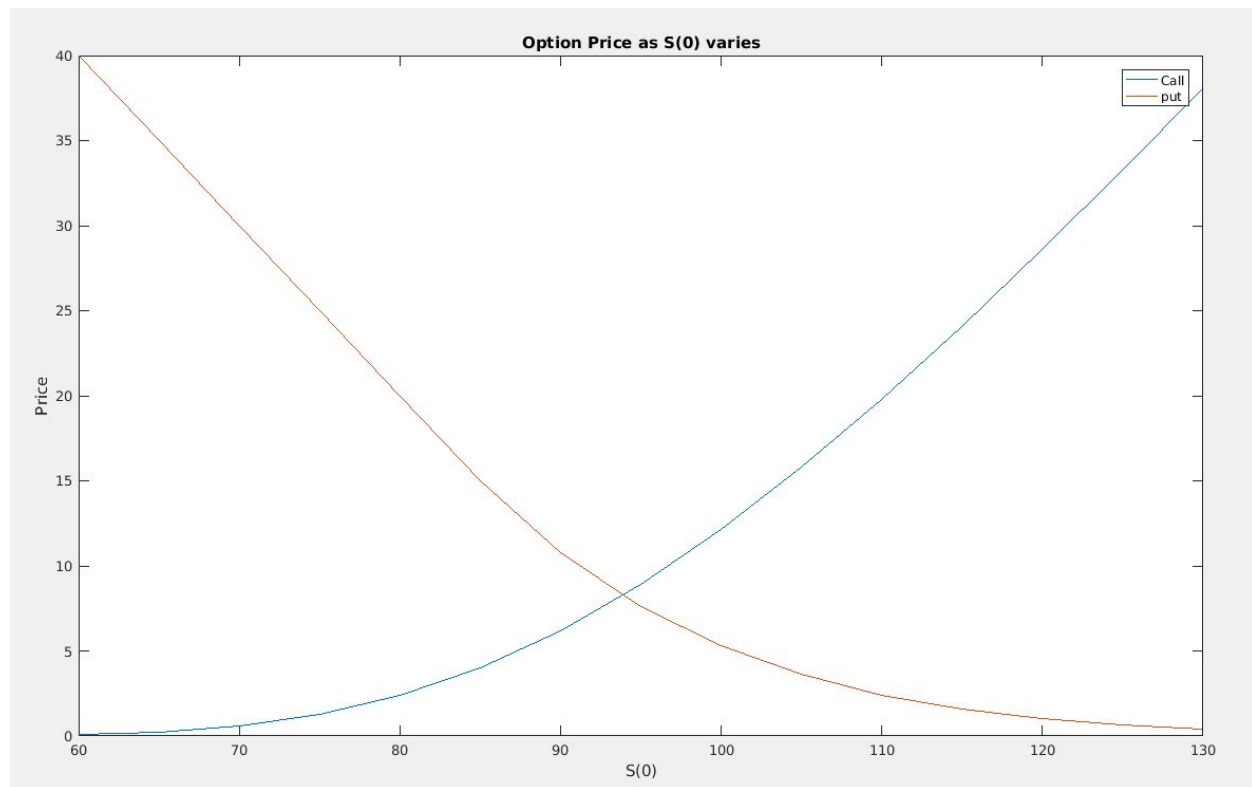
