



A satellite map of the island of Crete, Greece, showing its elongated shape and surrounding waters. The land is a mix of green and brown, indicating vegetation and terrain. The water is a deep blue. The text is overlaid on the top right of the map.

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CRETE: **Certified Refinement Types**

Curiculus Vitae

| | | | | |
|-----------|------------------------|--|-------|---|
| 2005-2010 | Diploma | Advisor: Nikos Papaspyrou | NTUA |  |
| 2011-2017 | PhD | Advisor: Ranjit Jhala Title: “Refinement Types for Haskell” | UCSD |  |
| 2017-2018 | Post-doc | Host: David Van Horn Victor Basili Postdoc Fellow | UMD |  |
| 2018-now | Research Ass. Prof. | Juan de la Cierva Fellow Atraccion de Talendo Fellow | IMDEA |  |

Active Member of ACM SIGPLAN **Published in POPL (3), PLDI (1), OOPSLA(2), and ICFP(2).**
Co-organized PLMW and 6 more venues.

Refinement Types

A type-based, SMT-automated verification technique,
designed to be **practical**, *but without* **strong foundations**.

Refinement Types

Library:

```
get :: [a] → Int → a  
zeros :: Int -> [Int]
```

User:

```
bad  i = get (zeros (i-1)) i ✓  
good i = get (zeros (i+1)) i ✓
```

Existing Programming Language:
In-bound indexing cannot be expressed by types.

Refinement Types

Existing Type: $\text{get} :: [a] \rightarrow \text{Int} \rightarrow a$

Refinement Type: $\text{get} :: xs:[a] \rightarrow i:\{\text{Int} \mid 0 \leq i < \text{len } xs\} \rightarrow a$

Logical predicate
here encodes safe indexing





Refinement Types are **Practical**

Library:

```
get :: xs:[a] → i:{Int | 0 ≤ i < len xs} → a  
zeros :: i:{Int | 0 ≤ i} → {o:[Int] | i = len o}
```

User:



```
bad  i = get (zeros (i-1)) i   
good i = get (zeros (i+1)) i 
```

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Specs are naturally encoded.

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User code is unmodified (thanks SMT!)

Refinement Types are **Practical**

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User:

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good i = get (zeros (i+1)) i 
```

Specs are naturally encoded.

User code is unmodified (thanks SMT!)

Successfully used in industry and academia!

Refinement Types are not Sound

Library:

```
get :: xs:[a] → i:{Int | 0 ≤ i < len xs} → a  
zeros :: i:{Int | 0 ≤ i} → {o:[Int] | i = len o}
```

User:

```
bad  i = get (zeros (i-1)) i ✗  
good i = get (zeros (i+1)) i ✓
```

```
>> good maxInt — maxInt = 263 - 1; maxInt+1 < 0  
*** Exception: Non-exhaustive patterns in function get
```

Runtime
Spec
Violation

* A *sound* system only accepts programs that never violate their specs

Refinement Types are not Sound

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get :: xs:[a] → i:{Int | 0 ≤ i < len xs} → a  
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Runtime
Spec
Violation

Axioms Can
Make System
Inconsistent

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Refinement Types are not Sound

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```
get :: xs:[a] → i:{Int | 0 ≤ i < len xs} → a  
zeros :: i:{Int | 0 ≤ i} → {o:[Int] | i = len o}
```

User:

```
bad  i = get (zeros (i-1)) i ✓ Unsoundly  
good i = get (zeros (i+1)) i ✓
```

Axioms:

E.g., “function extensionality”

