

## Lab 10

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### Matrix, Figures and Experiments

1) Starting from file Lab\_09.RScript, try to run yourself what you saw in “Matrix\_03” the primer session

*Identity matrix*

```
I1 <- diag(1)
I1
##      [,1]
## [1,]    1

I2 <- diag(2)
I2
##      [,1] [,2]
## [1,]    1    0
## [2,]    0    1

A <- matrix(1:4, nrow=2, ncol = 2)
A
##      [,1] [,2]
## [1,]    1    3
## [2,]    2    4

AI <- A%*%I2
AI
##      [,1] [,2]
## [1,]    1    3
## [2,]    2    4
```

*Symmetric matrix*

```
S <- cbind(c(1,2,3),c(2,1,4), c(3,4,3))
S
##      [,1] [,2] [,3]
## [1,]    1    2    3
```

```
## [2,]    2    1    4
## [3,]    3    4    3

trS <- t(S)
trS

##      [,1] [,2] [,3]
## [1,]    1    2    3
## [2,]    2    1    4
## [3,]    3    4    3
```

### *Basic properties*

```
X<- cbind(c(1,2), c(3,4), c(5,6))
Y <- cbind(c(7,8), c(9,10), c(11,12))
X+Y

##      [,1] [,2] [,3]
## [1,]    8   12   16
## [2,]   10   14   18

Z <- cbind(c(1,2), c(3,4))
W <- cbind(c(5,6), c(8,8))
ZW1 <- Z%*%W
ZW2 <- W%*%Z
ZW1

##      [,1] [,2]
## [1,]   23   32
## [2,]   34   48

ZW2

##      [,1] [,2]
## [1,]   21   47
## [2,]   22   50

trZW1 <- t(ZW1)
trZ <- t(Z)
trW <- t(W)
trWtrZ <- trW%*%trZ
trZW1

##      [,1] [,2]
## [1,]   23   34
## [2,]   32   48

trWtrZ

##      [,1] [,2]
## [1,]   23   34
## [2,]   32   48
```

```

trtrZ <- t(trZ)
trtrZ

##      [,1] [,2]
## [1,]    1    3
## [2,]    2    4

Z

##      [,1] [,2]
## [1,]    1    3
## [2,]    2    4

```

*Inverse matrix*

```

C <- matrix(c(1,0,3,1), nrow=2, ncol = 2)
C

##      [,1] [,2]
## [1,]    1    3
## [2,]    0    1

invC <- solve(C)
invC

##      [,1] [,2]
## [1,]    1   -3
## [2,]    0    1

CinvC <- C%*%invC
CinvC

##      [,1] [,2]
## [1,]    1    0
## [2,]    0    1

```

## 2) Using the file Lab02\_mkm\_Econometrics1\_RodBased\_DataHandling:

### a.Read dt.wages and apply 'data.table'

```

setwd("/Users/nikitagrabher-meyer/Desktop/PHD/Econometrics/Labs/Lab 10,
Homework")

library(data.table)
library(ggplot2)
library(stargazer)

##
## Please cite as:

## Hlavac, Marek (2018). stargazer: Well-Formatted Regression and Summary
## Statistics Tables.

## R package version 5.2.2. https://CRAN.R-project.org/package=stargazer

```

```
library(GGally)

## Registered S3 method overwritten by 'GGally':
##   method from
##   +.gg      ggplot2

library(Metrics)

load("dt_wages.RData")

dt.wages <- data.table(dt.wages)
```

### b. Get basic summary statistics. How many observations, how many variables?

```
str(dt.wages)

## Classes 'data.table' and 'data.frame':  526 obs. of  24 variables:
## $ wage      : num  3.1 3.24 3 6 5.3 ...
## $ educ      : int  11 12 11 8 12 16 18 12 12 17 ...
## $ exper     : int  2 22 2 44 7 9 15 5 26 22 ...
## $ tenure    : int  0 2 0 28 2 8 7 3 4 21 ...
## $ nonwhite   : int  0 0 0 0 0 0 0 0 0 0 ...
## $ female    : int  1 1 0 0 0 0 0 1 1 0 ...
## $ married   : int  0 1 0 1 1 1 0 0 0 1 ...
## $ numdep    : int  2 3 2 0 1 0 0 0 2 0 ...
## $ smsa      : int  1 1 0 1 0 1 1 1 1 1 ...
## $ northcen  : int  0 0 0 0 0 0 0 0 0 0 ...
## $ south     : int  0 0 0 0 0 0 0 0 0 0 ...
## $ west      : int  1 1 1 1 1 1 1 1 1 1 ...
## $ construc  : int  0 0 0 0 0 0 0 0 0 0 ...
## $ ndurman   : int  0 0 0 0 0 0 0 0 0 0 ...
## $ trcompu   : int  0 0 0 0 0 0 0 0 0 0 ...
## $ trade     : int  0 0 1 0 0 0 1 0 1 0 ...
## $ services  : int  0 1 0 0 0 0 0 0 0 0 ...
## $ profserv  : int  0 0 0 0 0 1 0 0 0 0 ...
## $ profocc   : int  0 0 0 0 0 1 1 1 1 1 ...
## $ clerocc   : int  0 0 0 1 0 0 0 0 0 0 ...
## $ servocc   : int  0 1 0 0 0 0 0 0 0 0 ...
## $ lwage     : num  1.13 1.18 1.1 1.79 1.67 ...
## $ expersq   : int  4 484 4 1936 49 81 225 25 676 484 ...
## $ tenursq   : int  0 4 0 784 4 64 49 9 16 441 ...
## - attr(*, ".internal.selfref")=<externalptr>

head(dt.wages, 3)
```

|       | wage | educ | exper | tenure | nonwhite | female | married | numdep | smsa | northcen | south |
|-------|------|------|-------|--------|----------|--------|---------|--------|------|----------|-------|
| ## 1: | 3.10 | 11   | 2     | 0      | 0        | 1      | 0       | 2      | 1    | 0        | 0     |
| ## 2: | 3.24 | 12   | 22    | 2      | 0        | 1      | 1       | 3      | 1    | 0        | 0     |
| ## 3: | 3.00 | 11   | 2     | 0      | 0        | 0      | 0       | 2      | 0    | 0        | 0     |

```

0
##      west construc ndurman trcommpu trade services profserv profocc clerocc
## 1:      1          0          0          0  0          0          0          0
## 2:      1          0          0          0  0          1          0          0
## 3:      1          0          0          0  1          0          0          0
##      servocc      lwage expersq tenursq
## 1:          0 1.131402          4          0
## 2:          1 1.175573        484          4
## 3:          0 1.098612          4          0

```

```
tail(dt.wages, 3)
```

```

##      wage educ exper tenure nonwhite female married numdep smsa northcen
south
## 1:  4.67   15   13   18          0          0          1          3          0
0
## 2: 11.56   16    5    1          0          0          1          0          0
0
## 3:  3.50   14    5    4          1          1          0          2          0
0
##      west construc ndurman trcommpu trade services profserv profocc clerocc
## 1:      1          1          0          0  0          0          0          1          0
## 2:      1          0          1          0  0          0          0          0          0
## 3:      1          0          0          0  0          0          1          0          1
##      servocc      lwage expersq tenursq
## 1:          0 1.541159        169        324
## 2:          0 2.447551         25          1
## 3:          0 1.252763         25          16

```

```
summary(dt.wages)
```

```

##      wage          educ          exper          tenure
## Min.   : 0.530    Min.   : 0.00    Min.   : 1.00    Min.   : 0.000
## 1st Qu.: 3.330    1st Qu.:12.00    1st Qu.: 5.00    1st Qu.: 0.000
## Median : 4.650    Median :12.00    Median :13.50    Median : 2.000
## Mean   : 5.896    Mean   :12.56    Mean   :17.02    Mean   : 5.105
## 3rd Qu.: 6.880    3rd Qu.:14.00    3rd Qu.:26.00    3rd Qu.: 7.000
## Max.   :24.980    Max.   :18.00    Max.   :51.00    Max.   :44.000
##      nonwhite      female      married      numdep
## Min.   :0.0000    Min.   :0.0000    Min.   :0.0000    Min.   :0.000
## 1st Qu.:0.0000    1st Qu.:0.0000    1st Qu.:0.0000    1st Qu.:0.000
## Median :0.0000    Median :0.0000    Median :1.0000    Median :1.000
## Mean   :0.1027    Mean   :0.4791    Mean   :0.6084    Mean   :1.044
## 3rd Qu.:0.0000    3rd Qu.:1.0000    3rd Qu.:1.0000    3rd Qu.:2.000
## Max.   :1.0000    Max.   :1.0000    Max.   :1.0000    Max.   :6.000
##      smsa      northcen      south      west
## Min.   :0.0000    Min.   :0.000    Min.   :0.0000    Min.   :0.0000
## 1st Qu.:0.0000    1st Qu.:0.000    1st Qu.:0.0000    1st Qu.:0.0000
## Median :1.0000    Median :0.000    Median :0.0000    Median :0.0000
## Mean   :0.7224    Mean   :0.251    Mean   :0.3555    Mean   :0.1692
## 3rd Qu.:1.0000    3rd Qu.:0.750    3rd Qu.:1.0000    3rd Qu.:0.0000

