

# **ANOSY:** **Approximated Knowledge Synthesis** with Refinement Types

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# IMDEA Software Institute

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Anosy @ PLDI'22

Haskell: Pure with Monads

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Ideal to track information that goes in the monad

a.k.a. Information Flow Control

# Monadic Information Flow Control



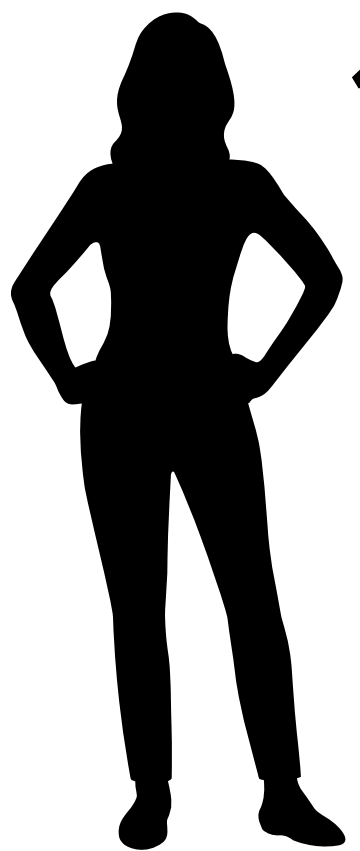
What is your  
name?

```
ifc :: IFC _  
ifc = do  
  lname    <- ask userName
```

...



# Monadic Information Flow Control



What is your  
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```
ifc :: IFC _  
ifc = do  
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```



Bob

# Monadic Information Flow Control



What is your  
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Let me  
unlock that...

```
ifc :: IFC _  
ifc = do  
  lname <- ask userName
```



Bob

# Monadic Information Flow Control



What is your  
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Let me  
unlock that...

Locks State

```
ifc :: IFC _  
ifc = do  
  lname    <- ask userName  
  
— unlock :: Locked a → IFC a
```



Bob

# Monadic Information Flow Control

What is your  
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Let me  
unlock that...

Locks State



```
ifc :: IFC _  
ifc = do  
  lname    <- ask userName  
  name     <- unlock lname
```

Bob



# Monadic Information Flow Control



What is your name?

How do I run IFCs?

Locks State



```
ifc :: IFC _  
ifc = do  
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  name     <- unlock lname
```

```
runIFC :: IFC a → Perm → a  
runIFC m p =  
  if locksOf m are below p  
  then valueOf m  
  else Permission Error
```



Bob



# Monadic Information Flow Control



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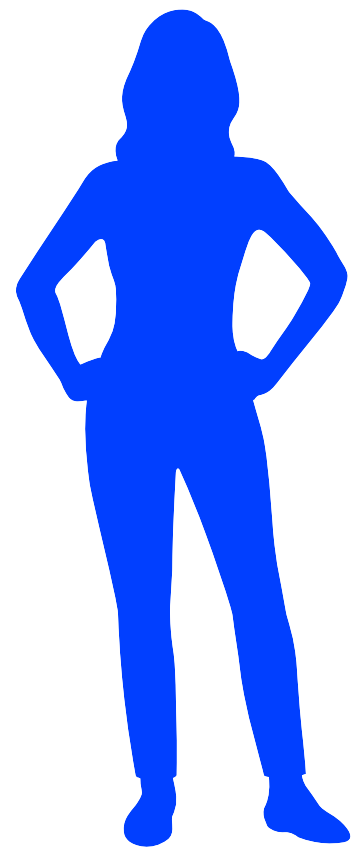
Bob



Haskell IFC systems:  
LIO, LWeb, STORM

# Monadic Information Flow Control

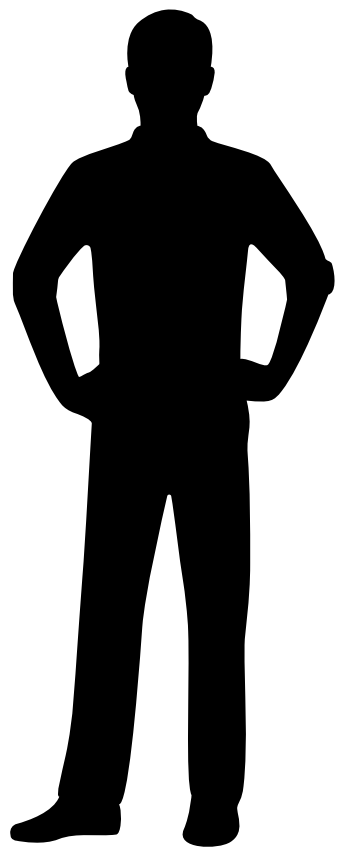
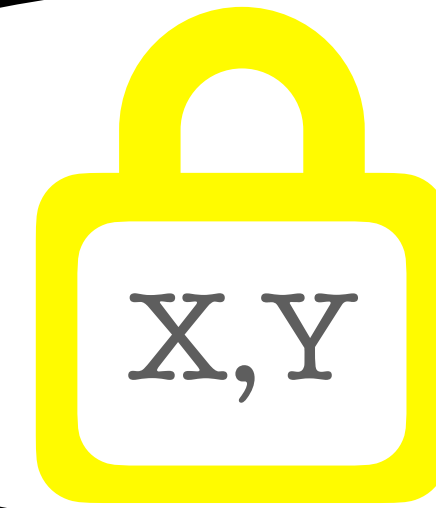
Who are your  
friends?



Locks State



```
ifc :: IFC _  
ifc = do  
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  name     <- unlock lname  
  lfriends <- ask userFriends
```



# Monadic Information Flow Control

Who are your  
friends?

Let me  
unlock that...

Locks State

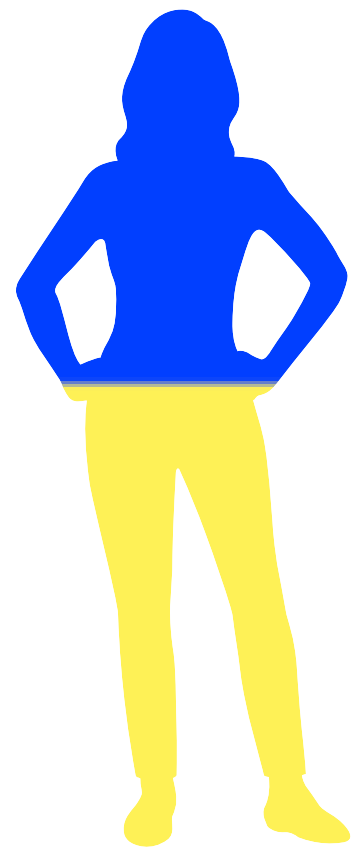


```
ifc :: IFC _  
ifc = do  
  lname    <- ask userName  
  name     <- unlock lname  
  lfriends <- ask userFriends  
  friends  <- unlock lfriend
```

X,Y

# Monadic Information Flow Control

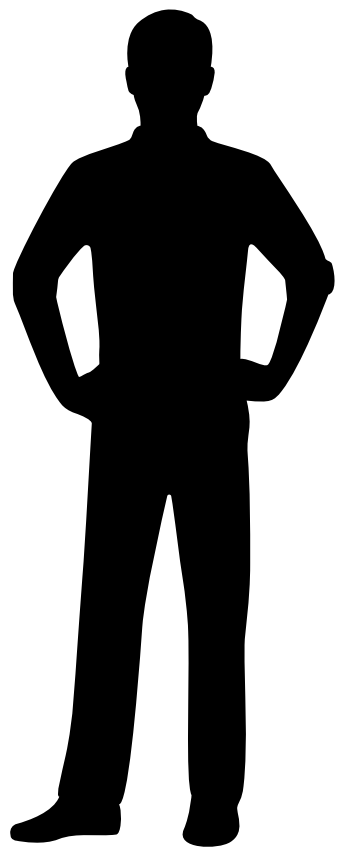
What is your location?



Locks State

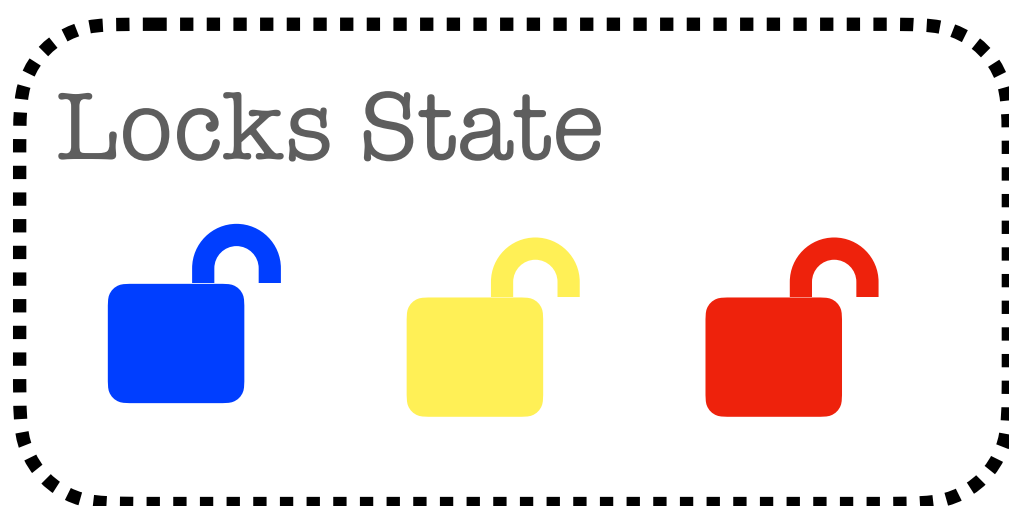
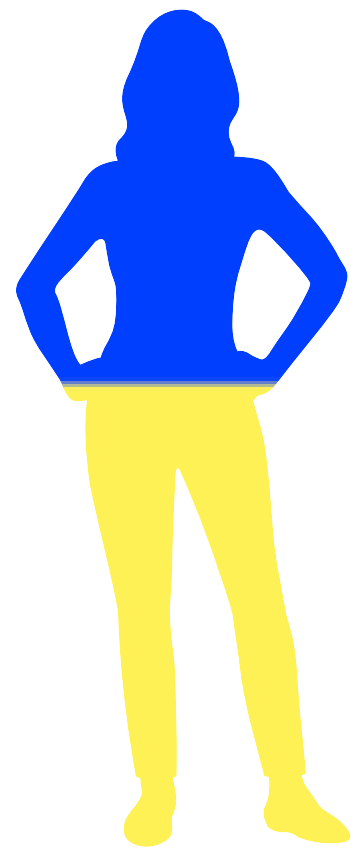


```
ifc :: IFC ()  
ifc = do  
  lname    <- ask userName  
  name     <- unlock lname  
  lfriends <- ask userFriends  
  friends  <- unlock lfriend  
  lloc     <- ask userLocation  
  loc      <- unlock lloc
```



