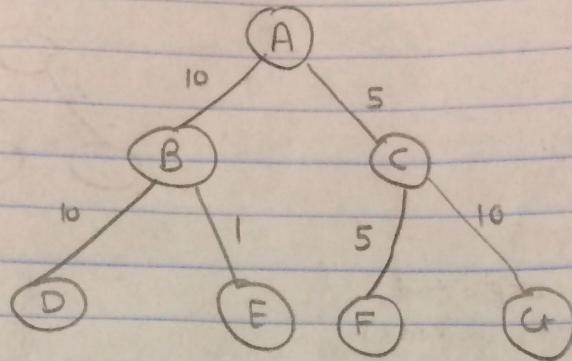
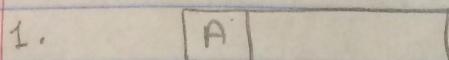


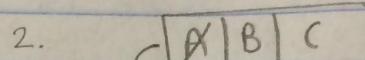
Q1]



* Breadth first search.

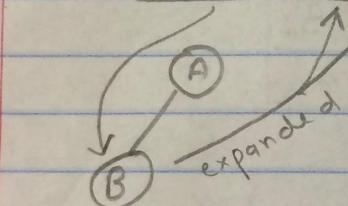
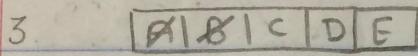


Initial start node
in queue

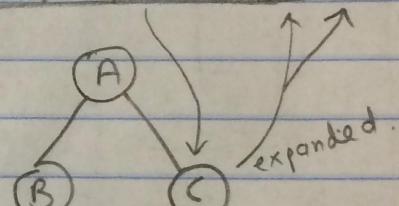
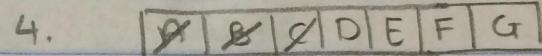


dequeue

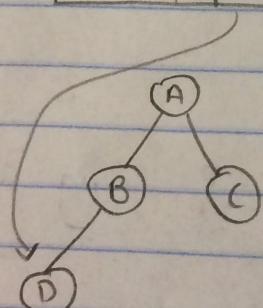
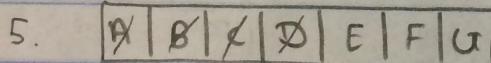
(Not the goal
state hence expanded)
& marked explored.



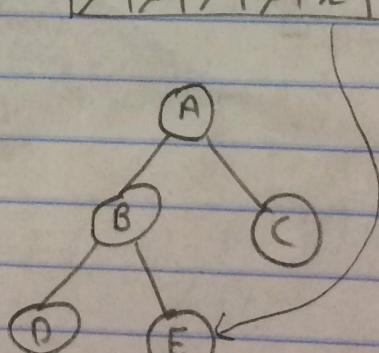
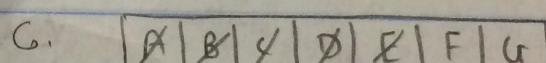
(Not goal
state)
marked explored



(not goal state,
marked explored).

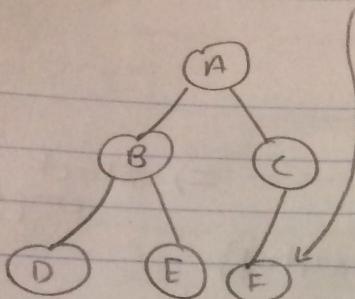


(not goal state,
marked explored)
nothing to expand

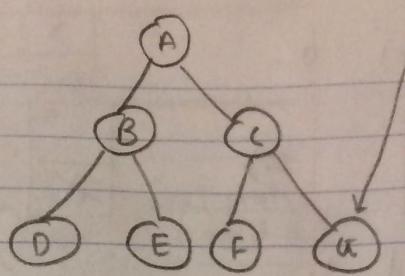


(not goal, marked explored
nothing to expand).