```

```
## Max. :1.0000 Max. :1.000 Max. :1.0000 Max. :1.0000
## construc ndurman trcommpu trade
## Min. :0.00000 Min. :0.0000 Min. :0.00000 Min. :0.0000
## 1st Qu.:0.00000 1st Qu.:0.0000 1st Qu.:0.00000 1st Qu.:0.0000
## Median :0.00000 Median :0.0000 Median :0.00000 Median :0.0000
## Mean :0.04563 Mean :0.1141 Mean :0.04373 Mean :0.2871
## 3rd Qu.:0.00000 3rd Qu.:0.0000 3rd Qu.:0.00000 3rd Qu.:1.0000
## Max. :1.00000 Max. :1.0000 Max. :1.00000 Max. :1.0000
## services profserv profocc clerocc
## Min. :0.0000 Min. :0.0000 Min. :0.0000 Min. :0.0000
## 1st Qu.:0.0000 1st Qu.:0.0000 1st Qu.:0.0000 1st Qu.:0.0000
## Median :0.0000 Median :0.0000 Median :0.0000 Median :0.0000
## Mean :0.1008 Mean :0.2586 Mean :0.3669 Mean :0.1673
## 3rd Qu.:0.0000 3rd Qu.:1.0000 3rd Qu.:1.0000 3rd Qu.:0.0000
## Max. :1.0000 Max. :1.0000 Max. :1.0000 Max. :1.0000
## servocc lwage expersq tenursq
## Min. :0.0000 Min. : -0.6349 Min. : 1.0 Min. : 0.00
## 1st Qu.:0.0000 1st Qu.: 1.2030 1st Qu.: 25.0 1st Qu.: 0.00
## Median :0.0000 Median : 1.5369 Median : 182.5 Median : 4.00
## Mean :0.1407 Mean : 1.6233 Mean : 473.4 Mean : 78.15
## 3rd Qu.:0.0000 3rd Qu.: 1.9286 3rd Qu.: 676.0 3rd Qu.: 49.00
## Max. :1.0000 Max. : 3.2181 Max. :2601.0 Max. :1936.00
```

```
stargazer (dt.wages, type="text")
```

```
##
## =====
## Statistic N Mean St. Dev. Min Pctl(25) Pctl(75) Max
## -----
## wage 526 5.896 3.693 0.530 3.330 6.880 24.980
## educ 526 12.563 2.769 0 12 14 18
## exper 526 17.017 13.572 1 5 26 51
## tenure 526 5.105 7.224 0 0 7 44
## nonwhite 526 0.103 0.304 0 0 0 1
## female 526 0.479 0.500 0 0 1 1
## married 526 0.608 0.489 0 0 1 1
## numdep 526 1.044 1.262 0 0 2 6
## smsa 526 0.722 0.448 0 0 1 1
## northcen 526 0.251 0.434 0 0 0.8 1
## south 526 0.356 0.479 0 0 1 1
## west 526 0.169 0.375 0 0 0 1
## construc 526 0.046 0.209 0 0 0 1
## ndurman 526 0.114 0.318 0 0 0 1
## trcommpu 526 0.044 0.205 0 0 0 1
## trade 526 0.287 0.453 0 0 1 1
## services 526 0.101 0.301 0 0 0 1
## profserv 526 0.259 0.438 0 0 1 1
## profocc 526 0.367 0.482 0 0 1 1
## clerocc 526 0.167 0.374 0 0 0 1
## servocc 526 0.141 0.348 0 0 0 1
```

```

## lwage      526  1.623   0.532  -0.635  1.203   1.929   3.218
## expersq    526 473.435 616.045    1      25    676   2,601
## tenursq    526 78.150  199.435    0      0     49   1,936
## -----

stargazer (dt.wages, type="text", iqr=TRUE)

##
## =====
## Statistic  N    Mean    St. Dev.  Min    Pctl(25) Pctl(75)  Max
## -----
## wage      526  5.896    3.693    0.530    3.330    6.880    24.980
## educ      526 12.563    2.769     0        12        14        18
## exper     526 17.017   13.572    1         5        26        51
## tenure    526  5.105    7.224     0         0         7        44
## nonwhite   526  0.103    0.304     0         0         0         1
## female    526  0.479    0.500     0         0         1         1
## married   526  0.608    0.489     0         0         1         1
## numdep    526  1.044    1.262     0         0         2         6
## smsa      526  0.722    0.448     0         0         1         1
## northcen  526  0.251    0.434     0         0         0.8        1
## south     526  0.356    0.479     0         0         1         1
## west      526  0.169    0.375     0         0         0         1
## construc  526  0.046    0.209     0         0         0         1
## ndurman   526  0.114    0.318     0         0         0         1
## trcompu   526  0.044    0.205     0         0         0         1
## trade     526  0.287    0.453     0         0         1         1
## services  526  0.101    0.301     0         0         0         1
## profserv  526  0.259    0.438     0         0         1         1
## profocc   526  0.367    0.482     0         0         1         1
## clerocc   526  0.167    0.374     0         0         0         1
## servocc   526  0.141    0.348     0         0         0         1
## lwage     526  1.623    0.532   -0.635   1.203   1.929   3.218
## expersq   526 473.435 616.045    1        25    676   2,601
## tenursq   526 78.150  199.435    0         0     49   1,936
## -----

ncol(dt.wages)

## [1] 24

table(dt.wages[, list(female, nonwhite)])

##      nonwhite
## female  0    1
##      0 245  29
##      1 227  25

table(dt.wages[, list (female, nonwhite, south)])

## , , south = 0
##

```

```
##          nonwhite
## female    0    1
##          0 158  13
##          1 154  14
##
## , , south = 1
##
##          nonwhite
## female    0    1
##          0  87  16
##          1  73  11

table(dt.wages[, list (female , tenure)])

##          tenure
## female  0  1  2  3  4  5  6  7  8  9 10 11 12 13 14 15 16 17 18 19 20 21
22 23
##          0 75 19 32 22  8 19  7 11 11  5  7  5  4  8  1  2  2  1  3  2  2  4
2  3
##          1 88 32 31 20 19 11  8  4  4  4  6  4  4  0  1  4  2  2  0  0  3  1
0  0
##          tenure
## female 24 25 26 28 30 31 33 34 39 44
##          0  4  3  2  2  3  2  1  0  1  1
##          1  1  1  1  0  0  0  0  1  0  0

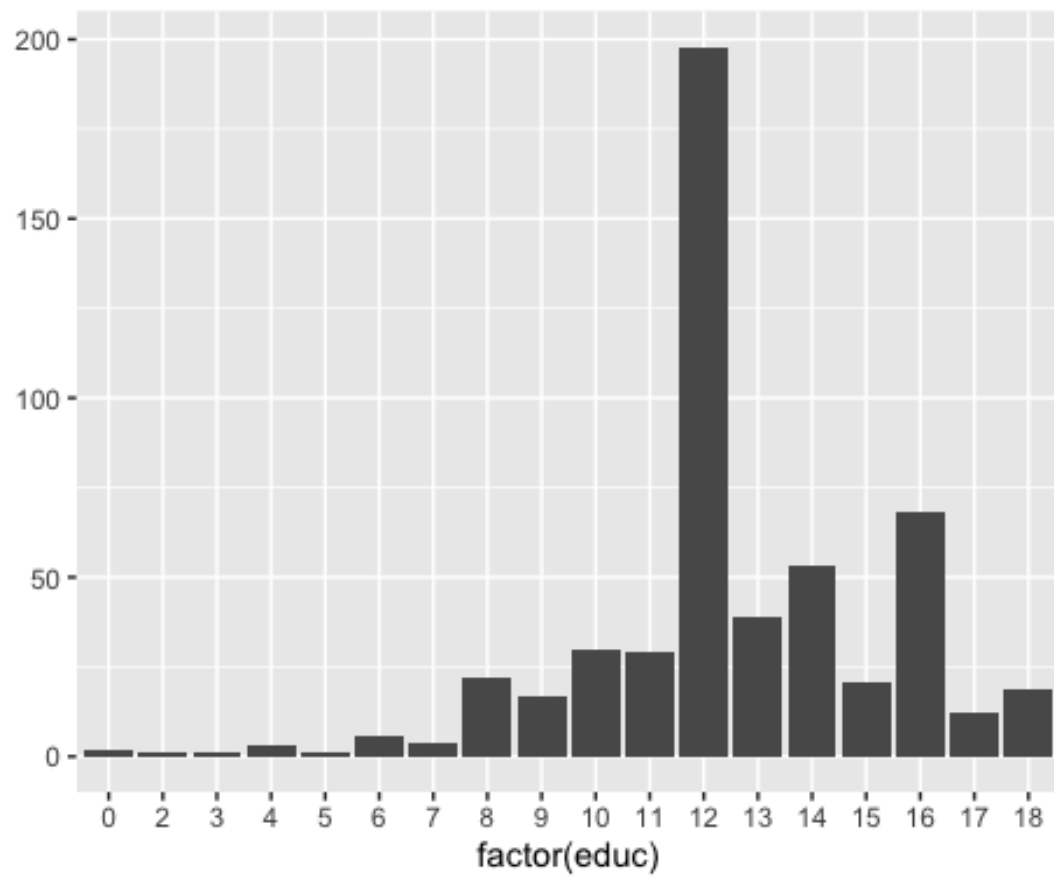
table(dt.wages[, list (nonwhite , tenure)])

##          tenure
## nonwhite  0  1  2  3  4  5  6  7  8  9 10 11 12 13 14 15
16
##          0 151  48  54  35  24  26  13  13  14  6  12  9  8  7  2  5
4
##          1  12  3  9  7  3  4  2  2  1  3  1  0  0  1  0  1
0
##          tenure
## nonwhite 17 18 19 20 21 22 23 24 25 26 28 30 31 33 34 39
44
##          0  3  2  2  5  4  2  2  4  4  3  2  2  2  1  1  1
1
##          1  0  1  0  0  1  0  1  1  0  0  0  1  0  0  0  0
0
```

