



Relational Database Design

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2NF(2nd Normal Form)

- A Relation schema R with FD is said to be in 2NF w.r.t F^+ if there doesn't exist any partial functional dependency in F^+ .

Partial Functional Dependency:- Consider a relation schema that has a composite key k. The relation schema is said to exhibit partial FD of the form x 'determines' y or $x \rightarrow y$ if x is a proper subset of k (key of R) and y is a non key attribute.

Alt Def: When a part of key (key being composite) functionally determines non key attribute then the functional dependency shall be a partial functional dependency.

2NF(2nd Normal Form) Example

- $R = (A, B, C, D, E)$
 $F = \{A \rightarrow B, C \rightarrow D, AC \rightarrow E\}$
Key = {AC}

Verify R satisfy 2NF or not??

Key=AC

There exist partial FDs of the form $A \rightarrow B, C \rightarrow D$

Hence it is not in 2NF

??? SO what should we do??

Goals of Normalization

- Let R be a relation scheme with a set F of functional dependencies.
- Decide whether a relation scheme R is in “good” form.
- In the case that a relation scheme R is not in “good” form, decompose it into a set of relation scheme $\{R_1, R_2, \dots, R_n\}$ such that
 - each relation scheme is in good form
 - the decomposition is a lossless-join decomposition
 - Preferably, the decomposition should be dependency preserving.

2NF(2nd Normal Form) Example

- $R = (A, B, C, D, E)$
 $F = \{A \rightarrow B, C \rightarrow D, AC \rightarrow E\}$
Key = $\{AC\}$

Decomposition

- $R_1 = (A, B)$ key = A $F_1 = \{A \rightarrow B\}$ key = A
- $R_2 = (C, D)$ key = C $F_2 = \{C \rightarrow D\}$ key = C
- $R_3 = \{A, C, E\}$ key = AC $F_3 = \{AC \rightarrow E\}$ key = AC

This is lossless decomposition because

$R_1 \cap R_3 = A \rightarrow B$ is the key of R_1

$R_2 \cap R_3 = C \rightarrow D$ is the key of R_2

Its also dependency preserving because

$$(F_1 \cup F_2 \cup \dots \cup F_n)^+ = F^+$$

Third Normal Form

- A relation schema R is in **third normal form (3NF)** if for all:

$$\alpha \rightarrow \beta \text{ in } F^+$$

at least one of the following holds:

- $\alpha \rightarrow \beta$ is trivial (i.e., $\beta \in \alpha$)
- α is a super key for R
- At least one attribute in right hand side i.e. β must contain a prime attribute (i.e. a part of candidate key)

(**NOTE:** each attribute may be in a different candidate key)

key \rightarrow nonkey \rightarrow nonkey leads to redundancy and hence must be eliminated

Alternative Definition: A relation schema(R) is in 3NF if R is in 2NF and doesn't exhibit any transitive chain of dependency of the form key \rightarrow nonkey \rightarrow nonkey

3NF Example

■ Relation *dept_advisor*:

- *dept_advisor* (*s_ID*, *i_ID*, *dept_name*)
 $F = \{s_ID, dept_name \rightarrow i_ID, i_ID \rightarrow dept_name\}$
- Two candidate keys: *s_ID*, *dept_name*, and *i_ID*, *s_ID*
- *R* is in 3NF
 - ▶ $s_ID, dept_name \rightarrow i_ID$
s_ID, *dept_name* is a superkey
 - ▶ $i_ID \rightarrow dept_name$
dept_name is contained in a candidate key

Testing for 3NF

- Optimization: Need to check only FDs in F , need not check all FDs in F^+ .
- Use attribute closure to check for each dependency $\alpha \rightarrow \beta$, if α is a superkey.
- If α is not a superkey, we have to verify if each attribute in β is contained in a candidate key of R
 - this test is rather more expensive, since it involve finding candidate keys
 - testing for 3NF has been shown to be NP-hard
 - Interestingly, decomposition into third normal form (described shortly) can be done in polynomial time

3NF Decomposition Algorithm

Let F_c be a canonical cover for F ;

$i := 0$;

for each functional dependency $\alpha \rightarrow \beta$ in F_c **do**
 if none of the schemas R_j , $1 \leq j \leq i$ contains $\alpha \beta$
 then begin

$i := i + 1$;

$R_i := \alpha, \beta$

end

if none of the schemas R_j , $1 \leq j \leq i$ contains a candidate key for R
 then begin

$i := i + 1$;

$R_i :=$ any candidate key for R ;

end

/* Optionally, remove redundant relations */

repeat

if any schema R_j is contained in another schema R_k
 then /* delete R_j */

$R_j = R$;

$i = i - 1$;

return (R_1, R_2, \dots, R_i)

Optional---Erase Unnecessary Tables

3NF Decomposition Algorithm (Cont.)

■ Summary of the Above Algorithm:

1. To Find Canonical Cover F_c for the F.D set.
2. For each F.D in F_c we create a new Relational schema.
3. If any schema doesn't contain the candidate key then make a new schema for the candidate key itself.
4. Remove unnecessary relation schemas

■ Above algorithm ensures:

- each relation schema R_i is in 3NF
- decomposition is dependency preserving and lossless-join
- Proof of correctness is at end of this chapter

3NF Decomposition: An Example

- Relation schema:

cust_banker_branch = (customer_id, employee_id, branch_name, type)

- The functional dependencies for this relation schema are:

1. *customer_id, employee_id → branch_name, type*
2. *employee_id → branch_name*
3. *customer_id, branch_name → employee_id*

- We first compute a canonical cover

- *branch_name* is extraneous in the r.h.s. of the 1st dependency
- No other attribute is extraneous, so we get $F_C =$

customer_id, employee_id → type

employee_id → branch_name

customer_id, branch_name → employee_id

Key = {employee_id, customer_id}

3NF Decompsition Example (Cont.)

- The **for** loop generates following 3NF schema:

(customer_id, employee_id, type)

(employee_id, branch_name)

(customer_id, branch_name, employee_id)

- Observe that *(customer_id, employee_id, type)* contains a candidate key of the original schema, so no further relation schema needs be added

- At end of for loop, detect and delete schemas, such as *(employee_id, branch_name)*, which are subsets of other schemas

- result will not depend on the order in which FDs are considered

- The resultant simplified 3NF schema is:

(customer_id, employee_id, type)

(customer_id, branch_name, employee_id)

Redundancy in 3NF

- There is some redundancy in this schema
- Example of problems due to redundancy in 3NF
- $J = s_ID$, $K = dept_name$, $L = i_ID$

- $R = (J, K, L)$
 $F = \{JK \rightarrow L, L \rightarrow K\}$

J	L	K
j_1	l_1	k_1
j_2	l_1	k_1
j_3	l_1	k_1
<i>null</i>	l_2	k_2

- repetition of information (e.g., the relationship l_1, k_1)
 - $(i_ID, dept_name)$
- need to use null values (e.g., to represent the relationship l_2, k_2 where there is no corresponding value for J).
 - $(i_ID, dept_name)$ if there is no separate relation mapping instructors to departments

Thank You