7. $\alpha|8|\times|8|8|8|u$



8. $\alpha|8|\times|8|R|F|G$

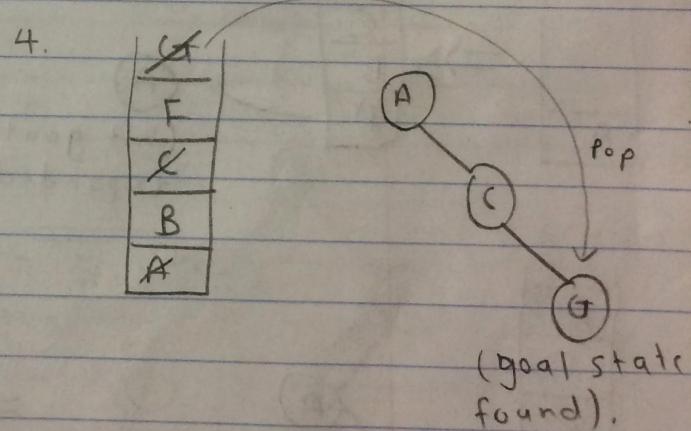
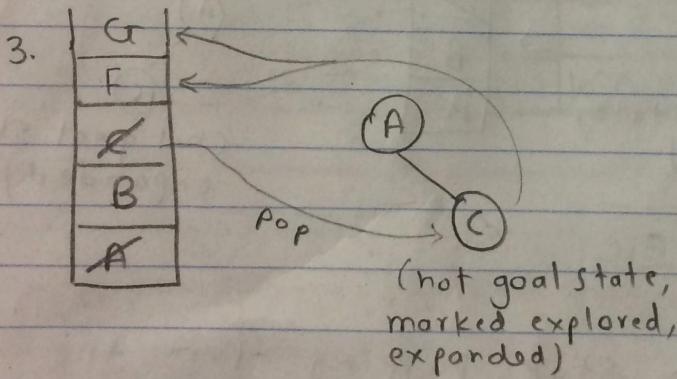
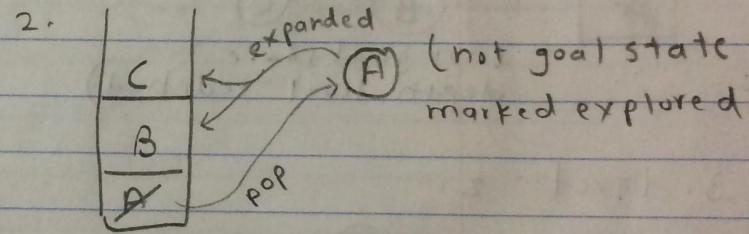
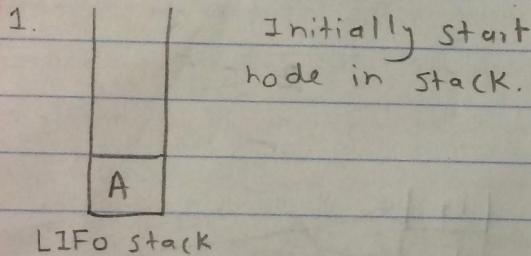


Note: from step 2, keep dequeuing the queue till it is empty.

Sequence \rightarrow

$A \rightarrow B \rightarrow C \rightarrow D \rightarrow E \rightarrow F \rightarrow G$

* Depth First Search.



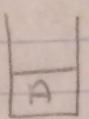
Note: from step 2 Start popping stack till it is empty or till goal state is found.

Sequence:

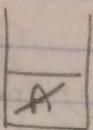
$A \rightarrow C \rightarrow G$

* Iterative Deepening Search.

1. level 0.



\Rightarrow

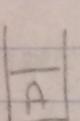


(not goal state, level halted).

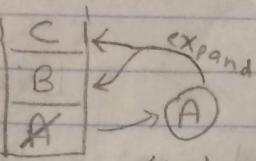
\Rightarrow stack empty.

level 1.

2. level 1

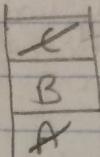


\Rightarrow

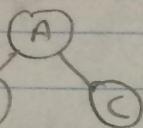
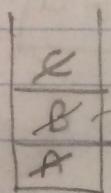


(not goal state, expanded).

\Rightarrow



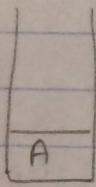
(not goal, depth level reached).