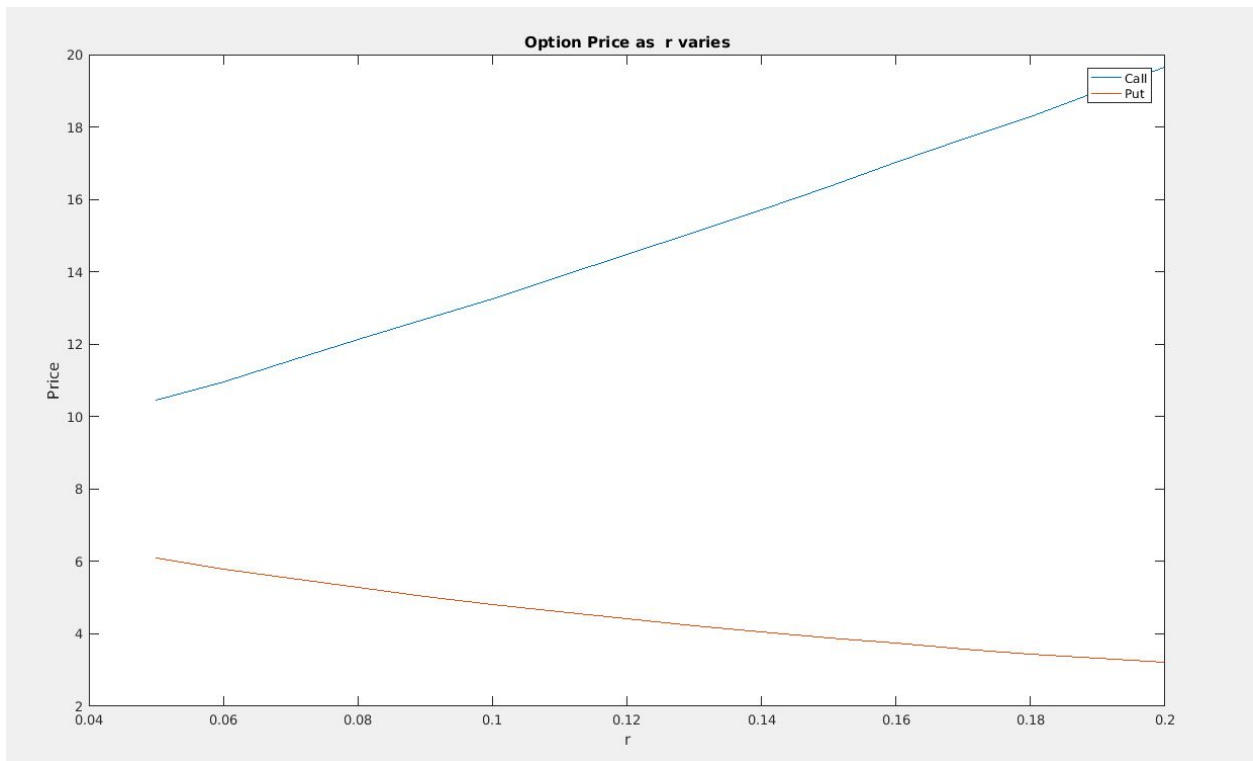
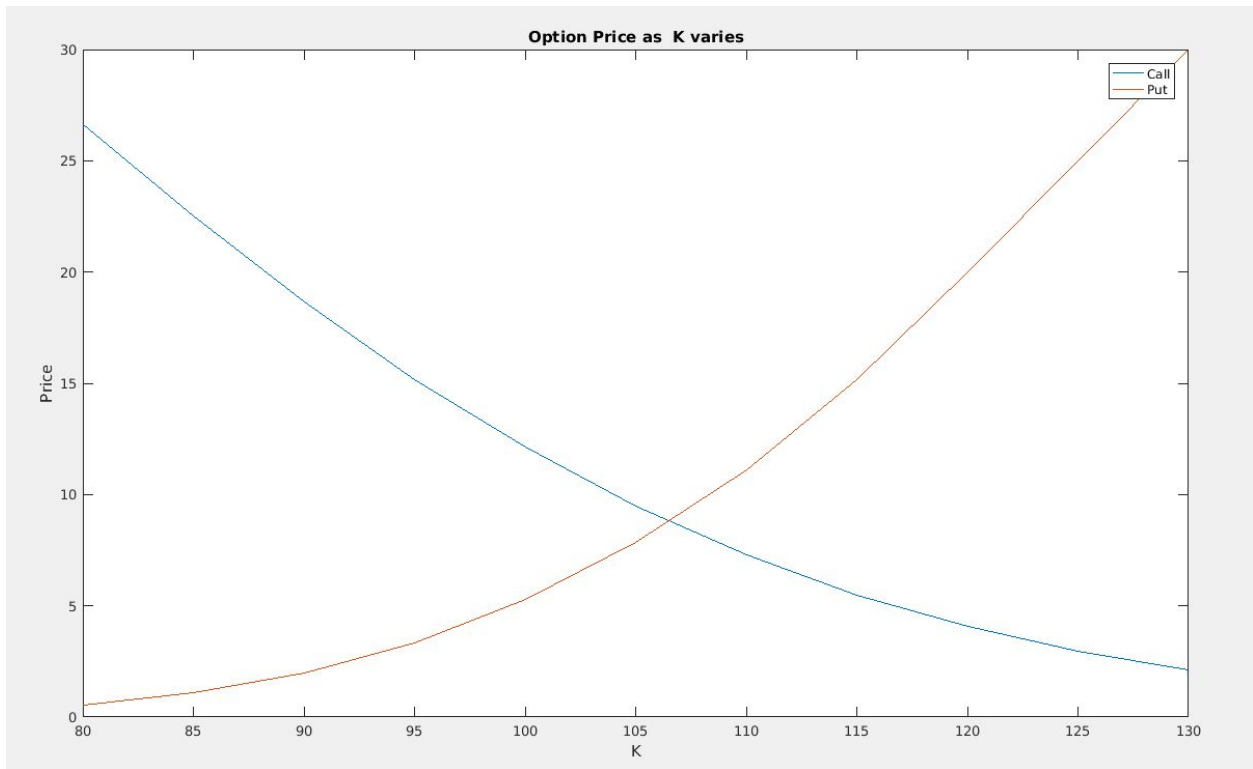
