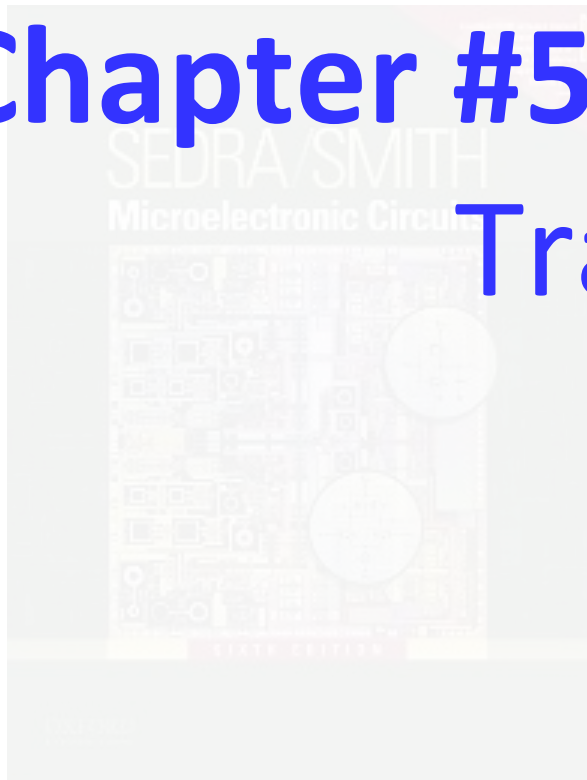


# Chapter #5: Bipolar Junction Transistors



# Introduction

## ■ IN THIS CHAPTER YOU WILL LEARN

- The **physical structure** of the bipolar transistor and how it works.
- How the voltage between two terminals of the transistor **controls the current that flows through the third terminal**, and the equations that describe these current-voltage relationships.
- How to **analyze and design circuits** that contain bipolar transistors, resistors, and dc sources.
- How the transistor can be used to **make an amplifier**.

# Introduction

## ■ IN THIS CHAPTER YOU WILL LEARN

- How to obtain **linear amplification** from the fundamentally nonlinear BJT.
- The **three basic ways for connecting a BJT** to be able to construct amplifiers with different properties.
- **Practical circuits** for bipolar-transistor amplifiers that can be constructed by using discrete components.

# Introduction

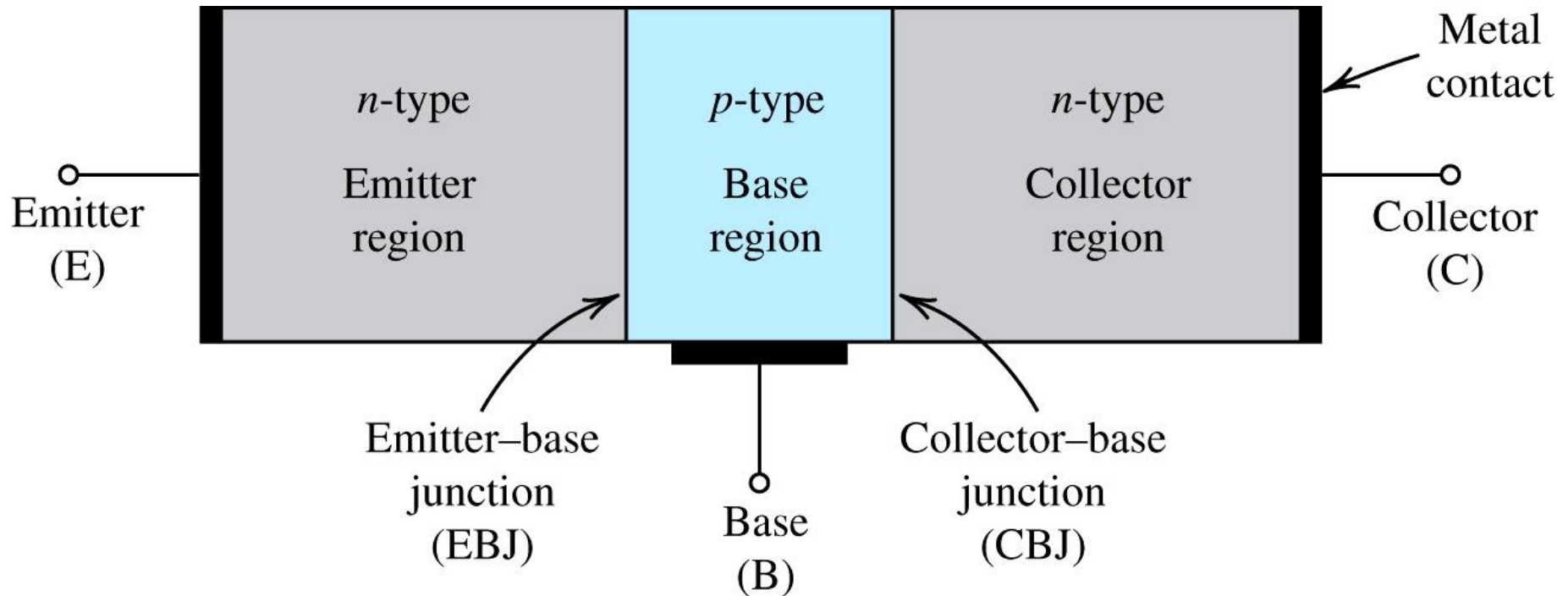
- This chapter examines another **three-terminal device**.
  - **bipolar junction transistor**
    - Presentation of this material mirrors **chapter 5**.
- BJT was **invented in 1948** at Bell Telephone Laboratories.
  - Ushered in a new era of **solid-state circuits**.
  - It was **replaced by MOSFET** as predominant transistor used in modern electronics.

## 5.1. Device Structure and Physical Operation

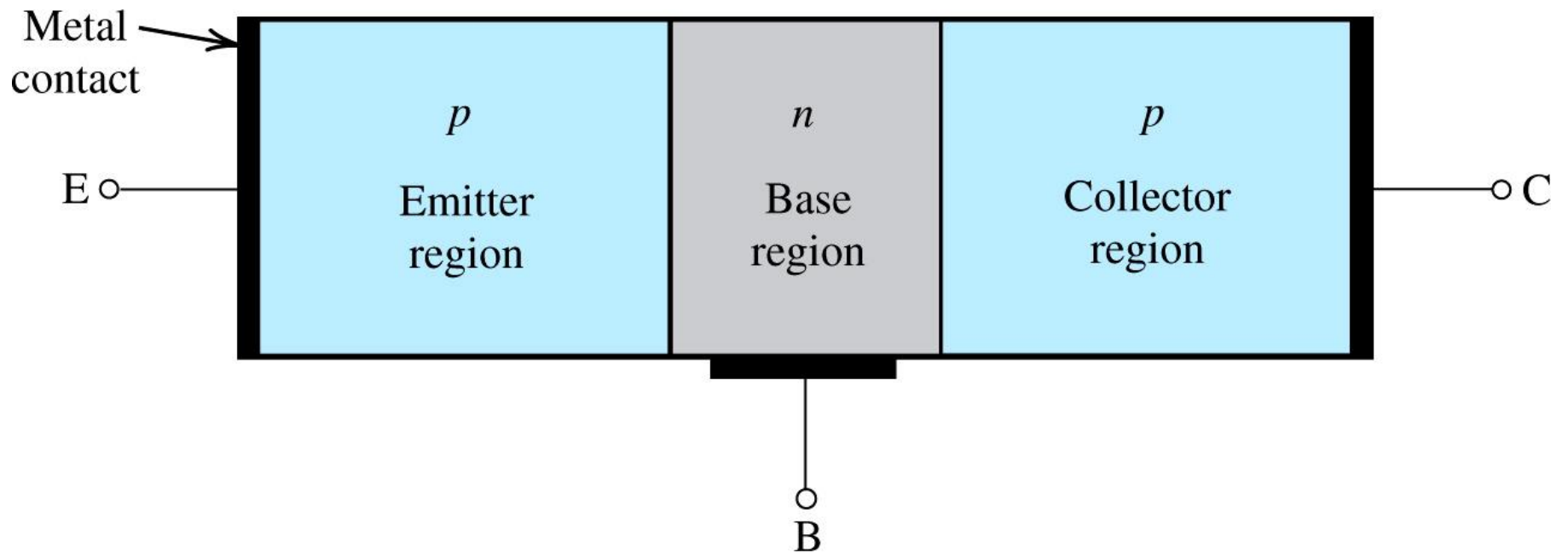
- Figure 5.1. shows **simplified structure** of BJT.
- Consists of **three semiconductor regions**:
  - **emitter** region ( $n$ -type)
  - **base** region ( $p$ -type)
  - **collector** region ( $n$ -type)
- Type described above is referred to as *npn*.
  - However, *pnp* types do exist.

## 5.1.1. Simplified Structure and Modes of Operation

- Transistor consists of **two *pn*-junctions**:
  - **emitter-base** junction (EBJ)
  - **collector-base** junction (CBJ)
- Operating **mode** depends on biasing.
  - **active** mode – used for amplification
  - **cutoff** and **saturation** modes – used for switching.



**Figure 5.1:** A simplified structure of the *npn* transistor.



**Figure 5.2:** A simplified structure of the  $pnp$  transistor.



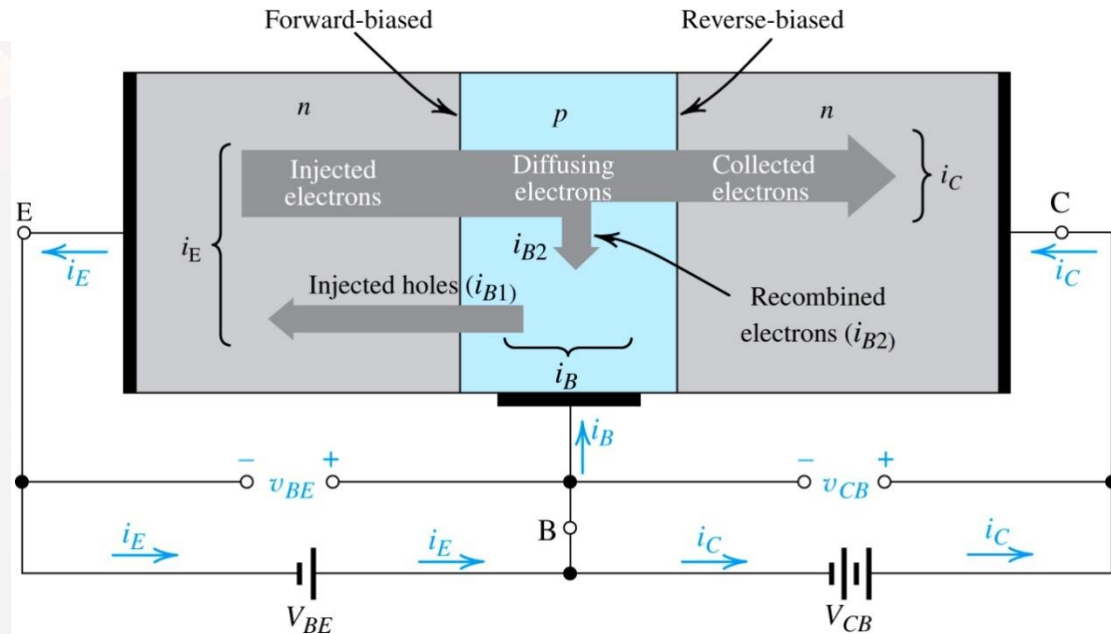
# Modes Of Operation in BJT

- There are two diode PN junctions involved – Emitter Base or EB and Collector Base or CB.
- Each can be set in forward or reverse mode. This gives rise to 4 combinations:

Mode	EB Junction	CB Junction	Used as
<b>Cut Off</b>	<b>Reverse</b>	<b>Reverse</b>	<b>Switch OFF</b>
<b>Active</b>	<b>Forward</b>	<b>Reverse</b>	<b>Amplifier</b>
<b>Reverse Active</b>	<b>Reverse</b>	<b>Forward</b>	<b>Not Used</b>
<b>Saturation</b>	<b>Forward</b>	<b>Forward</b>	<b>Switch ON</b>

## 5.1.2. Operation of the *npn*-Transistor in the Active Mode

- Active mode is “most important.”
- Two external voltage sources are required for biasing to achieve it.
- Refer to Figure 5.3.



**Figure 5.3:** Current flow in an *npn* transistor biased to operate in the active mode. (Reverse current components due to drift of thermally generated minority carriers are not shown.)

# Current Flow

- Forward bias on emitter-base junction will **cause current to flow**.
- This current has **two components**:
  - **electrons** injected from emitter into base
  - **holes** injected from base into emitter.
- It will be shown that **first (of the two above) is desirable**.
  - This is achieved with **heavy doping of emitter**, light doping of base.

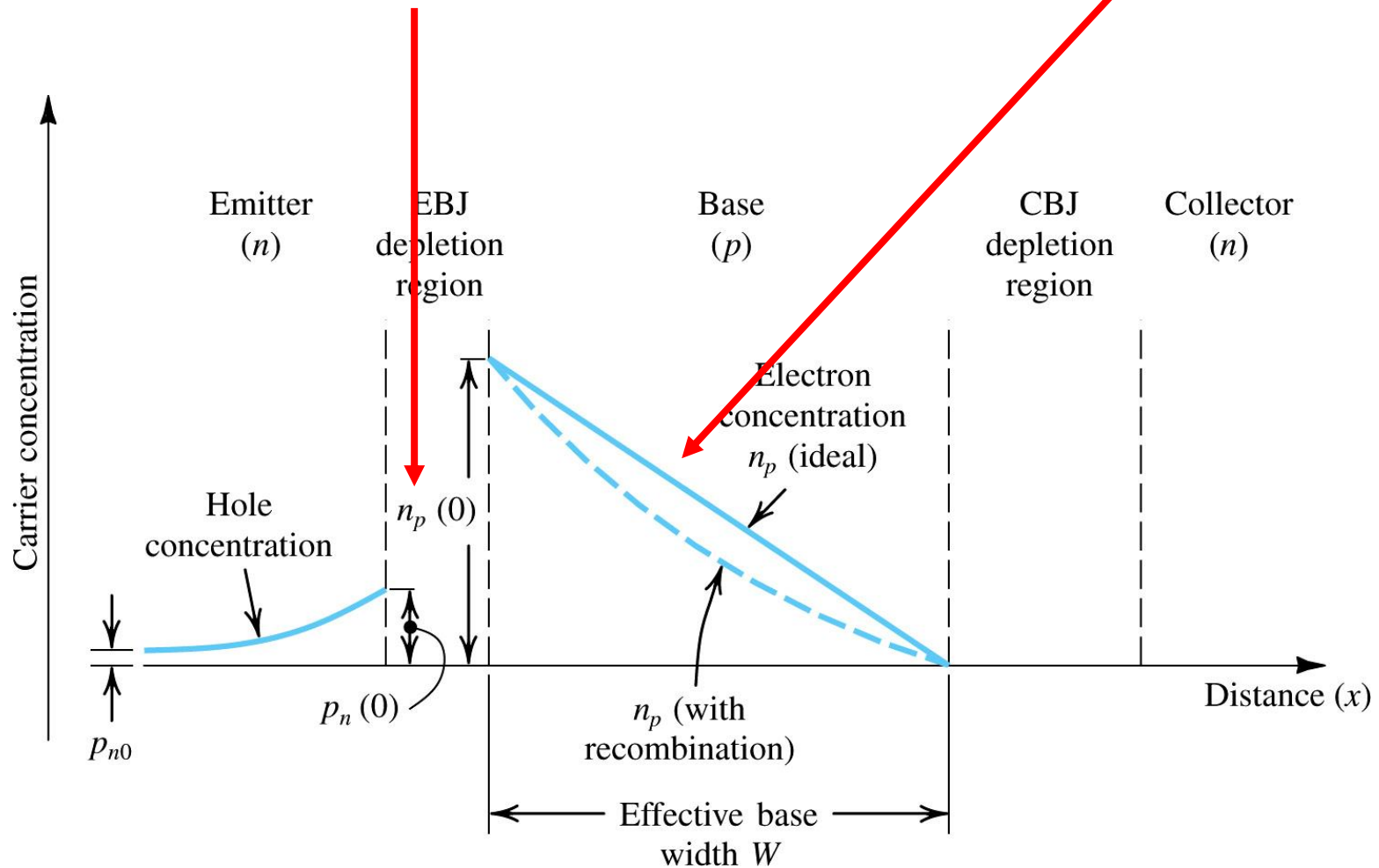
# Current Flow

- **emitter current** ( $i_E$ ) – is current which **flows across EBJ**
  - Flows “out” of emitter lead
- **minority carriers** – in  $p$ -type region.
  - These electrons will be **injected from emitter** into base.
  - Opposite direction.
- Because base is thin, concentration of excess minority carriers within it **will exhibit constant gradient.**

$n_p(x)$  = concentration of minority carriers at position  $x$  (where 0 represents EBJ boundary)  
 $n_{p0}$  = thermal-equilibrium value of minority carrier (electron) concentration in base region  
 $v_{BE}$  = voltage applied across base-emitter junction  
 $V_T$  = thermal voltage (constant)

$$(eq5.1) \quad n_p(0) = n_{p0} e^{v_{BE}/V_T}$$

Straight line represents constant gradient.



**Figure 6.4** Profiles of minority-carrier concentrations in the base and in the emitter of an  $nnp$  transistor operating in the active mode:  
 $v_{BE} > 0$  and  $v_{CB} \geq 0$ .

# Current Flow

- Concentration of **minority carrier  $n_p$  at boundary EBJ** is defined by (5.1).
- Concentration of **minority carriers  $n_p$  at boundary of CBJ** is zero.
  - Positive  $v_{CB}$  causes these electrons to be swept across junction.

$n_p(x)$  = concentration of minority carriers a position...  
 ... $x$  (where 0 represents EBJ boundary)  
 $n_{p0}$  = thermal-equilibrium value of minority carrier...  
 ...(electron) concentration in base region  
 $v_{BE}$  = voltage applied across base-emitter junction  
 $V_T$  = thermal voltage (constant)

$$\text{(eq5.1)} \quad n_p(0) = n_{p0} e^{v_{BE}/V_T}$$

# Current Flow

- Tapered minority-carrier concentration profile exists.
- It causes **electrons injected into base to diffuse** through base toward collector.
- As such, **electron diffusion current** ( $I_n$ ) exists.