Runtime
Spec
Violation

Axioms Can
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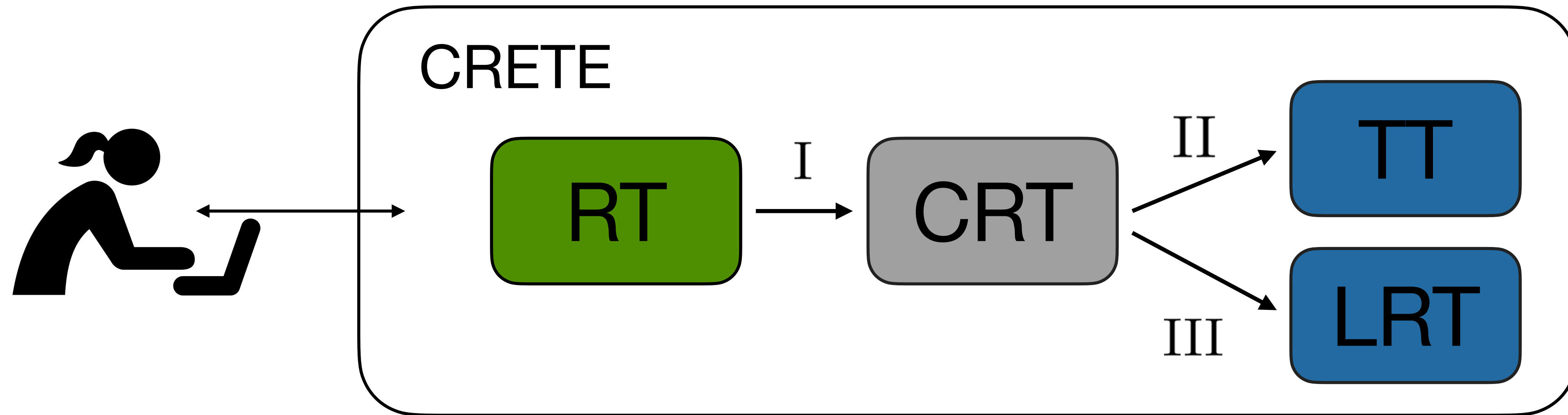
* A *sound* system only accepts programs that never violate their specs

Practical & Sound



CRETE:
A Practical *and* Sound Refinement Type System

Objectives of CRETE



User Interacts with **Refinement Types (RT)**

Objective I: **RT** → Certified Refinement Types (CRT)

Objective II: CRT → **Sound Type Theory (TT)**

Objective III: CRT → **Logic of Refinement Types (LRT)**

Objective I: $RT \rightarrow CRT$

Explicit certificates that capture SMT automation.

```
good i = get (zeros (i+1)) i
```



```
good i = get (zeros (i+1)) (cert i {v:N | v < i + 1} {i:N})
```



Explicit Certificate

Method: Type-based Syntactic Translation

Goal: Validate/test explicit certificates

Objective I: $RT \rightarrow CRT$

Explicit certificates that capture SMT automation.

```
good i = get (zeros (i+1)) i
```



```
good i = get (zeros (i+1)) (cert i {v:N | v < i + 1} {i:N})
```

Testing certificate $i < i + 1$: 

Error counter-example found for $i = \text{maxInt}$

Challenge: Custom test generators (for corner cases)

Objective II: $CRT \rightarrow TT$

The system is now as **sound** as TT (here **Coq**).

```
good i = get (zeros (i+1)) (cert i {v:N | v < i + 1} {i:N})
```



```
Definition good (i:N) : N :=  
  get (zeros (1+i)) (exist (fun v:N => v < 1 + i) i (lemma i)).
```



Proof of $i < i+1$

Method: Type-based Syntactic Translation

Objective II: $\text{CRT} \rightarrow \text{TT}$

The system is now as **sound** as TT (here **Coq**).

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good i = get (zeros (i+1)) (cert i {v:N | v < i + 1} {i:N})
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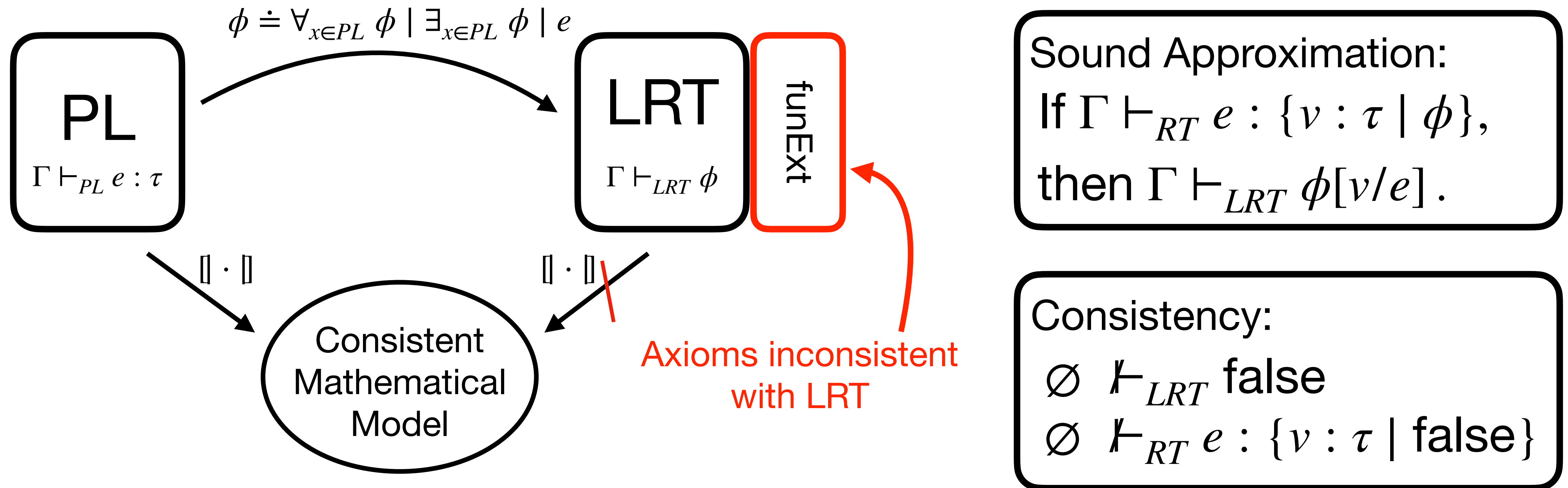
Proof of $i < i+1$

