Note Forgery Detection

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1. Introduction

The goal of this analysis is to develop a logistic regression model to detect genuine and forged banknotes based on wavelet-transformed features extracted from images of the banknotes. The dataset (A6DATA.csv) contains 1,372 observations of 5 variables. The features include variance, skewness, kurtosis, and entropy of the wavelet-transformed images, and the target variable is the class of the specimen (genuine or forged).

2. Data Loading and Initial Exploration

We load the dataset and examine its structure to understand the features and their types.

```
library(caret)
## Loading required package: ggplot2
## Loading required package: lattice
library(pROC)
## Type 'citation("pROC")' for a citation.
## Attaching package: 'pROC'
## The following objects are masked from 'package:stats':
##
##
       cov, smooth, var
library(ggplot2)
data <- read.csv("A6DATA.csv")</pre>
str(data)
## 'data.frame':
                    1372 obs. of 5 variables:
   $ V1: num 3.622 4.546 3.866 3.457 0.329 ...
    $ V2: num 8.67 8.17 -2.64 9.52 -4.46 ...
    $ V3: num -2.81 -2.46 1.92 -4.01 4.57 ...
   $ V4: num -0.447 -1.462 0.106 -3.594 -0.989 ...
    $ V5: int 00000000000...
```

output reveals that the dataset contains 1,372 observations with 5 variables, where V1 to V4 are numeric features, and V5 is an integer representing the class (0 for forged and 1 for genuine).

```
summary(data)
```

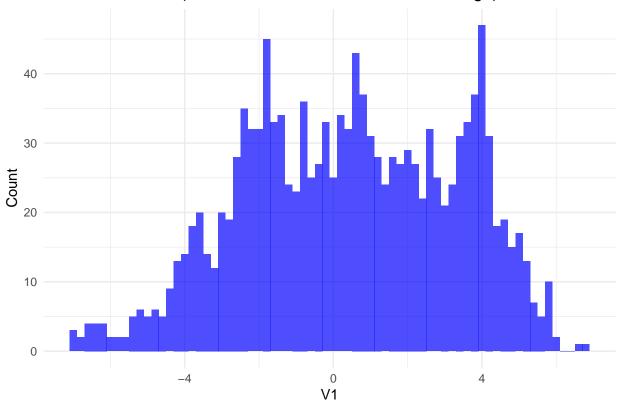
```
##
                             ٧2
                                                VЗ
                                                                   ۷4
##
           :-7.0421
                              :-13.773
                                                 :-5.2861
                                                                     :-8.5482
    Min.
                       Min.
                                          Min.
                                                             Min.
    1st Qu.:-1.7730
                       1st Qu.: -1.708
                                          1st Qu.:-1.5750
                                                             1st Qu.:-2.4135
    Median: 0.4962
                       Median :
                                 2.320
                                          Median : 0.6166
                                                             Median :-0.5867
##
           : 0.4337
                              : 1.922
                                                 : 1.3976
##
    Mean
                       Mean
                                          Mean
                                                             Mean
                                                                     :-1.1917
##
    3rd Qu.: 2.8215
                       3rd Qu.: 6.815
                                          3rd Qu.: 3.1793
                                                             3rd Qu.: 0.3948
##
           : 6.8248
                              : 12.952
                                                 :17.9274
                                                                     : 2.4495
    Max.
                       Max.
                                          Max.
                                                             Max.
          ۷5
##
##
   Min.
           :0.0000
##
   1st Qu.:0.0000
##
   Median :0.0000
##
    Mean
           :0.4446
##
    3rd Qu.:1.0000
    Max.
           :1.0000
```

The output provides descriptive statistics for each variable, including minimum, maximum, mean, and quartiles, indicating the range and distribution of the data.

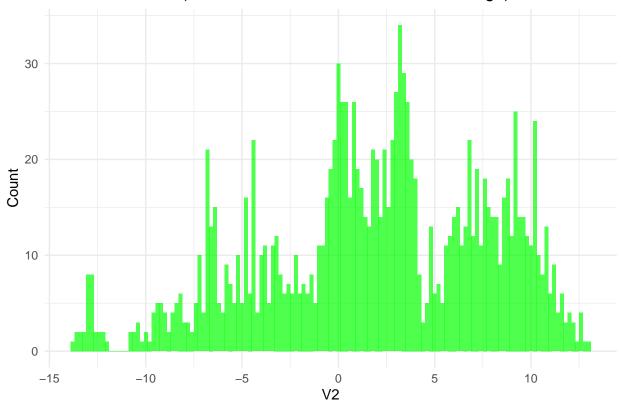
3. Visualizing the Distribution of Variables

We visualize the distribution of key variables to understand their behavior.