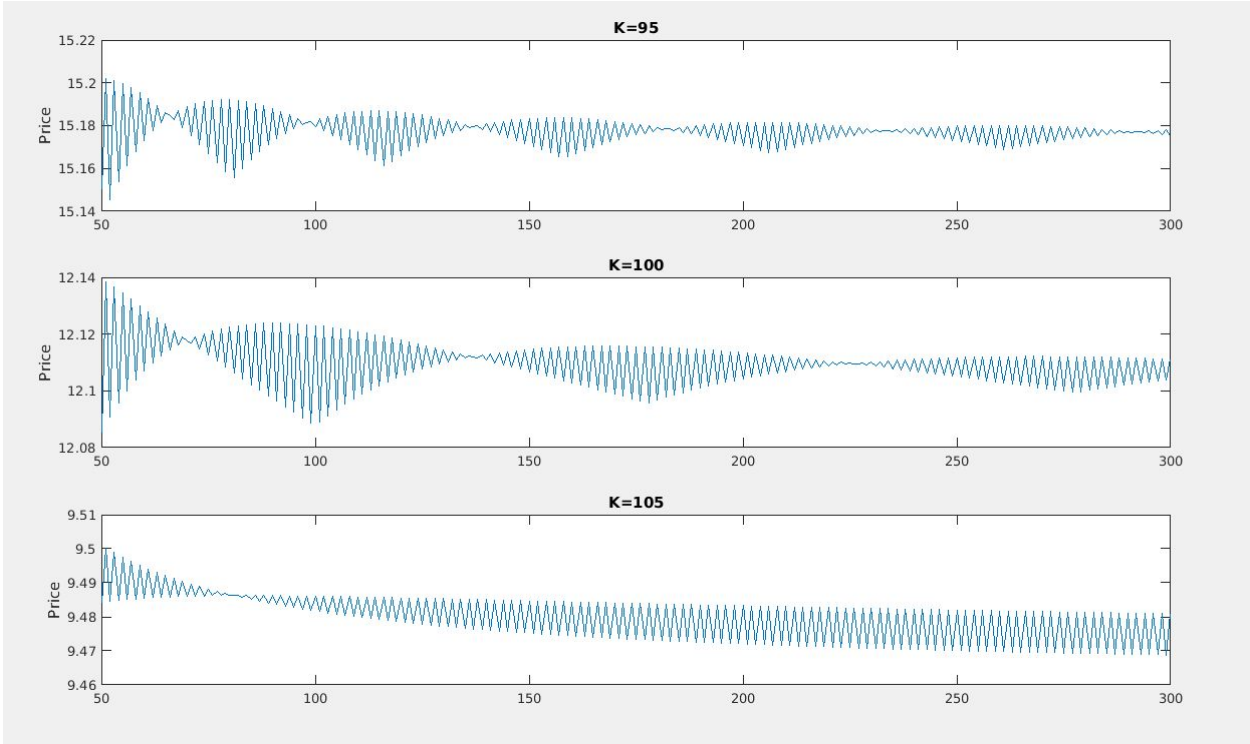