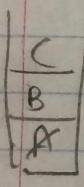
\Rightarrow stack empty.

(not goal state, depth level reached)

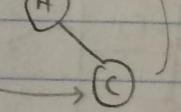
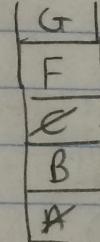
3. level 2.



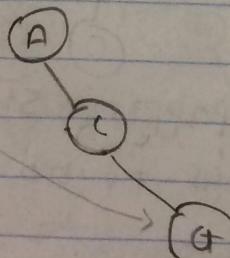
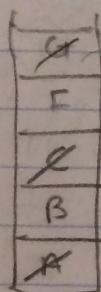
\Rightarrow



(not goal state, expanded)



(not goal state, expanded).



\Rightarrow stop popping from the queue

(goal state found)

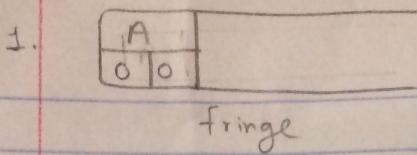
Note:- We increase level, d from 0 till depth ' d ' of the given graph.

We do not expand nodes beyond level d .

Path traversed.

$A \rightarrow C \rightarrow G$.

* Uniform Cost Search



2.

A	B	C
0	10	10

{A}.

3. sorting fringe

cumulative cost calculation

A	C	B	F	G
0	0	5	10	15

(A) → {A, C}

(not goal state, add in closed set, expand)

4.

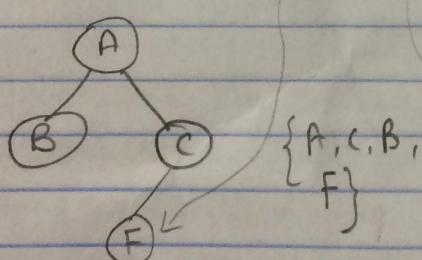
A	C	B	F	G
0	5	5	10	10

{A, C, B}

(not goal state, add in closed set, expand)

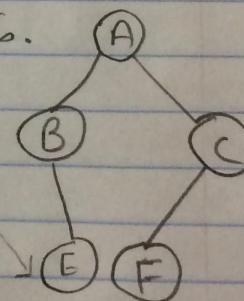
5. Sort fringe

A	C	B	F	E	G	D
0	0	5	5	10	10	10



(not goal state, add in closed set, leaf node)

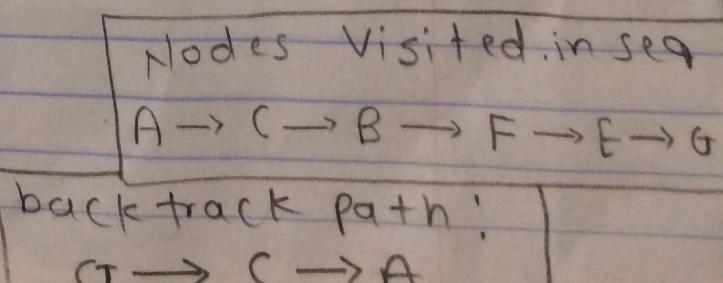
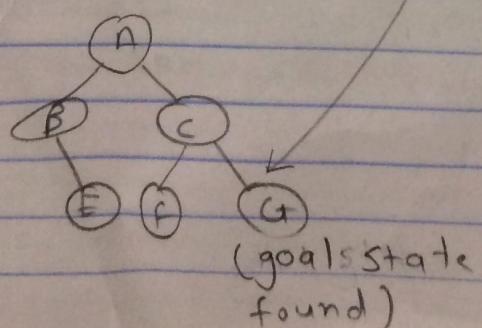
6.