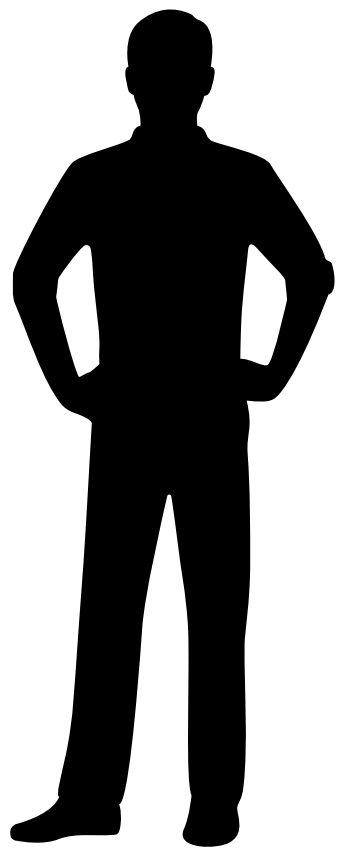
# Exact Location is usually Well Protected

What is your location?



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  lfriends <- ask userFriends  
  friends  <- unlock lfriend  
  lloc     <- ask userLocation  
  loc      <- unlock lloc
```

```
>> runIFC ifc p  
>> Permission Error
```



# Approximate Location is Required by Location-Based Apps



...



Any good  
restaurant  
around?

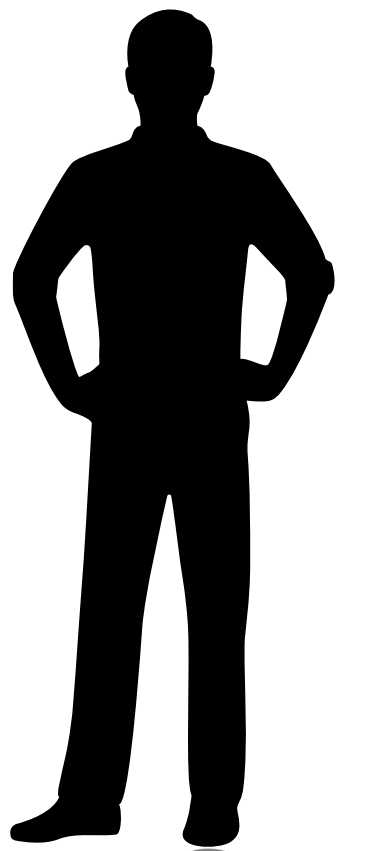
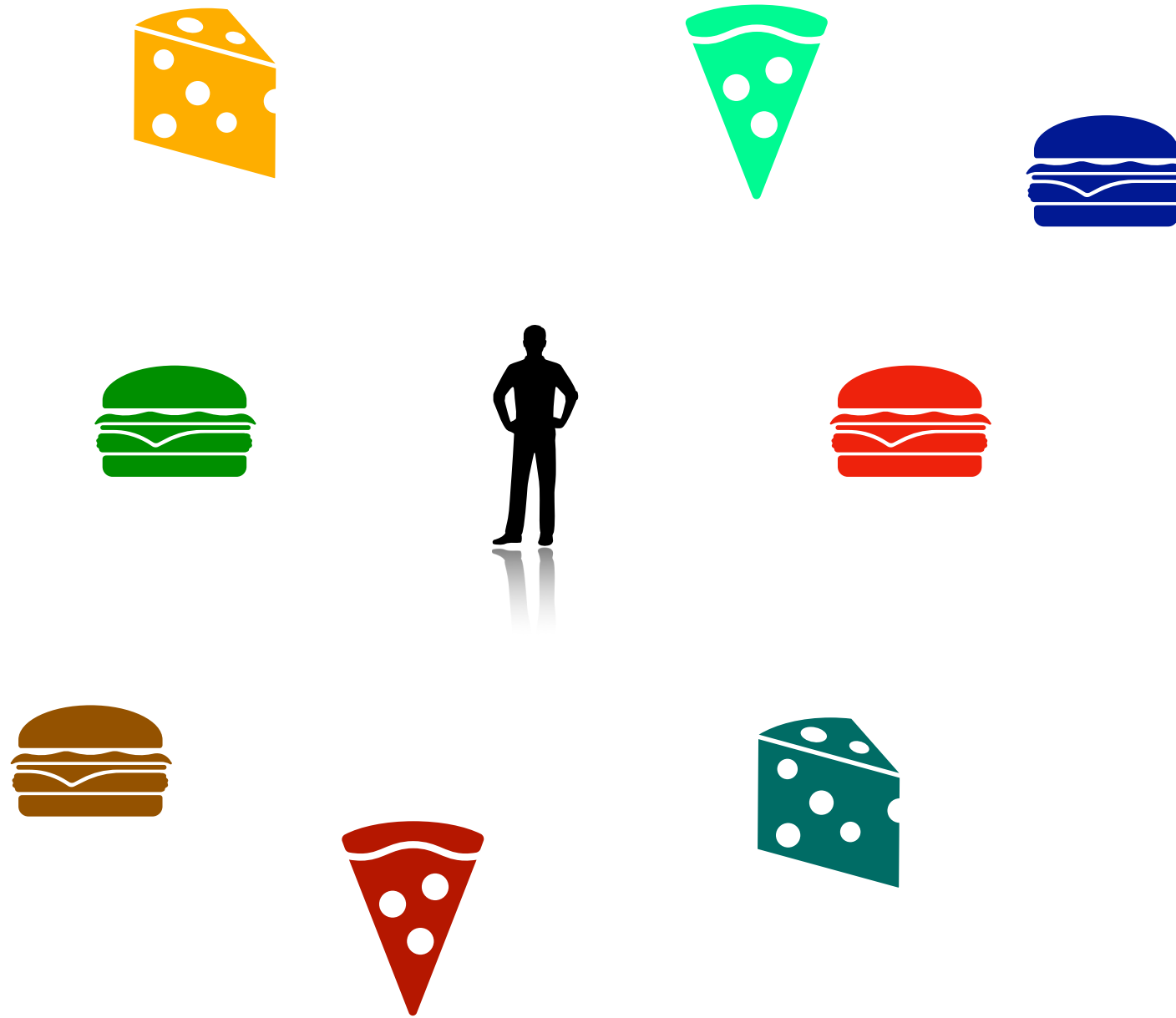
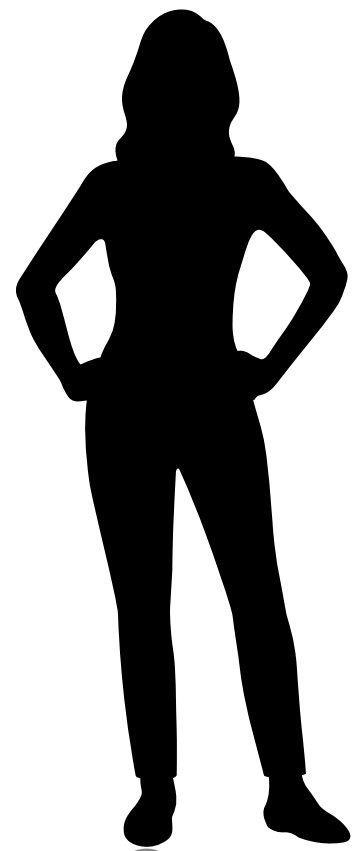




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Any good  
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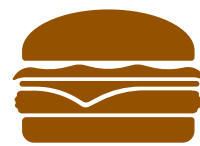
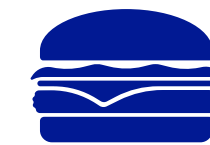
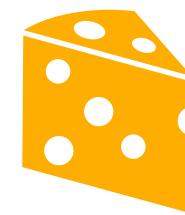
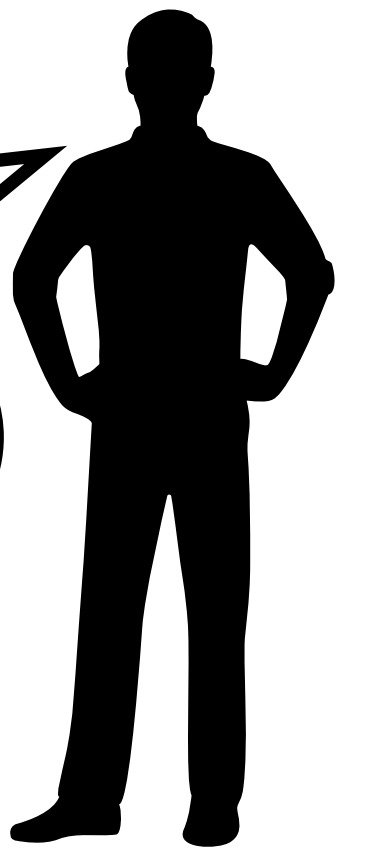
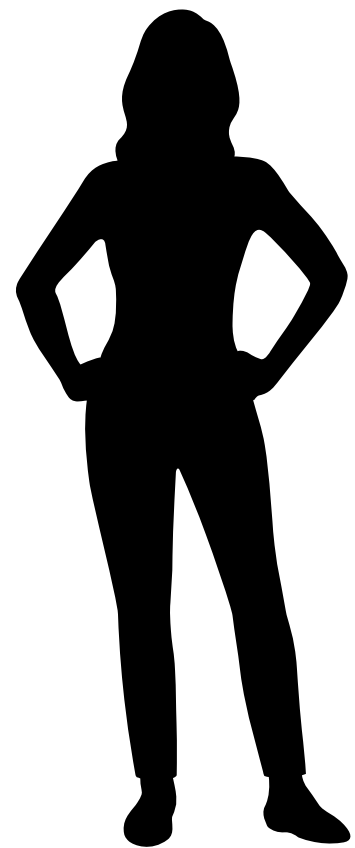


# Approximate Location is Required by Location-Based Apps

What is your location?

Any good restaurant around?

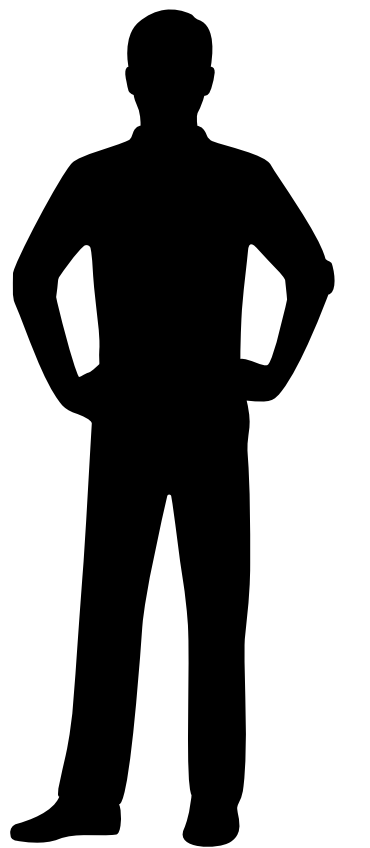
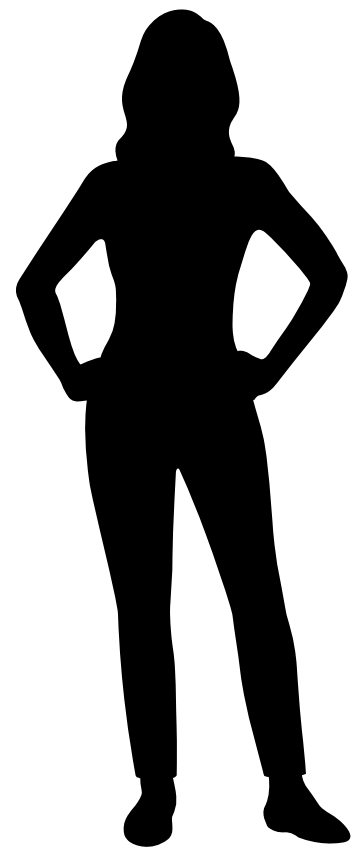
Permission Error!



# Approximate Location is Required by Location-Based Apps

Are you  
nearby 🍔 ?

Any good  
restaurant  
around?



# Downgrade for Approximate Location Information



Are you  
nearby 🍔 ?

Any good  
restaurant  
around?



