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## Foundations of Data Science

### Exercise sheet 7

#### Exercise 4

a)

For  $m_1$  the result of the power iteration after 5 steps is:

$$y = \begin{pmatrix} 1 \\ 0.3357 \end{pmatrix}, \lambda = -2.0278$$

For  $m_2$  the result of the power iteration after 5 steps is:

$$y = \begin{pmatrix} 0.5017 \\ 0.4949 \\ 1 \end{pmatrix}, \lambda = 2.9886$$

b)

$$y_1 = \begin{pmatrix} 1 \\ 1 \\ -1 \end{pmatrix} \quad y_2 = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} \quad y_3 = \begin{pmatrix} 1 \\ 1 \\ -1 \end{pmatrix} \quad y_4 = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}$$

The algorithm fails to converge.

c)

In each update step we now calculate  $y = A^{-1}x$ . This give us the eigenvalue  $\lambda = -1$  and the eigenvector  $y = \begin{pmatrix} 1 \\ 0.25 \end{pmatrix}$

d)

For  $M_4$  the algorithm needs 4 iterations. For  $M_5$  68 iterations are needed.