$A_E$  = cross-sectional area of the base-emitter junction  
 $q$  = magnitude of the electron charge  
 $D_n$  = electron diffusivity in base  
 $W$  = width of base

$$(eq5.2) \quad I_n = A_E q D_n \frac{dn_p(x)}{dx}$$

$$(eq5.2) \quad I_n = A_E q D_n \left( \frac{-dn_p(0)}{W} \right)$$

this simplification  
 may be made if  
 gradient assumed  
 to be straight line

# Current Flow

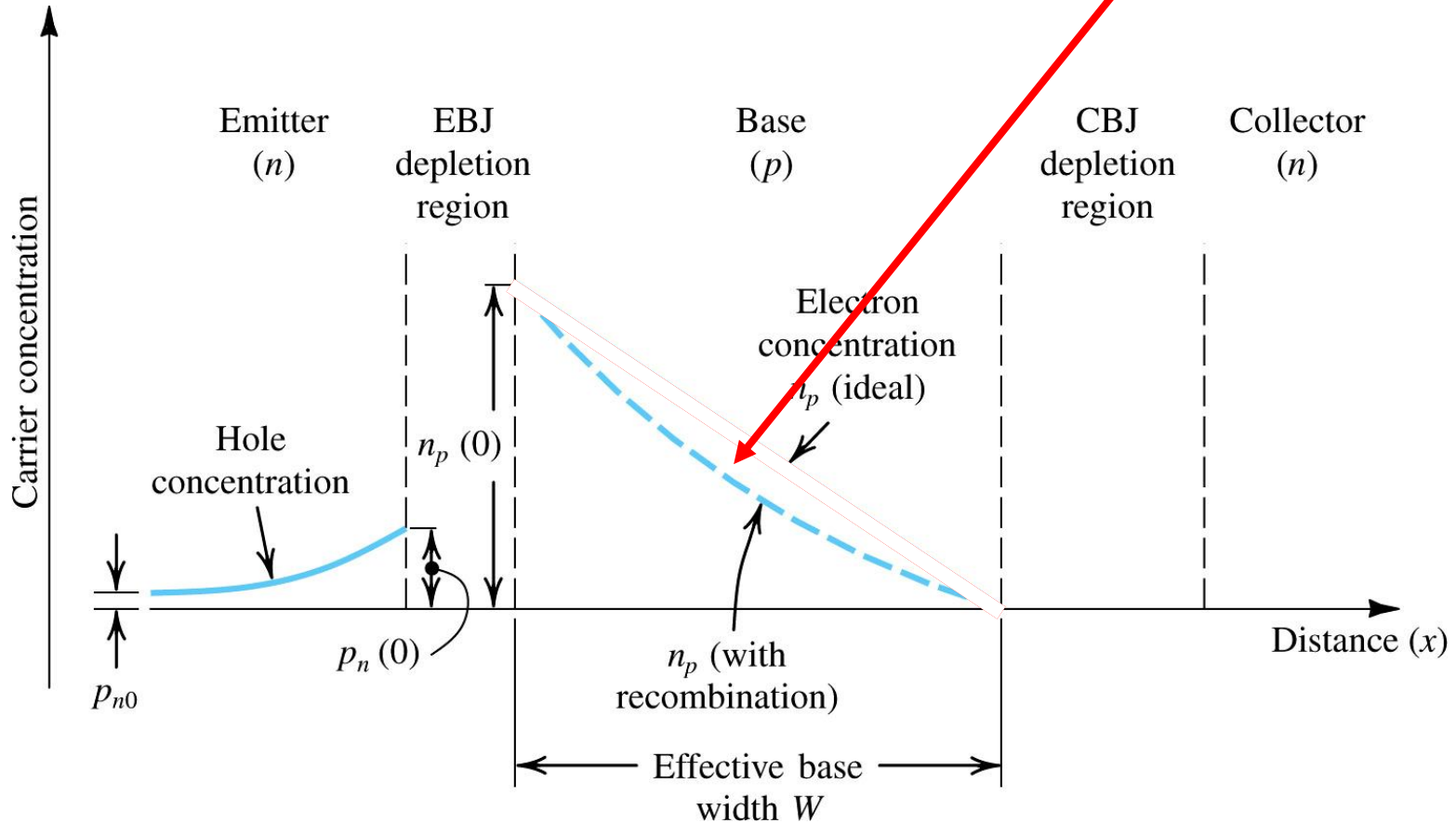
- Some “diffusing” electrons **will combine with holes** (majority carriers in base).
- Base is thin, however, and **recombination is minimal**.
- Recombination does, however, **cause gradient to take slightly curved shape**.
  - The straight line is assumed.



$n_p(x)$  = concentration of minority carriers at position  $x$  (where 0 represents EBJ boundary)  
 $n_{p0}$  = thermal-equilibrium value of minority carrier (electron) concentration in base region  
 $v_{BE}$  = voltage applied across base-emitter junction  
 $V_T$  = thermal voltage (constant)

$$(eq6.1) \quad n_p(0) = n_{p0} e^{v_{BE}/V_T}$$

Recombination causes actual gradient to be curved, not straight.



**Figure 6.4** Profiles of minority-carrier concentrations in the base and in the emitter of an  $nnp$  transistor operating in the active mode:  
 $v_{BE} > 0$  and  $v_{CB} \geq 0$ .

# The Collector Current

- It is observed that **most diffusing electrons will reach boundary of collector-base depletion region.**
- Because collector is more positive than base, these **electrons are swept into collector.**
  - collector current ( $i_C$ )** is approximately equal to  $I_n$ .
  - $i_C = I_n$

$$(eq5.3) \quad i_C = I_s e^{v_{BE} / V_T}$$


---

saturation current:  $I_s = \frac{A_E q D_n n_{p0}}{W}$

---

$$(eq5.4) \quad I_s = \frac{A_E q D_n}{W} \frac{n_i^2}{N_A}$$

$n_i$  = intrinsic carrier density  
 $N_A$  = doping concentration of base

# The Collector Current

- Magnitude of  $i_C$  is independent of  $v_{CB}$ .
  - As long as collector is positive, with respect to base.
- **saturation current ( $I_S$ )** – is inversely proportional to  $W$  and directly proportional to area of EBJ.
  - Typically between  $10^{-12}$  and  $10^{-18}A$
  - Also referred to as **scale current**.

# The Base Current

- **base current ( $i_B$ )** – composed of **two components**:
  - $i_{b1}$  – due to **holes injected from base** region into emitter.
  - $i_{b2}$  – due to **holes that have to be supplied by external circuit** to replace those recombined.

$\beta$  = transistor parameter

$$(eq5.10) \quad i_B = \frac{i_C}{\beta}$$

---


$$(eq5.11) \quad i_B = \frac{I_S}{\beta} e^{v_{BE} / V_T}$$

# The Base Current

- **common-emitter current gain ( $\beta$ )** – is influenced by **two factors**:
  - width of base region ( $W$ )
  - relative doping of base emitter regions ( $N_A/N_D$ )
- **High Value of  $\beta$** 
  - **thin base** (small  $W$  in nano-meters)
  - **lightly doped base / heavily doped emitter** (small  $N_A/N_D$ )

# The Emitter Current

- All current which enters transistor must leave.

- $i_E = i_C + i_B$

- Equations (5.13) through (5.19) expand upon this idea.

this expression is generated through combination of (5.10) and 5.13

(eq5.14/5.15) 
$$i_E = \frac{\beta + 1}{\beta} i_C = \frac{\beta + 1}{\beta} \underbrace{\left( I_S e^{v_{BE}/V_T} \right)}_{i_C}$$

(eq5.16) 
$$i_C = \alpha i_E$$

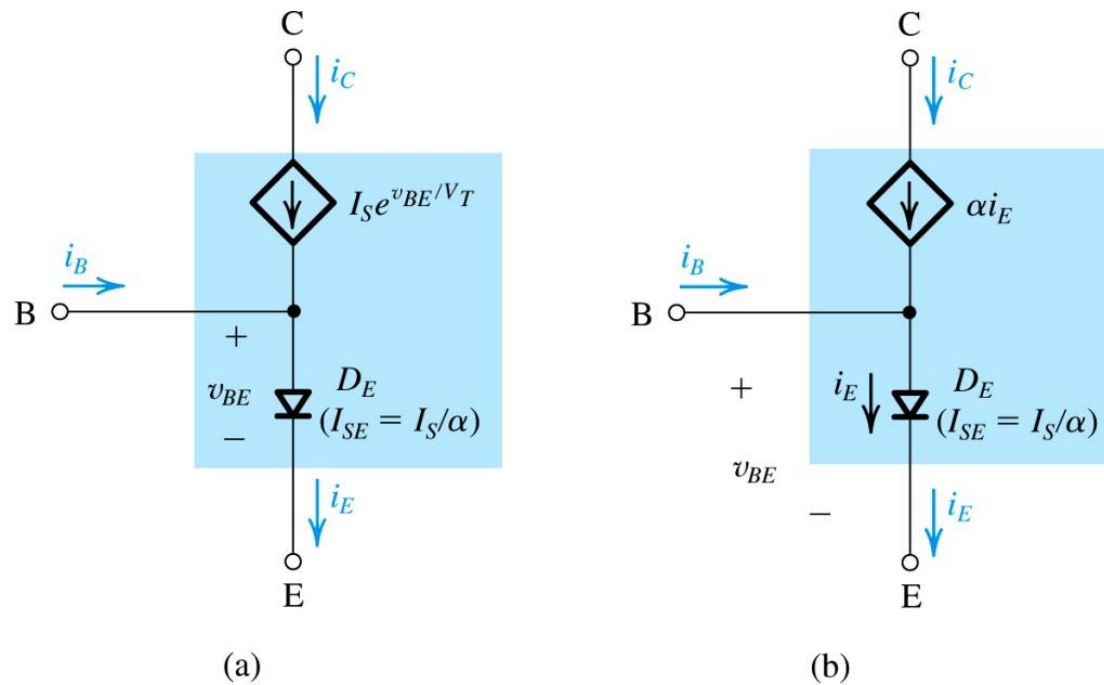
this parameter is referred to as **common-base current gain**

(eq5.17) 
$$\alpha = \frac{\beta}{\beta + 1}$$
 (eq5.19) 
$$\beta = \frac{\alpha}{1 - \alpha}$$

(eq5.18) 
$$i_E = \frac{I_S}{\alpha} e^{v_{BE}/V_T}$$

# Recapitulation and Equivalent-Circuit Models

- Previous slides present **first-order BJT model**.
  - Assumes ***npn* transistor in active mode**.
- Basic relationship is collector current ( $i_C$ ) is **related exponentially** to forward-bias voltage ( $v_{BE}$ ).
  - It remains independent of  **$v_{CB}$  as long as this junction remains reverse biased**.
    - $v_{CB} > 0$



**Figure 5.5:** Large-signal equivalent-circuit models of the *npn* BJT operating in the forward active mode.

## Two models of NPN transistor:

### 1. Voltage Controlled Current Source

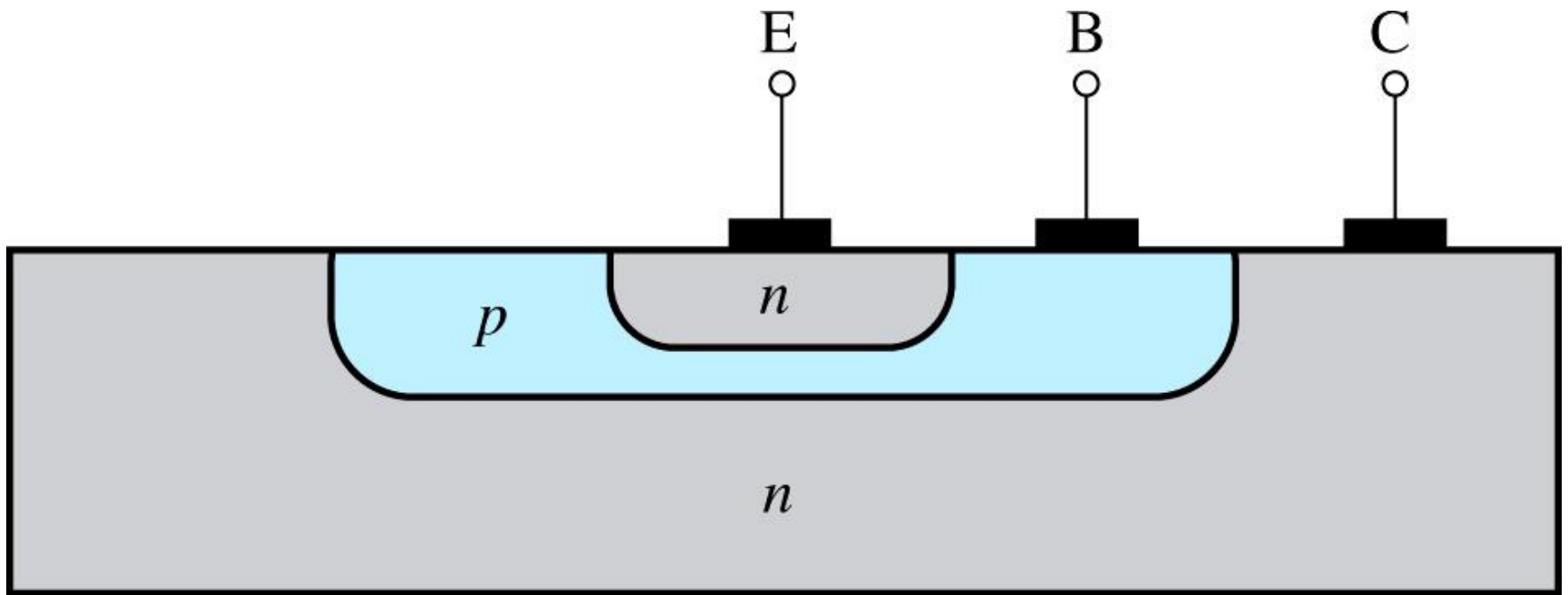
- $i_C$  proportional to  $\exp(v_{BE})$  - **nonlinear**
- Ideal diode  $D_E$  between B and E.
- $\alpha$  is forward active mode value close to 1.

### 2. Current Controlled Current Source



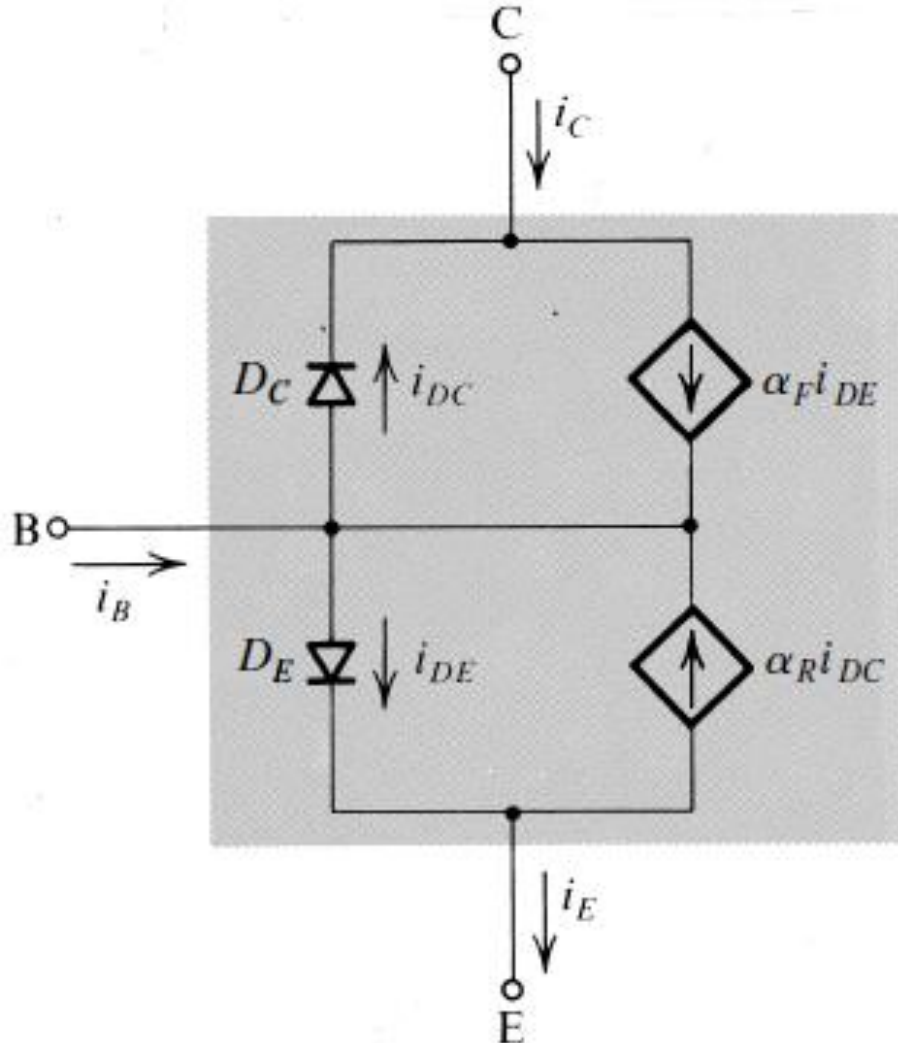
## 5.1.3. Structure of Actual Transistors

- Figure 5.6 shows a **more realistic BJT cross-section**.
- Collector **virtually surrounds** entire emitter region.
  - This makes it difficult for electrons injected into base to **escape collection**.
- Device is **not symmetrical**.
  - As such, emitter and collector **cannot be interchanged**.
  - Device is **uni-directional**.