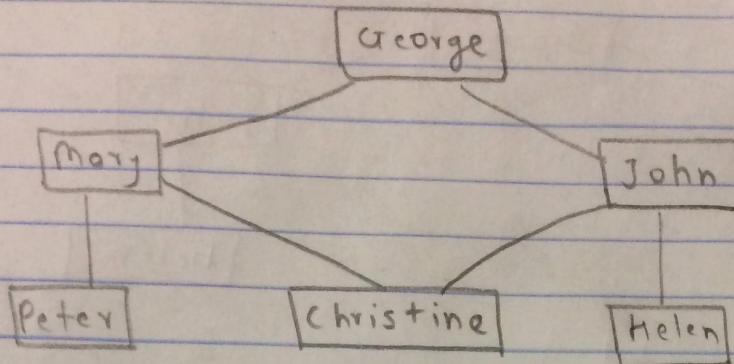
{A, C, B, F, E}

(not goal state, add in closed set, leaf node)

7.

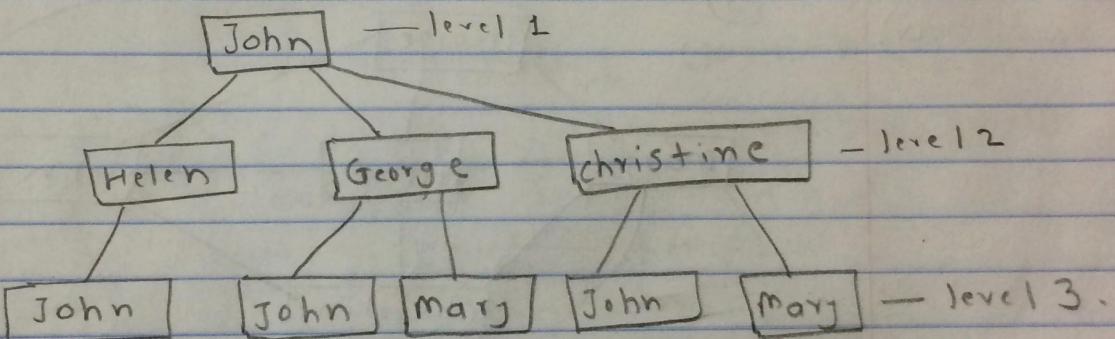


Question 2]



i) BFS, Iterative Deepening Search, Uniform cost Search for above given graph does provide correct number of degrees of separation.

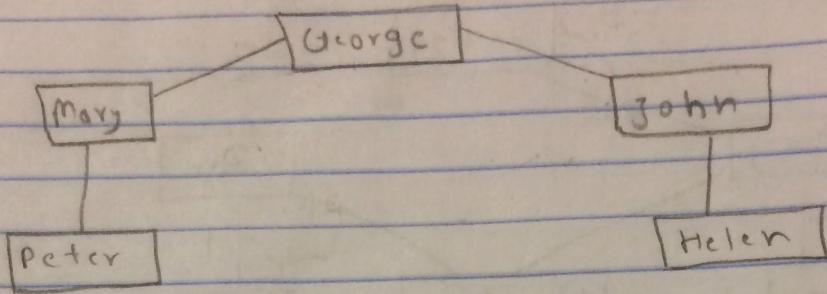
ii)



Search tree

Nodes in above search tree does not have one to one correspondence with vertices in SNG, meaning that though vertices in SNG are nodes in search tree SNG and search tree are not similar/analogs. Search tree does not have cyclic dependencies as in SNG. Search tree redundantly specifies paths between two nodes, hence there are multiple nodes representing same vertex in SNG.

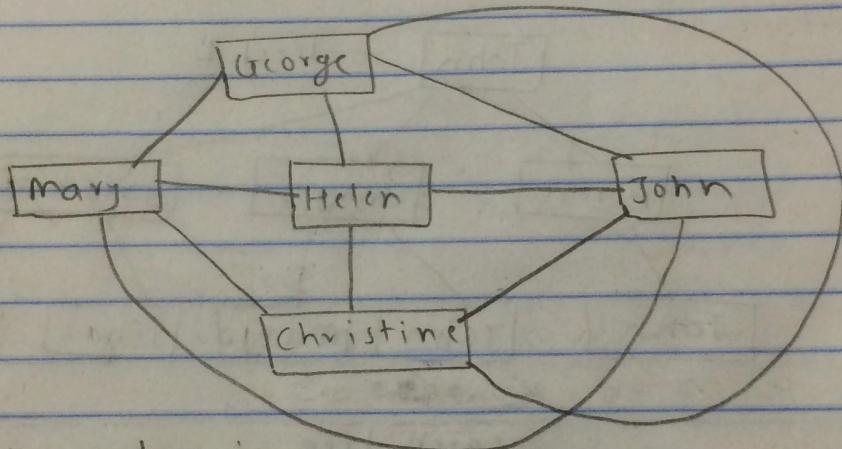
(iii)



In above SNG Peter has 4 degree of separation from Helen.