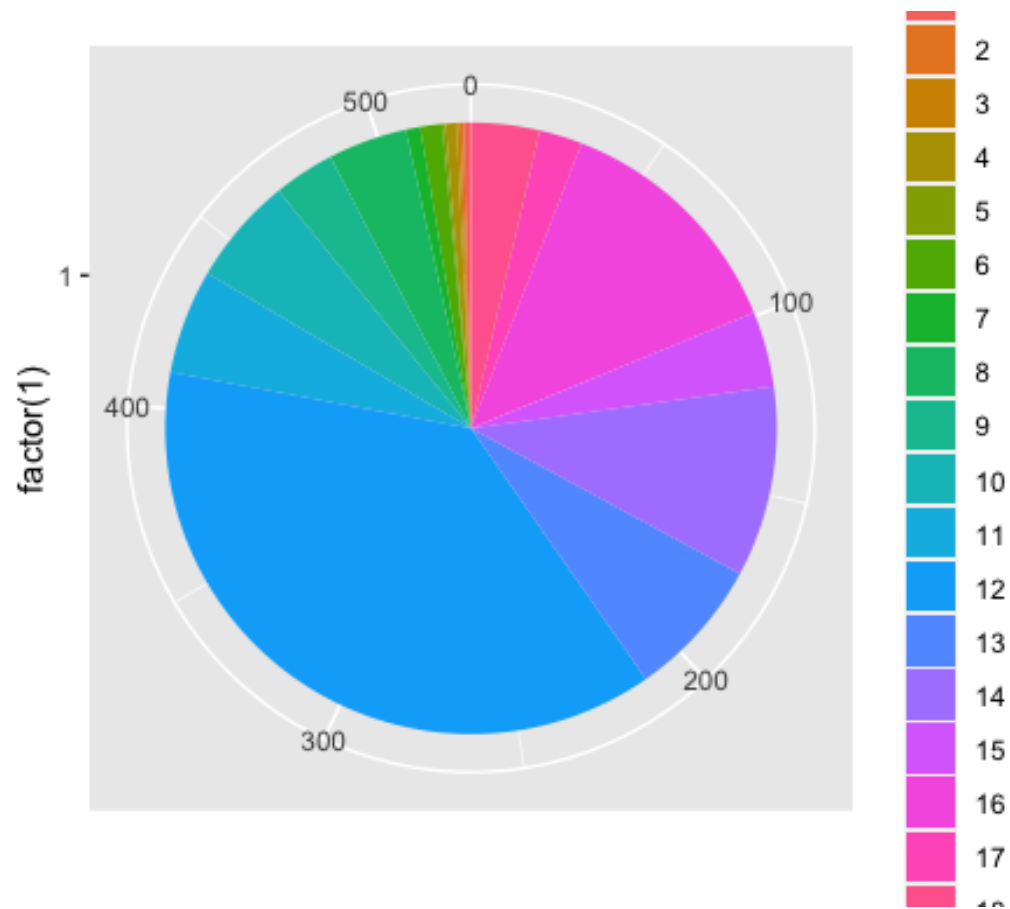
### c.Reproduce the data-handling steps shown in the slides (and dt.wages)

```
qplot(factor(educ),data=dt.wages,geom="bar")
```

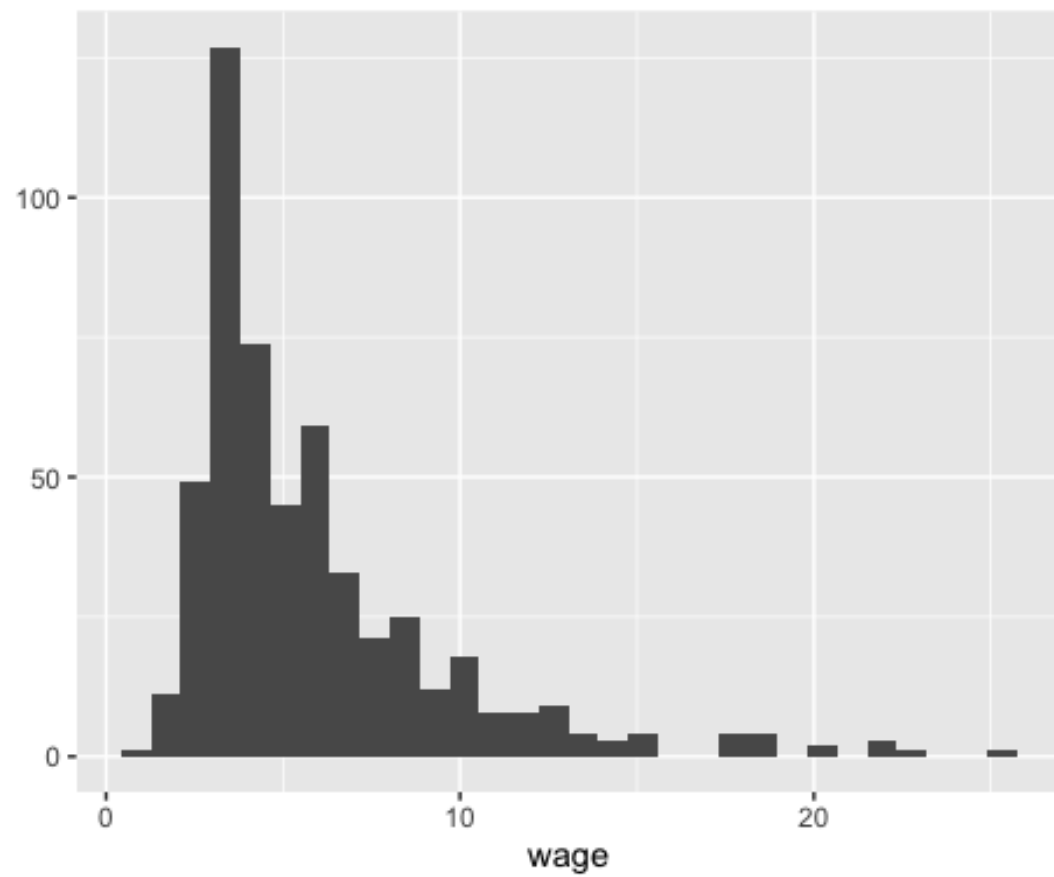




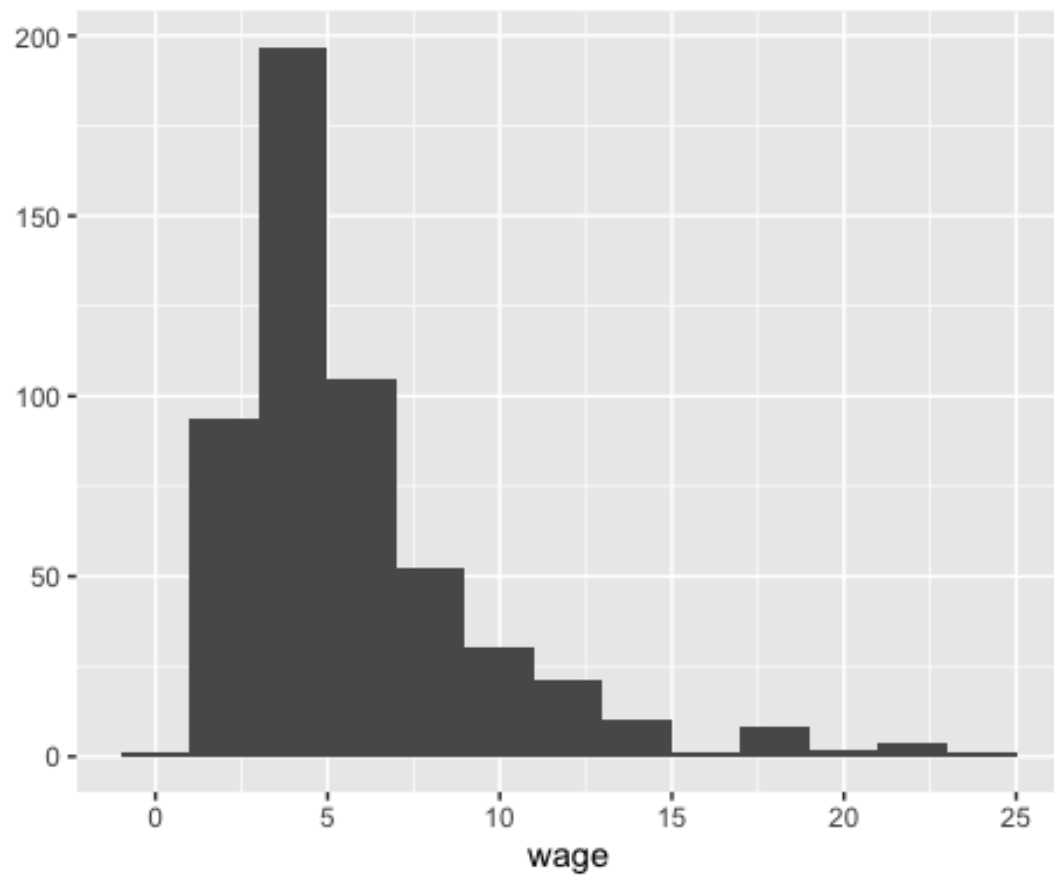
```
qplot(x=factor(1), fill=factor(educ), data=dt.wages, geom="bar") +  
coord_polar(theta="y")
```