**Figure 5.6:** Cross-section of an  $npn$  BJT.

# EBERS MOLL (EM) MODEL FOR BJT



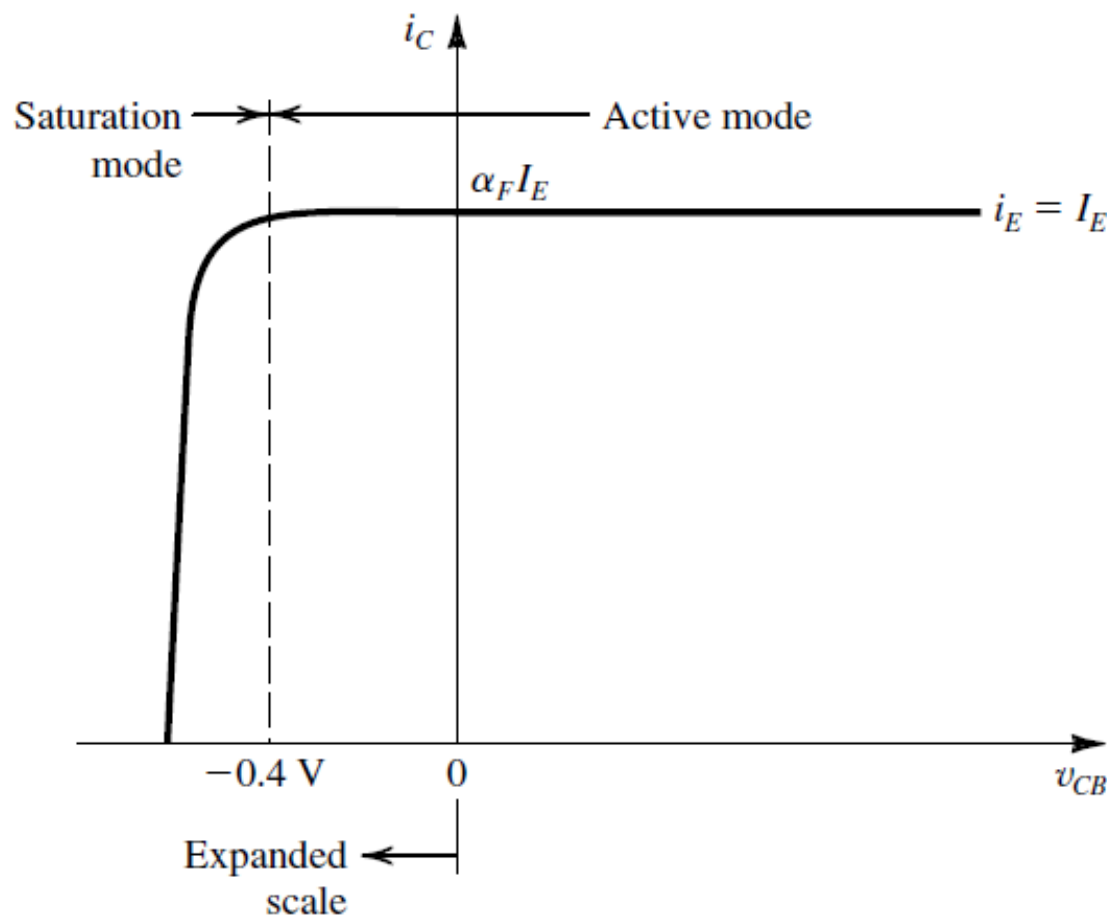
1. This is combination of two models – forward and reverse useful to predict behavior in all modes.
2. Diode  $D_C$  and ccs  $\alpha_R i_{DC}$
3. Diode  $D_E$  and ccs  $\alpha_F i_{DE}$

# EBERS MOLL (EM) MODEL FOR BJT

- EM model gives more accurate estimates of terminal currents -  $i_C$ ,  $i_B$  and  $i_E$  using two components – forward mode and reverse mode currents.
- In forward active mode, when  $v_{CB} > 0$ , the leakage current in reversed CB junction are very small and can be neglected leading to original current equations.

# 1.5. Operation in Saturation Mode

$i_C$ - $v_{CB}$  characteristics when NPN driven by a cc source in emitter

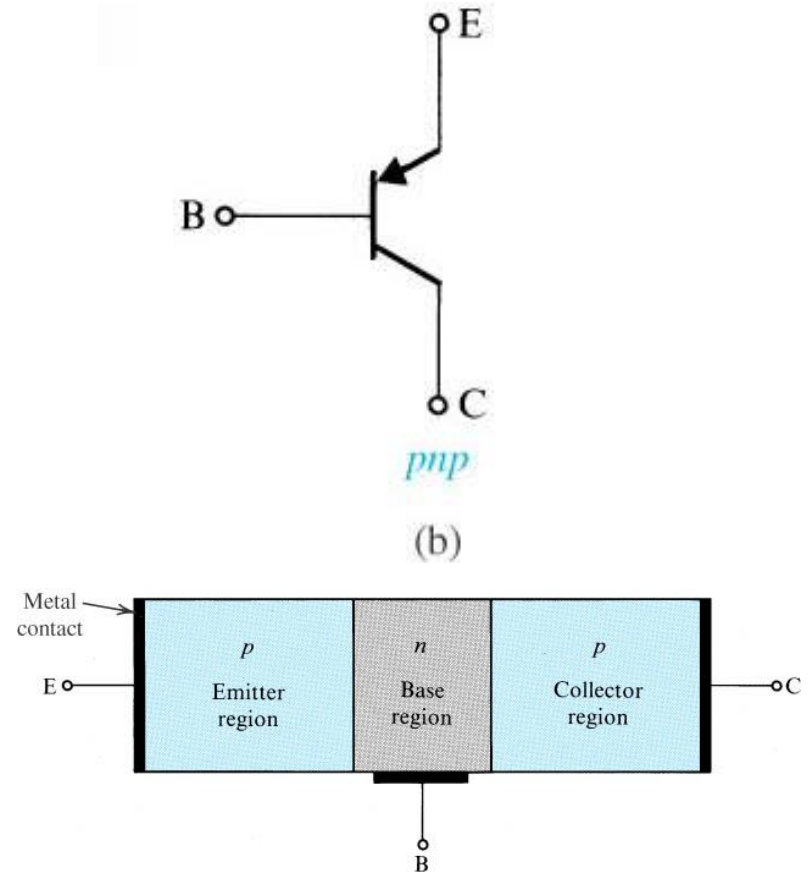
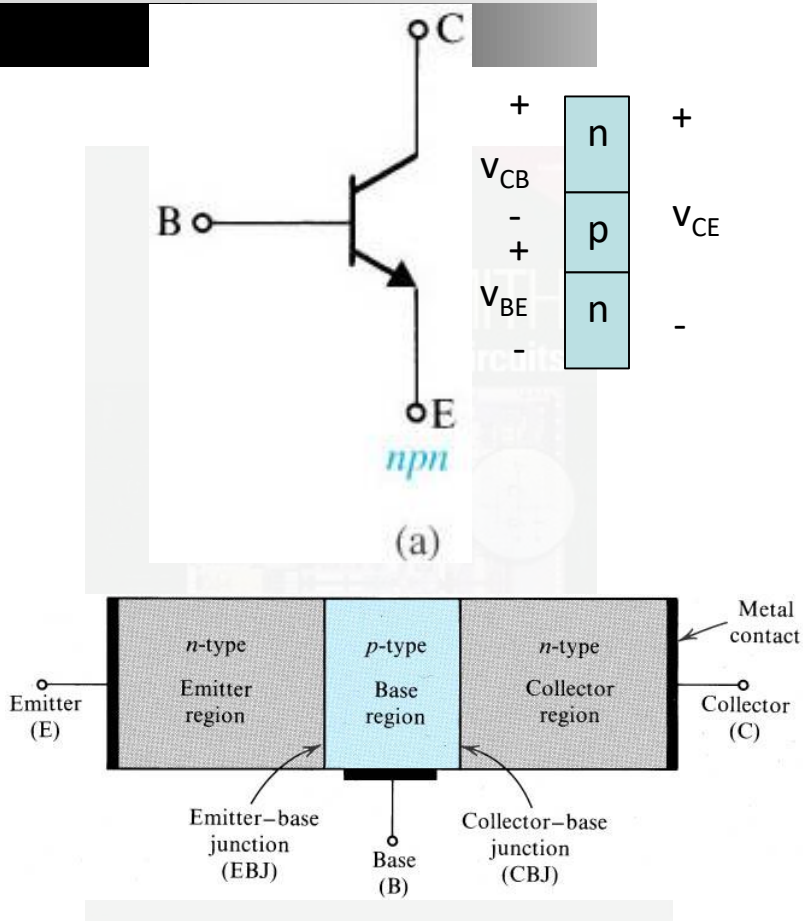


- For  $v_{CB} > -0.4\text{ V}$ , the BJT is in active mode.
- $i_C$  is  $\alpha_F$  times current source value.
- As CB becomes forward biased,  $v_{CB}$  falls below  $-0.4\text{ V}$ , it reaches saturation.

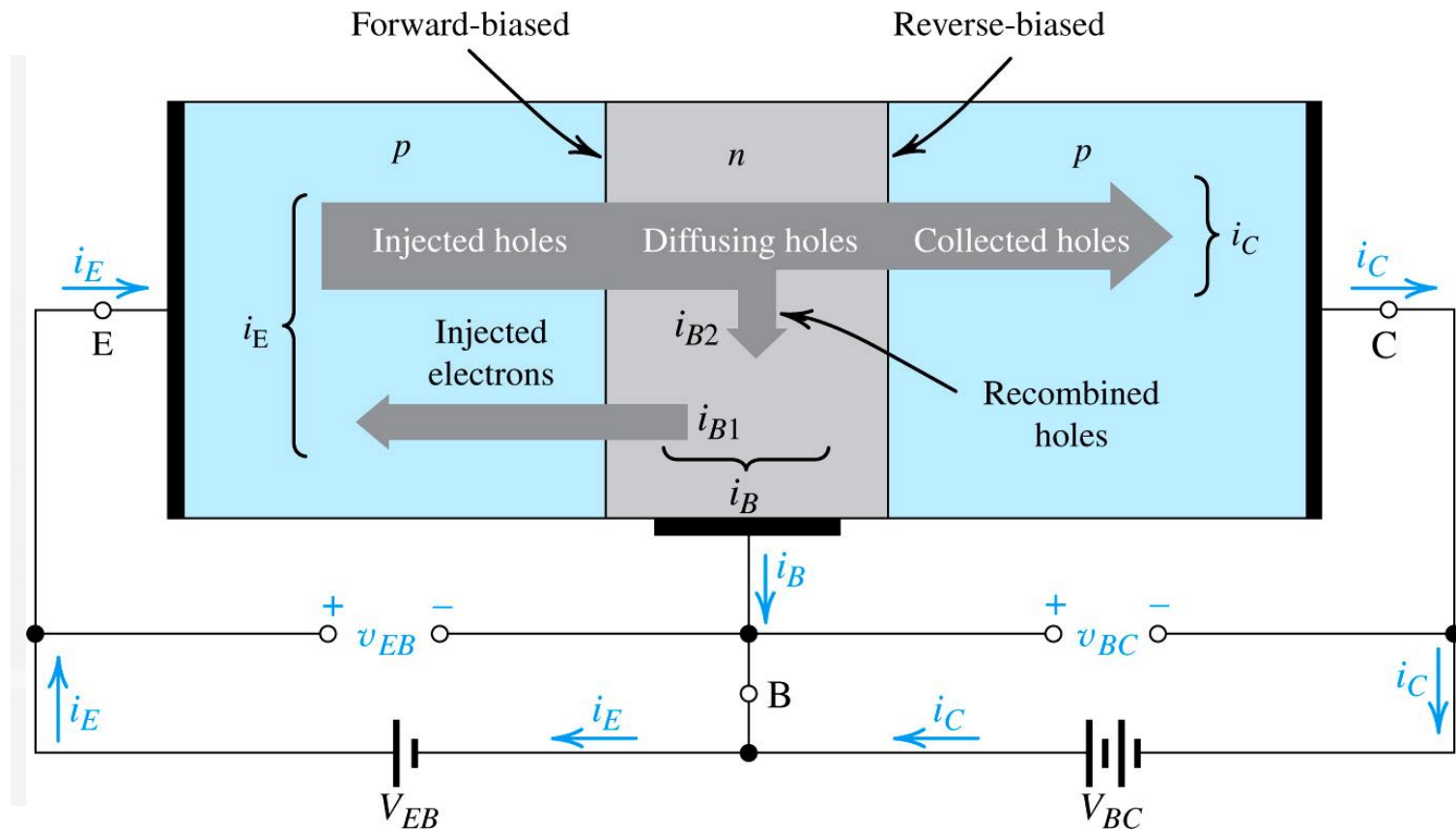
**FIGURE 5.9** The  $i_C$ - $v_{CB}$  characteristic of an *npn* transistor fed with a constant emitter current  $I_E$ . The transistor enters the saturation mode of operation for  $v_{CB} < -0.4\text{ V}$ , and the collector current diminishes.

# Circuit Symbols

The arrow is at the emitter, and it points to the n-type region. In the npn, the emitter is n type; in the pnp, the base is n-type.

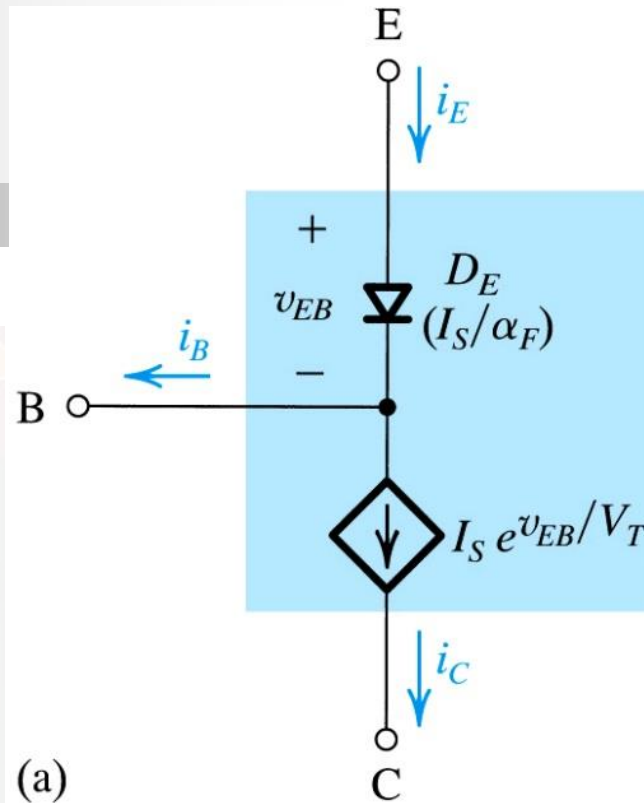


## 5.1.5. The *pnp* Transistor



**Figure 5.10:** Current flow in a *pnp* transistor biased to operate in the active mode.

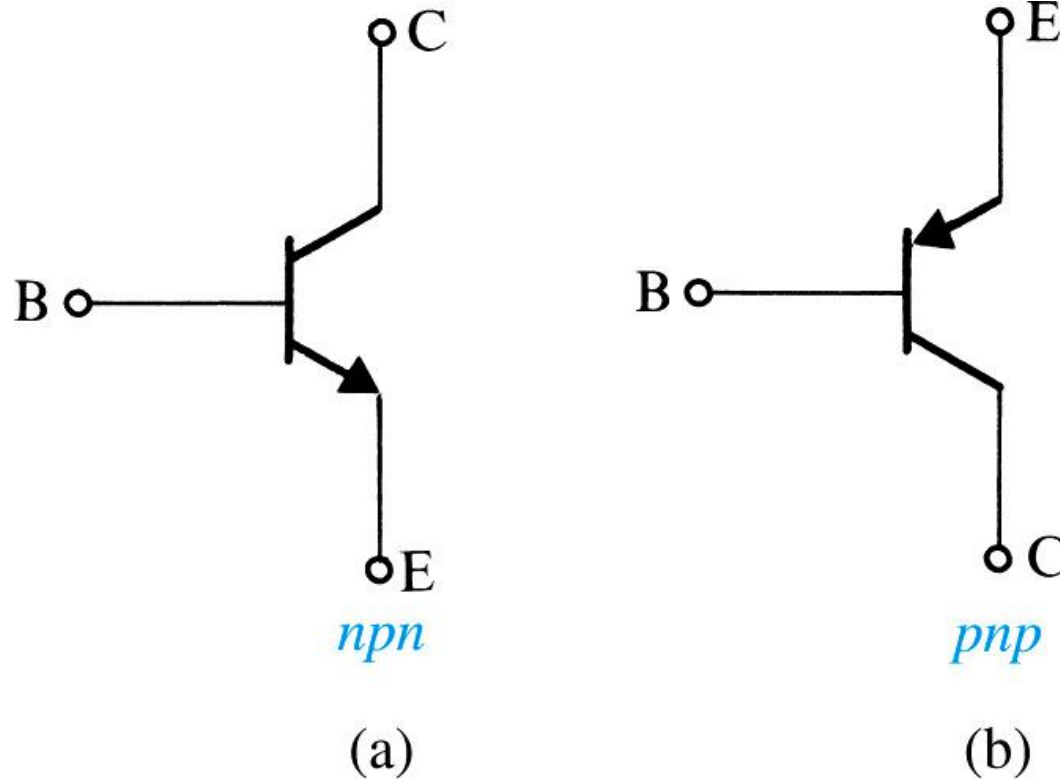
## 5.1.5. The *pnp* Transistor



**Figure 5.11:** Large-signal models for the *pnp* transistor operating in the active mode.

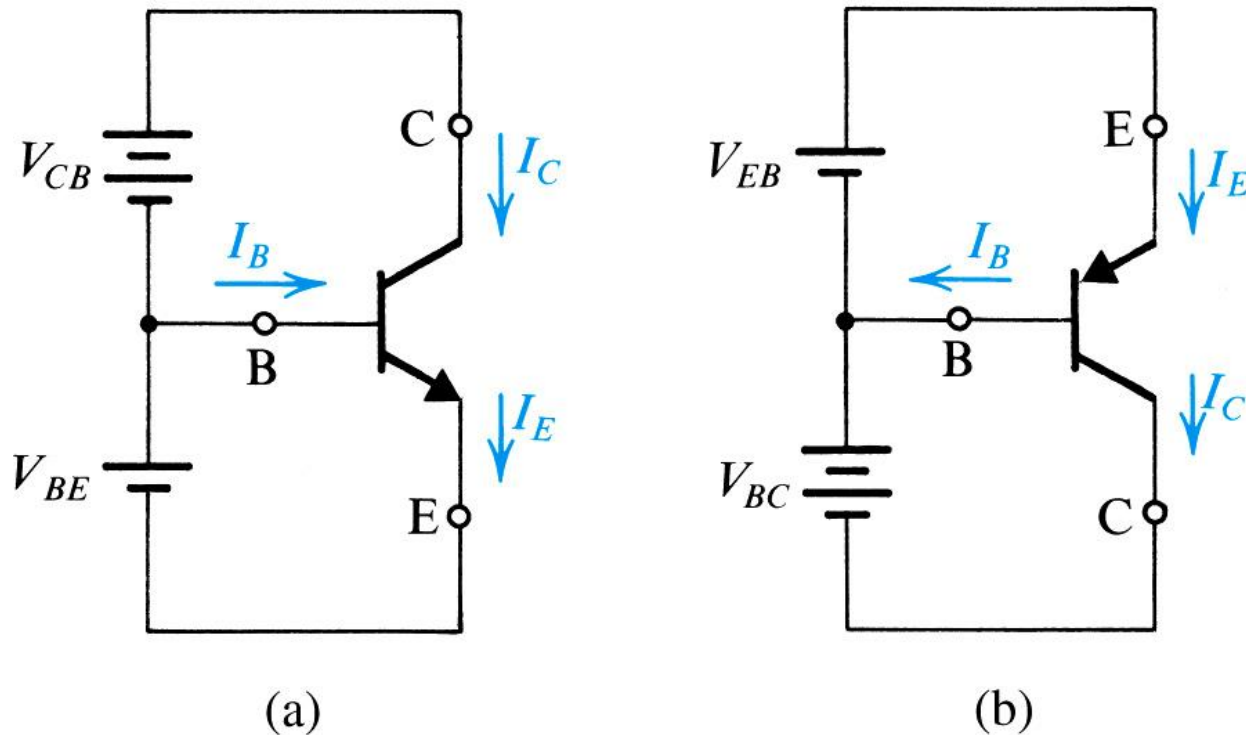


## 5.2. Current-Voltage Characteristics



**Figure 5.12:** Circuit symbols for BJTs.

## 5.2.1. Circuit Symbols and Conventions



**Figure 5.13:** Voltage polarities and current flow in transistors biased in the active mode.

## 5.2.1. Circuit Symbols and Conventions

**Table 6.2** Summary of the BJT Current-Voltage Relationships in the Active Mode

$$i_C = I_S e^{v_{BE}/V_T}$$

$$i_B = \frac{i_C}{\beta} = \left(\frac{I_S}{\beta}\right) e^{v_{BE}/V_T}$$

$$i_E = \frac{i_C}{\alpha} = \left(\frac{I_S}{\alpha}\right) e^{v_{BE}/V_T}$$

*Note:* For the *pnp* transistor, replace  $v_{BE}$  with  $v_{EB}$ .