Risk: $\text{CRT} \rightarrow \text{TT}$ is not always possible

Theoretical Gain: Relationship between **RT** and **TT**

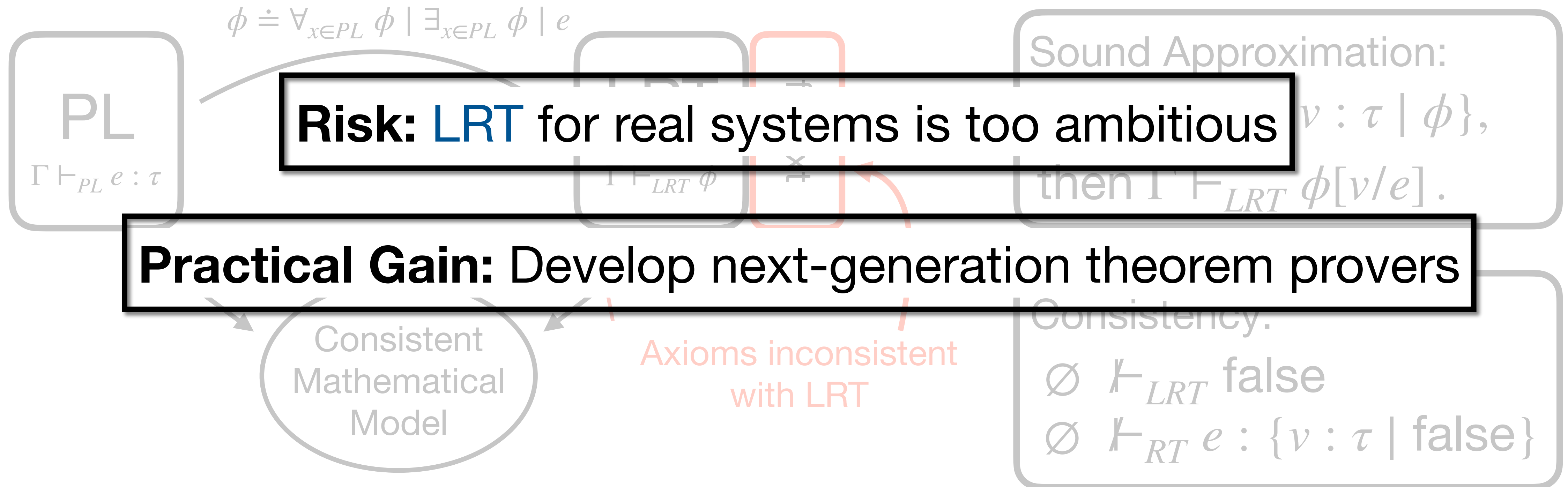
Objective III: Logic of Refinement Types (LRT)

Set **Sound** Foundations of **RT** using Program Semantics



Objective III: Logic of Refinement Types (LRT)

Set Sound Foundations of RT using Program Semantics



Objective IV: Implementation & Evaluation

| Implementation | Haskell | Rust |
|----------------|--------------------------|-------------------------|
| Current State: | Practical, but not sound | Under development |
| Target: | Secure Web Applications | Cryptographic Protocols |