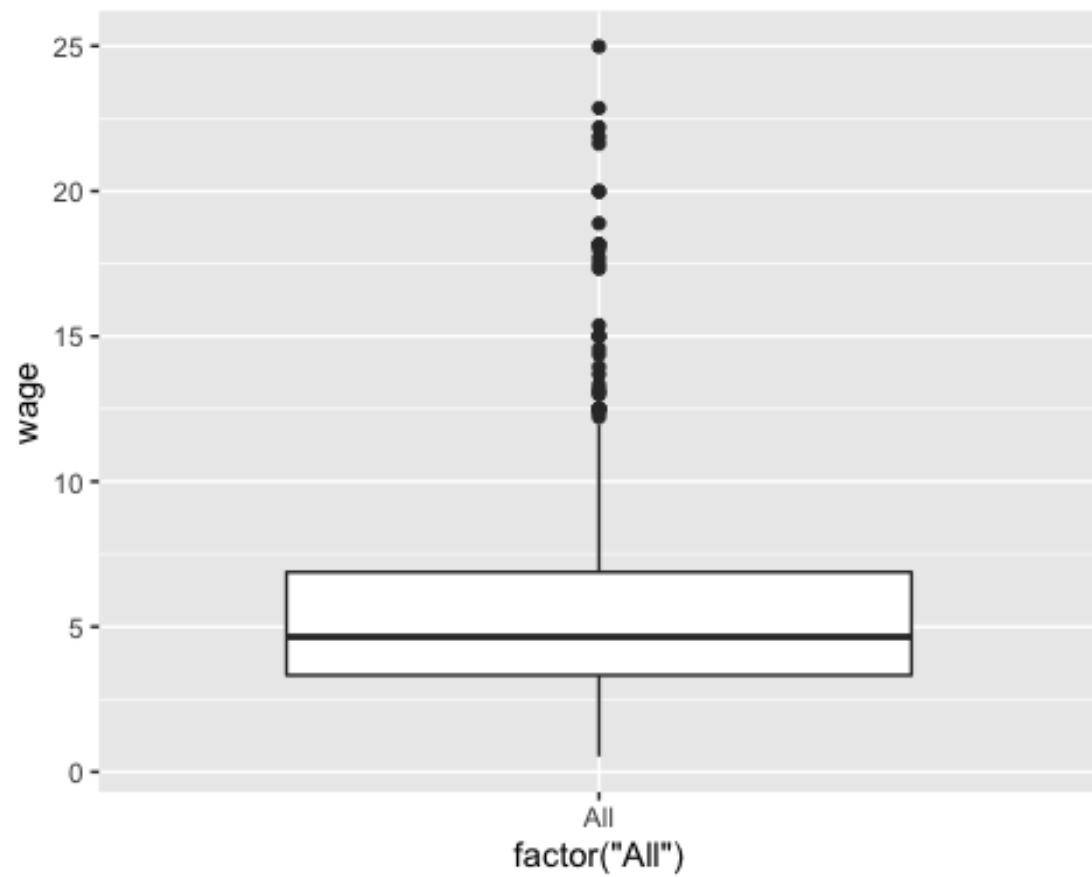
```
qplot(wage, data=dt.wages, geom="histogram")
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



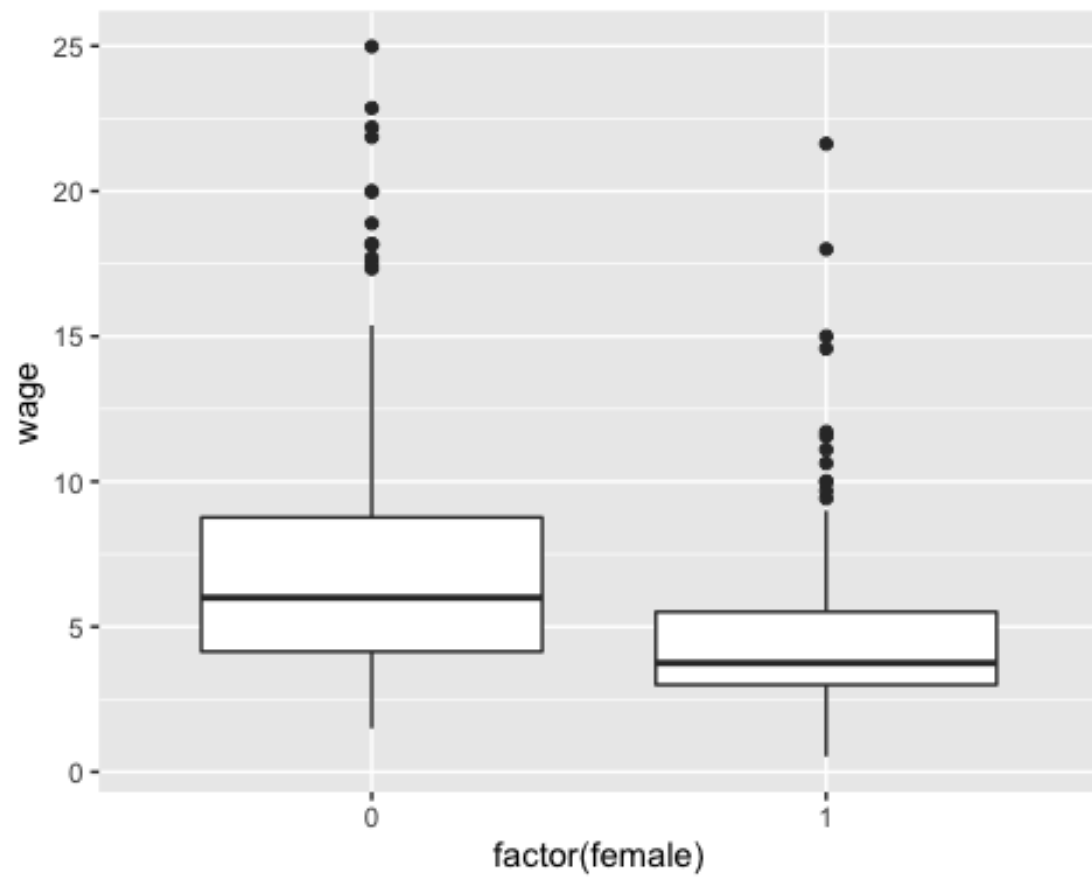
```
qplot(wage, data=dt.wages, geom="histogram", binwidth=2)
```



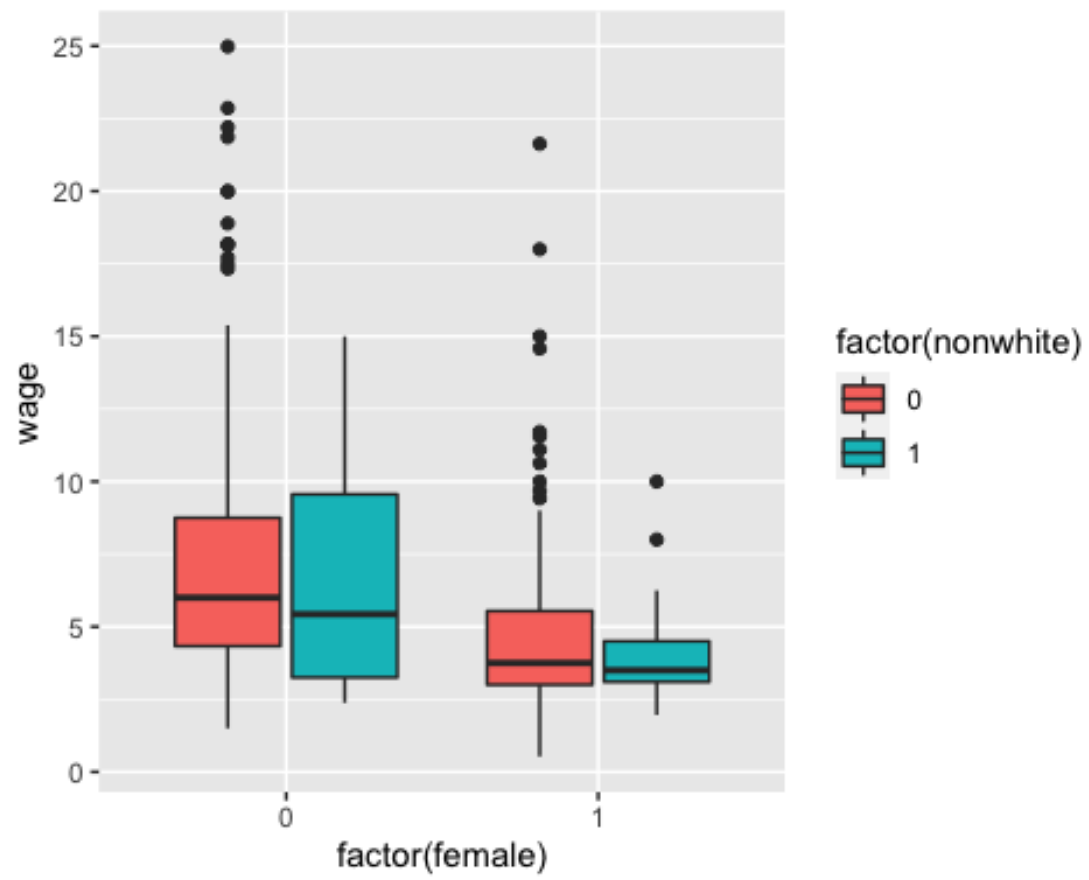
```
qplot(x=factor("All"),y=wage,data=dt.wages,geom="boxplot")
```



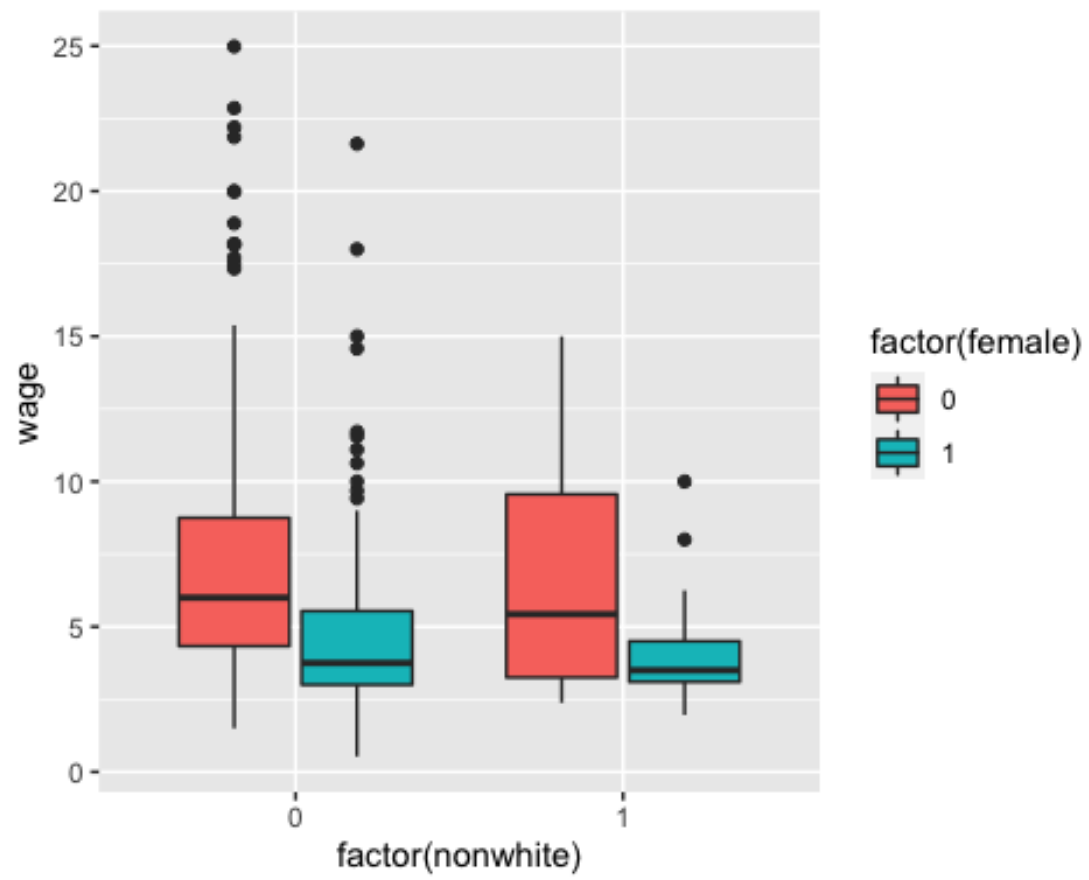
```
qplot(factor(female), wage, data=dt.wages, geom="boxplot")
```