```
ifc :: IFC Bool
ifc = do
  lloc    <- ask userLocation
  isclose <- downgrade lloc
            nearbyPlace
```

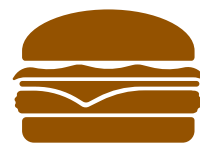
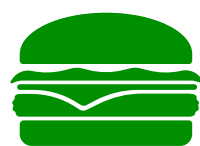
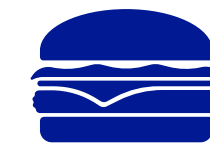
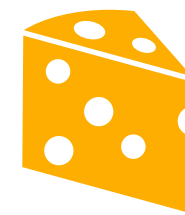
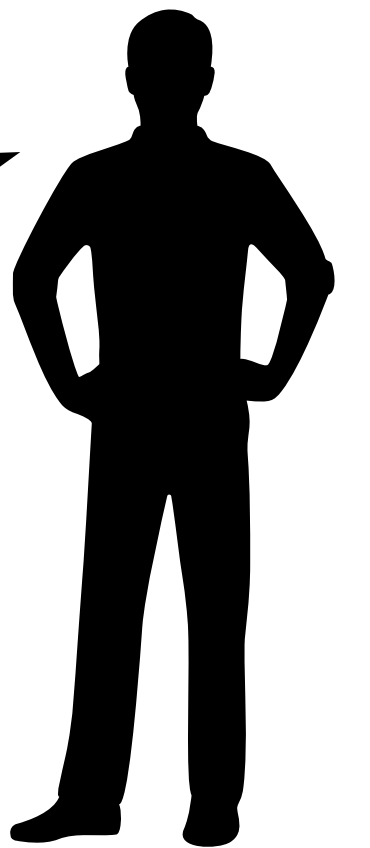
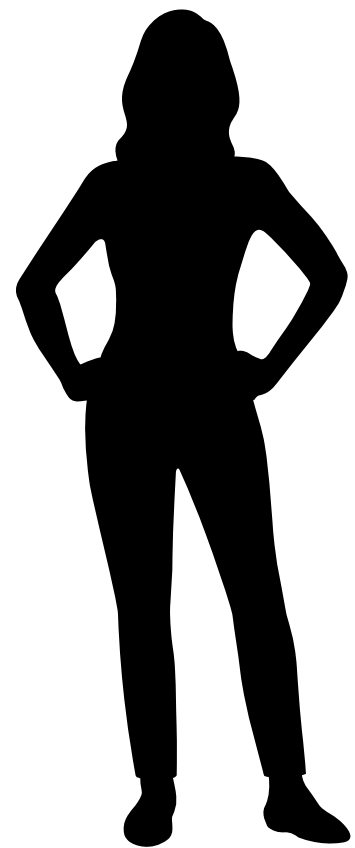
```
downgrade :: Locked s
            → (s → Bool)
            → IFC Bool
```

# Downgrade for Approximate Location Information

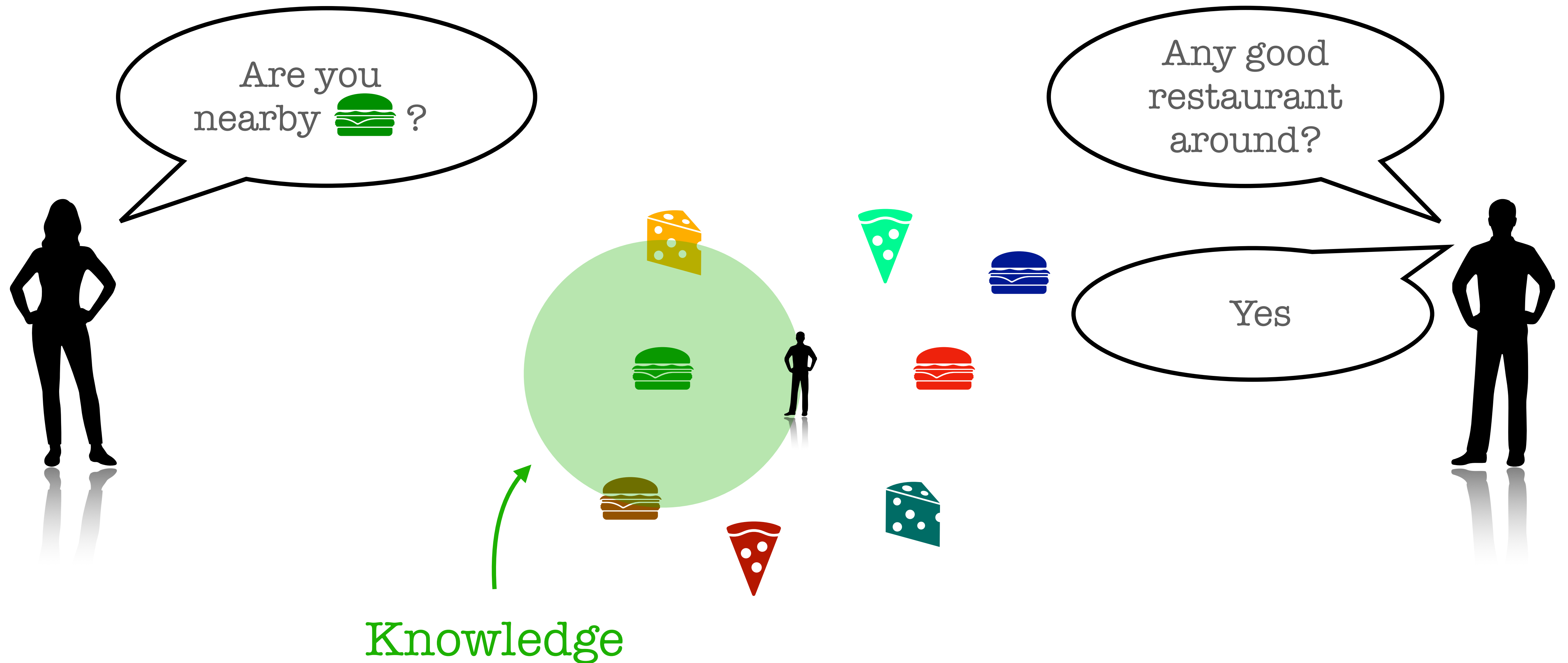
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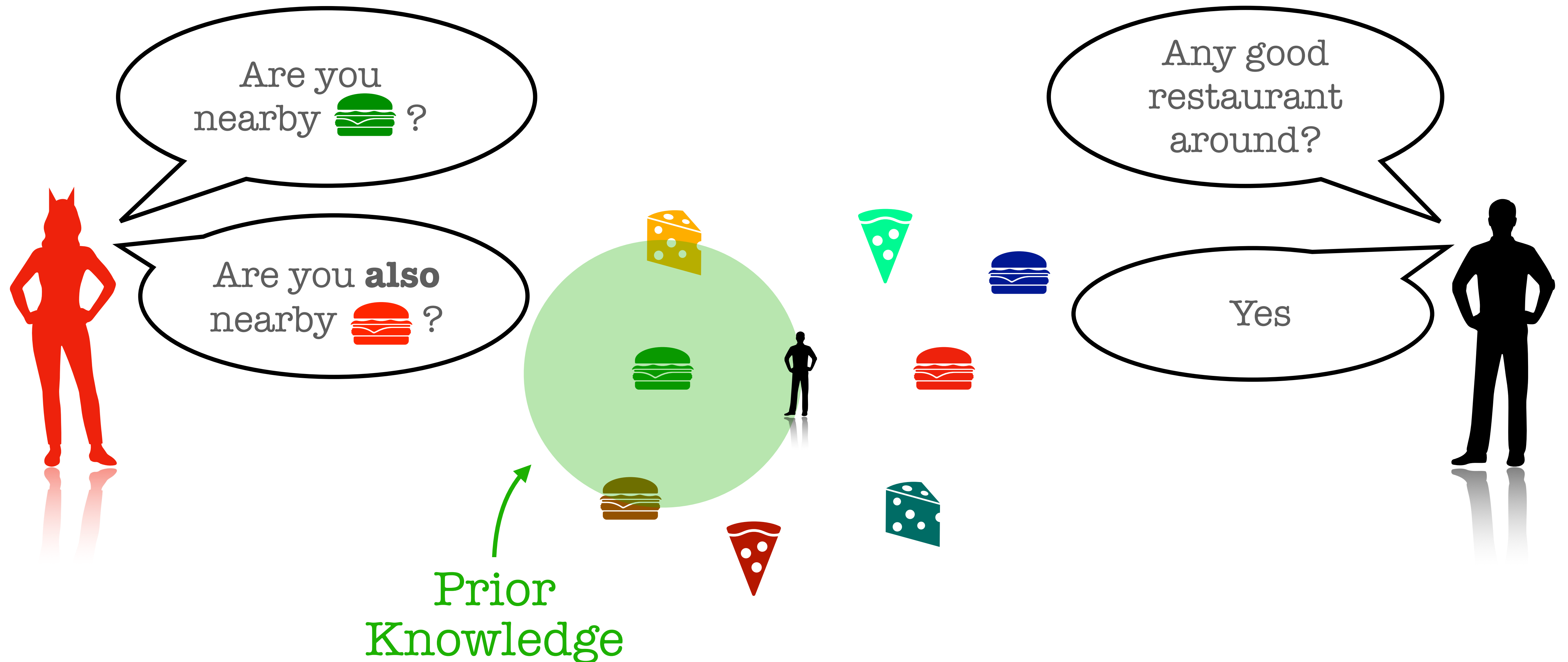
Yes