$$i_C = \alpha i_E \qquad i_B = (1 - \alpha) i_E = \frac{i_E}{\beta + 1}$$

$$i_C = \beta i_B \qquad i_E = (\beta + 1) i_B$$

$$\beta = \frac{\alpha}{1 - \alpha} \qquad \alpha = \frac{\beta}{\beta + 1}$$

$$V_T = \text{thermal voltage} = \frac{kT}{q} \simeq 25 \text{ mV at room temperature}$$

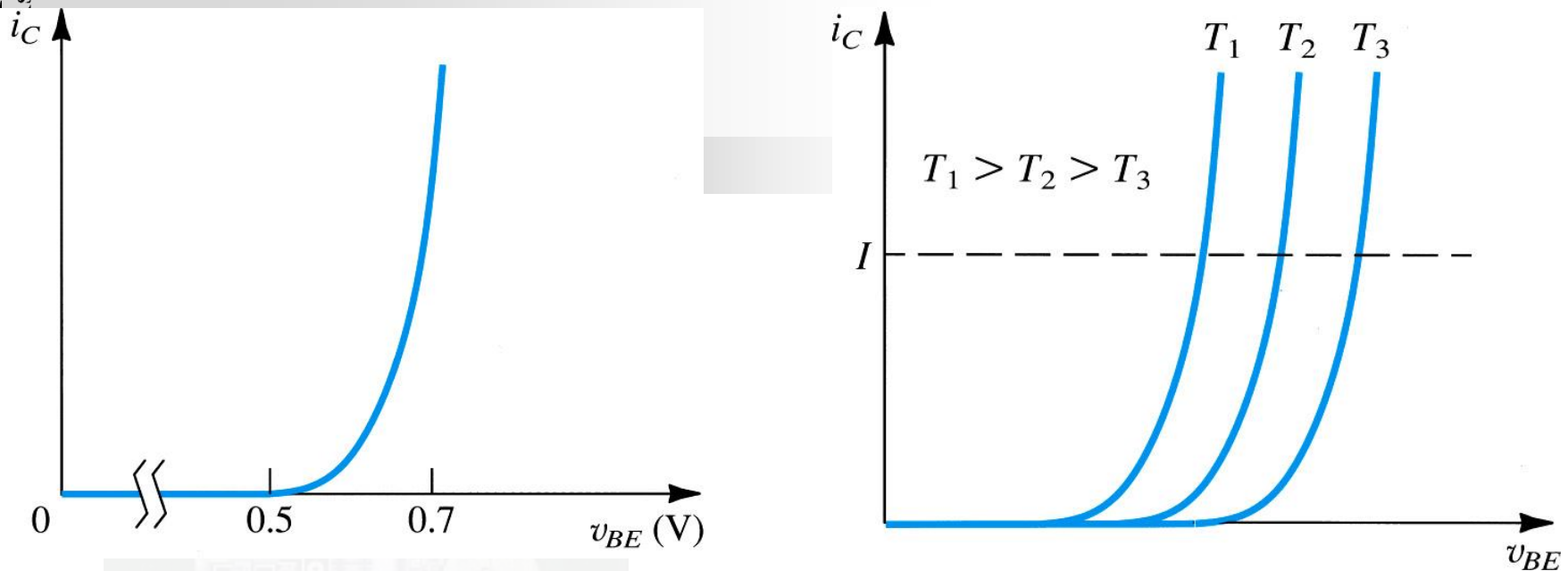
# The Collector-Base Reverse Current

$$(I_{CBO})$$

- Previously, small **reverse current was ignored**.
  - This is carried by **thermally-generated minority carriers**.
- However, it does **deserve** to be addressed.
- The **collector-base junction current** ( $I_{CBO}$ ) is normally in the nano-ampere range.
  - **Many times higher** than its theoretically-predicted value.
  - $I_{CBO}$  doubles for every 10 C rise in temperature.

## 5.2.2. Graphical Representation of Transistor Characteristics

### The Common – Base Characteristics



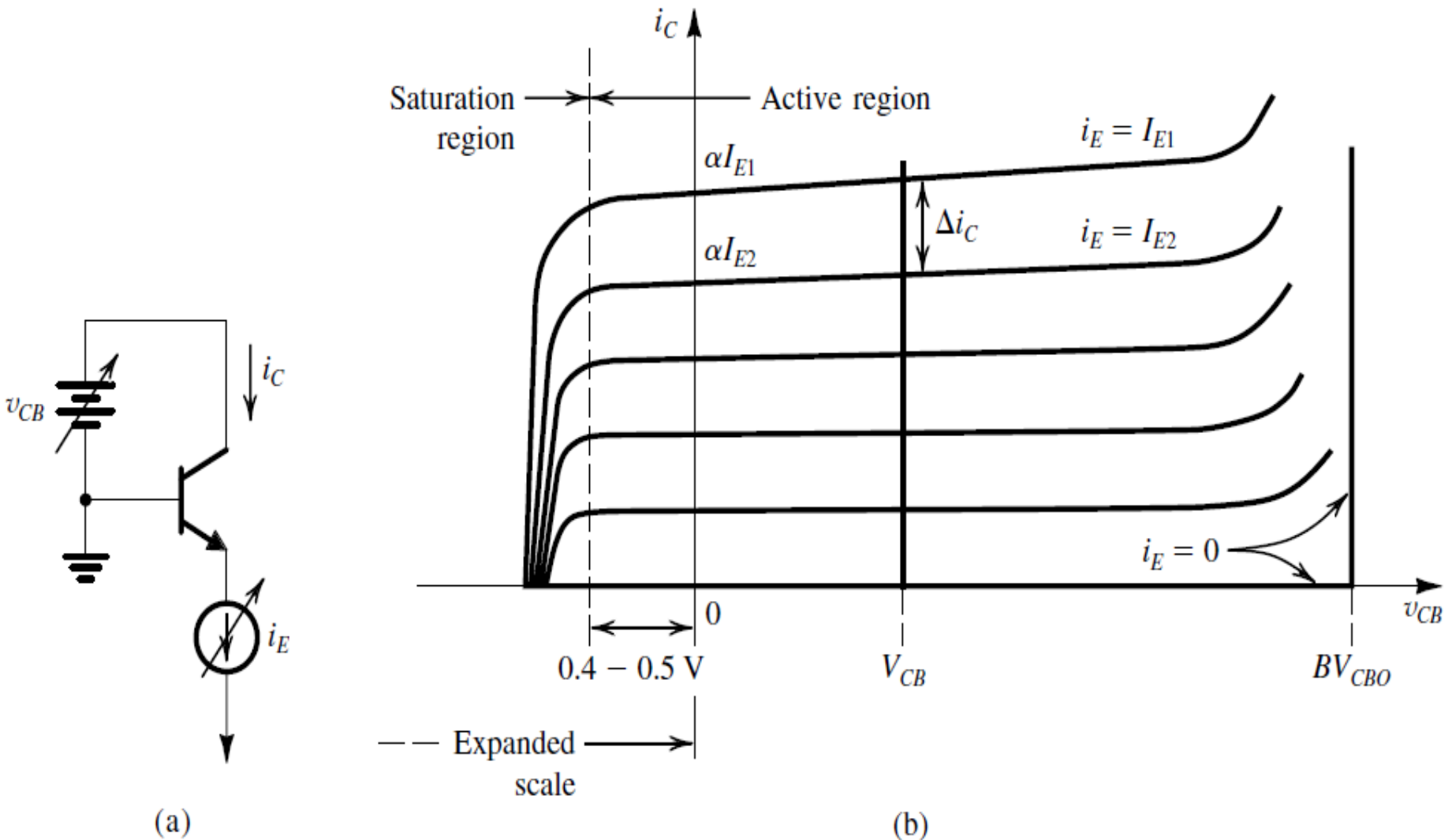
**Figure 5.15/15:** (left) The  $i_C$ - $v_{BE}$  characteristic for an npn transistor. (right) Effect of temperature on the  $i_C$ - $v_{BE}$  characteristic. Voltage polarities and current flow in transistors biased in the active mode.

**$V_{BE}$  decreases by about 2 mV for each rise of  $1^\circ\text{C}$  in temperature.**

$$i_C = I_S e^{v_{BE}/V_T} \quad i_B = \frac{i_C}{\beta} = \left(\frac{I_S}{\beta}\right) e^{v_{BE}/V_T} \quad i_E = \frac{i_C}{\alpha} = \left(\frac{I_S}{\alpha}\right) e^{v_{BE}/V_T}$$

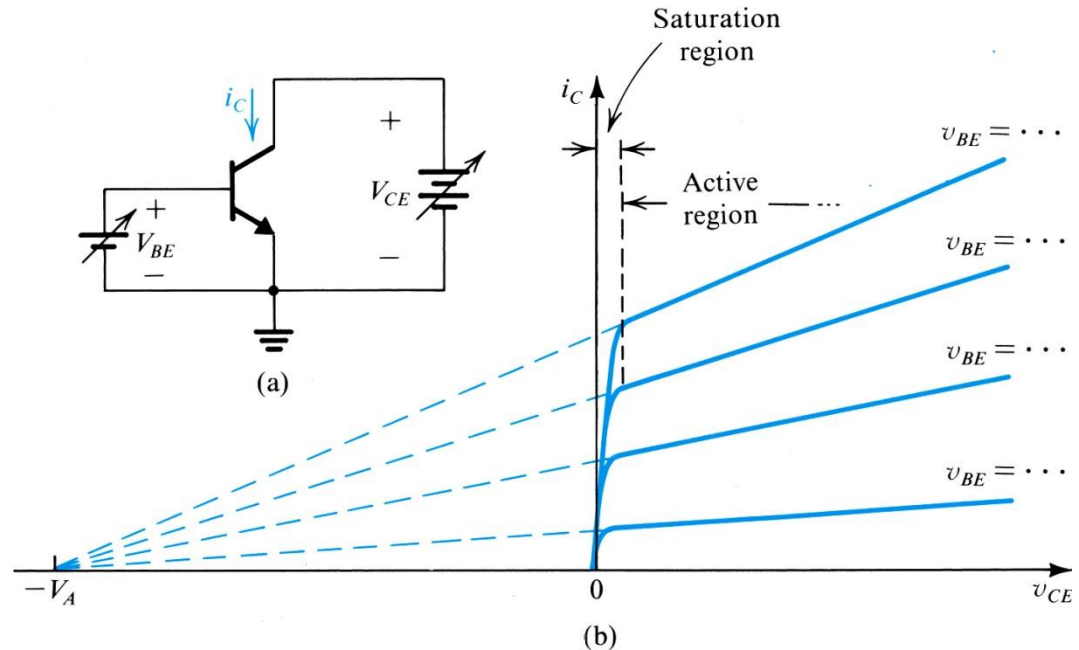
**For pnp transistor  $V_{BE}$  should be replaced with  $V_{EB}$**

# $i_C$ - $v_{CB}$ characteristics when NPN driven by a cc source in emitter

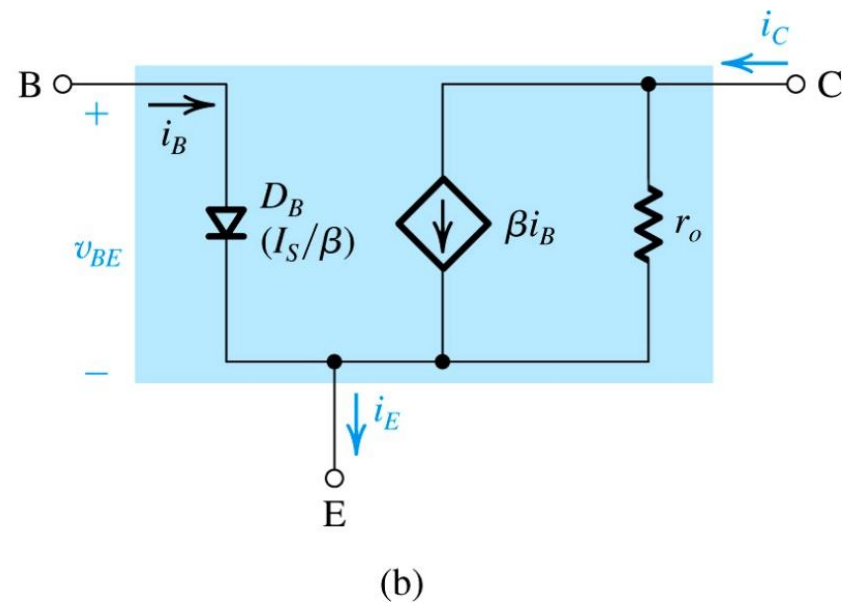
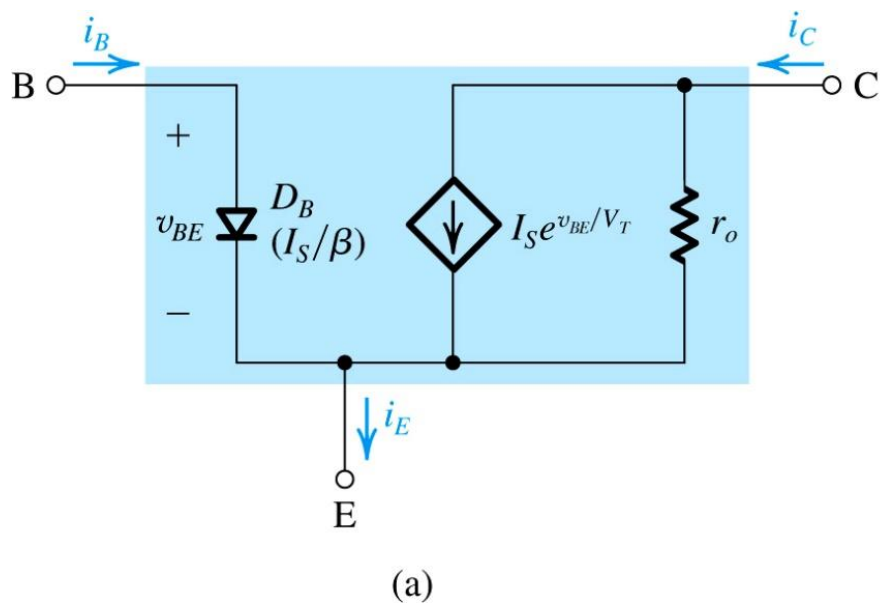


## 5.2.3. Dependence of $i_C$ on Collector Voltage – The Early Effect

- When operated in active region, practical BJT's show some **dependence of collector current on collector voltage**.
- As such,  $i_C$ - $v_{CE}$  characteristic is **not “straight”**.



**Figure 6.17** (a) Conceptual circuit for measuring the  $i_C$ - $v_{CE}$  characteristics of the BJT. (b) The  $i_C$ - $v_{CE}$  characteristics of a practical BJT.

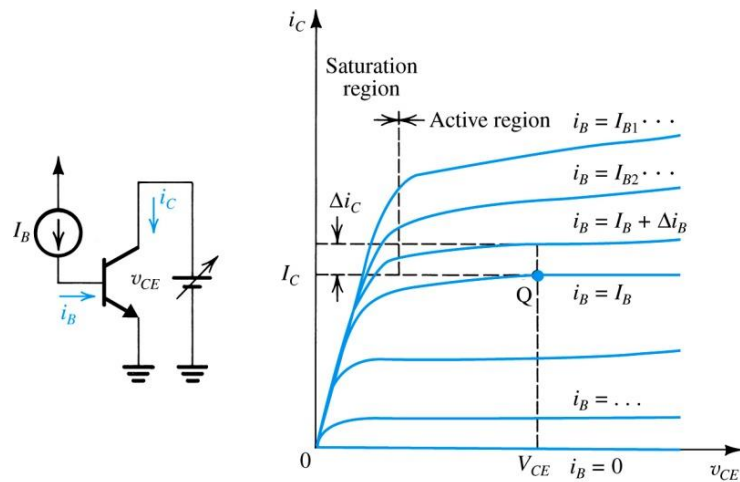


**Figure 5.18:** Large-signal equivalent-circuit models of an *nnp* BJT operating in the active mode in the common-emitter configuration with the output resistance  $r_o$  included.