```
qplot(factor(female),wage,fill=factor(nonwhite),data=dt.wages,geom="boxplot")
```

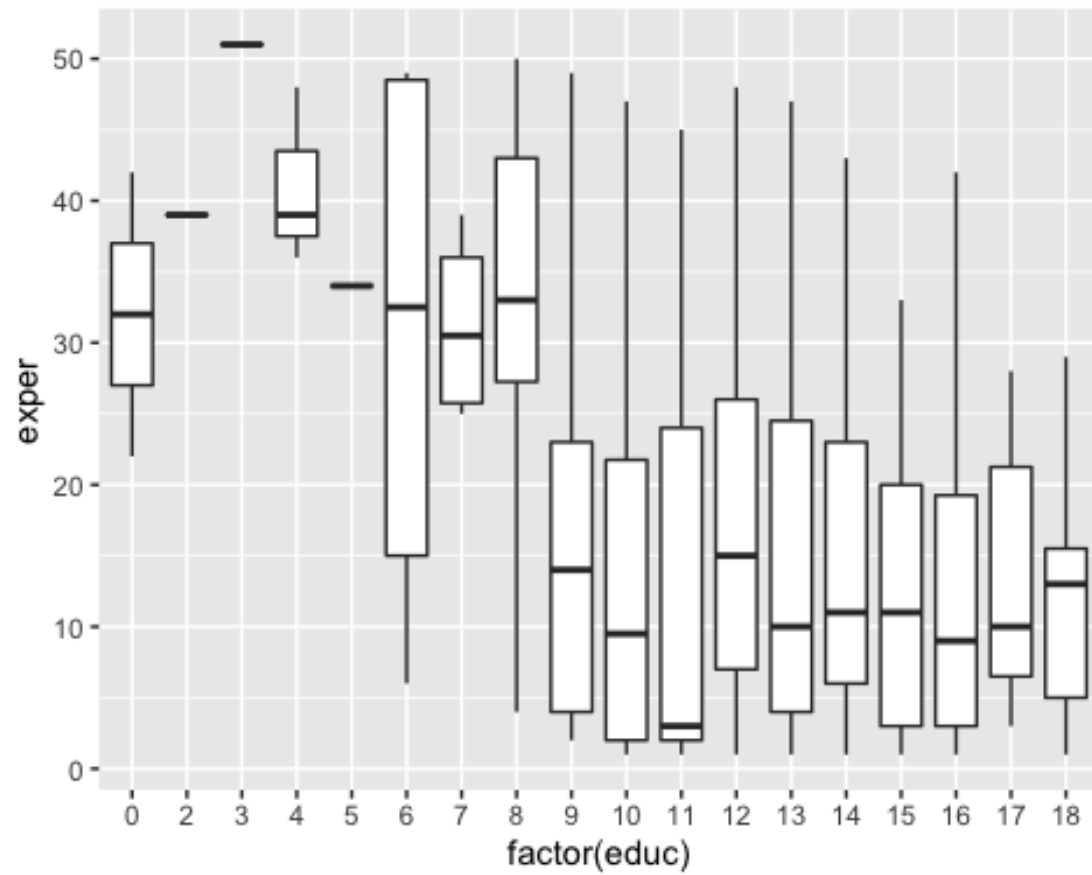


```
qplot(factor(nonwhite), wage, fill=factor(female), data=dt.wages, geom="boxplot")
```

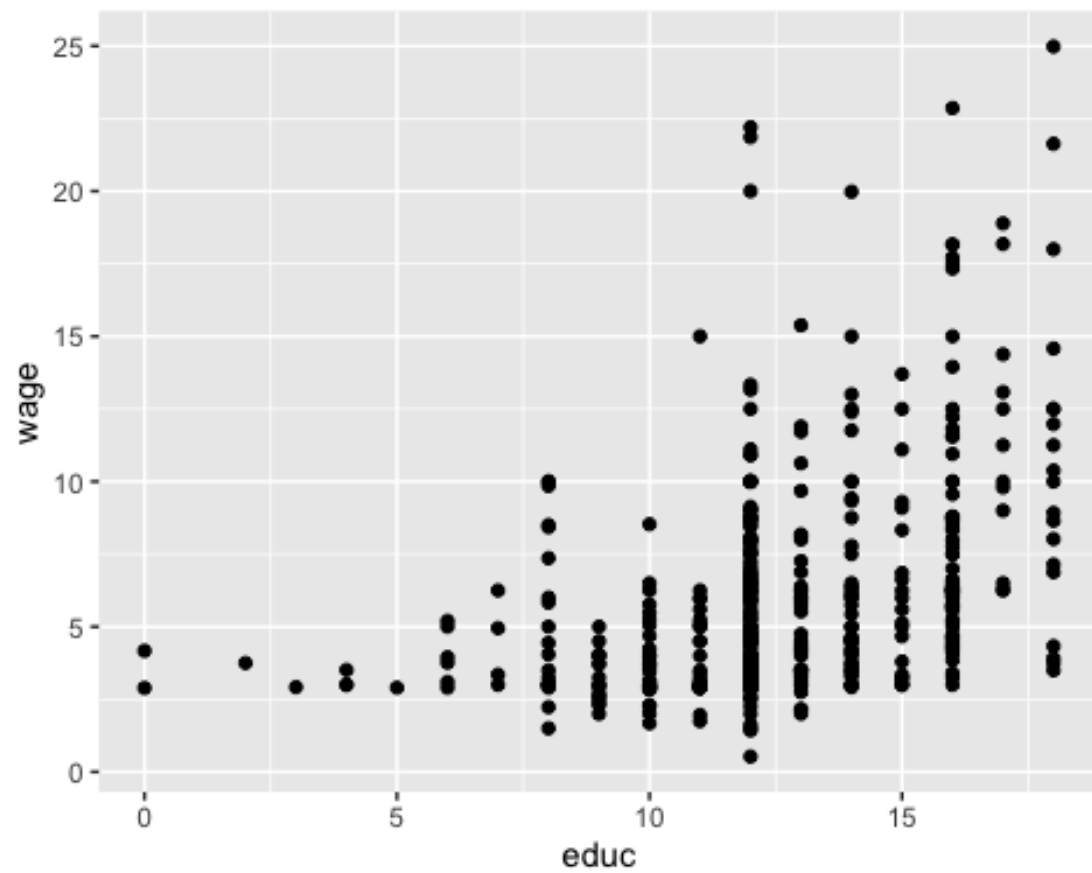