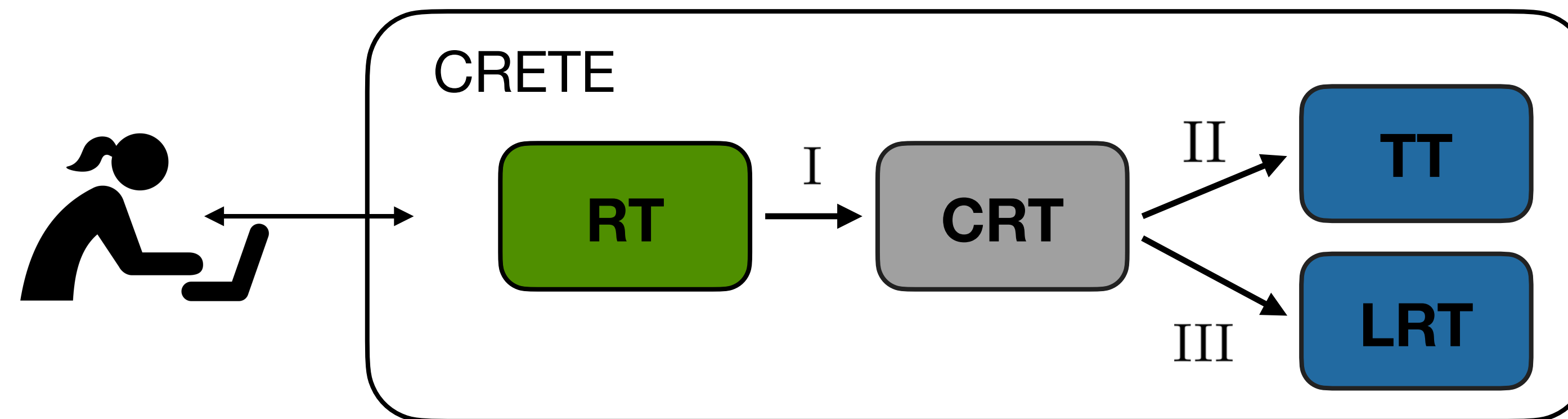
Evaluation:

Feasibility: Is CRETE both sound and practical in real programs?

Generality: Can we apply CRETE to more programming languages?

CRETE:

A **Practical** and **Sound** Refinement Type System used to verify real world application



Risk: **RT** → **TT** is not always possible

Gain: Set Foundations of Refinement Types

Risk: **LRT** for real systems is too ambitious

Gain: Novel **low-cost** **high-gain** verification

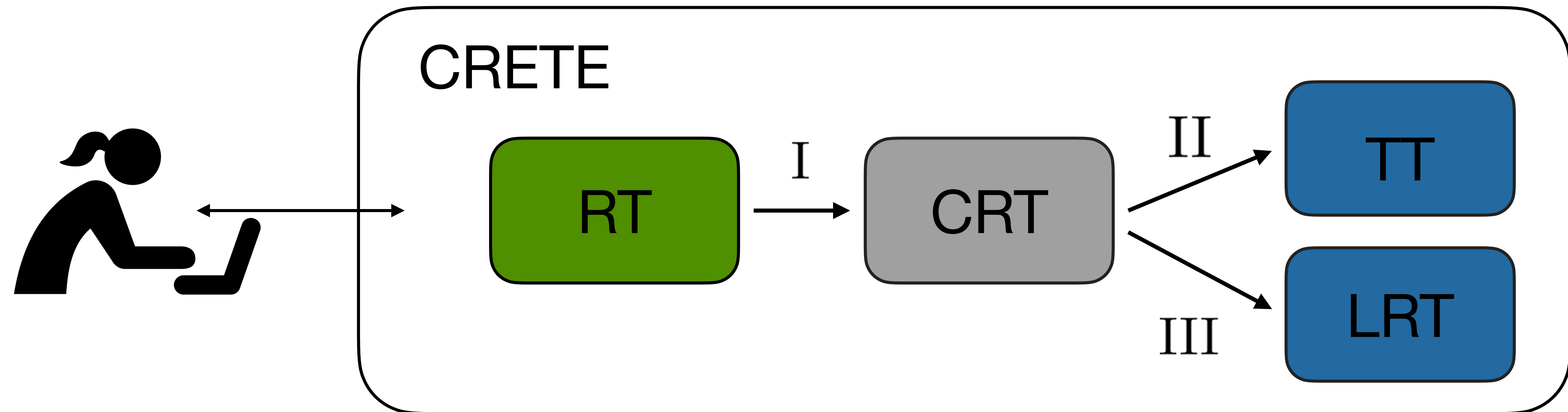
CRETE Group: Me (75%), 1 postdoc, 3 PhD, 1 engineer
+ Existing Collaborations (UCSD, UMD, ...)

Thanks!

