

Note: This is the summary note from Udacity Introduction to Deep Learning with PyTorch

Neural Network

- Find the boundary that separate two / more data set
- Complicated data -> need complicate algorithm
- Classify problem

Classification

- Classify problem
- How do we find the line / boundary between two data set

Linear Boundary

- Linear boundary -- Linear equation

Equation: $w_1x_1 + w_2x_2 + b = 0$

Vector notation: $WX + b = 0$

Weight: $W(w_1, w_2)$

Input: $X(x_1, x_2)$

Label: $y = 0 \text{ or } 1$

$$\text{prediction: } \hat{y} = \begin{cases} 1 & \text{if } WX + b \geq 0 \\ 0 & \text{if } WX + b < 0 \end{cases}$$

- **Mission:** have \hat{Y} resemble to Y as close as possible in order to create linear boundary

Higher Dimension

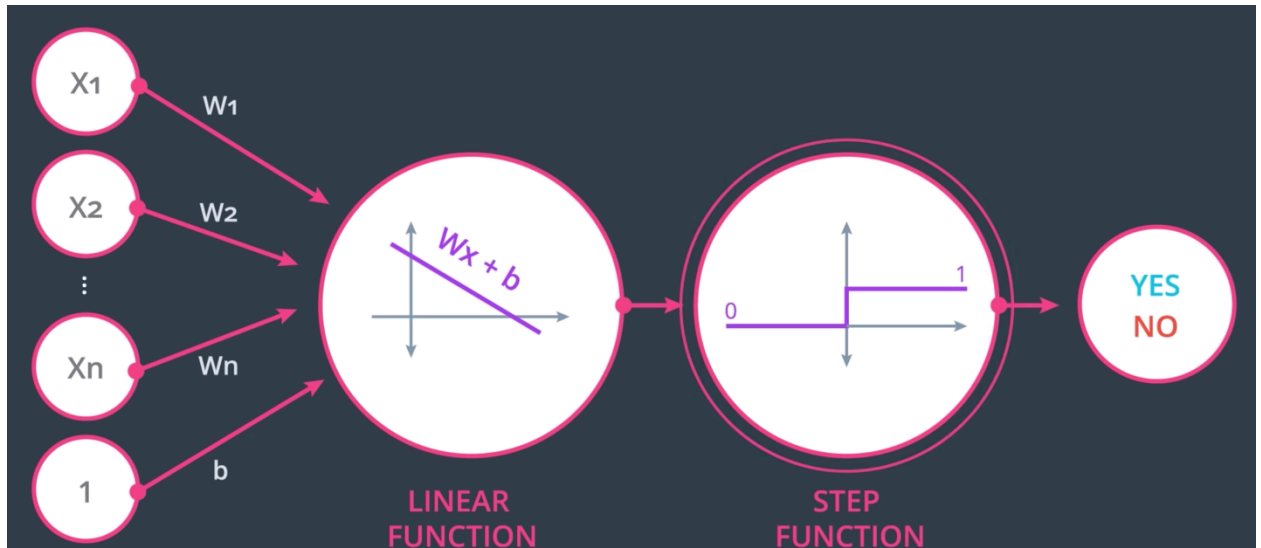
- Focus on what if we have more features / inputs