```
ggplot(dt.wages)+geom_boxplot(aes(factor(educ),exper))
```

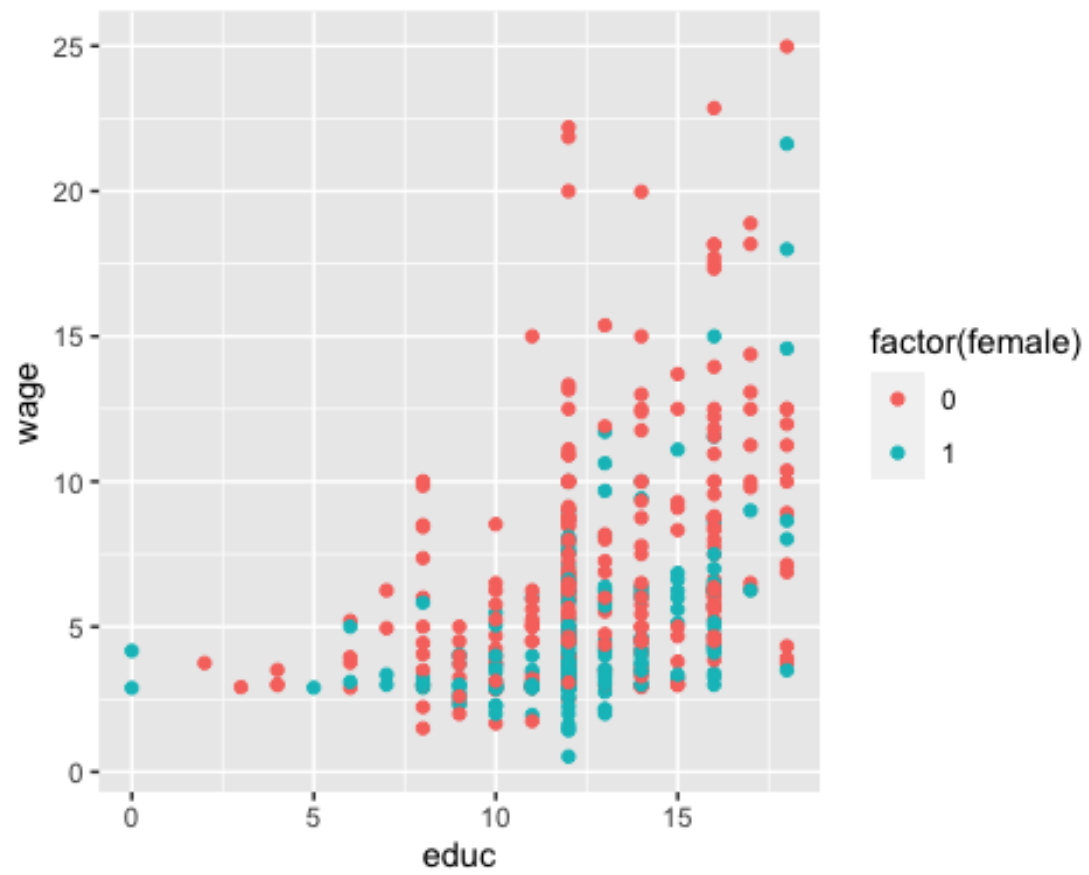




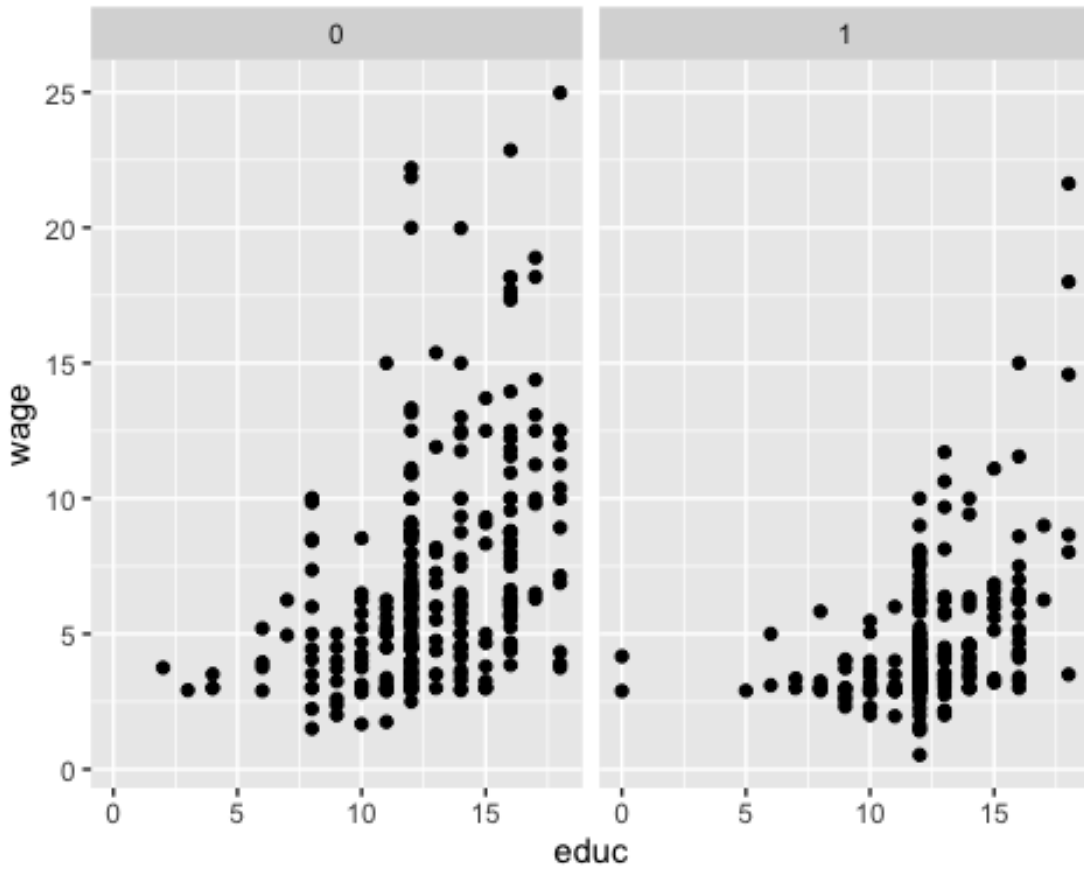
```
qplot(educ, wage, data=dt.wages, geom="point")
```



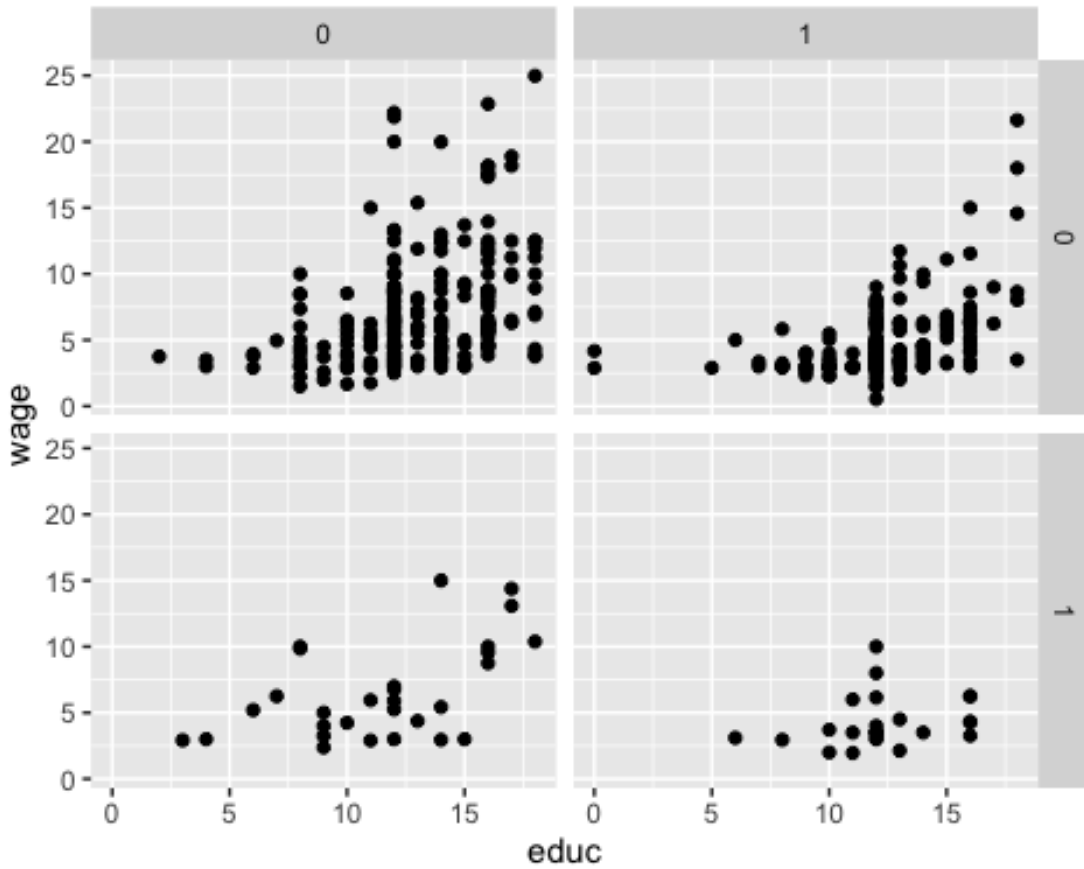
```
qplot(educ,wage,color=factor(female),data=dt.wages,geom="point")
```



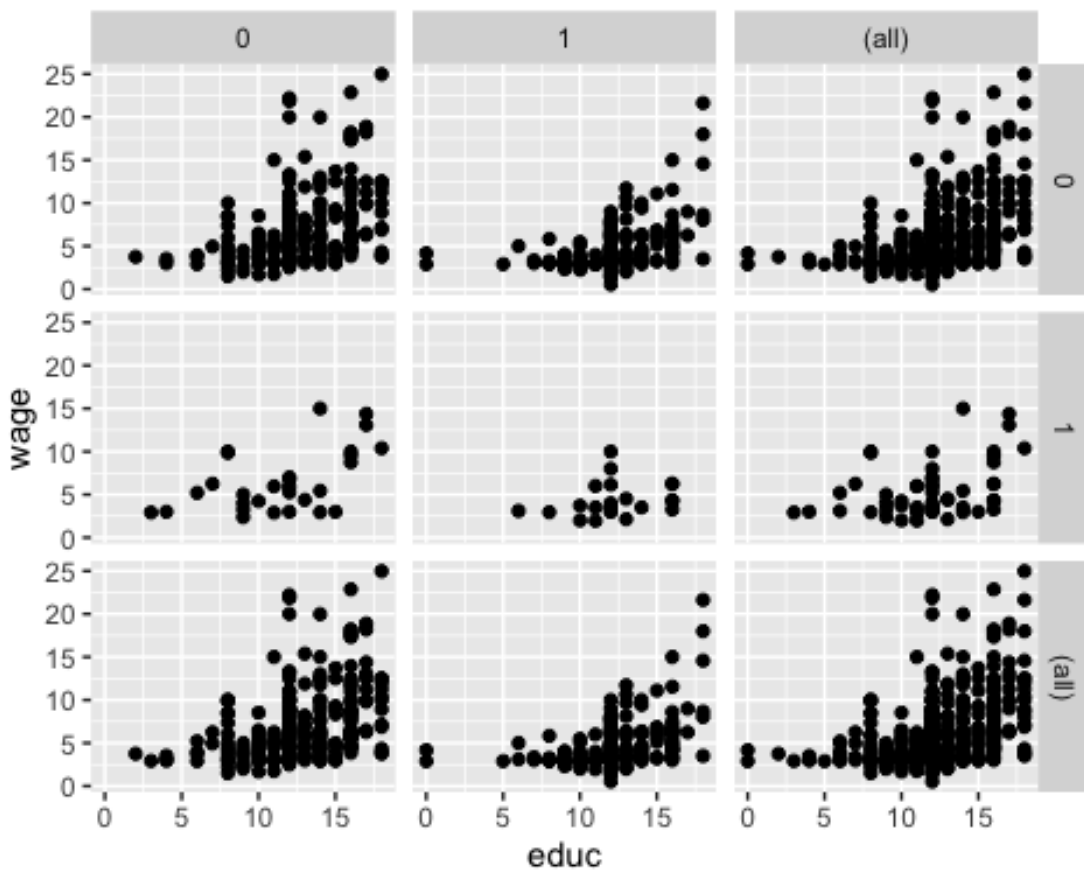
```
ggplot(dt.wages)+geom_point(aes(educ,wage))+facet_grid(~female)
```



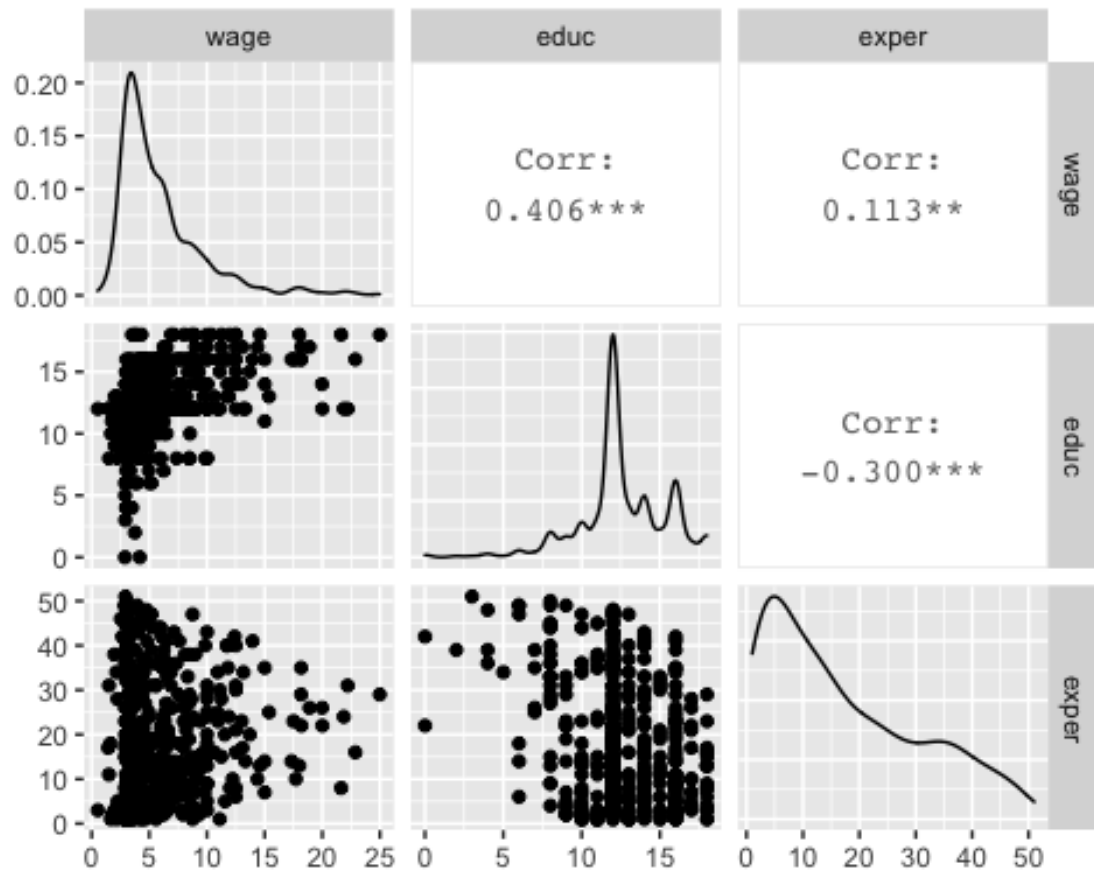
```
ggplot(dt.wages)+geom_point(aes(educ,wage))+facet_grid(nonwhite~female)
```



