.02924 17.28996 18.88542 15.40745 21.65887
##          9         10         11         12         13         14         15         16
## 20.84992 18.55379 18.55379 15.14994 16.23929 16.07909 12.02179 11.89490
##         17         18         19         20         21         22         23         24
## 12.50221 27.84866 32.63195 30.24587 24.56317 17.57441 17.91776 15.03111
##         25         26         27         28         29         30         31         32
## 15.93596 29.53900 26.71871 28.56630 15.36033 19.52990 13.54587 22.31363
```

```
hp1=c(126,167,189,211,272,312)
wt1=c(1.5,2.2,2.9,3.2,3.8,4.2)
new2=c(hp1,wt1)
new3=as.data.frame(new2)
predict(car.fit,new3,interval="prediction")
```

```
## Warning: 'newdata' had 12 rows but variables found have 32 rows
```

```
##          fit          lwr          upr
## 1  23.572329 18.152053 28.99261
## 2  22.583483 17.173052 27.99391
## 3  25.275819 19.814373 30.73726
## 4  21.265020 15.836451 26.69359
## 5  18.327267 12.926266 23.72827
## 6  20.473816 14.994498 25.95313
## 7  15.599042  9.993171 21.20491
## 8  22.887067 17.284608 28.48953
## 9  21.993673 16.532703 27.45464
## 10 19.979460 14.552353 25.40657
## 11 19.979460 14.552353 25.40657
## 12 15.725369 10.274249 21.17649
## 13 17.043831 11.631452 22.45621
## 14 16.849939 11.434088 22.26579
## 15 10.355205  4.579380 16.13103
## 16  9.362733  3.530661 15.19480
## 17  9.192487  3.414919 14.97006
## 18 26.599028 21.087052 32.11100
## 19 29.312380 23.691616 34.93314
## 20 28.046209 22.484454 33.60796
## 21 24.586441 19.143493 30.02939
## 22 18.811364 13.413350 24.20938
## 23 19.140979 13.749010 24.53295
## 24 14.552028  8.981473 20.12258
## 25 16.756745 11.335804 22.17769
## 26 27.626653 22.083269 33.17004
## 27 26.037374 20.548743 31.52601
## 28 27.769769 22.072733 33.46681
## 29 16.546489 10.725413 22.36756
## 30 20.925413 15.446364 26.40446
## 31 12.739477  6.476550 19.00240
## 32 22.983649 17.570829 28.39647
```



```
predict(car.fit,new3,interval="confidence")
```

```
## Warning: 'newdata' had 12 rows but variables found have 32 rows
```

```
##           fit           lwr           upr
## 1  23.572329 22.456232 24.68843
## 2  22.583483 21.516224 23.65074
## 3  25.275819 23.974405 26.57723
## 4  21.265020 20.109318 22.42072
## 5  18.327267 17.308891 19.34564
## 6  20.473816 19.099332 21.84830
## 7  15.599042 13.784634 17.41345
## 8  22.887067 21.083228 24.69091
## 9  21.993673 20.694257 23.29309
## 10 19.979460 18.830645 21.12827
## 11 19.979460 18.830645 21.12827
## 12 15.725369 14.467994 16.98274
## 13 17.043831 15.966740 18.12092
## 14 16.849939 15.755529 17.94435
## 15 10.355205  8.069065 12.64134
## 16  9.362733  6.937998 11.78747
## 17  9.192487  6.901946 11.48303
## 18 26.599028 25.099641 28.09842
## 19 29.312380 27.452469 31.17229
## 20 28.046209 26.373069 29.71935
## 21 24.586441 23.364981 25.80790
## 22 18.811364 17.808947 19.81378
## 23 19.140979 18.171643 20.11032
## 24 14.552028 12.849864 16.25419
## 25 16.756745 15.637422 17.87607
## 26 27.626653 26.015632 29.23767
## 27 26.037374 24.626220 27.44853
## 28 27.769769 25.690706 29.84883
## 29 16.546489 14.148322 18.94466
## 30 20.925413 19.551999 22.29883
## 31 12.739477  9.409231 16.06972
## 32 22.983649 21.904339 24.06296
```