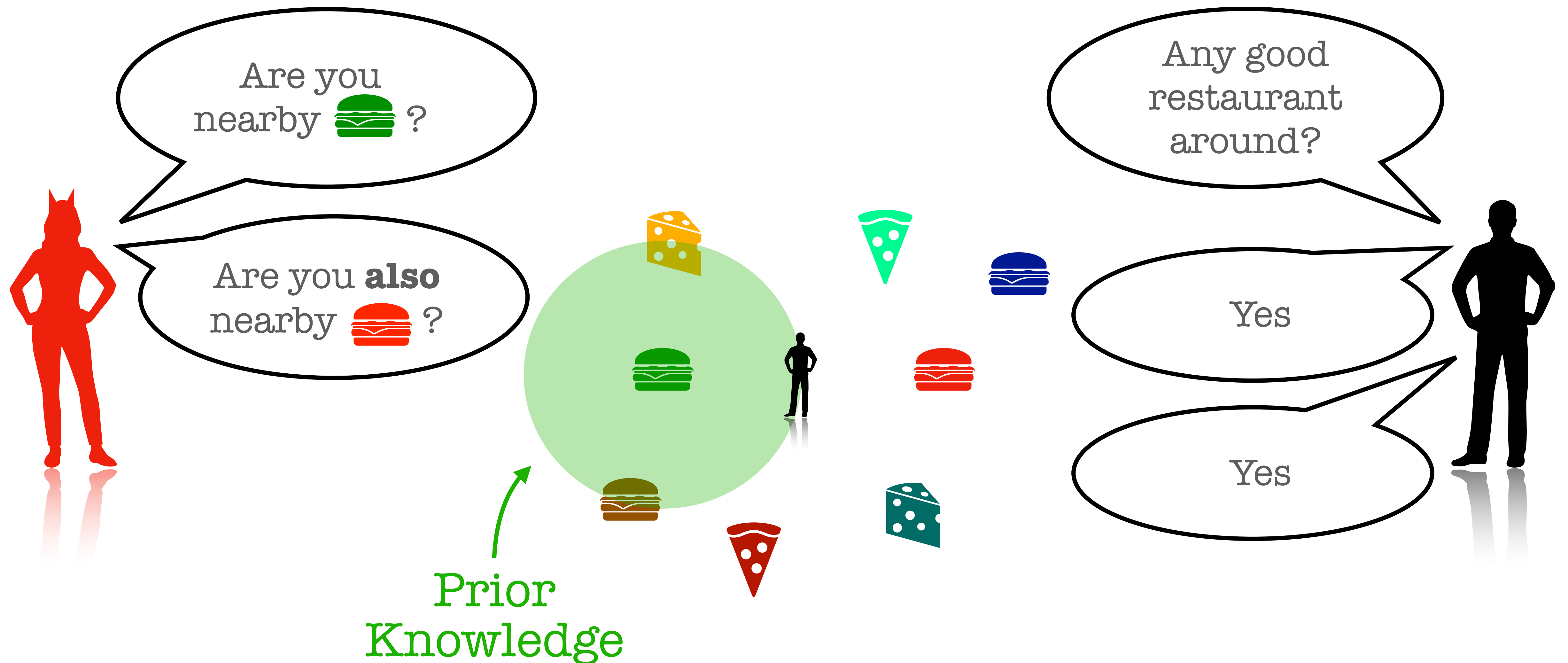
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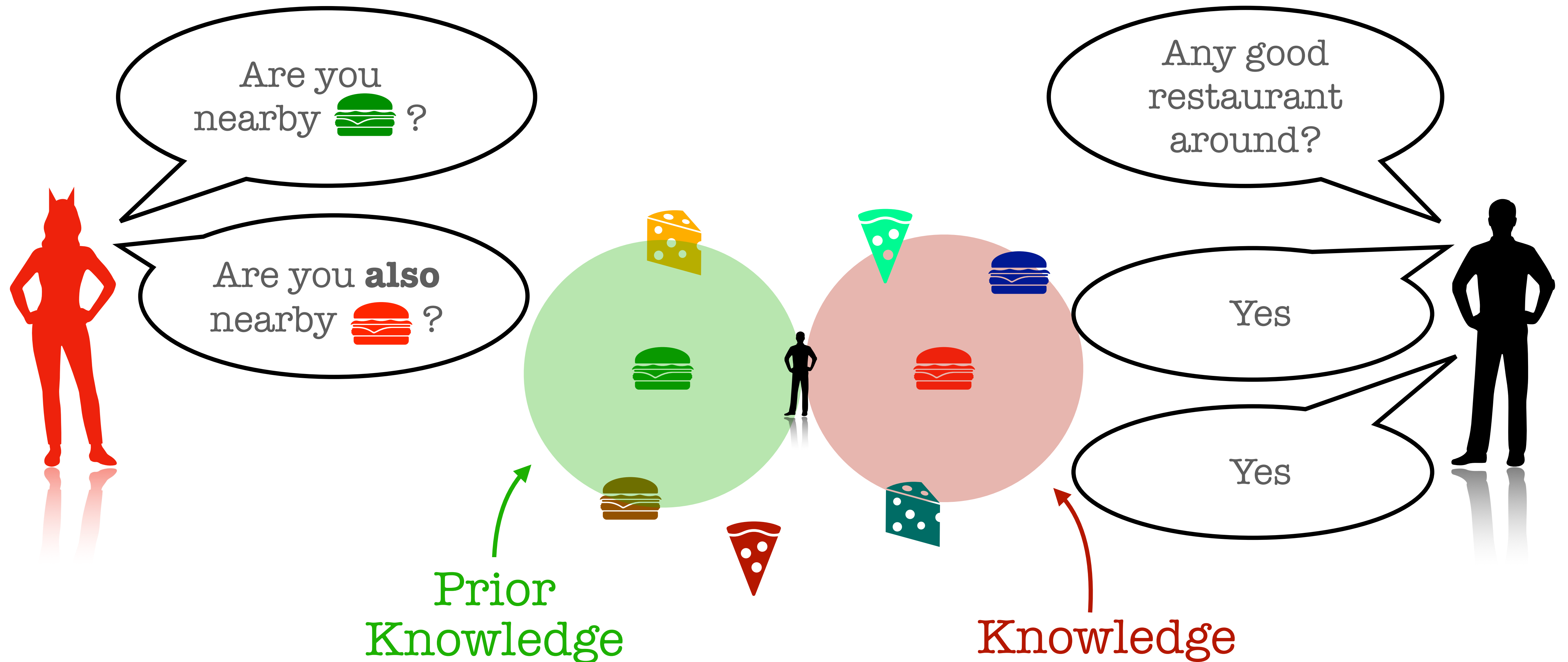


# Downgrade for Approximate Location Information



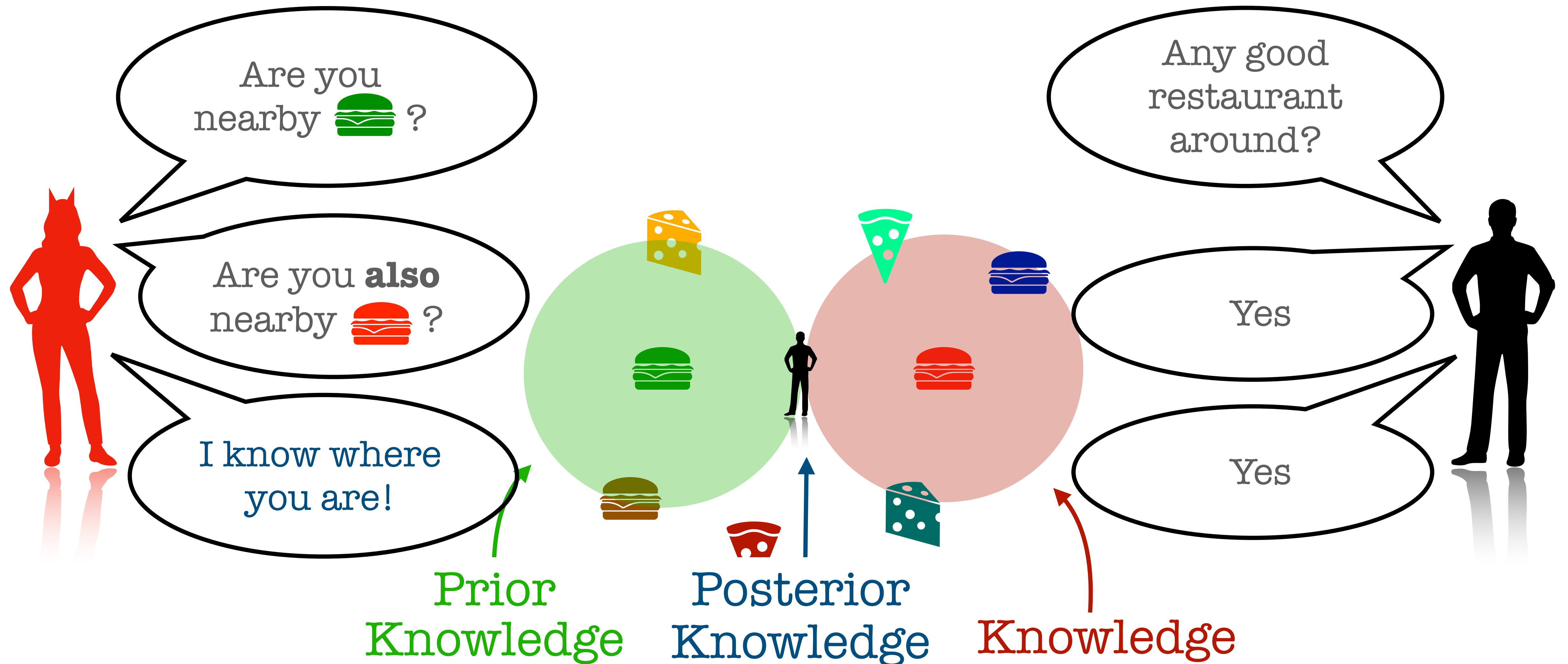


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**Problem:** Downgrade can Leak Exact Location

Bounded Downgrade:

Answer only when posterior is “general enough”

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Bounded Downgrade:

Answer only when posterior is “general enough”

`policy :: a → Bool`

`policy a = size a > 100`

# Bounded Downgrade:

Answer only when posterior is “general enough”

State