```
ggplot(dt.wages)+geom_point(aes(educ,wage))+facet_grid(nonwhite~female,  
margins=TRUE)
```



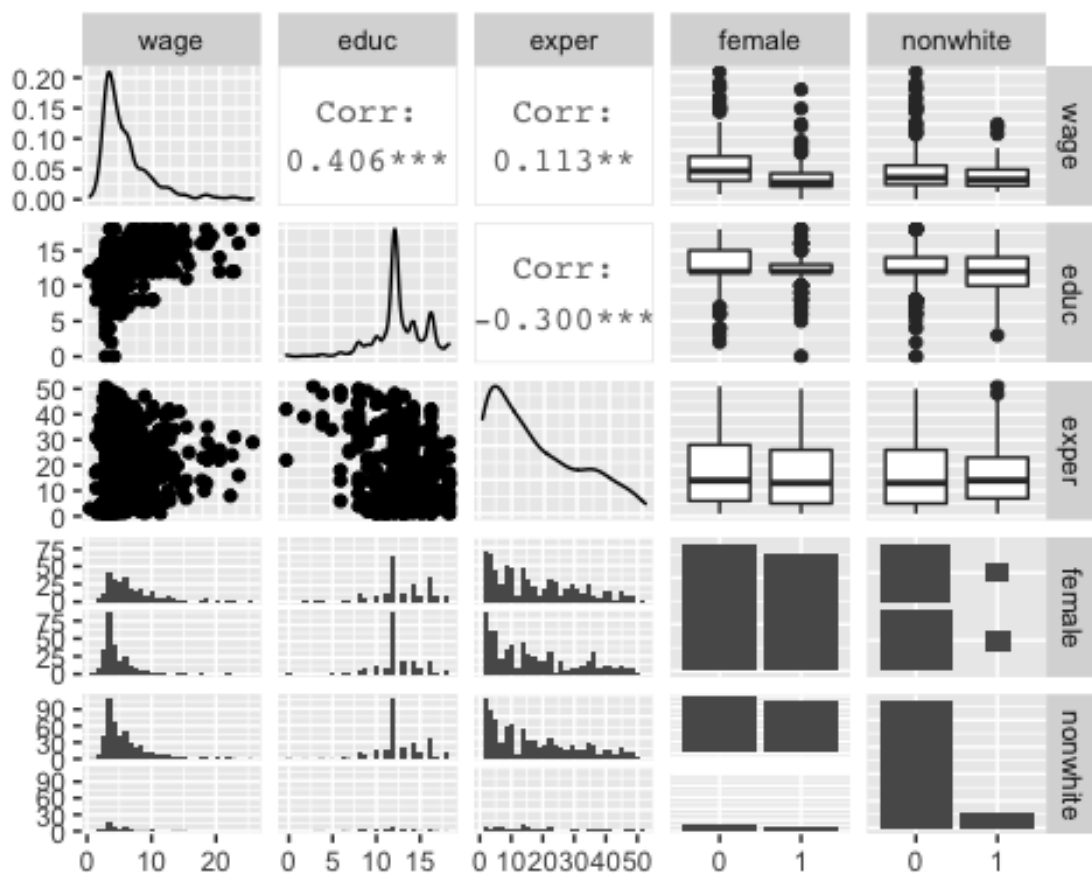
```
ggpairs(dt.wages[,list(wage,educ,exper)])
```