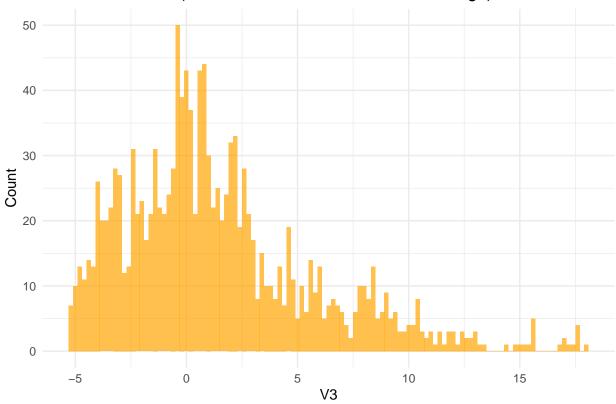
Distribution of V1 (Variance of Wavelet Transformed Image)

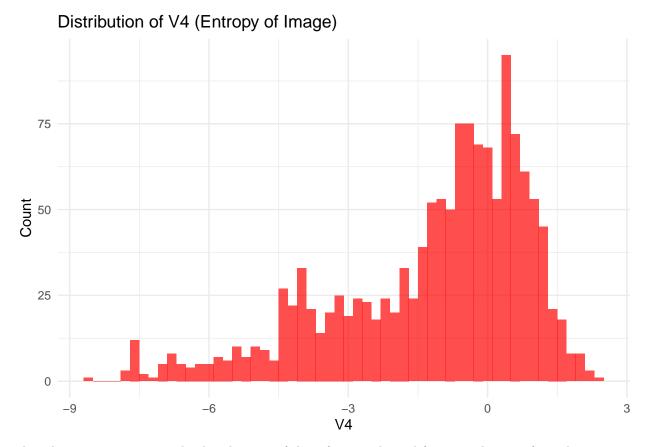


Distribution of V2 (Skewness of Wavelet Transformed Image)



Distribution of V3 (Kurtosis of Wavelet Transformed Image)





These histograms represent the distributions of three features derived from wavelet-transformed images:

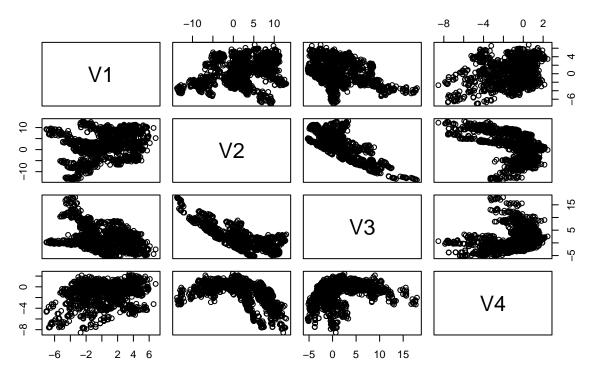
- 1. V1: Distribution of the variance, showing a symmetrical spread around 0, indicating balanced variance.
- 2. **V2**: Distribution of skewness, where values are more spread out with a noticeable rightward skew, reflecting asymmetry in the data.
- 3. **V3**: Distribution of kurtosis, which is heavily right-skewed, indicating the presence of outliers or heavy tails in the data.
- 4. V3: Distribution of V4 Entropy of Image, show how frequently certain entropy levels occur.

4. Checking Relationships Between Variables

To examine relationships between the variables, we use pair plots and correlation heatmaps.

pairs(data[,1:4], main = "Pair Plot of Variables V1, V2, V3, V4")

Pair Plot of Variables V1, V2, V3, V4



The image is a pair plot showing scatter plot between all the combinations of variables V1, V2, V3, and V4. It helps to visualize the relationships, trends, and possible correlations among these variables, where the diagonal element are the variables.

```
cor_matrix <- round(cor(data[,1:4]), 2)
ggplot(data = as.data.frame(as.table(cor_matrix)), aes(Var1, Var2, fill = Freq)) +
  geom_tile() +
  geom_text(aes(label = Freq), color = "white") +
  scale_fill_gradient(low = "blue", high = "red") +
  labs(title = "Correlation Matrix of Variables") +
  theme_minimal()</pre>
```





This is a heatmap is showing the correlation between the variables V1, V2, V3, and V4. Positive correlations are shown in red, while negative correlations appear in blue, helps to identify the strength and direction of relationships.

