$$\vec{E}(\vec{r}) = \frac{1}{4\pi60} \int_{V} \frac{g(\vec{r})}{|\vec{r}-\vec{r}|^{3}} (\vec{r}-\vec{r}') d^{3}\vec{r}'$$

$$\vec{\nabla} \times \vec{E}(\vec{r}) = \frac{1}{4\pi6} \left[r' \right] \left[\vec{r} \times \frac{(\vec{r} - \vec{r}')}{(\vec{r} - \vec{r}')^3} \right] d^3 \vec{r}'$$

$$\vec{\nabla} \times \frac{(\vec{\gamma} - \vec{\gamma})}{|\vec{\gamma} - \vec{\gamma}|^3} = \frac{1}{|\vec{\gamma} - \vec{\gamma}|^3} \vec{\nabla} \times (\vec{\gamma} - \vec{\gamma}) + \vec{\vec{r}} (\vec{r} - \vec{\gamma}) \times (\vec{\gamma} - \vec{\gamma})$$

$$\vec{\nabla} \times (\vec{\gamma} - \vec{\gamma}') = 0$$

$$\vec{\nabla} \left(\frac{1}{|\vec{\gamma} - \vec{\gamma}'|^3} \right) = -\frac{3}{|\vec{\gamma} - \vec{\gamma}'|^5} (\vec{r} - \vec{r}')$$

$$\nabla \times (\overrightarrow{S} - \overrightarrow{\gamma}) = 0$$

:
$$\vec{r} = \vec{r} = 0$$
 for any charge distribution.
 $\vec{r} = \vec{r} = \vec{r} = 0$ for any charge distribution.
 $\vec{r} = \vec{r} = \vec{r} = 0$ some scar function $\vec{r} = (\vec{r})$

Bo the direction of $\vec{\xi}$ is in the direction of maximum. increase of the function F and it is perpendicular to. the surface over which F is constant. Conventionally. È is considered to be directed along the fortest decrease. of a function rather thom furtest increase. Such a. function is obviously -F, let $\mathcal{F}(\vec{r}) = -F(\vec{r})$. 80 产= 节里· The function $\Phi(3)$ is called the potential function. of the charge configuration. It is offen a more convenient of the charge configuration. It is a scalar. It is a scalar of the charge than the hopodle than \$\frac{1}{2} \text{ since it is a scalar of the country find the hopodle know \$\Pi(P)\$ we can easily find of course once we know \$\Pi(P)\$ us. It is a scalar of the convenient of the course of the course of the course of the convenient of the course of t $\vec{E}(\vec{r})$. Note that if $\vec{P}' = \vec{\Phi} + \vec{c}$ where \vec{c} is a substitute $\vec{E}(\vec{r})$. countant then. $\vec{\nabla} \vec{\Phi}' = \vec{\nabla} \vec{\Phi}$. 80. $\vec{\Phi}'$ is also a valid. potantial for the charge configuration. So the potantial. 4 always arbitrary upto a constant value. However. the potential différence is indépendent of this arbitrarines. $\mathcal{J}'(b) - \mathcal{J}'(a) = (\mathcal{J}(b) + c) - (\mathcal{J}(a) + c) = \mathcal{J}(b) - \mathcal{J}(a)$

If we know the potential due to charges q_1, q_2, \dots, q_n as $\bar{f}_1, \bar{f}_2, \dots, \bar{f}_m$, then the potential for the configuration is can be obtained as a linear superposition of this potentials. $\bar{f}:=\bar{f}_1+\bar{f}_2+\dots+\bar{f}_m$

This is obtained from the linear superpositions of electric

 $\vec{E} = \vec{E}_1 + \vec{E}_2 + \dots + \vec{E}_n$ $= -\vec{\nabla} \vec{P}_1 \cdot \vec{P}_2 - \dots - \vec{P} \vec{P}_n$ $= -\vec{\nabla} (\vec{P}_1 + \vec{P}_2 + \dots + \vec{P}_n) = -\vec{P} \vec{P}$ You if \vec{P}_1' in any other potential. satisfyin

Now if \vec{b}' is any other potential. satisfying $\vec{t} = -\vec{P} \vec{b}'$ then. we have.

0= - 7 (] - 9')

This implies the scalar function $\bar{\Phi} - \bar{\Phi}'$ is containt. As we stated earlier $\bar{\Phi}' = \bar{\Phi} + c$ are equivalent. So $\bar{\Phi}$ is indeed the potential for the given charge. Configuration.

In. M.K.S. anit. potential is measured in N m / coulomb = Jowe/Coulomb. This is called the volt.

So I Volt = I Jowle. Coulomb.

The arbitrary constant affecting in the potential that can be added to a potential can be used to measure the before added to a potential can be used to some convenient potential. At a poi with respect to some convenient point. So if we say

then present at every point is in measured. With respect to the point b. In this form. $\delta(b) = 0$.

Generally when the charge configuration is confined.