```
predict(car.fit1,new3,interval="prediction")
```

```
## Warning: 'newdata' had 12 rows but variables found have 32 rows
```

```
##           fit           lwr           upr
## 1  23.09547 18.581687 27.60926
## 2  21.78138 17.262031 26.30072
## 3  25.58488 21.041239 30.12852
## 4  20.02924 15.465956 24.59253
## 5  17.28996 12.764155 21.81576
## 6  18.88542 14.248302 23.52253
## 7  15.40745 10.745695 20.06920
## 8  21.65887 16.953143 26.36459
```

```
## 9 20.84992 16.267096 25.43274
## 10 18.55379 13.975233 23.13234
## 11 18.55379 13.975233 23.13234
## 12 15.14994 10.607150 19.69273
## 13 16.23929 11.718200 20.76037
## 14 16.07909 11.556876 20.60130
## 15 12.02179 7.134532 16.90904
## 16 11.89490 6.853171 16.93663
## 17 12.50221 7.370479 17.63393
## 18 27.84866 23.215676 32.48165
## 19 32.63195 27.620095 37.64381
## 20 30.24587 25.468673 35.02307
## 21 24.56317 20.038028 29.08832
## 22 17.57441 13.036154 22.11268
## 23 17.91776 13.385583 22.44994
## 24 15.03111 10.392521 19.66970
## 25 15.93596 11.406922 20.46500
## 26 29.53900 24.813678 34.26433
## 27 26.71871 22.140473 31.29694
## 28 28.56630 23.810027 33.32258
## 29 15.36033 10.477733 20.24293
## 30 19.52990 14.911525 24.14827
## 31 13.54587 8.320464 18.77127
## 32 22.31363 17.798713 26.82854
```

```
predict(car.fit1,new3,interval="confidence")
```

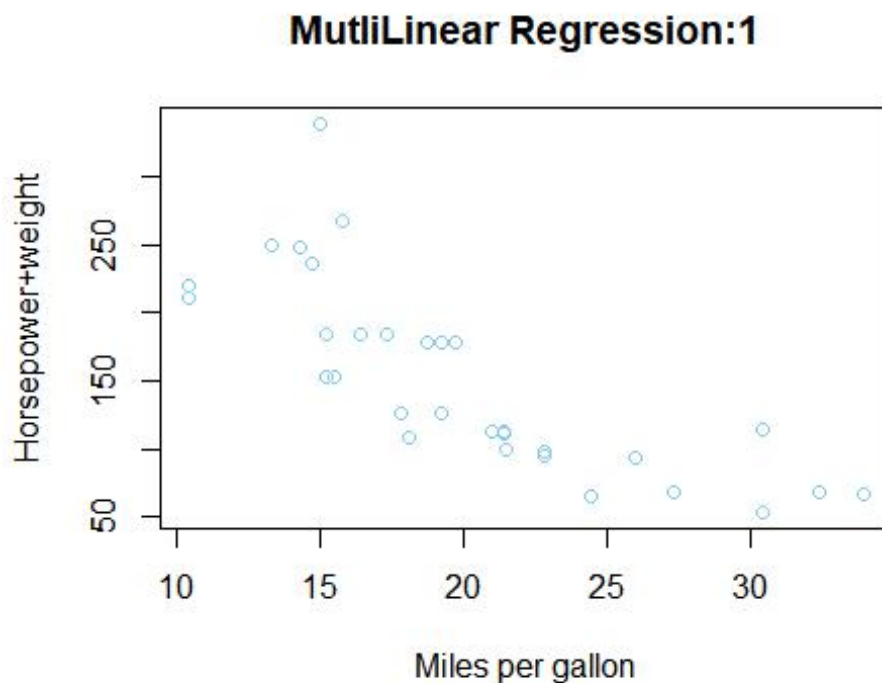
```
## Warning: 'newdata' had 12 rows but variables found have 32 rows
```