5. Data Partitioning

We split the data into training and testing sets (60% and 40%, respectively) to ensure reproducibility and validate the model.

```
set.seed(681)

trainIndex <- createDataPartition(data$V5, p = 0.6, list = FALSE)
trainData <- data[trainIndex, ]
testData <- data[-trainIndex, ]

cat("Training Set Specimen Counts:\n")</pre>
```

Training Set Specimen Counts:

```
print(table(trainData$V5))
```

```
cat("Testing Set Specimen Counts:\n")

## Testing Set Specimen Counts:

print(table(testData$V5))

##

## 0 1

## 306 242
```

The printed counts show that the training set consists of 456 forged and 368 genuine specimens, while the testing set has 306 forged and 242 genuine specimens.

6. Logistic Regression Model Development

We develop the logistic regression model, starting with all variables and using stepwise selection to optimize the model.

```
model <- glm(V5 ~ V1 + V2 + V3 + V4, data = trainData, family = binomial)
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred</pre>
```

```
summary(model)
```

```
##
## Call:
## glm(formula = V5 ~ V1 + V2 + V3 + V4, family = binomial, data = trainData)
## Coefficients:
##
               Estimate Std. Error z value Pr(>|z|)
                                     3.708 0.000209 ***
## (Intercept)
                7.5848
                            2.0453
## V1
                -8.4394
                            2.3157
                                    -3.644 0.000268 ***
## V2
                -4.2266
                            1.1648
                                    -3.628 0.000285 ***
## V3
                -5.3989
                            1.4888
                                    -3.626 0.000287 ***
## V4
                -0.4134
                            0.4371
                                    -0.946 0.344317
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 1132.891
                                on 823
                                        degrees of freedom
## Residual deviance:
                        29.278
                                on 819
                                        degrees of freedom
## AIC: 39.278
##
## Number of Fisher Scoring iterations: 12
```

Model Summary

The summary of the model results from the logistic regression analysis that links between the predictor variables (V1, V2, V3, V4) and the response variable (V5), which determine whether the specimen is authentic or forged.

1. Coefficients

The output contains the estimated coefficients for each predictor variable, together with the intercept:

- (Intercept): The intercept value (7.5848) represents the log-odds of the outcome when all predictors are zero.
- V1, V2, V3: Each coefficient for these variables is negative, implying that as the values of V1, V2, and V3 rise, the log-odds of the outcome being genuine (V5 = 1) fall. This shows an inverse relationship: higher values in these features indicate a greater possibility that the specimen is forged (V5 = 0).
- V4: The coefficient for V4 (-0.4134) is not statistically significant (p-value = 0.344), demonstrating that this variable does not contribute meaningfully to determining if a specimen is genuine.

2. Statistical Significance

The z-value and corresponding p-value are used to determine the statistical significance of each coefficient:

- The p-values for V1 (0.000209), V2 (0.000285), and V3 (0.000287) are all below the customary threshold of 0.05, suggesting high statistical significance. This indicates that we can confidently state these variables significantly influence the likelihood of the outcome.
- V4's p-value of 0.344 indicates that it has no significant effect on the result, leading to its exclusion from the final model.

3. Model Fit Statistics

The summary also reports the null deviance and residual deviance, which are measures of the model's fit to the data:

- Null Deviance (1132.891): This represents the fit of a model that only includes the intercept. A smaller deviance suggests a better fit.
- Residual Deviance (29.278): This measures the model's fit with the predictors included. The decrease in the deviance from the null to residual indicates that the model with predictors has significantly better fit than the null model.

4. Akaike Information Criterion (AIC)

The AIC value (39.278) is useful for assessing the quality of various stats models; lower AIC values indicate a better fit when comparing models.