```
priors :: Map s a  
policy :: a -> Bool
```

```
downgrade :: Knowledge a s  
           => Locked s  
           → (a → Bool)  
           → IFC Bool  
  
downgrade s q = do  
  val    <- unprotect s  
  prior  <- getPrior val  
  let post = posterior q val prior  
  if policy post  
    then do setPrior val post  
            return $ q val  
    else throwError “Policy Violation”
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## Observations:

No Dependence from IFC!  
How to compute posterior?

# Bounded Downgrade: AnosyT Monad Transformer

```
AnosyT a s =  
  StateT (StateA a s)
```

```
StateA
```

```
priors :: Map s a  
policy :: a -> Bool
```

```
downgrade :: Knowledge a s, Monad m  
            , Lockable l => l s  
            → (a → Bool)  
            → AnosyT a s m Bool
```

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StateA

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On top of any  
Haskell IFC system:  
LIO, LWeb, STORM

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downgrade :: Knowledge a s, Monad m  
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# Posterior Knowledge Computation

**Goal:** Definition of

posterior :: Knowledge a s

$\Rightarrow (s \rightarrow \text{Bool})$  — query

$\rightarrow s$  — secret

$\rightarrow a$  — prior

$\rightarrow a$



# Posterior Knowledge Computation

**Knowledge:** A Set of Secrets

```
class Knowledge a s where
  ⊤ :: a
  ⊥ :: a
  ∈ :: s → a → Bool
  ⊆ :: a → a → Bool
  ∩ :: a → a → a
```

**Goal:** Definition of

posterior :: Knowledge a s

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# Posterior Knowledge Computation

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**Goal:** Definition of

```
posterior :: Knowledge a s
  => (s → Bool)    — query
  → s              — secret
  → a              — prior
  → a
```

**Challenge:**

Precise Operations can be Uncomputable

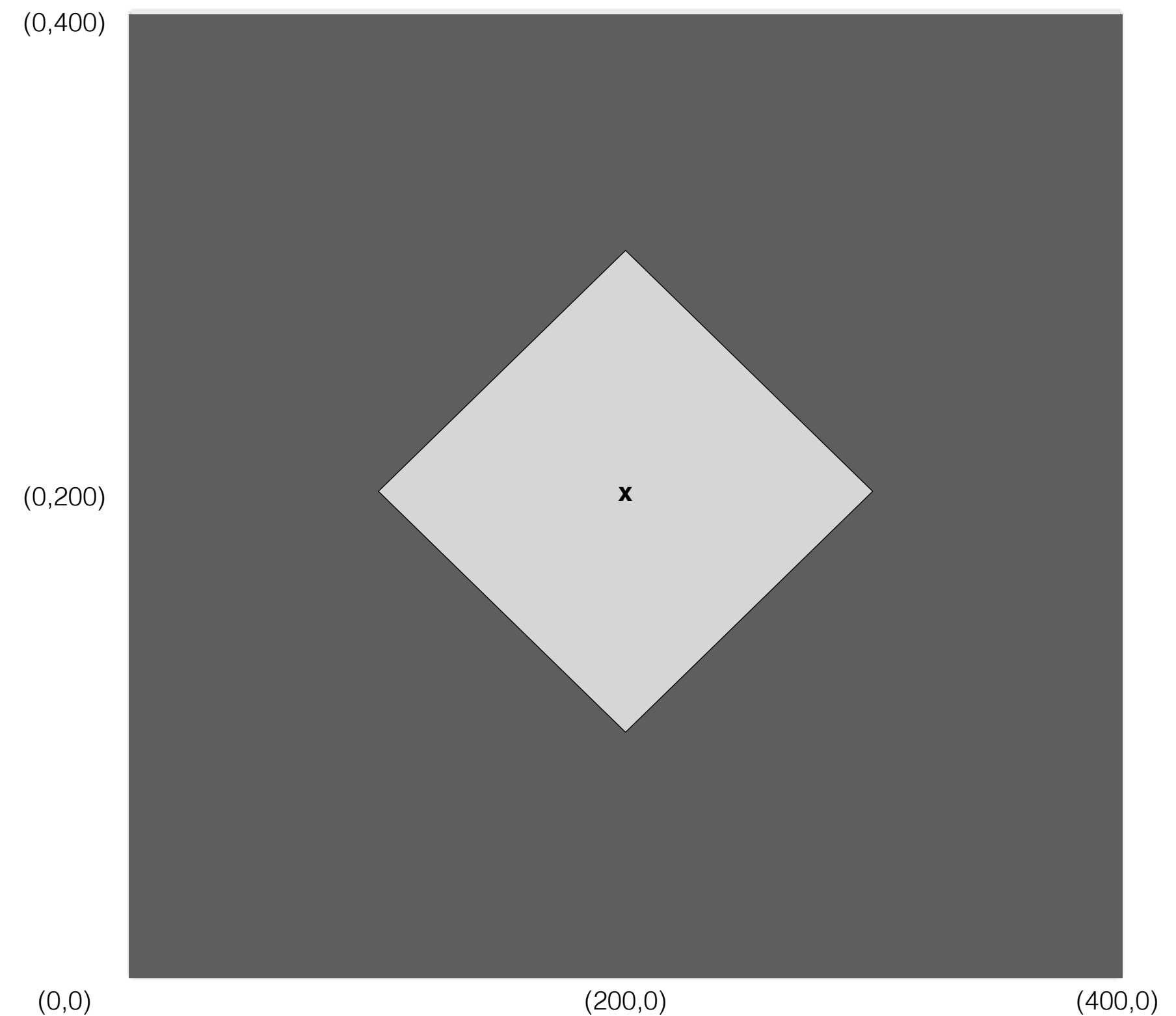
**Solution:**

Use Abstract Domains!