$$w_1x_1 + w_2x_2 + \dots + w_nx_n + b = 0$$

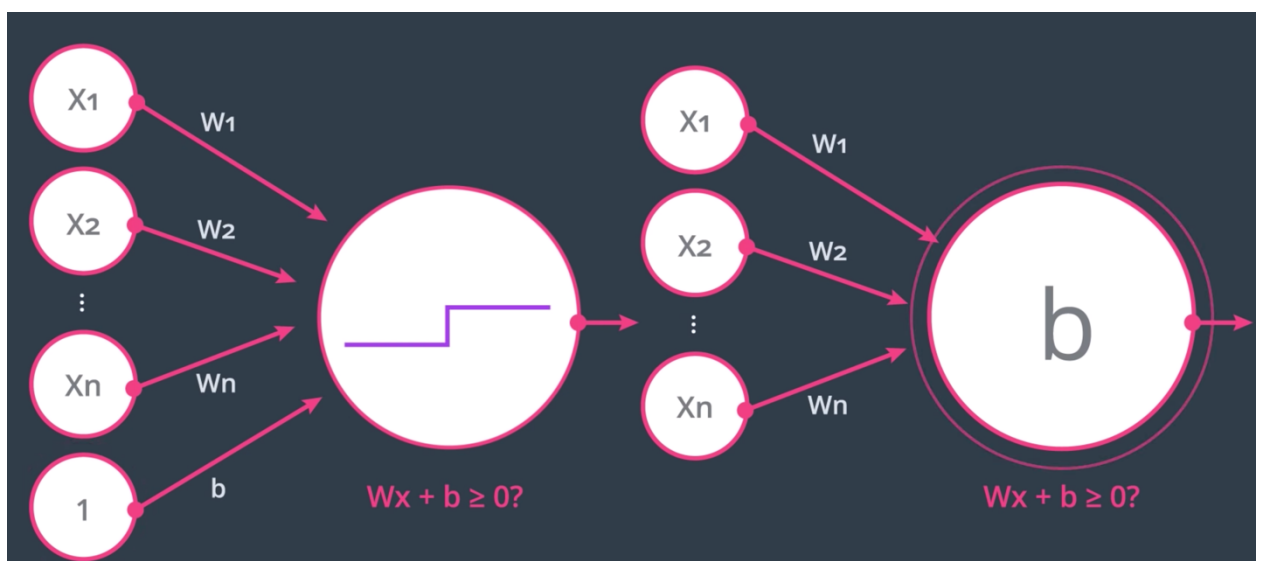
- Conclude: still same vector notation and prediction as in linear boundary

Perceptron

- Has features similar to human brain
- Building block of neural network ---> encoding the linear boundary equation into small graph
- Step function (can be discrete or continuous or some other functions) that's why it should live in a separate node



- Two ways represent precentron



Perceptron as Logical Operator

- Show application of perceptron as Logical operator
- <https://medium.com/@stanleydukor/neural-representation-of-and-or-not-xor-and-xnor-logic-gates-perceptron-algorithm-b0275375fea1>

Perceptron trick

- How we split the data?
 - Misclassified points want the line close to them
 - So move the line to the misclassified points
- Point $A(x, y)$, Line: $w_1x_1 + w_2x_2 + b = 0$, Learning Rate = 0.1: this is used so that the line doesn't move drastically over already correct classified points, so move little by little
 - If A in positive area want Line to come closer, we do subtraction
 - $d = w_1 - (x * 0.1)$
 - $e = w_2 - (y * 0.1)$
 - $f = b - (1 * 0.1)$ (1 is added for bias unit)
 - New Line: $dx_1 + ex_2 + f = 0$
 - If A in negative area want Line to come closer, we do addition
 - $d = w_1 + (x * 0.1)$
 - $e = w_2 + (y * 0.1)$
 - $f = b + (1 * 0.1)$ (1 is added for bias unit)
 - New Line: $dx_1 + ex_2 + f = 0$

Perceptron algorithm

- Algorithm

For a point with coordinates (p, q) , label y , learning rate α and prediction given by the equation $\hat{y} = \text{step}(w_1x_1 + w_2x_2 + b)$:

- If the point is correctly classified, do nothing.
- If the point is classified positive, but it has a negative label:
 - $\alpha p - w_1$
 - $\alpha q - w_2$
 - $(\alpha * 1) - b$
- If the point is classified negative, but it has a positive label:
 - $\alpha p + w_1$
 - $\alpha q + w_2$
 - $(\alpha * 1) + b$

Note:

- Step is the step function in this case the discrete step function that return either 1 or 0
- we do this until we have minimum classified points or until a given threshold given

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Mini summary:

- We know what is the problem that we try to solve: classification (Linear data)
- We know what the perceptron is = single layer neural network
- Why we use perceptron?
- Solution (The algorithm that create linear boundary between points)
- We can split two points with Perceptron algorithm

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