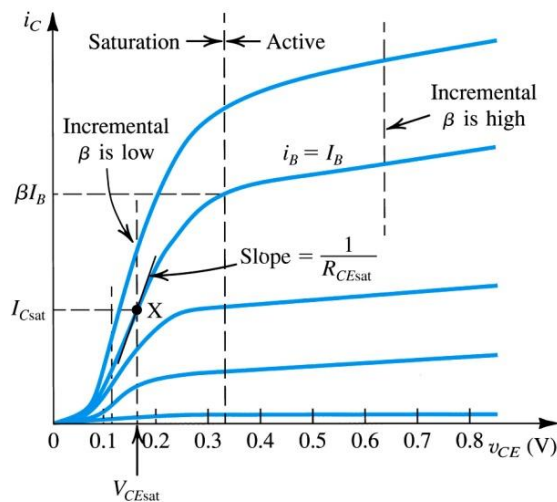
## 5.2.4. An Alternative Form of the Common-Emitter Characteristics

- The Common-Emitter Current Gain
  - A second way to quantify  $\beta$  is changing base current by  $\Delta i_B$  and measuring incremental  $\Delta i_C$ .
- The Saturation Voltage  $V_{CEsat}$  and Saturation Resistance



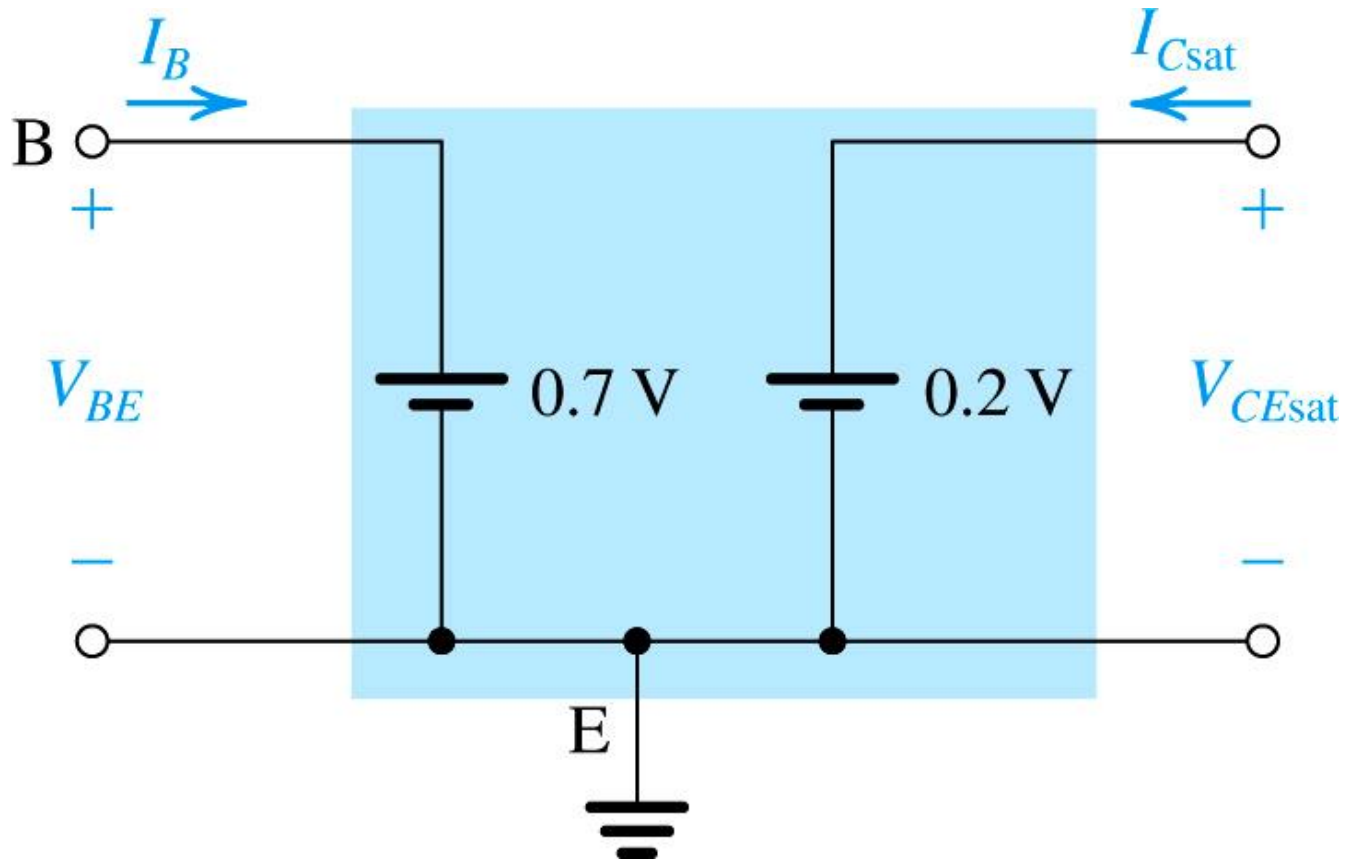
(a)

(b)



(c)

**Figure 5.19:** Common-emitter characteristics. (a) Basic CE circuit; note that in (b) the horizontal scale is expanded around the origin to show the saturation region in some detail. A much greater expansion of the saturation region is shown in (c).



**Figure 5.20:** A simplified equivalent-circuit model of the saturated transistor.

# BJT behavior in saturation

1. In active region, we assumed beta to be a constant depending upon transistor geometry and construction. Beta is ratio of  $i_C/i_B$  and has a value between 50 to 500.
2. As the BJT enters saturation, beta falls drastically as  $i_C$  becomes less than  $(\beta * i_B)$ . This beta is called as FORCED BETA which is less than beta.
3. The ratio of Beta to Forced Beta is called OVERDRIVE Factor.

# BJT behavior in saturation

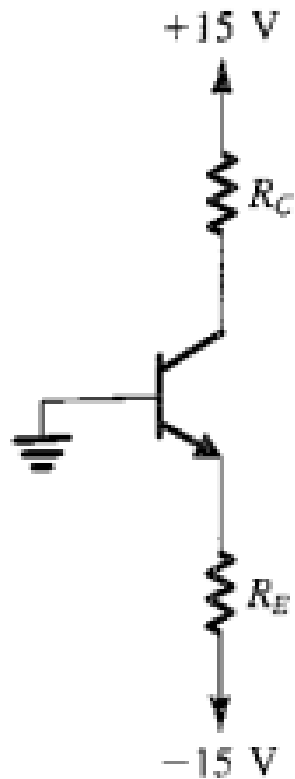
4. In saturation, the curve is nearly vertical showing behavior like a voltage source of voltage 0.2V to 0.4V with nearly zero source resistance.
5. Since the curve is sloping it gives a small resistance called

$$R_{CE \text{ sat}} = v_{CE} / i_C \quad (\text{when } i_C = i_{CE \text{ sat}})$$

This is usually of the order of tens of ohms.

## Example 5.1.

The transistor in the circuit of Fig. 5.15(a) has  $\beta = 100$  and exhibits a  $v_{BE}$  of 0.7 V at  $i_C = 1$  mA. Design the circuit so that a current of 2 mA flows through the collector and a voltage of +5 V appears at the collector.



(a)

**FIGURE 5.15** Circuit for Example 5.1.

## Solution

Refer to Fig. 5.15(b). We note at the outset that since we are required to design for  $V_C = +5$  V, the CBJ will be reverse biased and the BJT will be operating in the active mode. To obtain a voltage  $V_C = +5$  V the voltage drop across  $R_C$  must be  $15 - 5 = 10$  V. Now, since  $I_C = 2$  mA, the value of  $R_C$  should be selected according to

$$R_C = \frac{10 \text{ V}}{2 \text{ mA}} = 5 \text{ k}\Omega$$

Since  $v_{BE} = 0.7$  V at  $i_C = 1$  mA, the value of  $v_{BE}$  at  $i_C = 2$  mA is

$$V_{BE} = 0.7 + V_T \ln\left(\frac{2}{1}\right) = 0.717 \text{ V}$$

Since the base is at 0 V, the emitter voltage should be

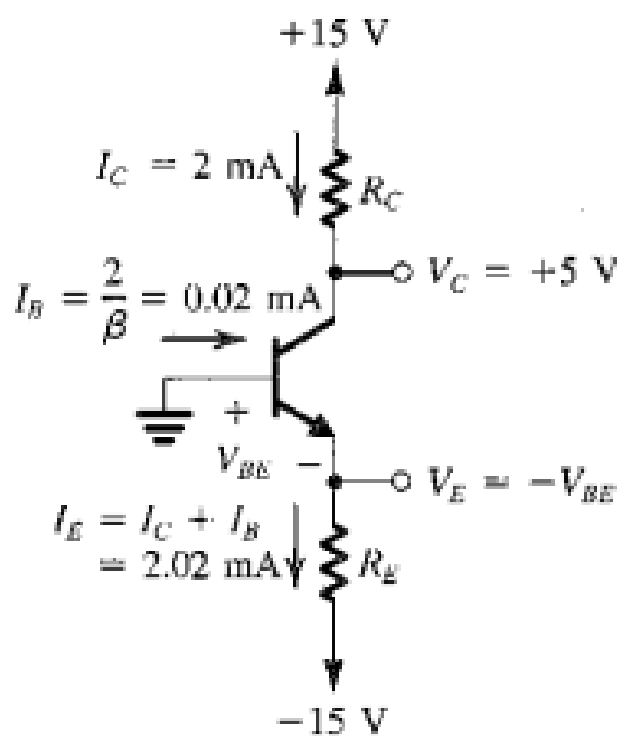
$$V_E = -0.717 \text{ V}$$

For  $\beta = 100$ ,  $\alpha = 100/101 = 0.99$ . Thus the emitter current should be

$$I_E = \frac{I_C}{\alpha} = \frac{2}{0.99} = 2.02 \text{ mA}$$

Now the value required for  $R_E$  can be determined from

$$\begin{aligned} R_E &= \frac{V_E - (-15)}{I_E} \\ &= \frac{-0.717 + 15}{2.02} = 7.07 \text{ k}\Omega \end{aligned}$$

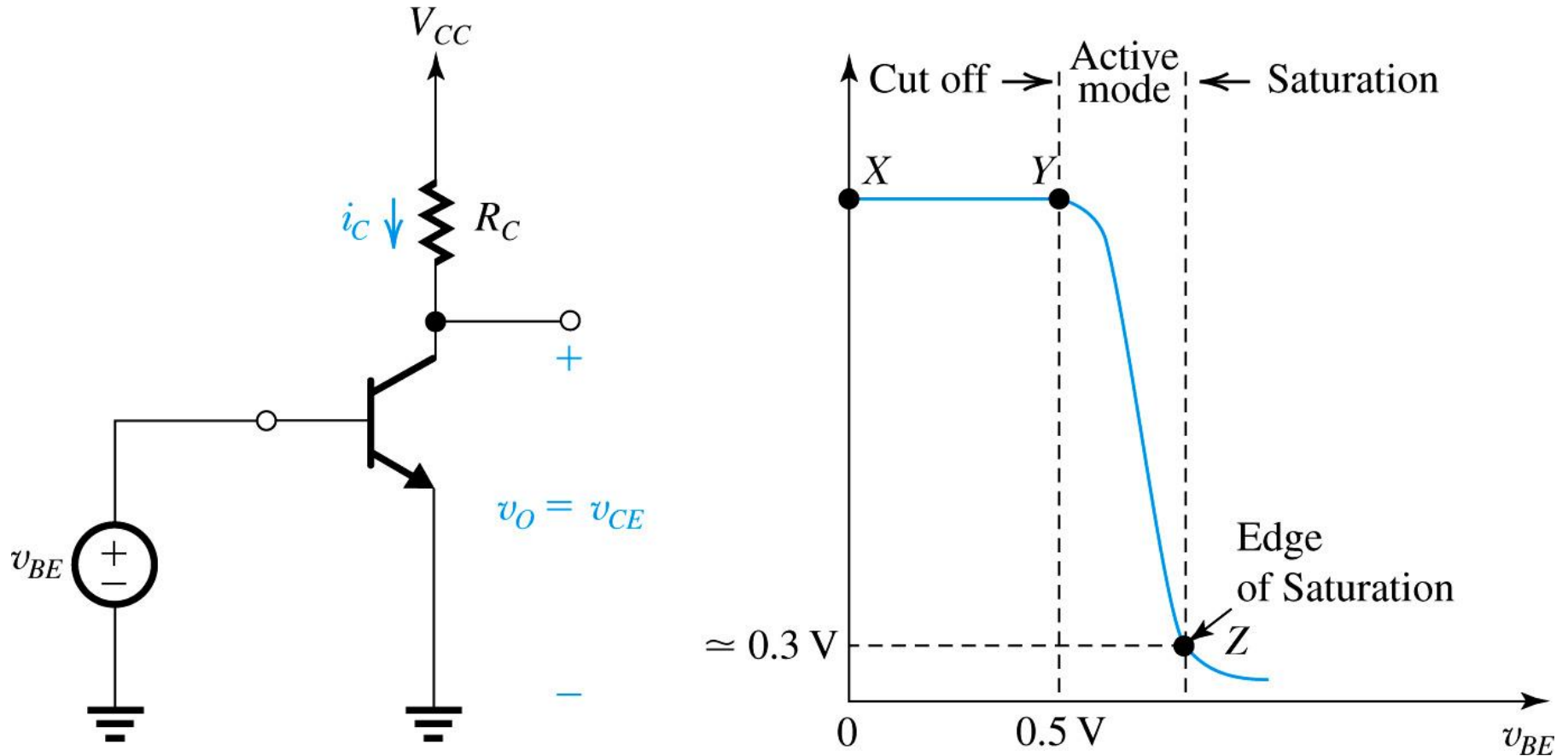


## 5.4. Applying the BJT in Amplifier Design

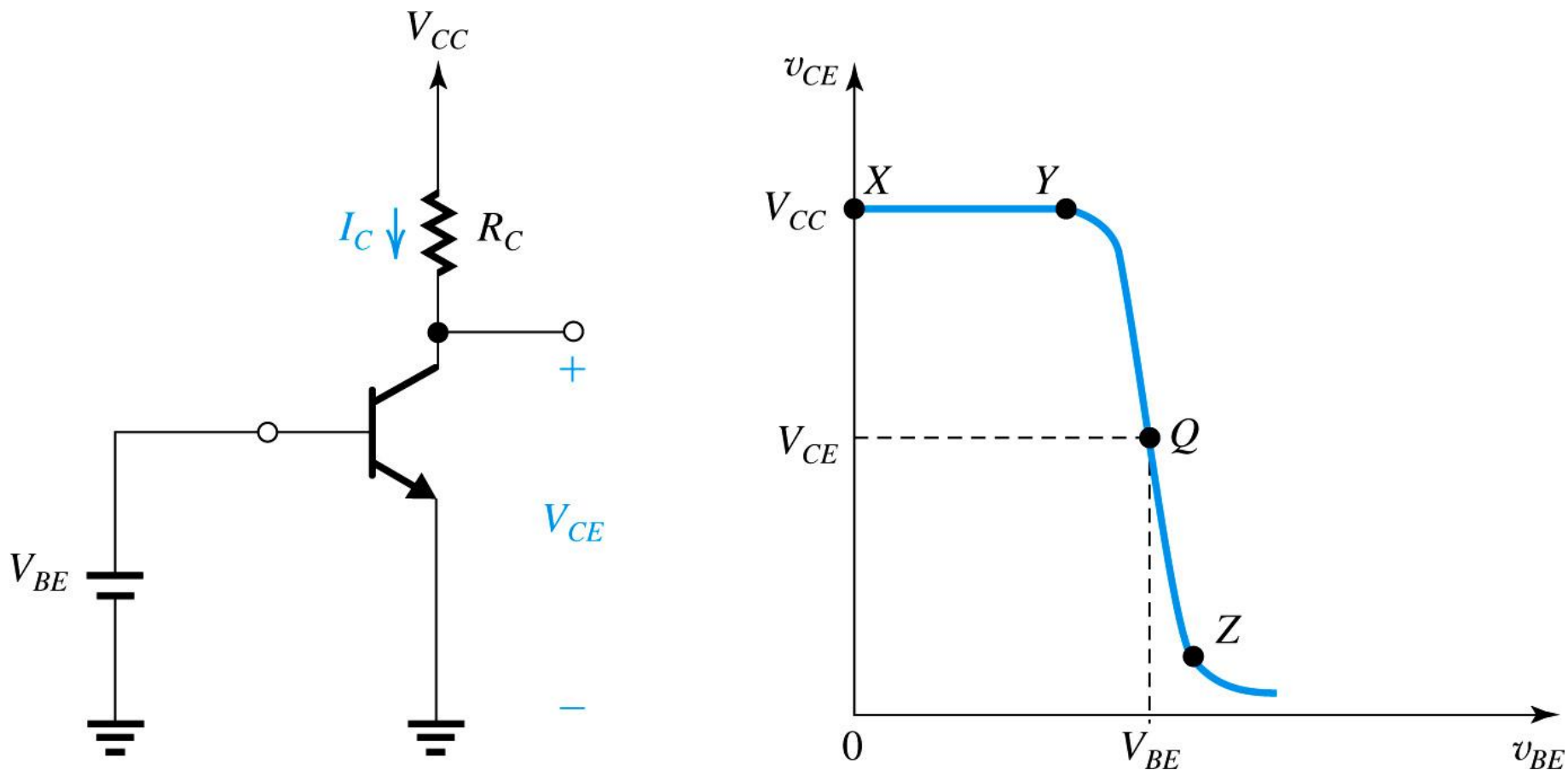
- Similar to the configuration presented in Chapter 5, an amplifier may be designed by **transistor and series resistance**.
- However, it is necessary to model the **voltage transfer characteristic (VTC)**.
  - Equation (5.25)
- Appropriate biasing is important to **ensure linear gain**, and appropriate input voltage swing.
  - Small-signal model is employed to model the amp's operation.



