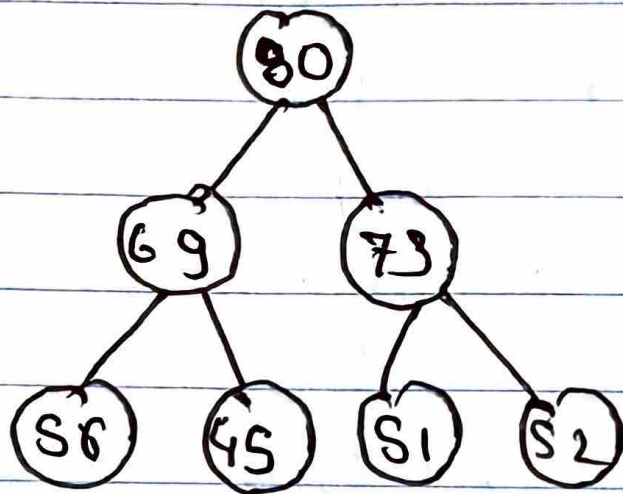
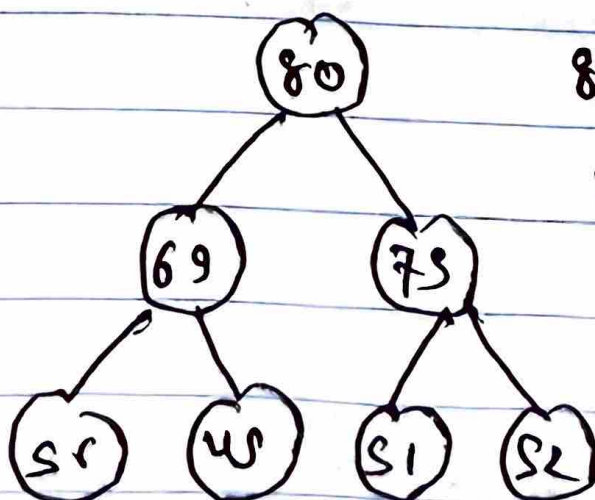


* Heaps :- In general we talk about binary heap where a node can have maximum of 2 children.



There are 2 types of heap
i) max heap
ii) min heap

i) Max heap :- In this the parent or root node must be greater than its child and same follows for the sub-tree.



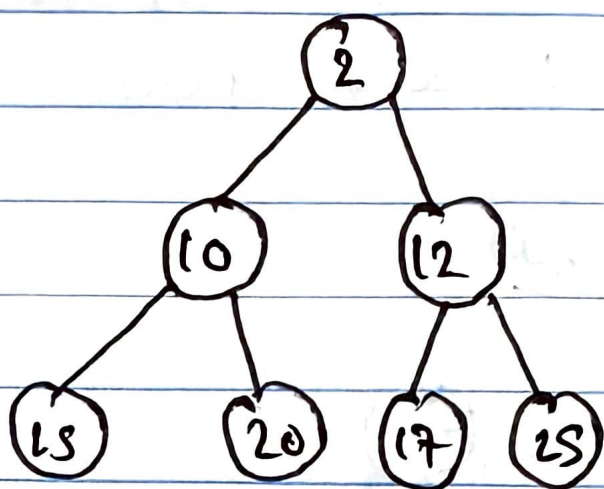
$$80 > 69, 73$$

For sub-tree,

$$69 > 56 \text{ and } 45$$

$$73 > 51 \text{ and } 52$$

Min heap :- In this the root node must be smaller than the child node.



$$\begin{array}{l}
 2 < 10 \ \& \ 12 \\
 10 < 15 \ \& \ 20 \\
 12 < 17 \ \& \ 25
 \end{array}$$

* height of any tree can be calculated using $h = \log(n)$

* When adding items into array it has to be followed level wise and left to right.