# Knowledge Representation

```
data Loc = L {x :: Int, y :: Int}
nearby :: Loc → Loc → Bool
nearby (L xo yo) (L x y) =
  abs (x - xo) (y - yo) <= 100
```

```
type S = Loc
query :: S → Bool
query s = nearby (L 200 200)
```



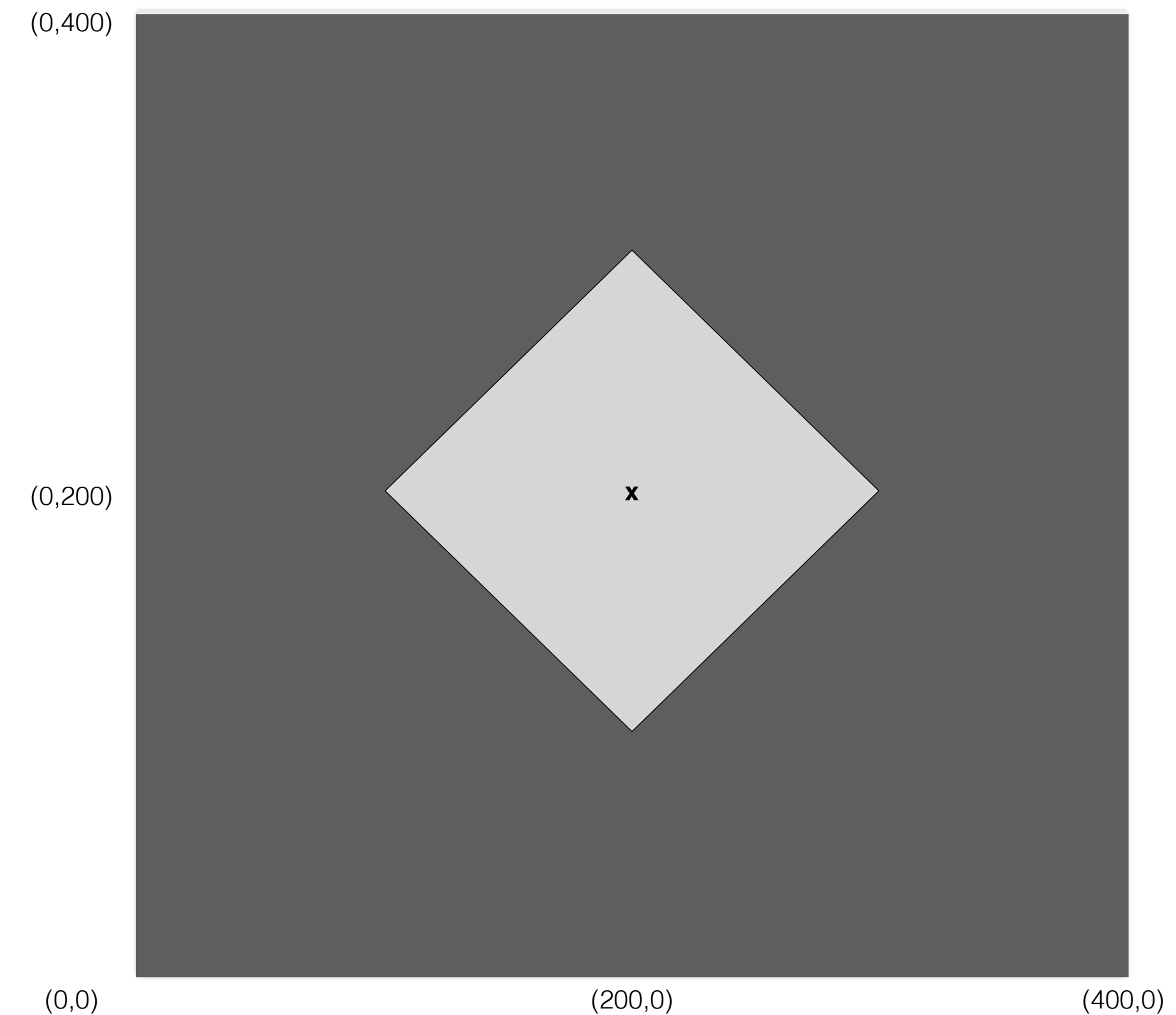
Knowledge on query  
(Separation into yes/no areas)

# Knowledge Representation

Difficult to  
Represent

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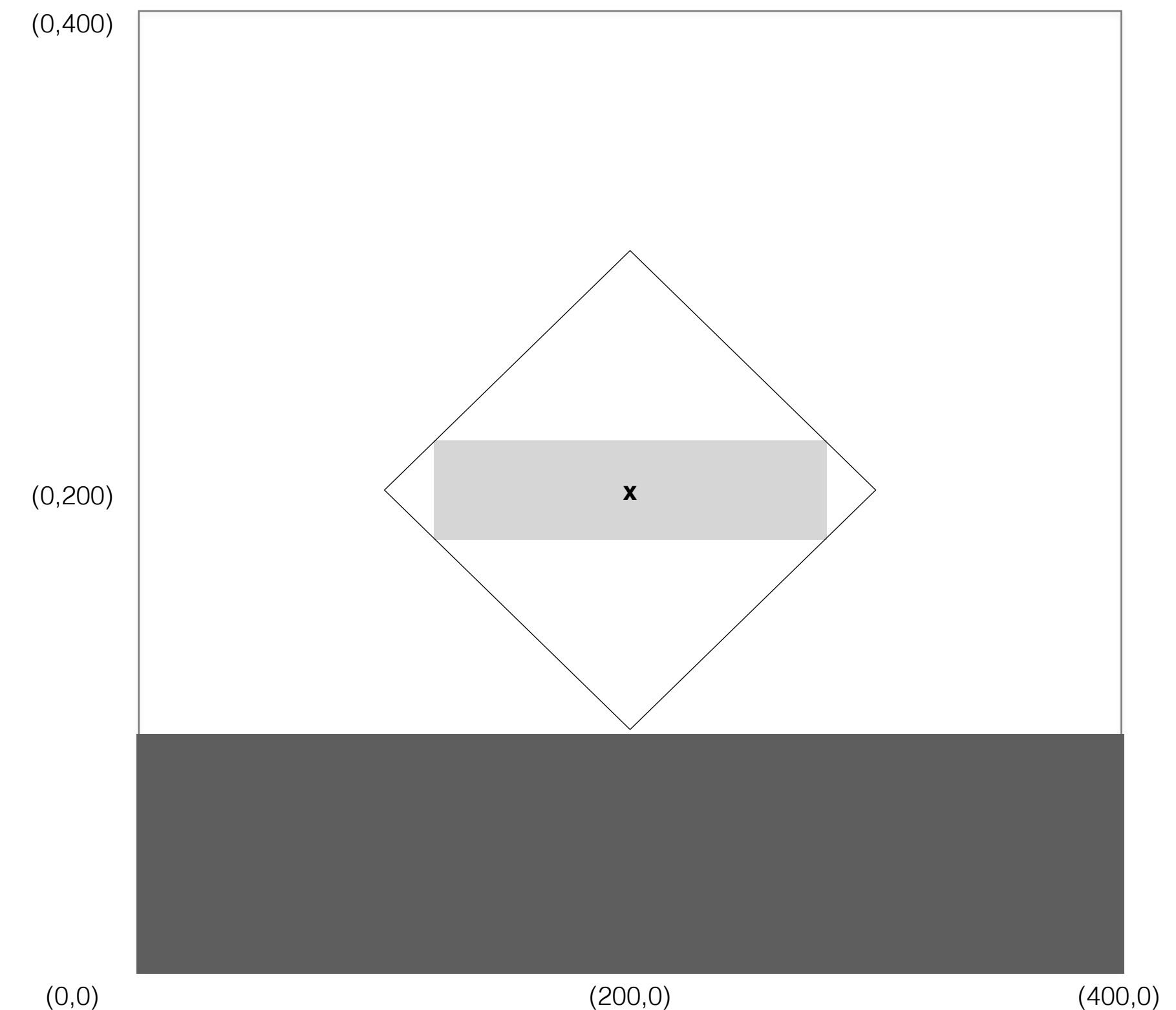
Knowledge on query  
(Separation into yes/no areas)

# Knowledge Approximation

```
type S = Loc — = L {x :: Int, y :: Int}
query :: S → Bool
query s = nearby (L 200 200)
```

```
data KInt = KInt {lo :: Int, hi :: Int}
data K     = K {kx :: KInt, ky :: KInt}
instance Knowledge K S where ...
```

```
approx :: (K,K)
approx = (yesK, noK)
yesK = K (KInt 121 279) (KInt 179 221)
noK  = K (KInt 0 400) (KInt 0 99)
```