Helen has 4 degrees of separation from Peter.

(iv)



Every vertex is directly connected to every other vertex
fully connected graph.

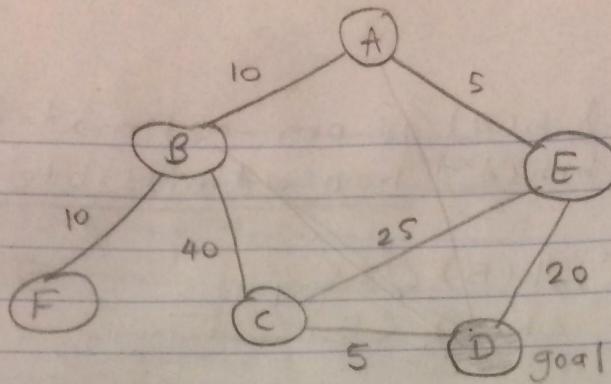
v)

For BFS search tree, if we have branching factor 'b' & depth as 'm'
total number of nodes = b^m ,
we want to store 1 million i.e 10^6 nodes, each representing a person

$$\therefore b^m = 10^6$$

\therefore we keep branching factor = 10 & depth = 6.

Q 3]



Heuristic 1]

$$h(A) = 5$$

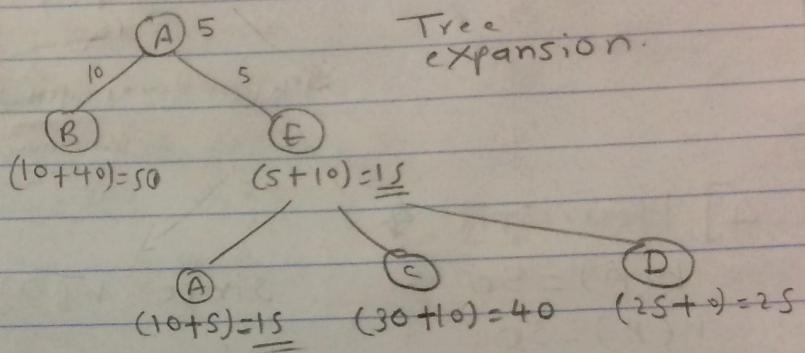
$$h(B) = 40$$

$$h(C) = 10$$

$$h(D) = 0$$

$$h(E) = 10$$

$$h(F) = 0$$



since C is directly connected to D & with distance 5 hence $h(C)$ is over-estimated hence

Non admissible

make $0 \leq h(C) \leq 5$

Heuristic 2]

$$h(A) = 8/\underline{11} \quad \text{Since node } \underline{D} \text{ is goal state}$$

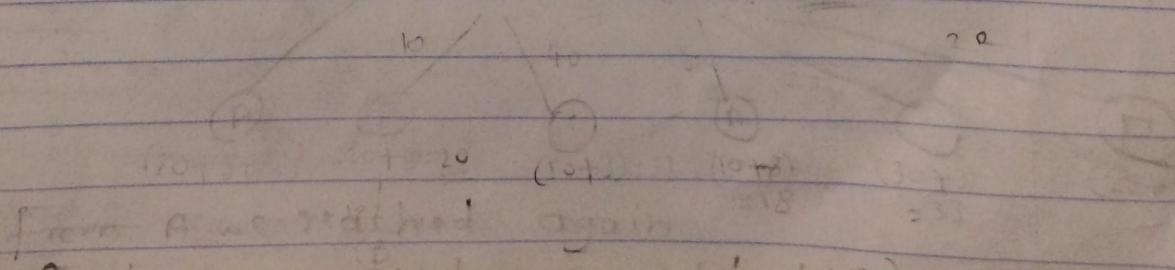
$$h(B) = 5 \quad h(D) \text{ should be } \underline{0} \text{ if hence } h(D) = 5$$