$$v_O = v_{CE} = V_{CC} - R_C i_C$$



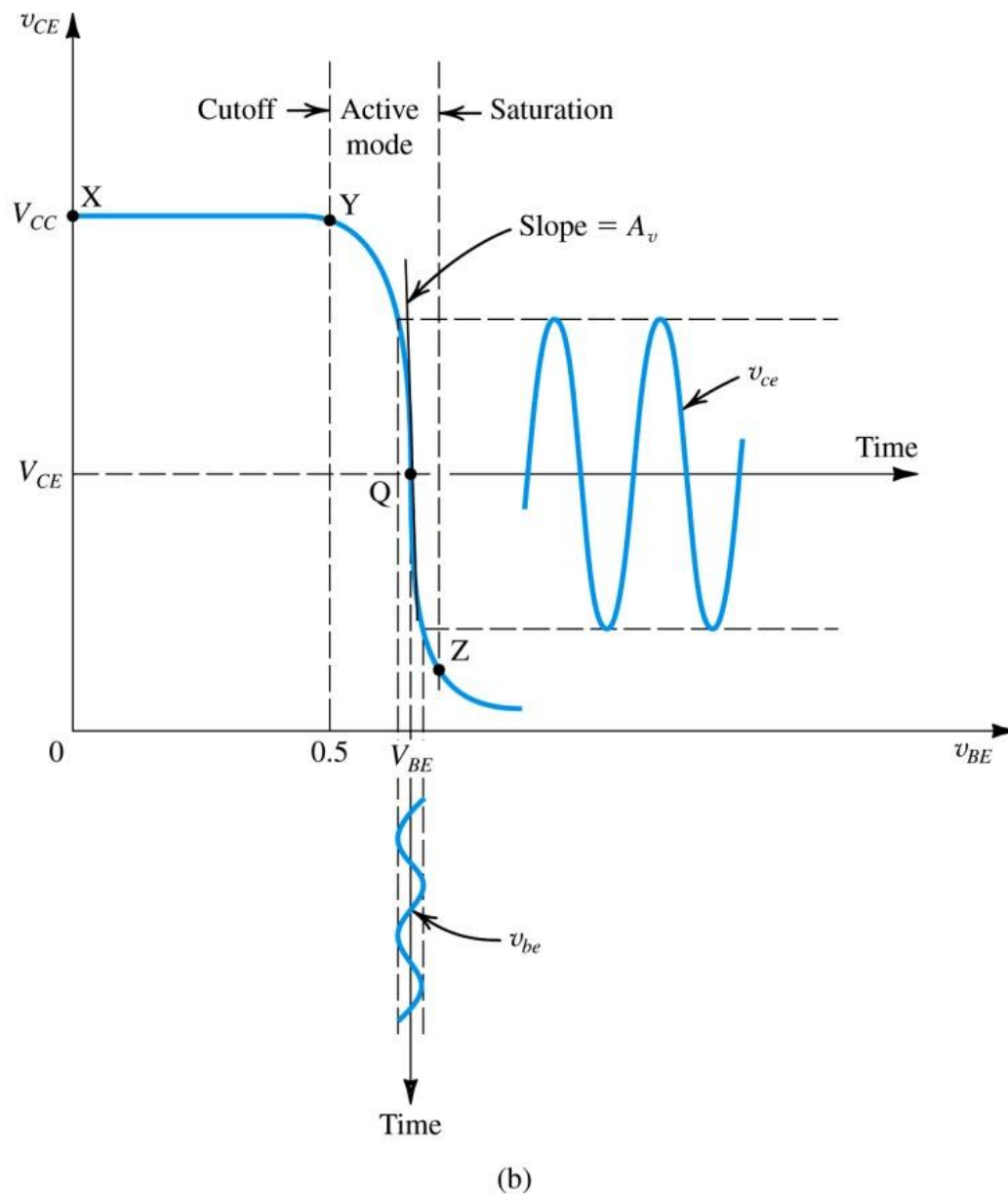
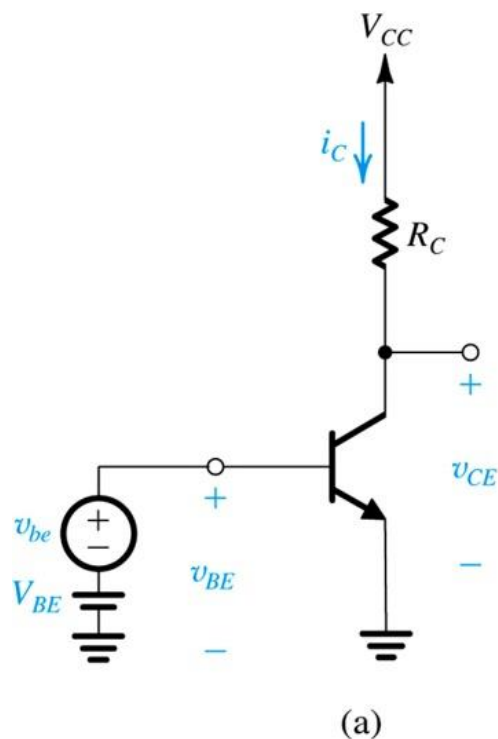
**Figure 6.31** (a) Simple BJT amplifier with input  $v_{BE}$  and output  $v_{CE}$ . (b) The voltage transfer characteristic (VTC) of the amplifier in (a). The three segments of the VTC correspond to the three modes of operation of the BJT.



**Figure 5.32:** Biasing the BJT amplifier at a point Q located on the active-mode segment of the VTC.

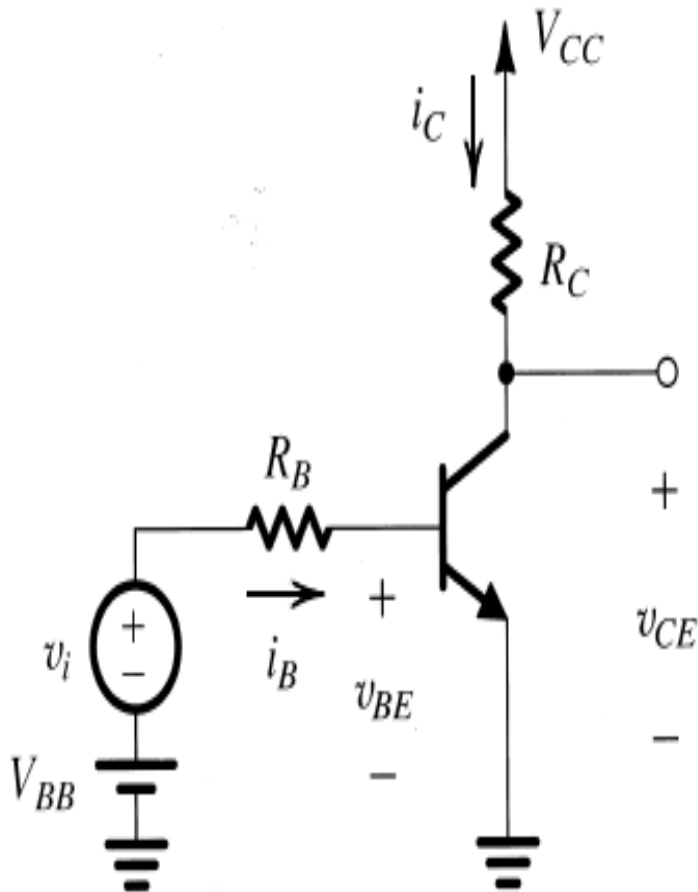
$$A_v = -\frac{V_{CC} - V_{CEsat}}{V_T}$$

$$A_{vmax} \equiv -\frac{V_{CC}}{V_T}$$



**Figure 6.33** BJT amplifier biased at a point Q, with a small voltage signal  $v_{be}$  superimposed on the dc bias voltage  $V_{BE}$ . The resulting output signal  $v_{ce}$  appears superimposed on the dc collector voltage  $V_{CE}$ . The amplitude of  $v_{ce}$  is larger than that of  $v_{be}$  by the voltage gain  $A_v$ .

# Determination of Quiescent Point Graphically

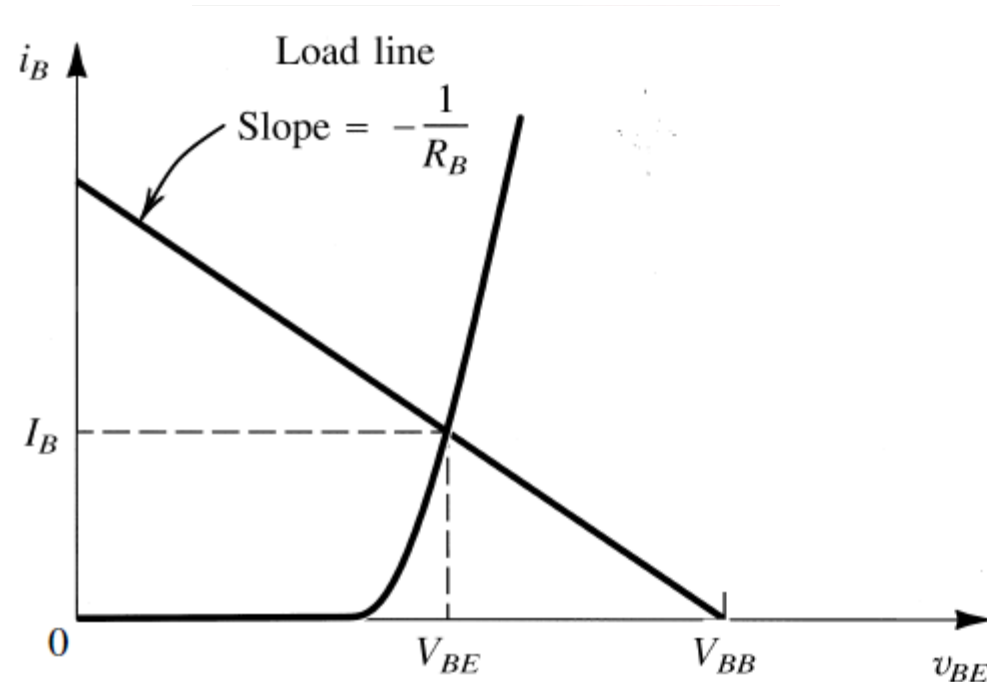


Quiescent Point or Q-point is the point plotted on  $v_{CE}$  vs.  $i_C$  characteristics based on output DC conditions namely  $i_C$  and  $v_{CE}$ .

First calculate input current  $i_B$  and then derive  $i_C$  and  $v_{CE}$  from it.

**Note input is AC + DC**

# Determination of Input parameters



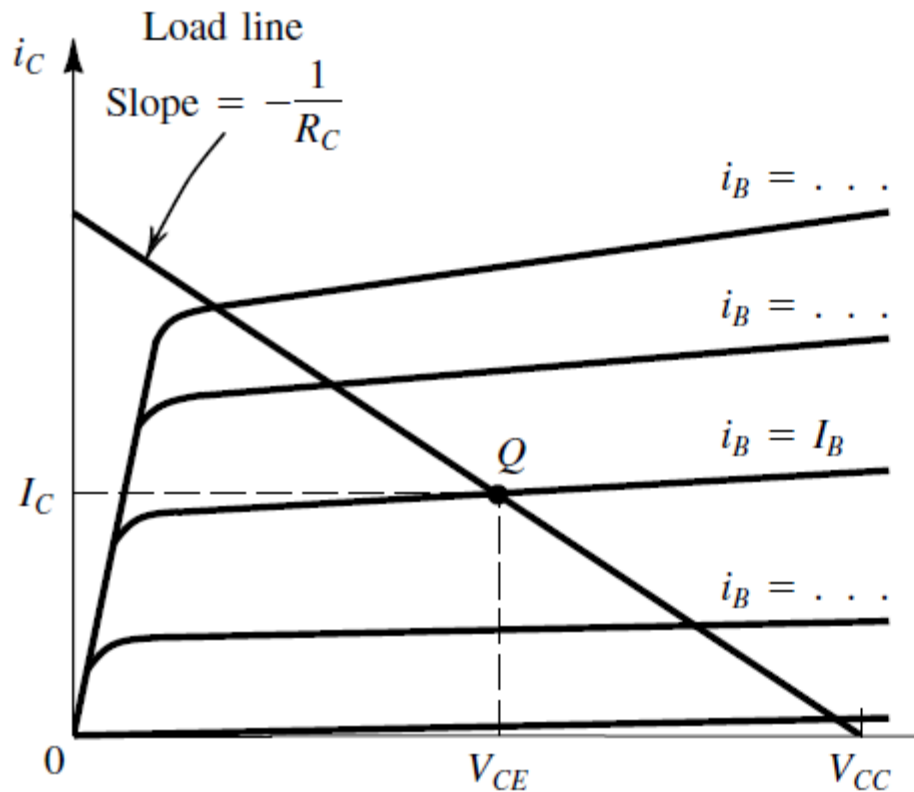
Note the  $i_B$  vs.  $v_{BE}$  characteristics. It has an exponential relationship of a diode. On this curve we plot equation of a straight line made by linear model:

$$V_{BB} - v_{BE} - i_B * R_b = 0.$$

This equation has a slope of  $-1/R_B$ . The point where it cuts the curve is Q-Point.

**FIGURE 3.28** Graphical construction for the determination of

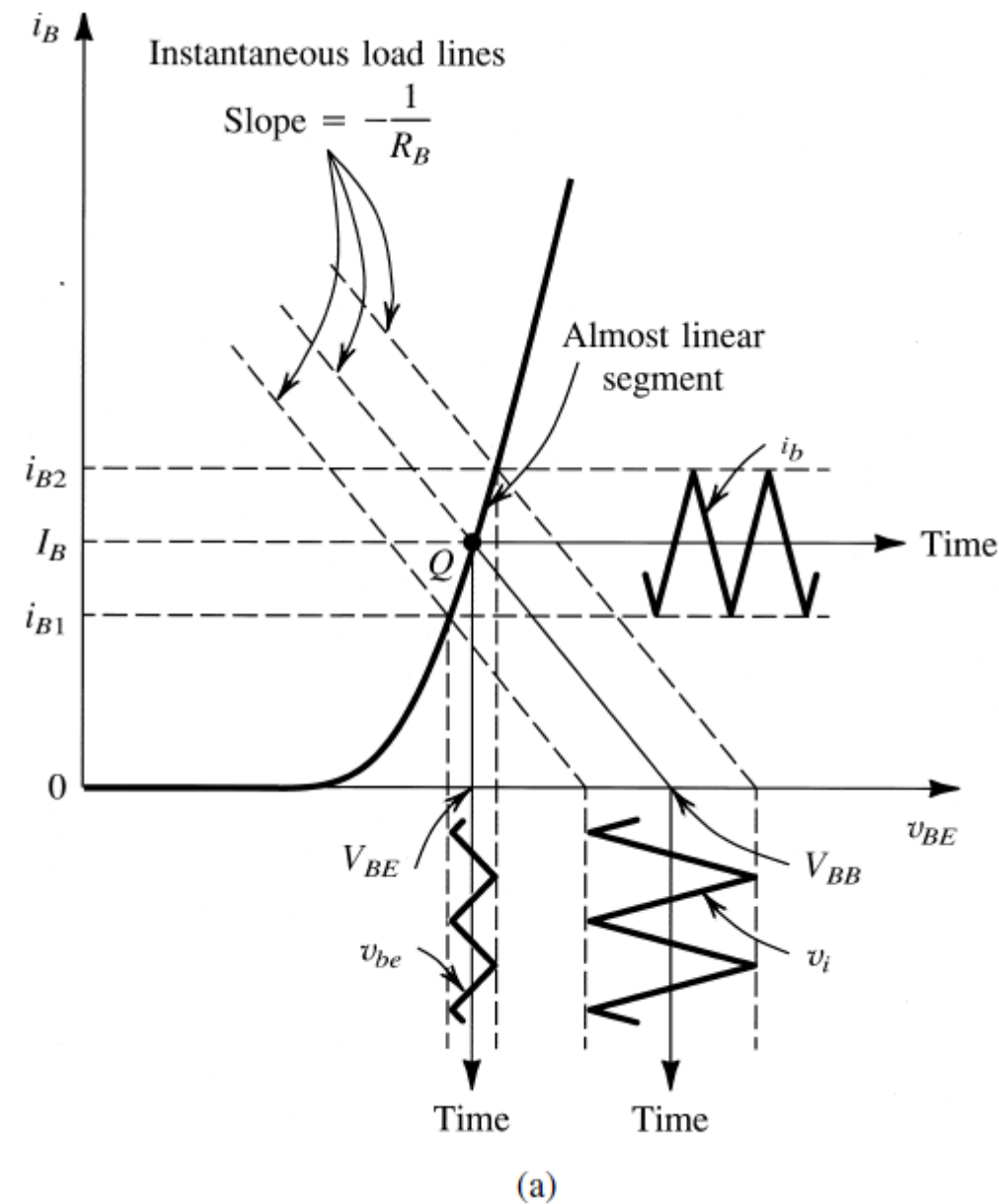
# Determination of Output parameters



**FIGURE 3.29** Graphical construction for determining the emitter voltage  $V_{CE}$  in the circuit of Fig. 3.27.

Note the  $i_C$  vs.  $v_{CE}$  characteristics is like a cc source with a shunt finite resistance  $R_o$ . Add to it st line of equation:  
 $V_{CC} - v_{CE} - i_C * R_C = 0.$

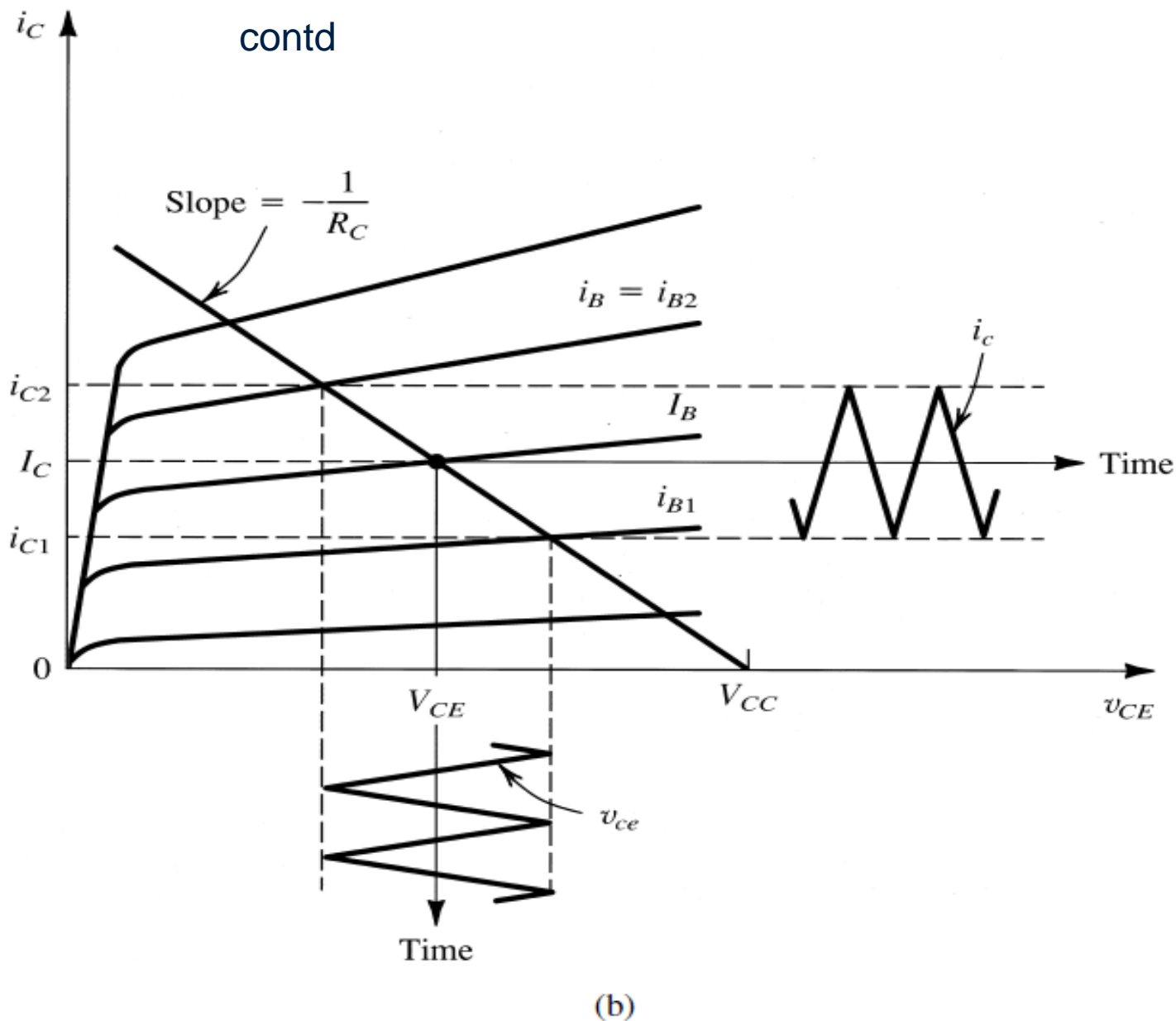
This equation has a slope of  $-1/R_C$ . The point where it cuts the curve for a given  $i_B$  value is Q-Point which gives us  $i_C$  and  $v_{CE}$  values.