END

CRETE:

A Practical and Sound Refinement Type System



Risk: $RT \rightarrow TT$ might not always be possible

Parallel Approach: Development of the Logic of Refinement Types (LRT).

Objective III: Logic of Refinement Types

Goal: Define a Consistent Logic for RT

Method: Classical Program Semantics

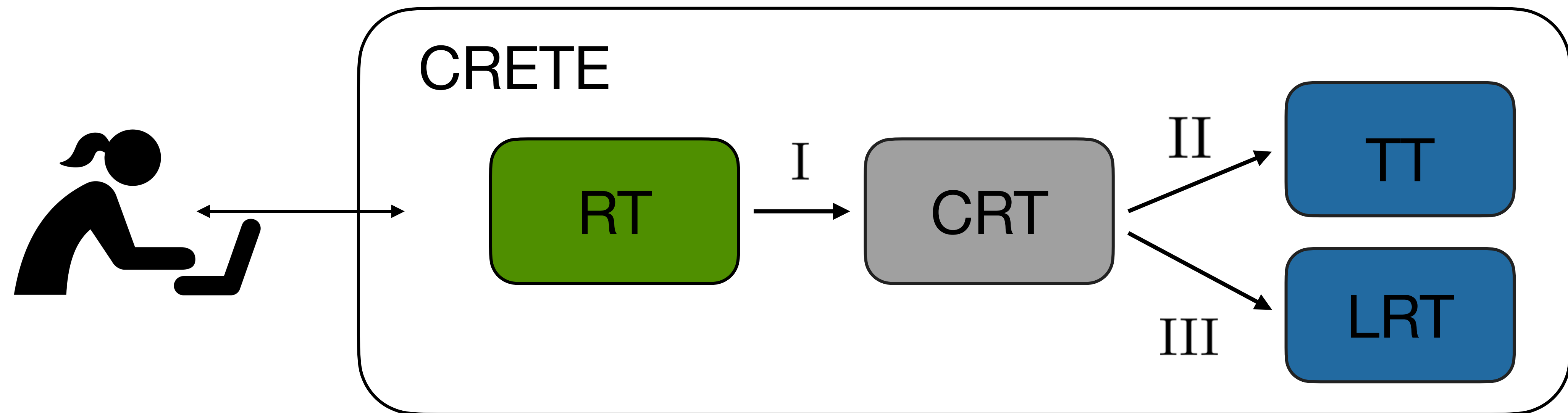
Risk: LRT for real systems is too ambitious

Theoretical Gain: Define Foundations of RT

Practical Gain: Develop next-generation theorem provers

CRETE:

A Practical and Sound Refinement Type System used to verify real world application



Thanks!

Objective II: CRT \rightarrow TT

Goal: Translation of RT to Coq

Method: Type-based Syntactic Translation

Risk: CRT \rightarrow TT is not always possible

Practical Gain: Tiny TCB, i.e., that of Coq

Theoretical Gain: Relationship between RT and TT

Sound Type Systems

Soundness Recipe

Ingredients:

1. One Deductive System (DS)
2. One consistent mathematical theory
3. One tiny Trusted Code Base (TCB)

Methodology:

1. Show the DS has a model in the consistent theory
2. Implement the DS
3. Your implementation is your tiny TCB

Practicality Suggestion:

Extend your implementation with automation ultimately checked by your TCB

Coq Isabelle

| | |
|------------|-----|
| CIC | HOL |
| Set Theory | |
| 15K | 5K |

**~1 critical bug/year
in Coq**

Refinement Types are Practical



Graham Hutton
@haskellhutt



Replying to [@alpha_convert](#) [@nikivazou](#) and 2 others

What I like about refinement types is the low barrier to entry. Even a simple Haskell programmer like me can do refinement types (not a joke).

7:11 PM · Jun 11, 2021 · Twitter for iPhone

Refinement Types are not Sound

In existing refinement type checkers

(e.g., Liquid Haskell, F*, Stainless)

~5 unsoundness errors/year

In sound systems

(e.g., Coq)

~1 critical bug/year

Lack sound foundations for Refinement Types

Practical



Sound



Currently:
Refinement types are Practical but not Sound

Objective I: $RT \rightarrow CRT$

Goal: Extract explicit certificates for testing/validation

Method: Type-based Syntactic Translation

Gain: Reduce Trusted Code Base (TCB)

Objective I: **RT** → CRT

Goal: Extract explicit certificates for testing/validation

Method: Type-based Syntactic Translation

Gain: Reduce Trusted Code Base (TCB)