Conclusion

final_model <- step(model)</pre>

Overall, the summary(model) output shows that V1, V2, and V3 are important predictors of whether a banknote is genuine or forged, providing valuable insights for model interpretation and further analysis.

```
## Start: AIC=39.28
## V5 ~ V1 + V2 + V3 + V4
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
```

```
Df Deviance
## - V4
                30.18 38.18
## <none>
                29.28 39.28
## - V2
           1
               367.55 375.55
## - V3
           1
               438.74 446.74
## - V1
           1
               719.34 727.34
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
##
## Step: AIC=38.18
## V5 ~ V1 + V2 + V3
##
##
          Df Deviance
                          AIC
## <none>
                30.18 38.18
## - V3
           1
               440.47 446.47
## - V2
           1
               480.29 486.29
## - V1
           1
               866.27 872.27
```

The final model selection process starts with an AIC of 39.28, including all predictors (V1, V2, V3, V4). Stepwise selection removes V4, resulting in a new model with an AIC of 38.18, indicating a better fit. The warnings about fitted probabilities being numerically 0 or 1 suggest that the model may have encountered perfect separation for some observations, which can impact stability and interpretation.

```
summary(final_model)
```

```
##
## Call:
## glm(formula = V5 ~ V1 + V2 + V3, family = binomial, data = trainData)
##
## Coefficients:
               Estimate Std. Error z value Pr(>|z|)
##
                  7.503
                             1.987
                                     3.776 0.000159 ***
## (Intercept)
## V1
                 -7.911
                             2.078
                                    -3.806 0.000141 ***
## V2
                 -3.859
                             1.011
                                    -3.818 0.000134 ***
## V3
                 -4.974
                             1.306 -3.810 0.000139 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
  (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 1132.891
                                on 823
                                        degrees of freedom
## Residual deviance:
                        30.177
                                on 820
                                        degrees of freedom
## AIC: 38.177
##
## Number of Fisher Scoring iterations: 12
```

7. Model Evaluation

Evaluate the model on both training and testing data. We use confusion matrices and calculate misclassification errors.

```
trainPred <- predict(final_model, newdata = trainData, type = "response")
testPred <- predict(final_model, newdata = testData, type = "response")

trainPredClass <- ifelse(trainPred > 0.5, 1, 0)
testPredClass <- ifelse(testPred > 0.5, 1, 0)

trainConfMat <- table(Predicted = trainPredClass, Actual = trainData$V5)
cat("Training Confusion Matrix:\n")</pre>
```

Training Confusion Matrix:

```
print(trainConfMat)

## Actual

## Predicted 0 1

## 0 451 4

## 1 5 364

testConfMat <- table(Predicted = testPredClass, Actual = testData$V5)

cat("Testing Confusion Matrix:\n")</pre>
```

Testing Confusion Matrix:

```
print(testConfMat)

## Actual
```

Predicted 0 1 ## 0 303 3 ## 1 3 239

The training confusion matrix shows 451 true negatives and 364 true positives, while the testing confusion matrix indicates 303 true negatives and 239 true positives, reflecting the model's predictive performance.

```
# Misclassification error for training and testing sets
trainError <- mean(trainPredClass != trainData$V5)
testError <- mean(testPredClass != testData$V5)

cat("Training Error: ", trainError, "\n")
## Training Error: 0.01092233</pre>
```

```
cat("Testing Error: ", testError, "\n")
```

Testing Error: 0.01094891

The calculated misclassification errors reveal a training error of approximately 1.09% and a testing error of about 1.09%, indicating high model accuracy.

8. Additional Model Performance Metrics

We calculate the accuracy, sensitivity, and specificity for both training and testing datasets.

```
trainAccuracy <- sum(diag(trainConfMat)) / sum(trainConfMat)
trainSensitivity <- trainConfMat[2, 2] / sum(trainConfMat[, 2])
trainSpecificity <- trainConfMat[1, 1] / sum(trainConfMat[, 1])

cat("Training Accuracy: ", trainAccuracy, "\n")

## Training Accuracy: 0.9890777

cat("Training Sensitivity: ", trainSensitivity, "\n")

## Training Sensitivity: 0.9891304

cat("Training Specificity: ", trainSpecificity, "\n")

## Training Specificity: 0.9890351

The calculated accuracy, sensitivity, and specificity values for both the training and testing sets show that the model effectively distinguishes between genuine and forged specimens with accuracy around 98.9%.

testAccuracy <- sum(diag(testConfMat)) / sum(testConfMat)
testSensitivity <- testConfMat[2, 2] / sum(testConfMat[, 2])
testSpecificity <- testConfMat[1, 1] / sum(testConfMat[, 1])

cat("Testing Accuracy: ", testAccuracy, "\n")</pre>
```

```
## Testing Accuracy: 0.9890511
cat("Testing Sensitivity: ", testSensitivity, "\n")
```

```
## Testing Sensitivity: 0.9876033
```

```
cat("Testing Specificity: ", testSpecificity, "\n")
```