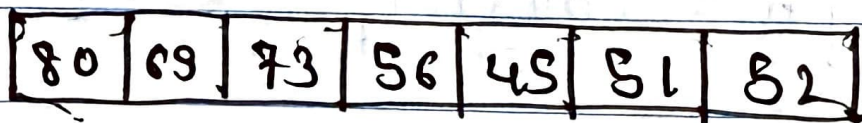
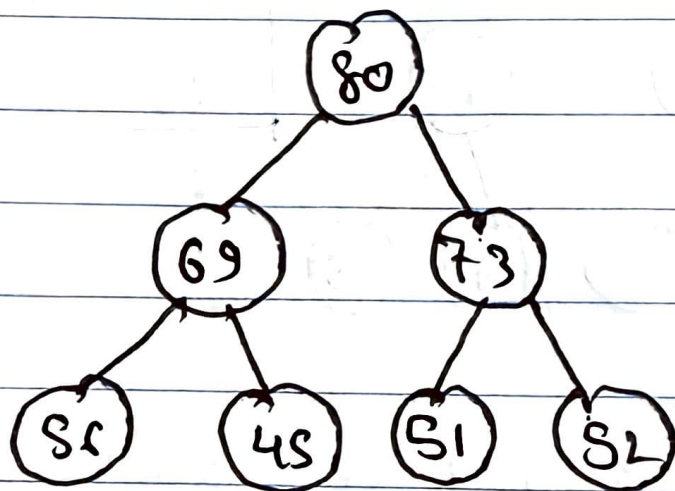
0	1	2	3	4	5	6
80	69	73	56	45	51	52

As this is structured tree so the index for left $[2i+1]$ and right $[2i+2]$. To get parent Node.

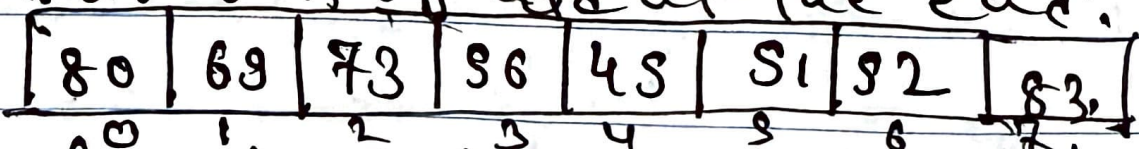
$$i = \frac{i}{2} - 1 \Rightarrow \frac{4}{2} - 1 \Rightarrow 1$$

begin Parent

- * Search and Heap together is a bad situation,
- * Search has $O(n)$ complexity.
- * Inserting a number which is greater than root node.



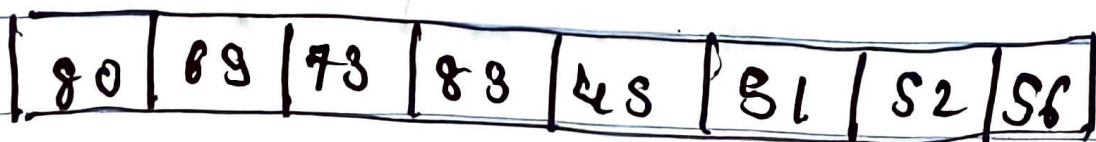
- * Suppose adding a number **83**.
- * First simply add at the end.



- * Let's calculate the parent of 83.

$$\frac{7}{2} - 1 = 3.5 \approx 2.5$$

Upper part of 2.5 is 3 [56] is the parent. Let's swap the position. If $83 > 56$ then swap.



Again same step :-

80	88	73	69	45	S1	S2	S1
----	----	----	----	----	----	----	----

again :-

88	88	73	69	45	S1	S2	S1
----	----	----	----	----	----	----	----

→ Insert complexity $\log(n)$.
or $O(\log n)$. In best case $O(1)$

* Deletion :- If deleting last element $O(1)$, If working with Binary heap we are only allowed to delete root node. $O(\log n)$.

* Heap Sort! Heap sort means sort either ascending to descending or descending to ascending.

* In terms of max heap we'll go from min to max.

* Priority Queue :- In priority queue the FIFO is not followed the element with priority and normal treated separately. Priority Queue is implemented by heap.

* Heapify is a process of converting any binary tree into a complete heap.