

# Foundations of Data Science

## Exercise sheet 2

### Exercise 1

$$w_1 = \begin{pmatrix} -0.4216370213557839 \\ -0.21081851067789195 \\ -0.10540925533894598 \\ -0.10540925533894598 \end{pmatrix} w_2 = \begin{pmatrix} 0.4216370213557839 \\ -0.4216370213557839 \\ -0.4216370213557839 \\ 0 \end{pmatrix} w = \begin{pmatrix} 0.31622776601683794 \\ -0.31622776601683794 \\ -0.5270462766947299 \\ -0.10540925533894598 \end{pmatrix}$$

### Exercise 2

The order of the set of examples matters, as the number of steps can change. With the given set  $S$  the algorithm needs to update  $w$  3 times. With  $S'$  as

$$S' = [[-1, 2, -4], 1], [[8, -2, -3], 1], [[2, -2, 5], -1], [[-6, 2, 7], -1], [[1, -1, 1], -1], [[4, 2, 1], -1]]$$

only 1 update step is needed.

### Exercise 4

a)

$$\begin{aligned} C_{11} &= \{A\}, P_{11} = (2, 12) \\ C_{12} &= \{B\}, P_{12} = (3, 11) \\ C_{13} &= \{C, D, E, F, G, H\}, P_{13} = (7.5, 6) \end{aligned}$$

$$\begin{aligned} C_{21} &= \{A\}, P_{21} = (2, 12) \\ C_{22} &= \{B, C\}, P_{22} = (3, 9.5) \\ C_{23} &= \{D, E, F, G, H\}, P_{23} = (8.4, 5.6) \end{aligned}$$

$$\begin{aligned} C_{31} &= \{A, B\}, P_{31} = (2.5, 11.5) \\ C_{32} &= \{C\}, P_{32} = (3, 8) \\ C_{33} &= \{D, E, F, G, H\}, P_{33} = (8.4, 5.6) \end{aligned}$$

c)

$$\begin{aligned} C_1 &= \{\}, P_1 = (100, 100) \\ C_2 &= \{\}, P_2 = (200, 200) \\ C_3 &= \{A, B, C, D, E, F, G, H\}, P_3 = (6.25, 7.375) \end{aligned}$$