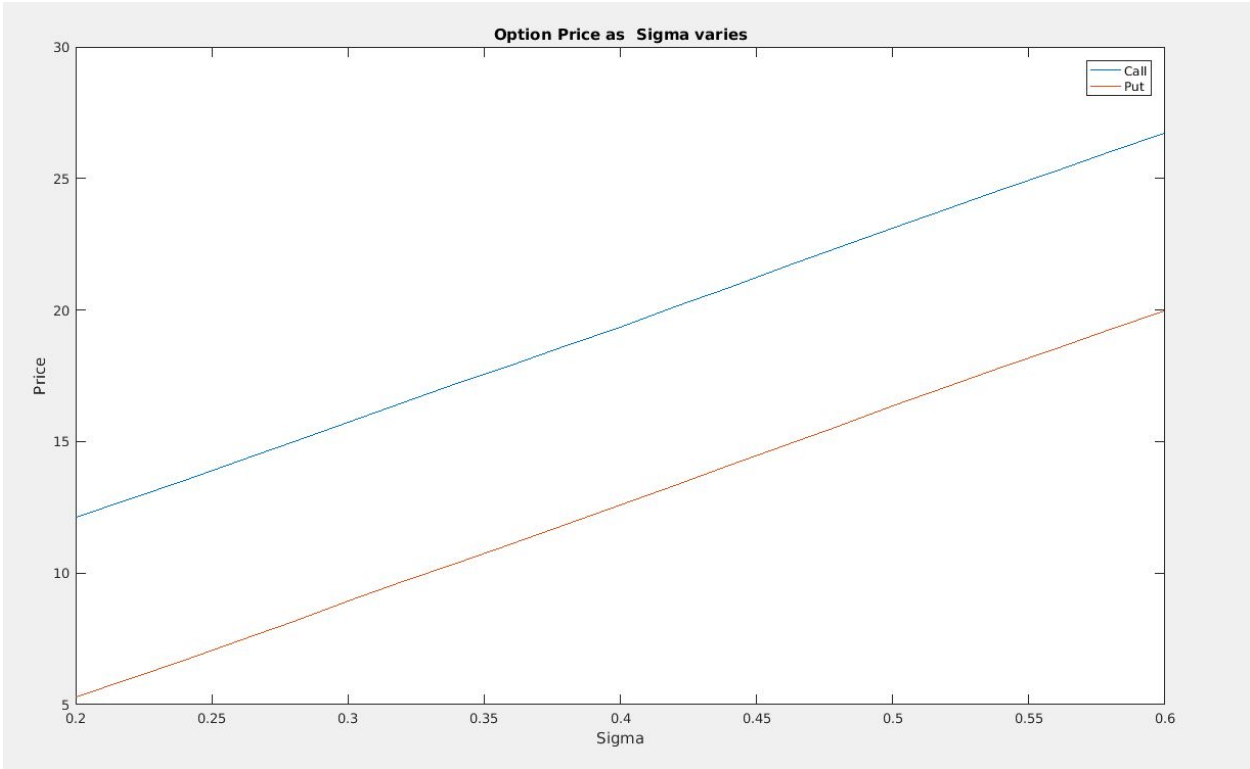