Let us now add signal  $v_i$  to  $V_{BB}$ . It will cause minute changes to  $v_{BE}$  and will cause minute changes in  $i_B$ .

The relationship between  $v_{BE}$  and  $i_B$  will be linear as long as the swing is much smaller around Q-point.

contd

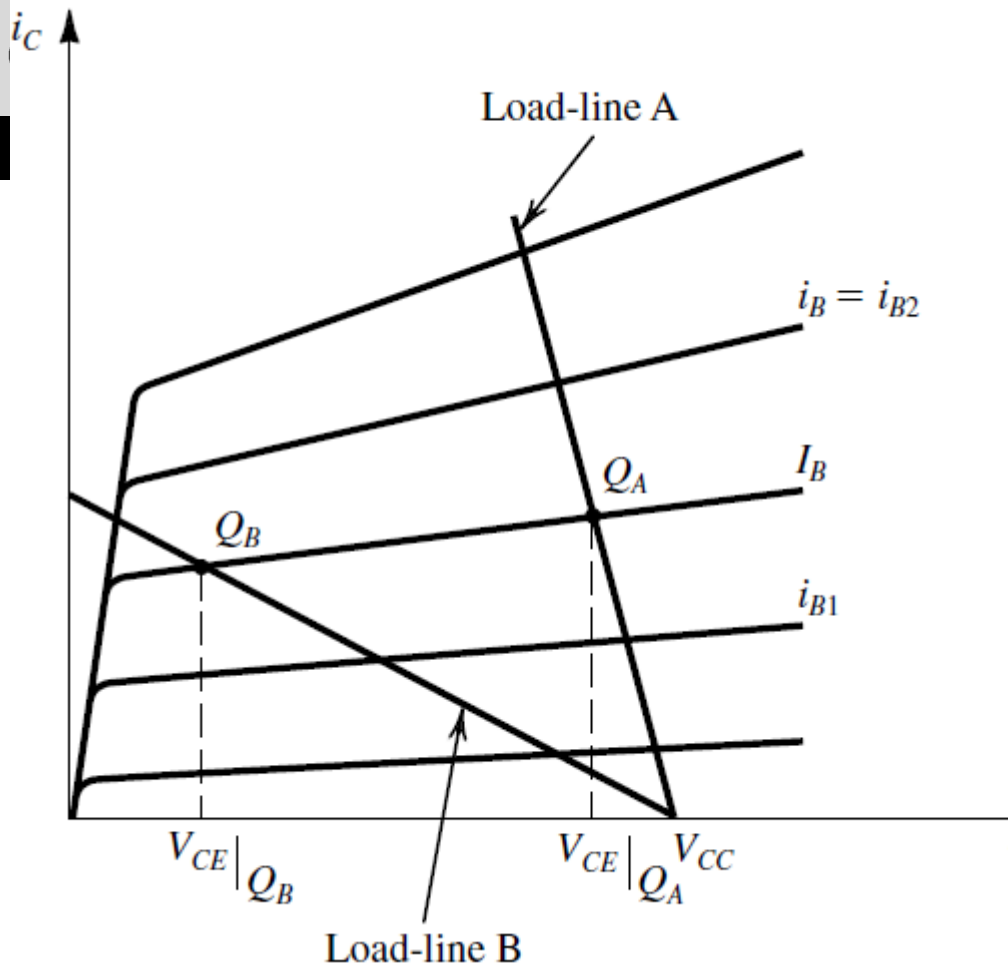


Note that changes in  $i_B$  around Q-Point, causes changes in  $i_C$  and  $v_{CE}$ , almost linearly.

**FIGURE 3.30** Graphical determination of the signal components  $v_{be}$ ,  $i_b$ ,  $i_c$ , and component  $v_i$  is superimposed on the dc voltage  $V_{BE}$  (see Fig. 3.27).



# Selection of Q Point



**FIGURE 3.31** Effect of bias-point location on allowable signal swing with a corresponding  $V_{CE}$  which is too close to  $V_{CC}$  and the extreme, load-line B results in an operating point too close to  $V_{CC}$  and a small swing of  $v_{CE}$ .

Let us now add signal  $v_i$  to  $V_{BB}$ . It will cause minute changes to  $v_{BE}$  and will cause minute changes in  $i_B$ .

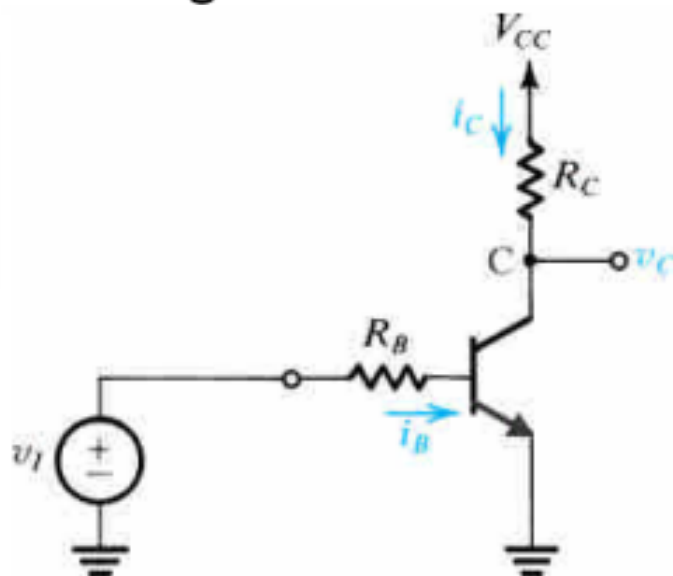
The relationship between  $v_{BE}$  and  $i_B$  will be linear as long as the swing is much smaller around Q-point.

## 5.3.4 Operation as a Switch

- To operate the BJT as a switch, we utilize the cutoff and the saturation modes of operation.
- For  $v_I$  less than about 0.5 V, the transistor will be cutoff; thus  $i_B = 0, i_C = 0$ , and  $v_C = V_{CC}$
- To turn the transistor on, we have to increase  $v_I$  above 0.5 V. In fact, for appreciable currents to flow,  $v_{BE}$  should be about 0.7 V and  $v_I$  should be higher.

$$i_B = \frac{v_I - V_{BE}}{R_B}$$

$$i_C = \beta i_B$$



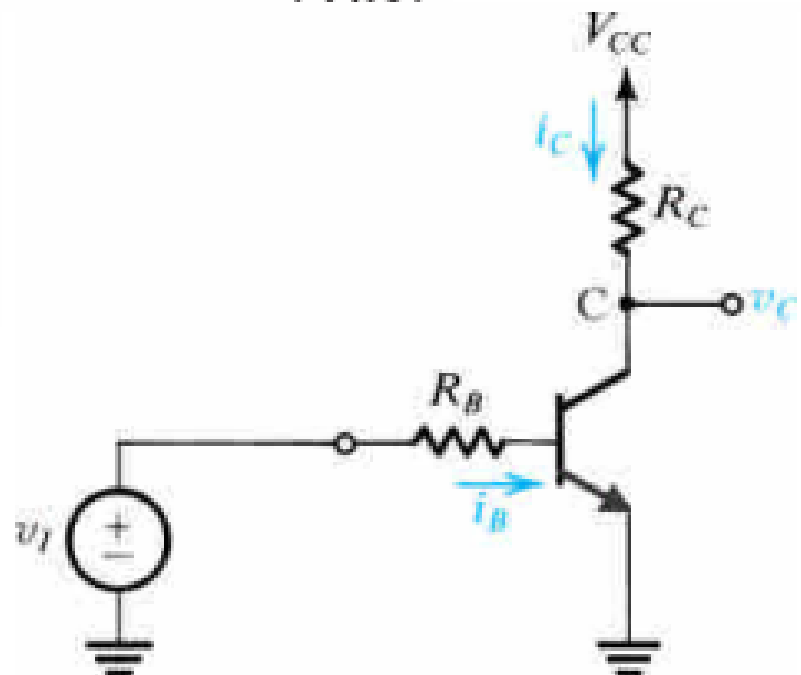
which applies only when the device is in the active mode. This will be the case as long as the CBJ is not forward biased, that is, as long as  $v_C > v_B - 0.4 \text{ V}$ ,

● Eventually,  $v_C$  will become lower than  $v_B$  by 0.4 V, at which point the transistor leaves the active region and enters the saturation region. This **edge-of-saturation (EOS)** point is defined by

$$I_{C(\text{EOS})} = \frac{V_{CC} - 0.3}{R_C} \quad (5.62)$$

$$I_{B(\text{EOS})} = \frac{I_{C(\text{EOS})}}{\beta}$$

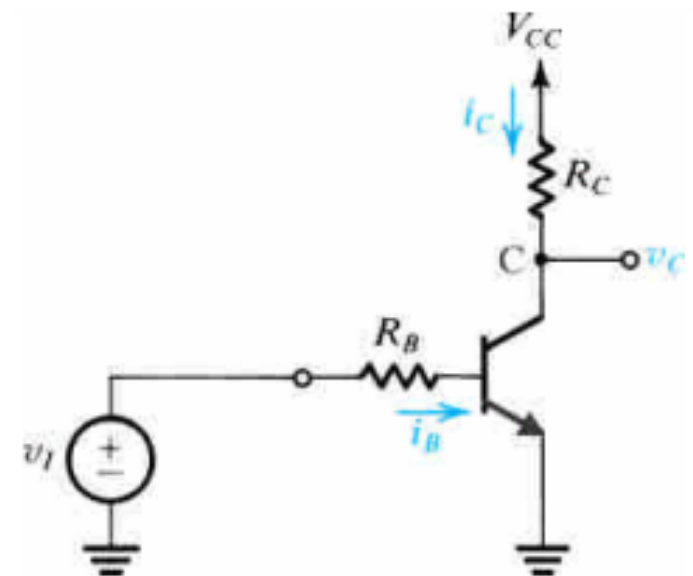
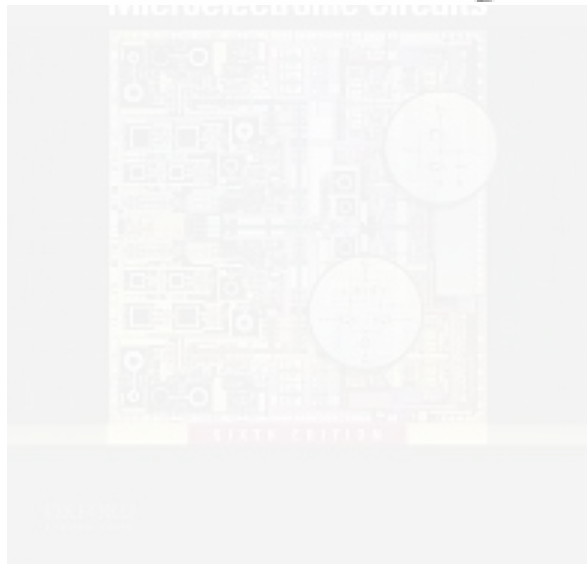
$$V_{I(\text{EOS})} = I_{B(\text{EOS})}R_B + V_{BE}$$



- we shall usually assume that for a saturated transistor,  $V_{CEsat} \approx 0.2 \text{ V}$ .

$$I_{Csat} = \frac{V_{CC} - V_{CEsat}}{R_C} \quad (5.66)$$

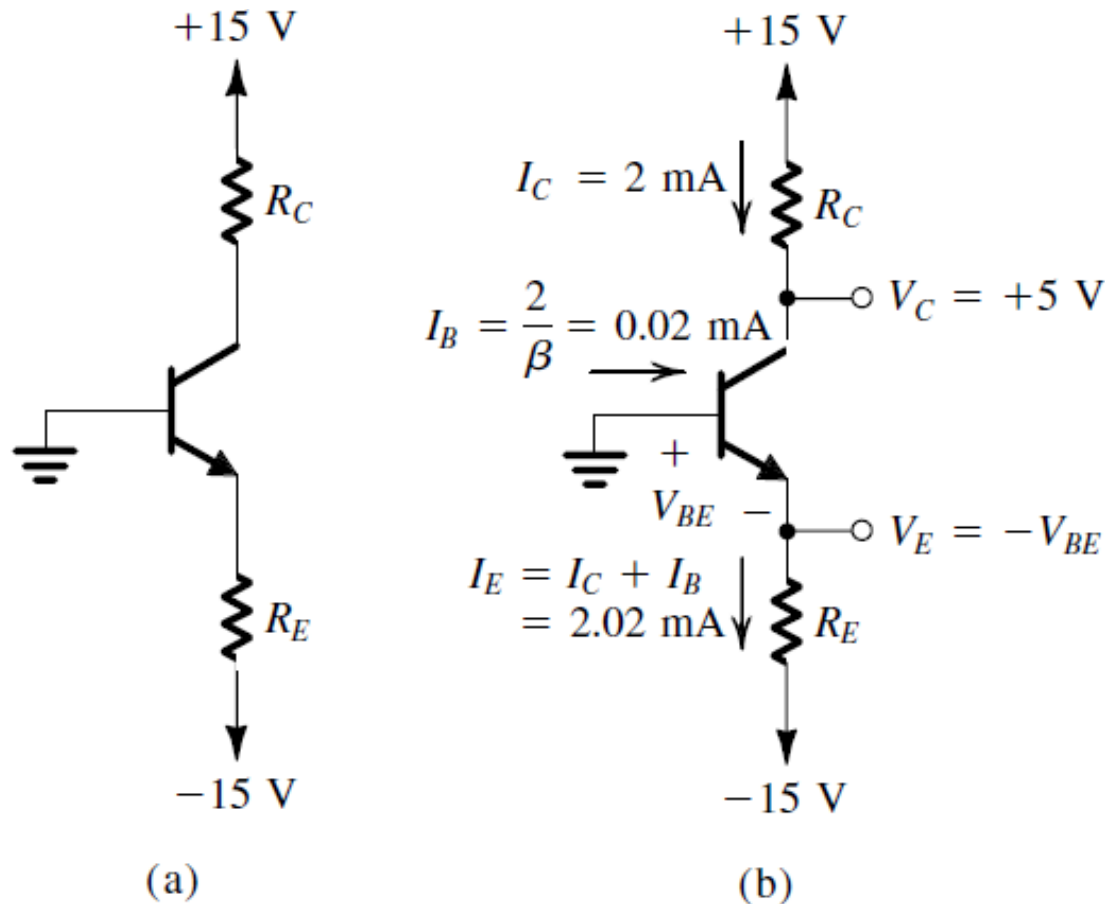
$$\beta_{forced} \equiv \frac{I_{Csat}}{I_B} \quad (5.67)$$



- **Let us solve some problems related to transistor currents and voltages. Use simpler and complex both models to see the error. Learn how to use given values to calculate unknown values.**

Given  $\beta = 100$ ,  $v_{BE} = 0.7\text{V}$  at  $1\text{ mA}$ .

Calculate  $R_C$  and  $R_E$  such that  $I_C = 2\text{ mA}$  and  $V_C$  (Voltage at collector wrt GND) =  $5\text{V}$



# Solution using crude model

1. Assume that  $v_{BE}$  is 0.7V at all currents --1 mA or 2 mA.
2. Since Base is at 0V, Collector at positive voltage and emitter at negative voltage, we can assume that transistor will be in active region.
3. If  $V_c = 5V$  and  $I_c = 2 \text{ mA}$  then
4. Using KVL,  $V_c = 15V - i_C R_c$   
or  $5V = 15V - 2 \text{ mA} \times R_c$ . We get  $R_c = 5K \text{ ohms}$ .
5.  $V_b = 0V$  or ground and since BJT is forward biased,  
 $V_e = V_b - 0.7V = -0.7V$
6. Using KVL,  $V_e = I_e R_e + (-15V)$   
If we neglect  $i_B$  then  $i_E = i_C = 2 \text{ mA}$  and that gives us  
 $R_e = (15 - 0.7V) / 2 \text{ mA} = 7.15K$  We get  $R_e = 7.15K \text{ ohms}$ .

