

1) houses ( $m$ ) = 2000  
features ( $n$ ) = 15

a) Total Count of elements in the Matrix A

$$2000 \times 15 = 30,000$$

b) SVD on the matrix

$U$  = left matrix

$\Sigma$  = Sigma

$V$  = right matrix

$$A = 2000 \times 15 = 30,000$$

$$U = 2000 \times 2000 = 4,000,000$$

$$V^T = 15 \times 15 = 225$$

$$\Sigma = 2000 \times 15 = 30,000$$

Total no of elements required for SVD

$$= 4,000,000 + 30,000 + 225$$
$$= 4,030,225$$

c) SVD with  $k=5$  Components

No of elements we need to preserve

$$A = 2000 \times 15 = 30,000$$

$$U = 2000 \times 5 = 10,000$$

$$V = 5 \times 15 = 75$$

$$\Sigma = 5 \times 5 = 25$$

Total elements required to preserve

$$U + \Sigma + V$$

$$= 10,000 + 25 + 75$$

$$= 10,100 \text{ elements}$$