Problem 1:





Problem 2:

For $M = 5$ the values at each intermediate level are

level 2 : 9.027951 9.504840

level 3 : 8.548076 9.799119 7.147916 12.168665

level 4 : 7.416771 9.955271 6.201916 13.712863 6.201916 8.324615
7.148418 17.582063

level 5 : 5.501639 9.571392 4.600480 15.631852 4.600480 8.003614
6.680843 21.188089 4.600480 8.003614 3.846929 13.071381
3.846929 10.680904 10.680904 25.051229

The initial price of the option for $M = 5$ is 9.119299

The initial price of the option for $M = 10$ is 10.080583

The initial price of the option for $M = 15$ is 10.519165

The initial price of the option for $M = 20$ is 10.805119

The initial price of the option for $M = 25$ is 11.003495

Time taken for $M=5$ is 0.007235 seconds.

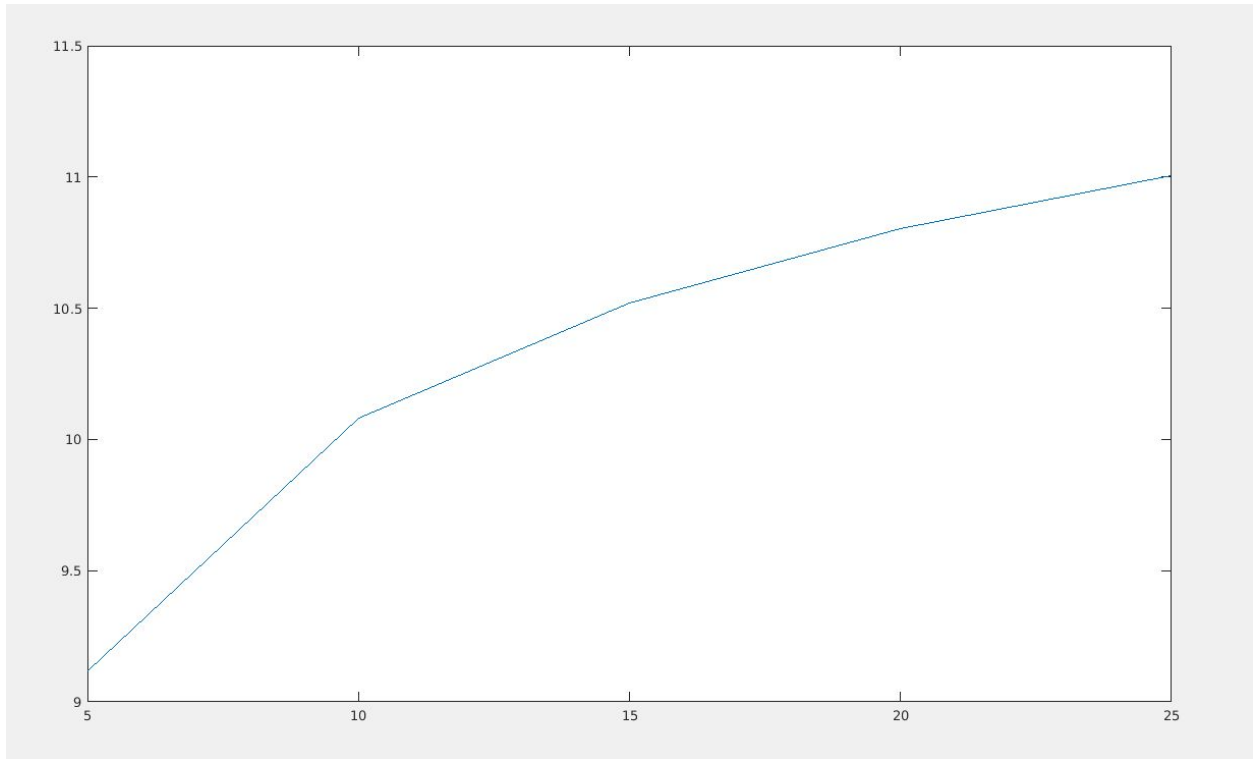
Time taken for $M=10$ is 0.003591 seconds.

Time taken for $M=15$ is 0.033504 seconds.

Time taken for $M=20$ is 0.887279 seconds.

Time taken for $M=25$ is 28.601824 seconds.

This is the graph for M vs initial option price for look back option.



Problem 3:

Elapsed time is 0.003419 seconds.

For $m=5$ the price of the lookback option is 9.119299

Elapsed time is 0.002818 seconds.

For $m=10$ the price of the lookback option is 10.080583

Elapsed time is 0.041241 seconds.

For $m=25$ the price of the lookback option is 11.003495

Elapsed time is 0.643968 seconds.

For $m=50$ the price of the lookback option is 11.510862

Elapsed time is 13.448697 seconds.

For $m=100$ the price of the lookback option is 11.888705

| Method | M=5 | M=10 | M=25 |
|------------------|-----------|-----------|------------|
| Not using Markov | 0.007235s | 0.003591s | 28.601824s |
| Markov | 0.003419s | 0.002818s | 0.041241s |

There isn't much change for small values of M but changes significantly for large M. For M above 30 without using markov process takes so much time to complete whereas using markov for M=100 also it takes half the time when compared to M=25 in non markov process.

Problem 4:

For m=5 The price of the European Call by using Markov is 12.163186

For m=10 The price of the European Call by using Markov is 12.277328

For m=25 The price of the European Call by using Markov is 12.136746

For m=50 The price of the European Call by using Markov is 12.085362

The price of the European Call option for m=5 is 12.163186

The price of the European Call option for m=10 is 12.277328

The price of the European Call option for m=25 is 12.136746