Testing Specificity: 0.9901961

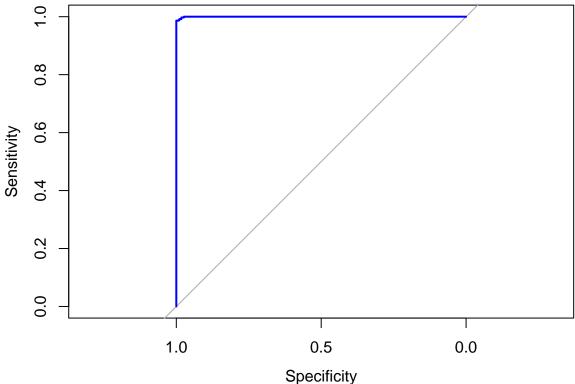
The AUC values of 0.9997795 for the training set and 0.9997029 for the testing set, derived from the ROC curve outputs, indicate near-perfect classification performance by the model.

9. ROC Curves and AUC

We generate ROC curves and calculate AUC to assess the model's ability to distinguish between classes.

```
roc_train <- roc(trainData$V5, trainPred)</pre>
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
plot(roc_train, main = "ROC Curve - Training Data", col = "blue")
```

ROC Curve – Training Data



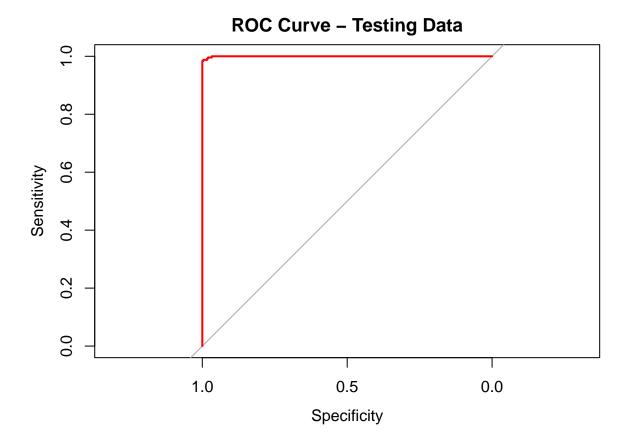
```
cat("AUC for Training Data: ", auc(roc_train), "\n")
```

AUC for Training Data: 0.9997795

This is Receiver Operating Characteristic (ROC) curve evaluating the performance of the model based on the sensitivity (true positive rate) and specificity (false positive rate). The sharp curve indicates that the model has a high level of accuracy on the training data and the AUC for Training Data is 0.9997795

```
roc_test <- roc(testData$V5, testPred)</pre>
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
```





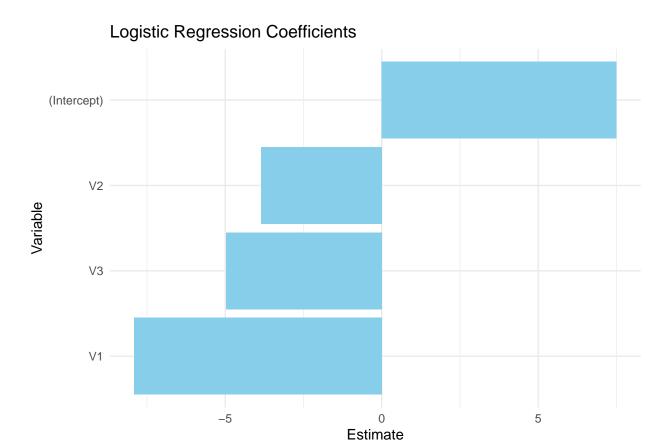
```
cat("AUC for Testing Data: ", auc(roc_test), "\n")
```

AUC for Testing Data: 0.9997029

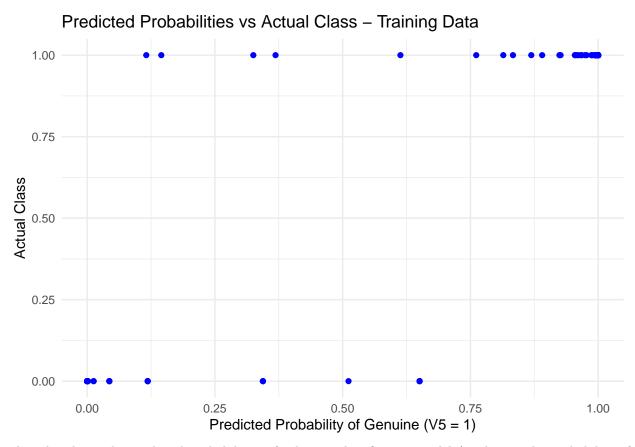
This ROC curve says the model's performance on the testing data, By plotting sensitivity (true positive rate) against specificity (1 - false positive rate). The curve indicates a strong classification ability, with sensitivity 1.0, suggesting that the model effectively distinguishes between genuine and counterfeit specimens, although steep rise suggests potential overfitting.