$$h(C) = 3 \quad \text{is over-estimated.}$$

$$h(D) = 5/\underline{0} \quad \therefore \underline{\text{Not Admissible.}}$$

$$h(E) = 5$$

$$h(F) = 0 \quad \text{update } \boxed{h(D)=0} \text{ to make it admissible}$$



3] Heuristic 3

$$h(A) = 35$$

$$h(B) = 30$$

$$h(C) = 20$$

$$h(D) = 0$$

$$h(E) = 0$$

$$h(F) = 50$$

$h(C), h(A)$ is over-estimated.
hence non admissible

$$0 \leq h(A) \leq 25$$

$$0 \leq h(C) \leq 5.$$

$$(10+35)$$

$$= 45$$

$$(30+20)$$

$$= 50$$

$$(25+0)$$

$$= 25$$

4] Heuristic 4

$$h(A) = 50$$

since $h(D) \neq 0$ it is not Admissible

$$h(B) = 50$$

let make $h(D) = 0$

$$h(C) = 50$$

$$0 \leq h(A) \leq 25$$

$$h(D) = 50/0$$

$$0 \leq h(B) \leq 45$$

$$h(E) = 50$$

$$0 \leq h(C) \leq 5$$

$$h(F) = 50$$

$$0 \leq h(E) \leq 20$$

5] Heuristic 5

$$h(A) = 0$$

Since no cost is over-estimated

$$h(B) = 0$$

this heuristic is Admissible.

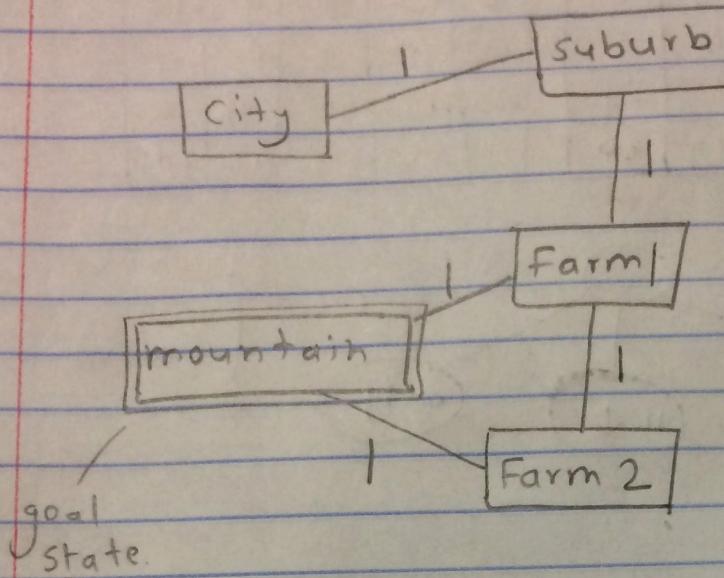
$$h(C) = 0$$

$$h(D) = 0$$

$$h(E) = 0$$

$$h(F) = 0$$

Question 4]



