NCERT Assignment

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In a family having three children, there may be no girl, one girl, two girls, or three girls. So the probability of each is 1/4. Is this correct? Justify your answer.

NO, it is not correct.

Let,

$$X = \{0, 1\} \tag{1}$$

$$p_X(k), k = \{0, 1, 2, 3\}$$
 (2)

$$p_X(0) = C(3,0) \left(\frac{1}{2}\right)^0 \left(\frac{1}{2}\right)^3$$
 (3)

$$p_X(1) = C(3,1) \left(\frac{1}{2}\right)^1 \left(\frac{1}{2}\right)^2$$
 (4)

$$p_X(2) = C(3,2) \left(\frac{1}{2}\right)^2 \left(\frac{1}{2}\right)^1$$
 (5)

$$p_X(3) = C(3,3) \left(\frac{1}{2}\right)^3 \left(\frac{1}{2}\right)^0$$
 (6)

$$\implies p_X(0) = \frac{1}{8} \tag{7}$$

$$\implies p_X(1) = \frac{3}{8} \tag{8}$$

$$\Rightarrow p_X(0) = \frac{1}{8}$$

$$\Rightarrow p_X(1) = \frac{3}{8}$$

$$\Rightarrow p_X(2) = \frac{3}{8}$$
(8)
$$\Rightarrow (9)$$

$$\implies p_X(3) = \frac{1}{8} \tag{10}$$

Parameter	Value	Description
X=0	$\frac{1}{8}$	no girl
X=1	<u>3</u>	1 girl
X=2	3/8	2 girls
X=3	1/8	3 girls

TABLE 0: Random Variables