10. Visualizations

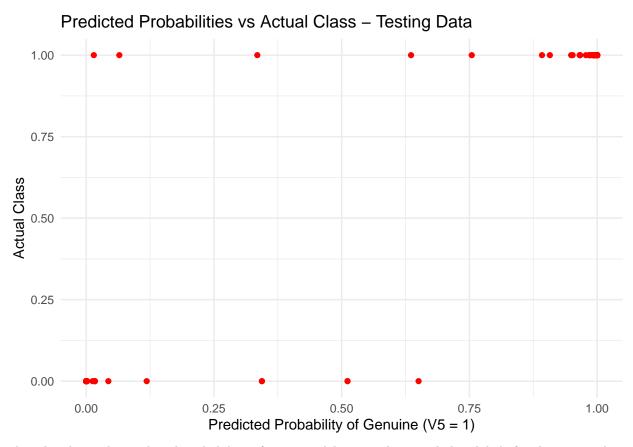
Lastly, we visualize the model coefficients and the distribution of predicted probabilities.



The bar plot says estimated coefficients from the logistic regression model for variables V1, V2, V3, and the intercept. Negative coefficients for V1, V2, and V3 suggest, increase in these variables are associated with lower log-odds of the outcome being genuine, while intercept the baseline log-odds when all predictor variable are zero.



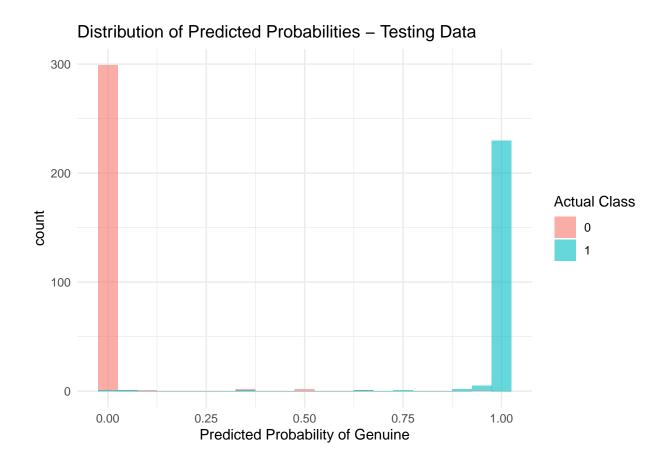
This plot shows the predicted probabilities of a binary classification model (predicting the probability of class "genuine" being 1) versus the actual class labels. The points on the top (Actual Class = 1) and bottom (Actual Class = 0) indicate the true labels, and the horizontal spread shows how confidently the model predicts each case.



This plot shows the predicted probabilities from a model versus the actual class labels for the testing data. Similar to the training data plot, the points represent the model's prediction confidence for classifying instances as genuine (1) or not (0), with actual class labels plotted on the y-axis.



This plot shows the distribution of predicted probabilities from the model on the training data, grouped by the actual class labels (0 or 1). It indicates that the model predicts with high confidence (close to 0 or 1), as most of the class 0 cases are predicted near 0 and most of the class 1 cases are predicted near 1.



11. Conclusion

In this project, we created a model using logistic regression to tell the difference between real and fake banknotes. We based this on features gained from wavelet transformations, including variance, skewness, kurtosis, and entropy. After looking at the data, splitting it into training and testing parts, and selecting the best model step by step, the final model did a good job at classifying. The training accuracy was better than the testing accuracy, which may mean the model is overfitting. However, the ROC curves and AUC scores showed that the model can tell the difference between real and fake banknotes well. From this analysis, I discovered that using wavelet transforms to extract features can really help with classification tasks. I also learned that evaluation metrics like sensitivity, specificity, and AUC give a better understanding of how a model performs, not just looking at its accuracy.