# Solution using better model

1. Assume that  $v_{BE}$  is 0.7V only at 1 mA. Now calculate  $v_{BE}$  at 2 mA.

$$v_{BE} \text{ at } 2 \text{ mA} = v_{BE} \text{ at } 1 \text{ mA} + V_T \ln (2/1) = 0.717V$$

2. Since Base is at 0V,  $V_c$  required = 5V and  $I_c = 2 \text{ mA}$  then

Using KVL,  $V_c = 15V - I_C R_c$

$$\text{or } 5V = 15V - 2 \text{ mA} \times R_c \quad . \quad \text{We get } R_c = 5K \text{ ohms.}$$

3.  $V_b = 0V$  or ground and since BJT is forward biased,

$$V_e = V_b - 0.717V = -0.717V$$

4. Calculate  $i_B = i_C / \beta = 2 \text{ mA} / 100 = 0.02 \text{ mA}$

5. Calculate  $i_E = i_B + i_C = 2.02 \text{ mA}$

6. Using KVL,  $V_e = I_e R_e + (-15V)$

$$R_e = (15 - 0.717V) / 2.02 \text{ mA} = 7.07K. \quad \text{We get } R_e = 7.07K$$

**The error is 0.08K in 7K or nearly 1% .**



Given  $v_E = -0.7\text{V}$  and  $\beta = 50$ , calculate all 3 currents and collector voltage.

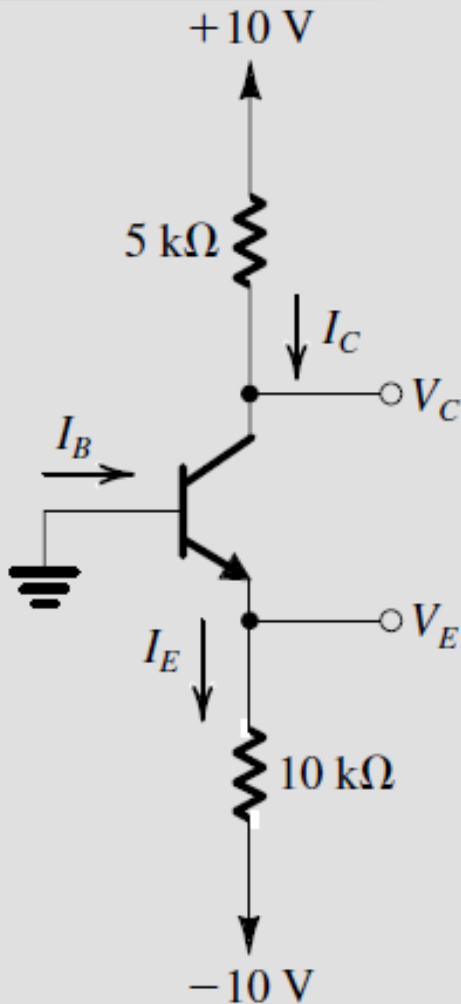
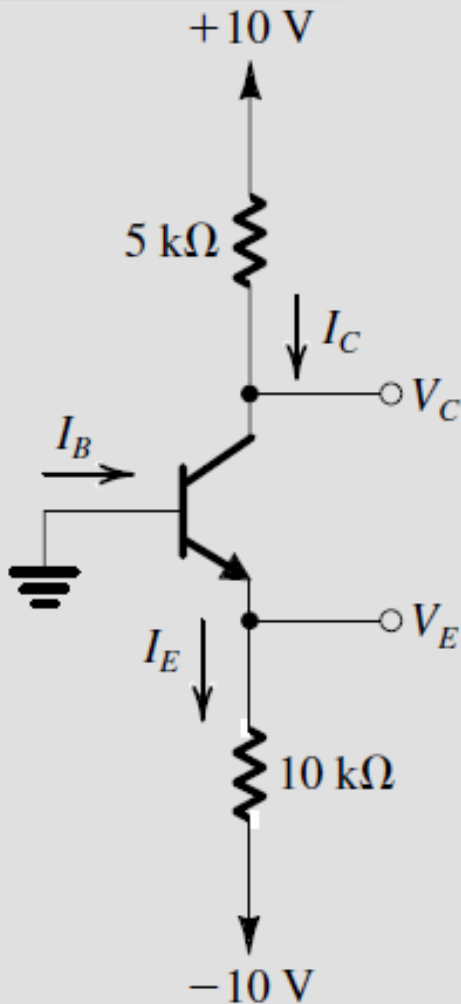


FIGURE E3.10

1. Calculate  $i_E$  from  $v_E$  and  $R_E$  and  $-10\text{V}$ .
2. Calculate  $i_B$  and  $i_C$ .
3. Calculate  $v_C$  from  $+10\text{V}$  and drop  $i_C R_C$ .

Given  $v_E = -0.7\text{V}$  and  $\beta = 50$ , calculate all 3 currents and collector voltage.



1.  $i_E = (-0.7 - (-10)) / 10\text{k} = 9.3\text{V} / 10\text{k} = 0.93\text{ mA}$
2.  $\alpha = \beta / (\beta + 1) = 50 / 51 = 0.980392$
3.  $i_C = 0.980392 * 0.93\text{ mA} = 0.911\text{ mA}$
4.  $i_B = i_C / \beta = 0.911 / 50 = 0.01822\text{ mA}$
5.  $V_C = 10\text{V} - i_C R_C = 10\text{V} - 0.911 * 5 = 5.441\text{ V}$

FIGURE E3.10

Given  $v_B = 1.0\text{V}$ ,  $v_E = 1.7\text{V}$ . Calculate alpha, beta and  $V_C$ .

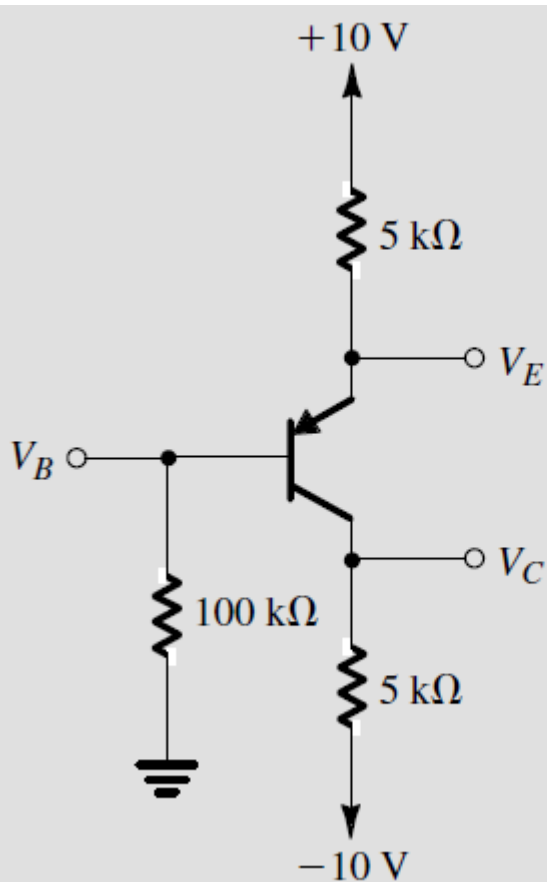


FIGURE E3.11

1. Calculate  $i_E$  from drop across  $R_E$ .
2. Calculate  $i_B$  from drop across  $100\text{K}$ .
3. Knowing these 2, get  $i_C$  and  $V_C$ .
4. Calculate alpha, beta.

Given  $v_B = 1.0\text{V}$ ,  $v_E = 1.7\text{V}$ . Calculate alpha, beta and  $V_C$ .

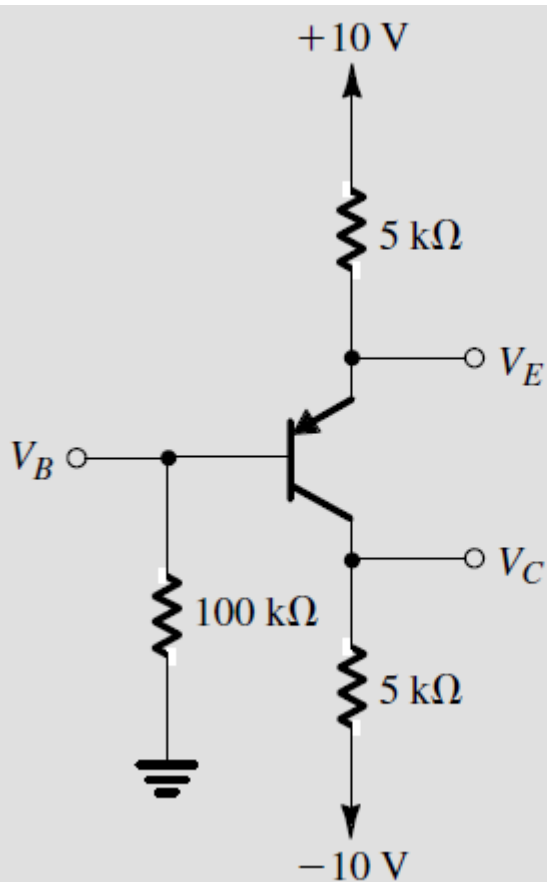


FIGURE E3.11

$$i_E = (10 - 1.7) / 5\text{K} = 1.66 \text{ mA}$$

$$i_B = 1\text{V} / 100\text{K} = 0.01 \text{ mA}$$

$$i_C = i_E - i_B = 1.66 - 0.01 \\ = 1.65 \text{ mA}$$

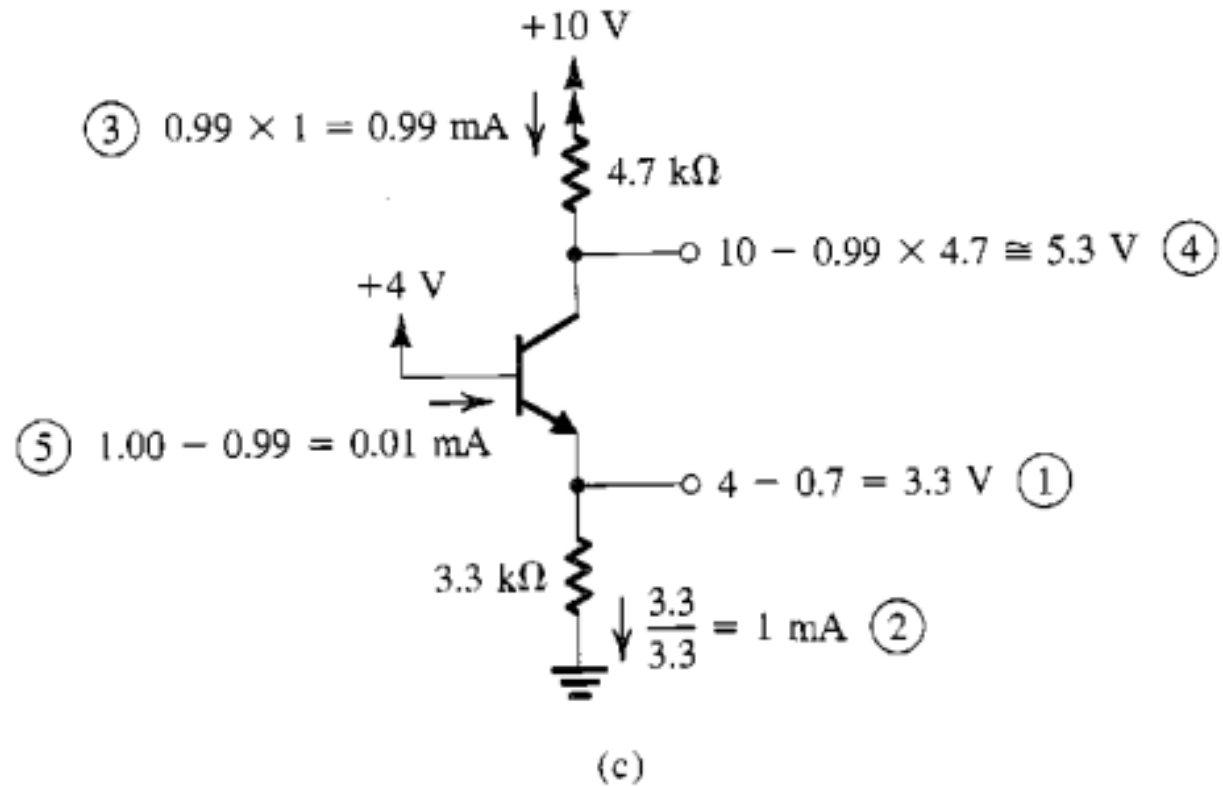
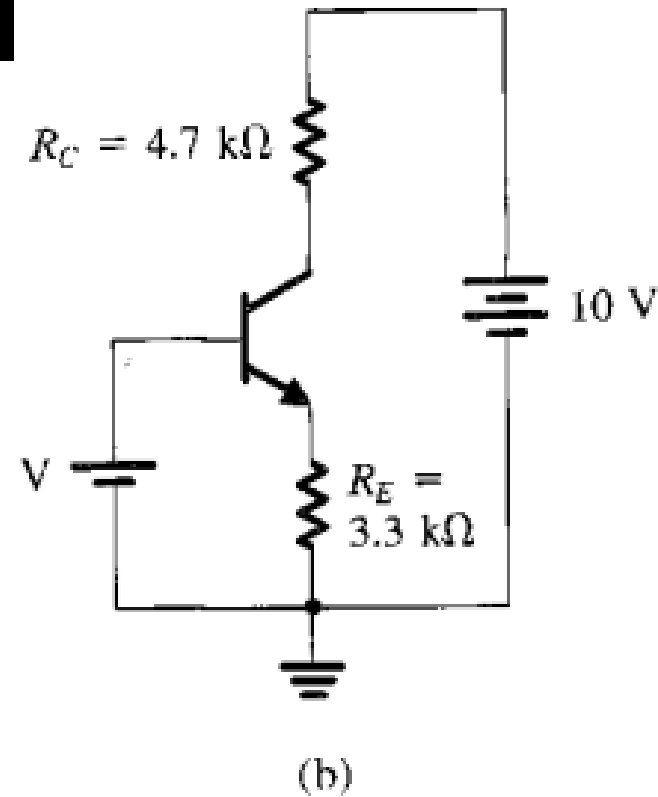
$$v_C = i_C R_C + (-10\text{V})$$

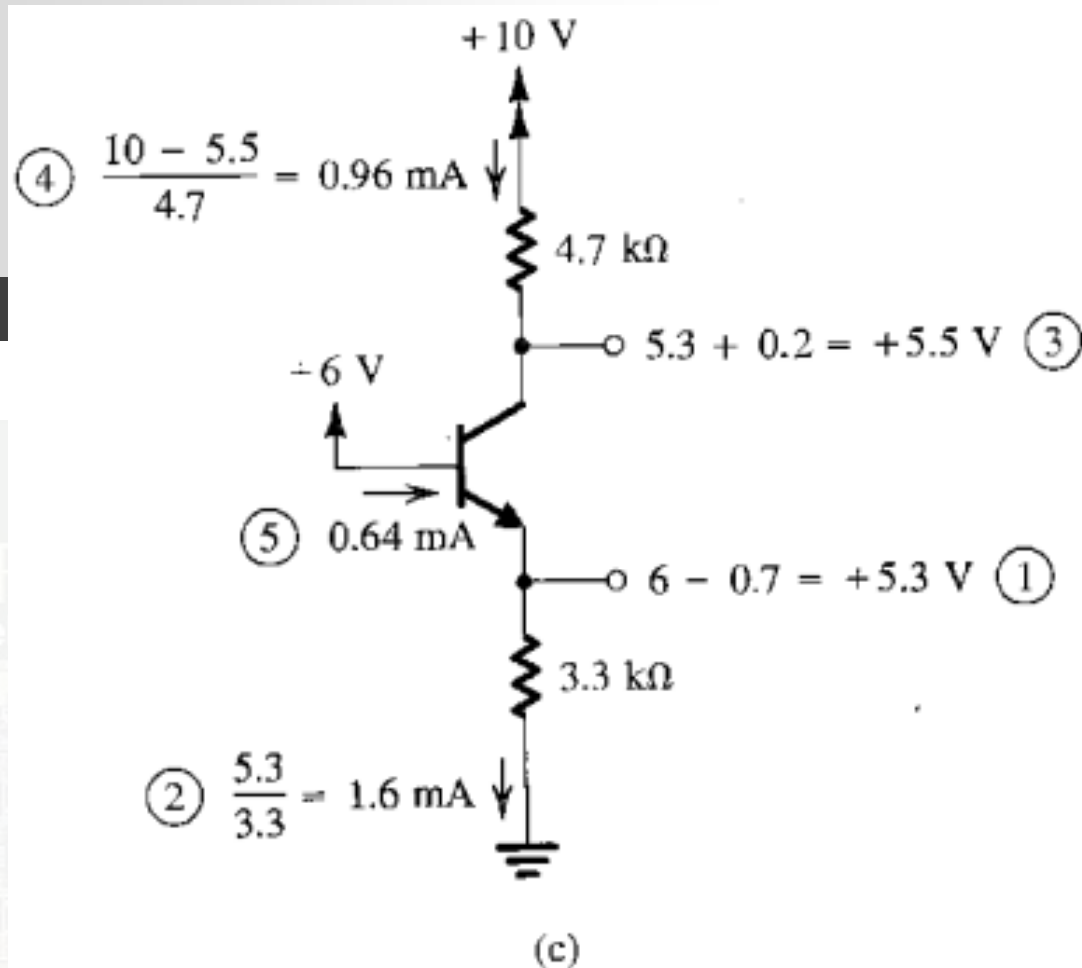
$$v_C = 1.65 \text{ mA} * 5\text{K} - 10\text{V} \\ = -1.75\text{V}$$

$$\text{Alpha} = i_C / i_E = 0.993976$$

$$\text{Beta} = i_C / i_B = 1.65 \text{ mA} / 0.01 \\ = 165$$

Analyze this circuit to determine all node voltages and branch currents. We will assume Beta as 100.





$$V_E = +6 - 0.7 = +5.3 \text{ V}$$

$$I_E = \frac{V_E}{3.3} = \frac{5.3}{3.3} = 1.6 \text{ mA}$$

$$V_C = V_E + V_{CE_{sat}} \approx +5.3 + 0.2 = +5.5 \text{ V}$$

$$I_C = \frac{+10 - 5.5}{4.7} = 0.96 \text{ mA}$$

$$I_B = I_E - I_C = 1.6 - 0.96 = 0.64 \text{ mA}$$