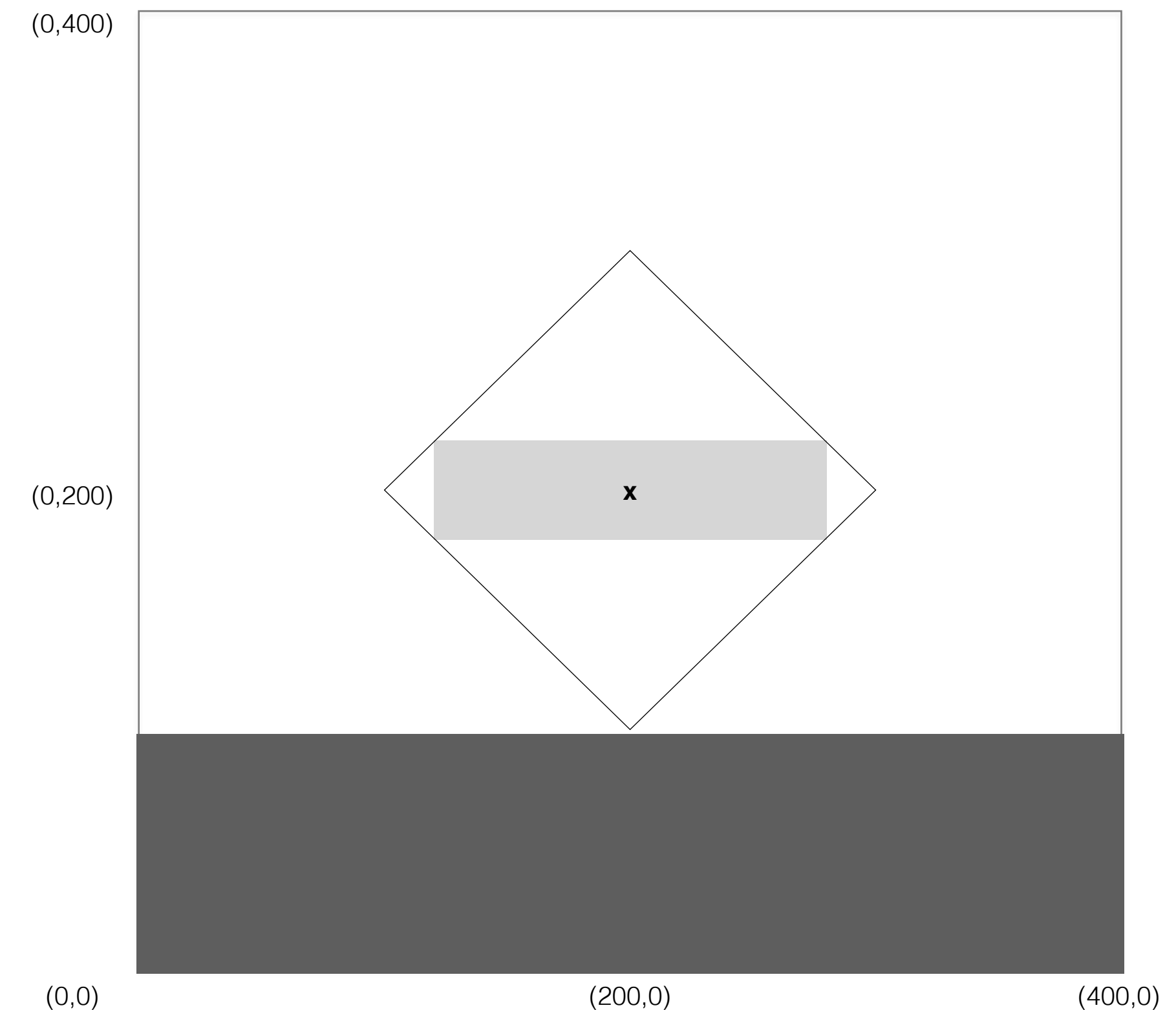
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Back to our Goal,  
posterior is easy to define

```
posterior :: S → K → K
posterior s p = p ∩
  if query s then yesK else noK
```



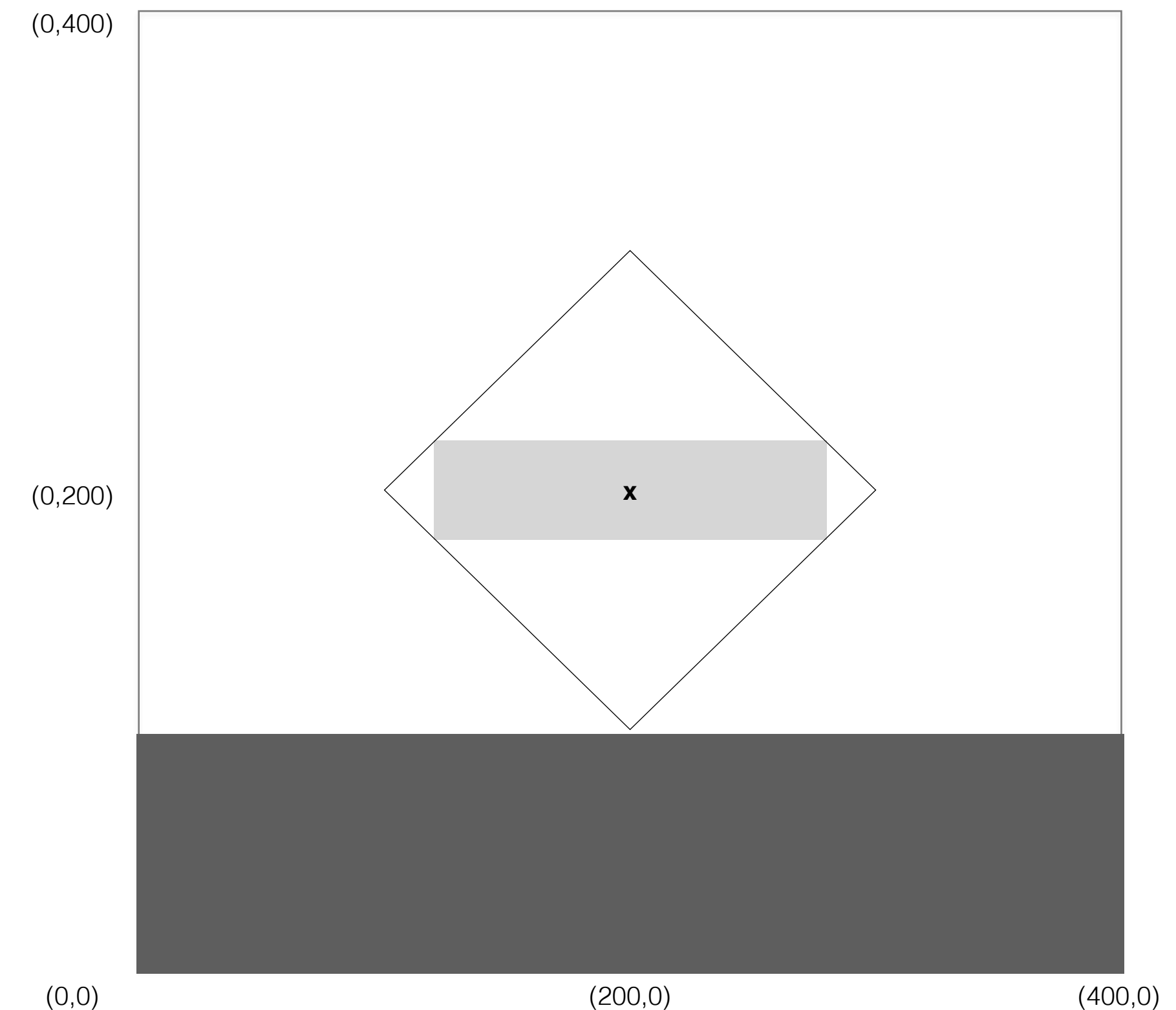
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Interval Knowledge Approximation

How do I come up with approx?  
How do I know it is correct?

# Refinement Types to the Rescue!

```
approx :: (K,K)
approx = (yesK, noK)
yesK = K (KInt 121 279) (KInt 179 221)
noK  = K (KInt 0   400) (KInt 0   99)
```

```
yesK :: K<\s -> query s>
noK  :: K<\s -> not (query s)>
```

$k :: K<p>$

All elements inside  $k$  satisfy  $p$

\* Knowledge contains secrets



# Refinement Types for Synthesis!

**Goal:**  $\text{yesK} :: K \langle s \rightarrow \text{query } s \rangle$

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**Step 1:** Syntax Directed

$\text{yesK} = K \text{ (KInt xl xh) (KInt yl yh)}$

# Refinement Types for Synthesis!

**Goal:**  $\text{yesK} :: K \langle s \rightarrow \text{query } s \rangle$

---

**Step 1:** Syntax Directed

$\text{yesK} = K (\text{KInt } x_l \ x_h) (\text{KInt } y_l \ y_h)$

**Step 2:** Constraint Generation

$\forall x, y. x_l \leq x \leq x_h \wedge y_l \leq y \leq y_h \Rightarrow \text{query } (L \ x \ y)$

maximise  $x_h - x_l$

maximize  $y_h - y_l$

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**Step 3:** SMT solves constraints

$x_l := 121, x_h := 279, y_l := 179, y_h := 221$

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**Step 3:** SMT solves constraints

$x_l := 121, x_h := 279, y_l := 179, y_h := 221$

**Finally:** Plug in the holes

$\text{yesK} = K (\text{KInt } 121 \ 279) (\text{KInt } 179 \ 221)$

## **Anosy: Bounded Downgrade**

AnosyT keeps track of prior leaked knowledge

**Challenge:** compute posterior  
Knowledge Abstraction + Synthesis.

For each query, abstract knowledge is  
synthesised via SMT  
verified via Liquid Haskell

## **Implementation**

AnosyT + GHC plugin to process queries.