```
ggpairs(dt.wages[,list(female=factor(female),nonwhite=factor(nonwhite))])
```







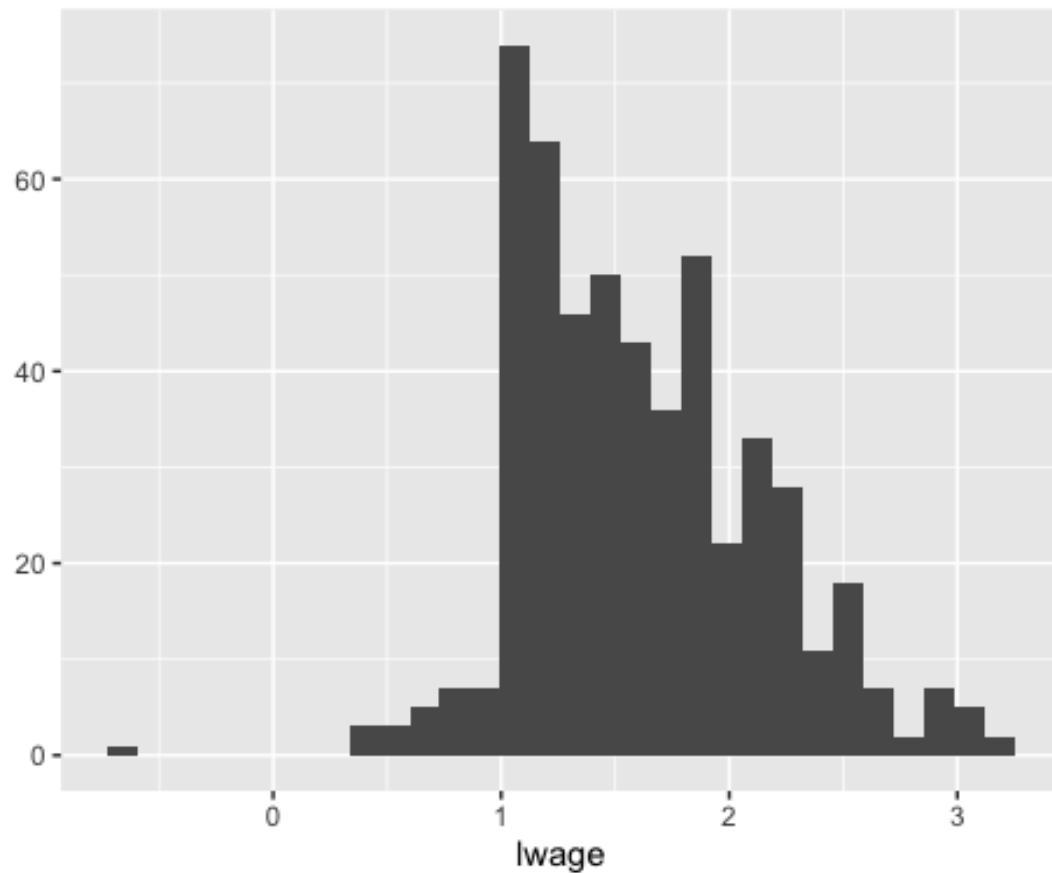
```
dt.wages[wage>20,][order(-wage)]
```

```
##      wage educ exper tenure nonwhite female married numdep smsa northcen
south
## 1: 24.98  18   29   25        0      0      1      0      1      0
0
## 2: 22.86  16   16    7        0      0      1      2      1      0
0
## 3: 22.20  12   31   15        0      0      1      1      1      0
0
## 4: 21.86  12   24   16        0      0      1      3      1      1
0
## 5: 21.63  18    8    8        0      1      0      0      1      0
0
##      west construc ndurman trcommpu trade services profserv profocc clerocc
## 1:    0         0        0         0    0         0         0      1      0
## 2:    0         0        0         0    0         0         0      1      0
## 3:    1         0        0         0    0         0         0      1      0
## 4:    0         0        0         0    1         0         0      1      0
## 5:    0         0        0         0    0         0         1      1      0
##      servocc      lwage expersq tenursq
## 1:         0 3.218076    841    625
## 2:         0 3.129389    256     49
```

```
## 3:      0 3.100092      961      225
## 4:      0 3.084659      576      256
## 5:      0 3.074081       64       64
```

```
qplot(lwage, data=dt.wages, geom="histogram")
```

```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



```
dt.wages[lwage < 0,]
```

```
##      wage educ exper tenure nonwhite female married numdep smsa northcen
## 1: 0.53   12    3     1       0       1       0       0       1       0
##
##      west construc ndurman trcommpu trade services profserv profocc clerocc
## 1:    1         0      0         0     0         1       0       0       0
##
##      servocc      lwage expersq tenursq
## 1:         1 -0.6348783      9       1
```

3) Let's do a thought experiment: Using the slide-deck UEA\_ecoR2PhD CoreLect\_06 ATENT\_Match\_Stk and dt.wages, let's pretend, for a moment "south," is a randomly assigned treatment in an experiment:

a. Compute a difference-in-means estimator when treatment is "south," and the outcome is wage

```
dt.wages[south==1, mean(wage)] - dt.wages[south==0, mean(wage)]  
## [1] -0.7900927
```

b. Now focus on race and gender as control variables (in "x") and run a regression estimation of treatment effects

```
reg1 <- lm(wage ~ south + nonwhite + female, data=dt.wages)  
stargazer(reg1, type = "text")
```

```
##  
## =====  
##                               Dependent variable:  
##                               -----  
##                               wage  
## -----  
## south                        -0.884***  
##                               (0.317)  
##  
## nonwhite                     -0.372  
##                               (0.499)  
##  
## female                      -2.552***  
##                               (0.302)  
##  
## Constant                     7.471***  
##                               (0.243)  
## -----  
## Observations                  526  
## R2                           0.130  
## Adjusted R2                   0.125  
## Residual Std. Error          3.454 (df = 522)  
## F Statistic                   26.104*** (df = 3; 522)  
## =====  
## Note:                        *p<0.1; **p<0.05; ***p<0.01
```

c. Now try to estimate the regression and account for potentially heterogeneous treatment effects.

```
reg2 <- lm(wage ~ south + nonwhite + female + nonwhite*south + female*south,  
data=dt.wages)  
stargazer(reg2, type = "text")
```

```
##
## =====
##                      Dependent variable:
##                      -----
##                      wage
## -----
## south                -1.288***
##                      (0.447)
##
## nonwhite              0.155
##                      (0.691)
##
## female                -2.953***
##                      (0.374)
##
## south:nonwhite        -1.047
##                      (0.996)
##
## south:female          1.117*
##                      (0.630)
##
## Constant              7.628***
##                      (0.269)
##
## -----
## Observations           526
## R2                     0.138
## Adjusted R2            0.129
## Residual Std. Error    3.446 (df = 520)
## F Statistic            16.591*** (df = 5; 520)
## =====
## Note:                  *p<0.1; **p<0.05; ***p<0.01
```

#### d. Try to implement a 2-step fitted regression.

```
south.yes <- subset(dt.wages, south==1)
south.no  <- subset(dt.wages, south==0)

reg3.1 <- lm(wage ~ nonwhite + female, data=south.yes)
reg3.2 <- lm(wage ~ nonwhite + female, data=south.no)

stargazer(reg3.1, reg3.2, type = "text")
```

```
##
## =====
##                      Dependent variable:
##                      -----
##                      wage
##                      (1)                (2)
## -----
## nonwhite                -0.892                0.155
```

```
##                (0.617)                (0.739)
##
## female          -1.836***             -2.953***
##                (0.436)             (0.400)
##
## Constant        6.341***             7.628***
##                (0.307)             (0.287)
##
## -----
## Observations      187                339
## R2                0.096                0.139
## Adjusted R2       0.086                0.134
## Residual Std. Error 2.963 (df = 184)    3.684 (df = 336)
## F Statistic      9.724*** (df = 2; 184) 27.234*** (df = 2; 336)
## =====
## Note:                                *p<0.1; **p<0.05; ***p<0.01

dt.wages$y_hat1 <- predict(reg3.1, newdata=dt.wages)
dt.wages$y_hat0 <- predict(reg3.2, newdata=dt.wages)
```