When a bounded Region, the potential at inthin a bounded to be and hence the pinfinity is in considered to be and hence the pinfinity be comes the Reference.

承(家): - 5 (家): - 5 (s): -

Potential due tia point charge.

マーマー (マ)

A point charge q is at the origin.

E(8): 4560 82 8.

元: でーで

The procent of at a point of is

\$\int (\frac{1}{2}) = -\int \int \int \frac{2}{4\tau 60} \int \frac{7}{12} \int \int \frac{2}{12} \delta \tau \int \frac{2}

If the reference point b. is at as then. $8_b \Rightarrow \infty$ $\therefore \bar{\phi}(\bar{\tau}) = \frac{2}{4\bar{\pi} 6 \bar{\sigma} \bar{\tau}}$

toopt Note: The startion function is generally denoted by.

Loplace's Equation: The divergence. Theorem states

that $\vec{\nabla} \cdot \vec{E} = \frac{8}{6}$

where \vec{r} is the charge density at the point where \vec{r} . \vec{r} is calculated. Now.

Since $\vec{r} = -\vec{r} \cdot \vec{r}$ we have.

 $\vec{\nabla} \cdot \vec{E} = - \vec{\nabla} \cdot (\vec{\nabla} \vec{\Phi}) = \frac{9}{6}$

 $\therefore -\nabla^2 \hat{\theta} = \frac{g}{60}$

Equation I. is called the baptace's Equation. It is a partial differential Equation. If we are.

given a charge distribution i.e. the alemity function g(g), then we can get g by solving. the Poisson's Equation from g we can find the electric field at all points. This is the central problem of Electro statics.

When the charge density at a point's o we

 $\nabla^2 \vec{\Phi} = 0$ \subseteq Σ .

This is called. The Laplace's Equation. This is a. homogeneous. differential Equation.

he will study methods to sofre the Laplace's Equation. in trave three disnersion in various co-ordinate systems. If we know any one. solution to the Poissen's. Equation, called a particular solution, we comfind. any other solution by adding the solution of Laplace's. Equation to it. & our essential. Job is to find to. all possible solutions to the. Caplace's. Equation. All this works. because. It is a line of operator. Hence the solutions. to thes. Laplace is. Equation forms. a. linear vector space

why do we need Laplace's Equation. when we are mainly interested in the Poisson's Eqn?

Genearally we would be requiring to find the Electric field & and the electric potential.

Franked due to a given charge distribution.

given by the function $S(\vec{r})$.

To understand the importance of Laplace's Egn. in Electrostatics. lef us compare it with a. more. familiar problem. This is the Newston's. Equation of motion.

Electrostatics.

$$abla^2 \hat{\phi} = -\frac{9}{60}$$

Mechanin.

$$\frac{d^2\vec{r}}{dt^2}: \frac{\vec{F}}{m}$$

$$\frac{d^2\vec{y}}{dt^2} = 0$$

Non ton's. Eqn. of motion. is significant to the. Po'ron's. Eqn. Both. are. 2nd order differential. Equations. In. Newton's. Eqn. the. R. H. S. has. the. Source. or the. course. of the motion. the source or the course. of the motion. Once we know . Fi we can find ly frajector. The thouse of the prison's. Eqn. Same is the case. with. the Prison's. Eqn. in Electrostation.

The second fam. are also equivalent. In mechanica. if we have. $\vec{F} = D$ in allegators the particle follows: a. straight line motion.

given by: $\vec{F}(t) = \vec{u}t + \vec{k}$ Whene is and a are - constant rectors to. be defermined from certain initial coordition. say the paritions at and the relocities at certain times instant of time- & Dome himer we don't have - well-defined for res. acting on the particle. The particle. Collider with certagin barriers at certain. times. and bounces. In between these. collissions tu particle fravels straight like. to to to the partiale danger.

The change in infinitesimal.

times. The forces imported during collision are.

Infinite for a very small hime. They are called.

the S- functions. In fine - they are called. the 8-functions. In time - They are called.
impulsive forces, be can obtain ouch trajectories. by solving the free particle. Egns in the various. Sime. intervals. and then match the trajectories. at the instants ti, tz, tz, ---; to get û, û, û, û:--. Even. in electrostation. often. Cha. source. teran. on the - R. H. S. of Polstonis. Egn. are. not [well-defined" an a. volume. donnity function. S(3). But they may box. some. surface.

Such distribution.

Sharges. or line charges. such distribution.

charges. or line if written as. volume-demilies

are. as we have discussed and seen in various. situation. These are exactly like the sources.

Situation. These are exactly like the sources.

Situation of impulsive forces. So here me rather solve. The fre space.

So here me rather watch. kn. solutions.

Egn. Viz the Laplace's. Egn. in various.

Region. and then watch. af em boundanier. of these. regions. confaining the subject of line (impulsive) charges. Shortly we mill see in defail her to do this This will be the central topic. for. in electrostation for some. from.