```
##      fit      lwr      upr
## 1 23.09547 22.131774 24.05917
## 2 21.78138 20.791974 22.77078
## 3 25.58488 24.489847 26.67991
## 4 20.02924 18.855346 21.20314
## 5 17.28996 16.271471 18.30844
## 6 18.88542 17.451097 20.31974
## 7 15.40745 13.895373 16.91952
## 8 21.65887 20.016220 23.30152
## 9 20.84992 19.602242 22.09759
## 10 18.55379 17.321878 19.78570
## 11 18.55379 17.321878 19.78570
## 12 15.14994 14.058437 16.24144
## 13 16.23929 15.241961 17.23661
## 14 16.07909 15.076670 17.08150
## 15 12.02179 9.914727 14.12885
## 16 11.89490 9.450830 14.33897
## 17 12.50221 9.877502 15.12691
## 18 27.84866 26.427743 29.26958
## 19 32.63195 30.250111 35.01380
## 20 30.24587 28.408467 32.08327
```

```
## 21 24.56317 23.547603 25.57874
## 22 17.57441 16.501916 18.64691
## 23 17.91776 16.871290 18.96424
## 24 15.03111 13.592025 16.47020
## 25 15.93596 14.903181 16.96874
## 26 29.53900 27.841019 31.23699
## 27 26.71871 25.487991 27.94942
## 28 28.56630 26.783998 30.34861
## 29 15.36033 13.264095 17.45657
## 30 19.52990 18.157379 20.90242
## 31 13.54587 10.742427 16.34931
## 32 22.31363 21.344667 23.28258
```

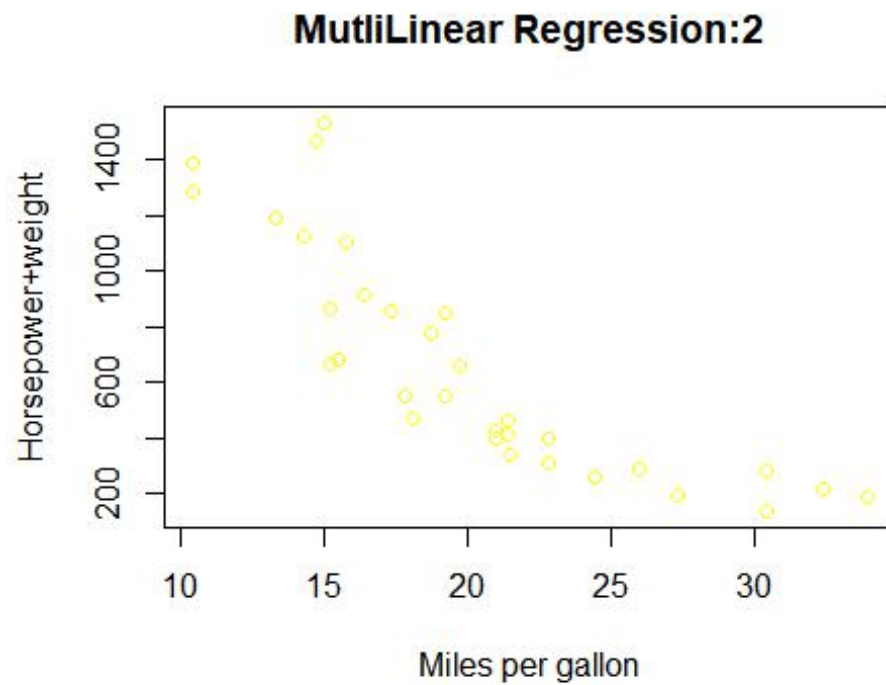
```
plot(cars$mpg,cars$hp+cars$wt,type="p",col="skyblue",xlab="Miles per gallon",
      ylab="Horsepower+weight",
      ,main="MutliLinear Regression:1")
abline(car.fit,col="skyblue")
```

```
## Warning in abline(car.fit, col = "skyblue"): only using the first two of 3
## regression coefficients
```



```
plot(cars$mpg,cars$hp+cars$wt+cars$hp*cars$wt,type="p",col="yellow",xlab="Miles per gallon",ylab="Horsepower+weight",
      ,main="MutliLinear Regression:2")
abline(car.fit1,col="Red")
```

```
## Warning in abline(car.fit1, col = "Red"): only using the first two of 4
## regression coefficients
```



#Multilinear model 1 performs better than 2 as confidence interval is shorter
#Both models, due to low pvalues, need improvement in terms of parameters considered.