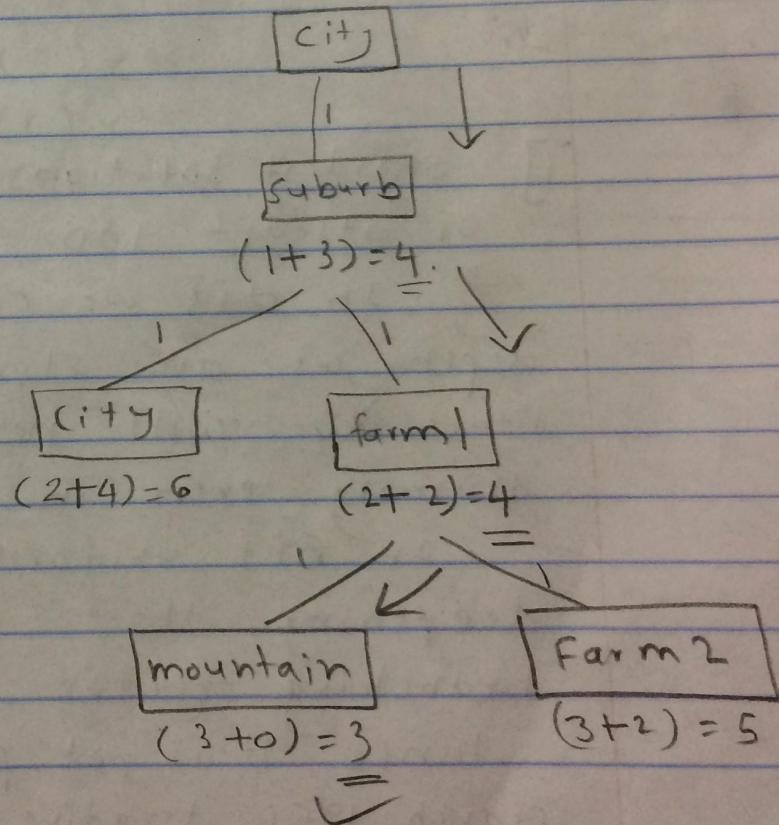
$$\rightarrow h(\text{mountain}) = 0$$

$$h(\text{city}) = 4$$

$$h(\text{farm1}) = 2$$

$$h(\text{Suburb}) = 3$$

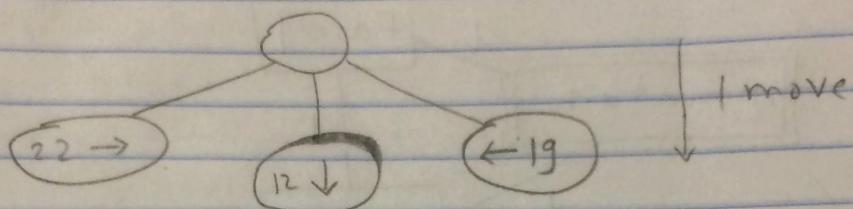
$$h(\text{Suburb}) = 3$$



Question 5

15	16	12	22	18	13	16	17	24	18	15	16	17	24	18
6	2	8	9	10	6	7	8	9	10	6	7	8	9	10
1	2	3	4	5	1	2	3	4	5	1	2	3	4	5
23	11	12	13	14	23	11	13	14	23	11	12	13	14	23
21	7	11	19	20	21	22	12	19	20	21	22	19	18	20

BFS :-



— depth d

Q] Shortest solution also needs more than or atleast 100 moves.

In DFS we can consider that at each depth we are storing only one node hence we will need atleast 100 kb of memory even in DFS.

In BFS, uniform cost search & iterative deepening there will be definitely branching factor more than 1 is needed.

hence it is not possible for BFS, Uniform cost search, DFS, iterative deepening search to store search nodes in 50 kb.

2] for all initial states, it takes at most 208 moves

hence depth of the search tree = 208

there are 4 possibilities to move tile up, down, right, left.

hence branching factor would be 4.

i) BFS \rightarrow Space needed to store all nodes in search tree would be $O(b^d)$
 $= 4^{208}$ Kb.

hence cannot guarantee.

ii) DFS \rightarrow Since in DFS if a path from root to leaf is not the path that includes goal state we can discard it hence, DFS needs space of $O(bm)$.

here $O(4 \times 208) = O(832)$ Kb.

But since the time complexity of DFS depends on size of state space which can be infinite, it is not guaranteed to obtain solution in finite time.

iii) Iterative deepening search - It needs space complexity of $O(bm) = O(832)$ Kb

It is same as DFS only with incremental levelling.

iv) Uniform cost Search - Space complexity needed is $O(b^d) = O(4^{208})$

Since it same as BFS with priority queue

Hence none of the above BFS, DFS, Uniform cost search, iterative deepening search can guarantee that we will never need more than 1200 Kb space to store search nodes.