**Queries** are straight line Bool functions

**Secrets** are products of Ints

**Abstract Domains** are Intervals and their Powersets

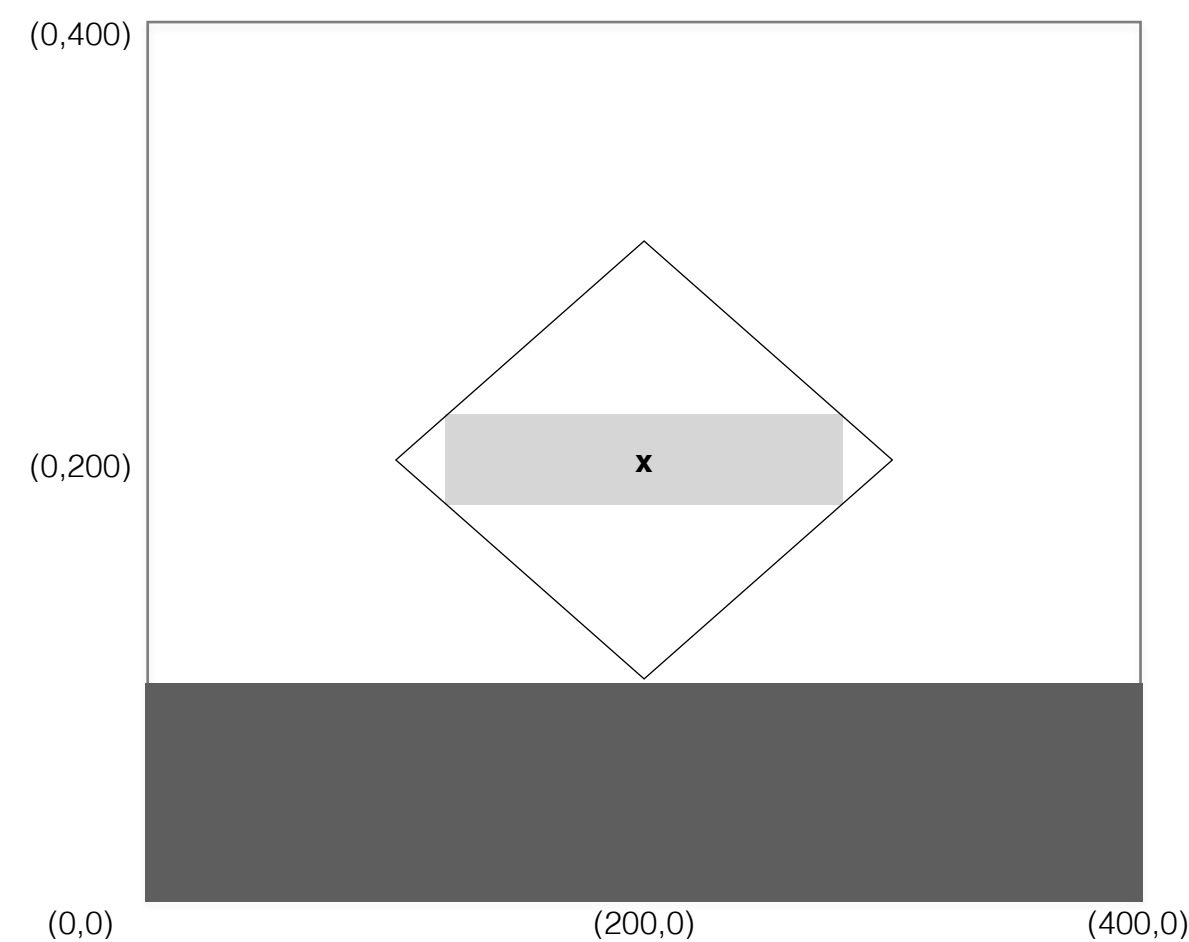
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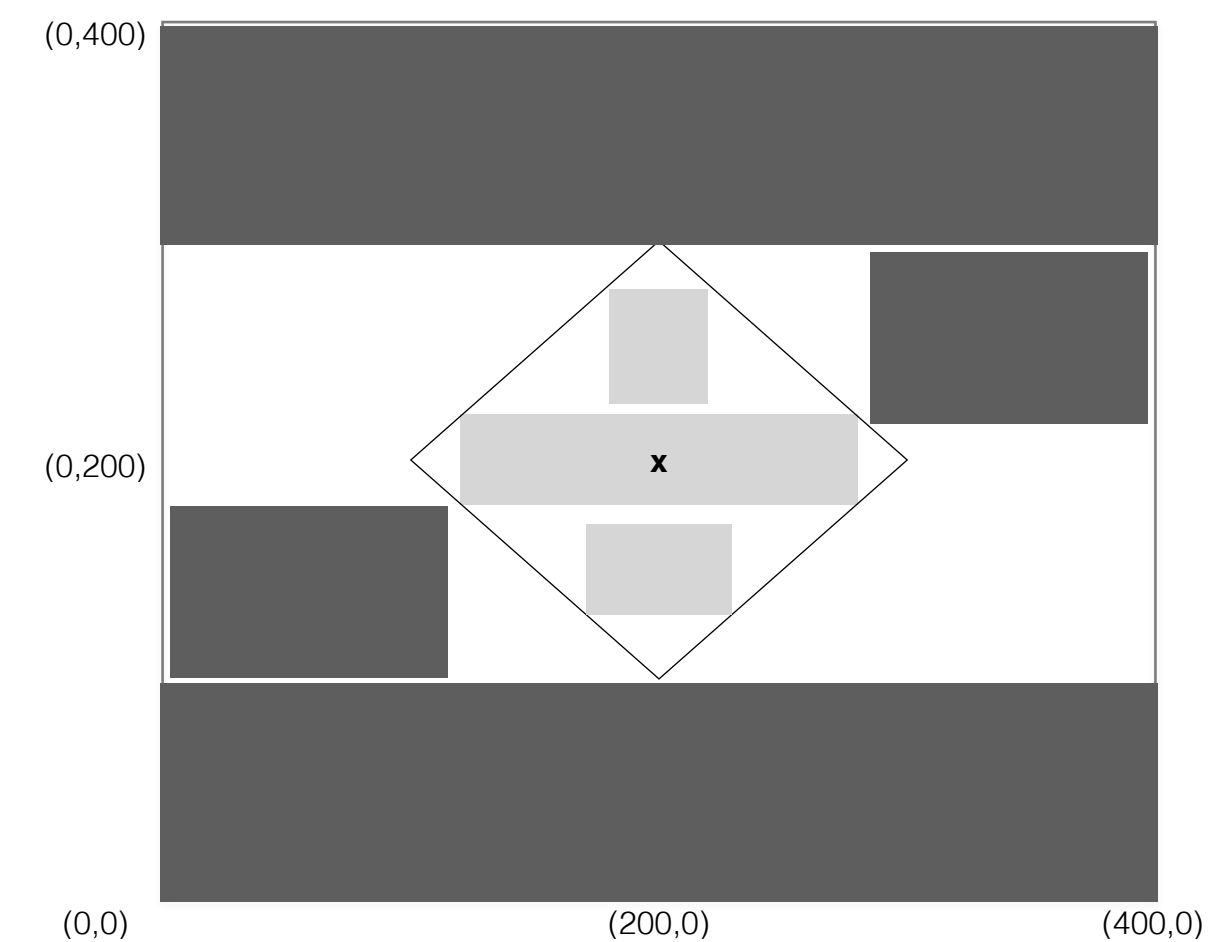
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Interval Knowledge



Powerset Knowledge



# Evaluation

#	Name	No. of fields	Size of ind. sets
B1	Birthday	2	259 / 13246
B2	Ship	3	1.01e+06 / 2.43e+07
B3	Photo	3	4 / 884
B4	Pizza	4	1.37e+10 / 2.81e+13
B5	Travel	4	2160 / 6.72e+06

We evaluate with secrets with multiple dimensions

#	Under-approximation							
	Size	% diff.	Verif. time	Synth. time				Synth. time
B1	259 / 9620	0 / 27	2.78 ± 0.03	1.11 ± 0.01	259 / 13505	0 / 2	2.64 ± 0.03	1.07 ± 0.01
B2	2.21e+05 / 1.01e+07	78 / 58	3.62 ± 0.02	9.26 ± 0.04	2.02e+06 / 2.54e+07	100 / 5	3.17 ± 0.02	4.00 ± 0.12
B3	4 / 664	0 / 25	3.12 ± 0.06	0.90 ± 0.07	4 / 888	0 / 0	2.83 ± 0.03	0.90 ± 0.01
B4	3.53e+04 / 1.35e+05	100 / 100	3.66 ± 0.04	20.92 ± 0.11	9.22e+12 / 2.81e+13	67200 / 0	3.29 ± 0.08	10.87 ± 0.01
B5	360 / 5.04e+06	83 / 25	3.81 ± 0.04	1.38 ± 0.04	35460 / 6.72e+06	1542 / 0	3.47 ± 0.04	0.89 ± 0.01

(a) Interval abstract domain

#	Under-approximation				Over-approximation			
	Size	% diff.	Verif. time	Synth. time	Size	% diff.	Verif. time	Synth. time
B1	259 / 13246	0 / 0	4.51 ± 0.05	1.13 ± 0.02	259 / 13505	0 / 2	4.34 ± 0.03	1.08 ± 0.01
B2	6.78e+05 / 1.62e+07	33 / 33	5.32 ± 0.09	14.34 ± 0.11	1.80e+06 / 2.54e+07	78 / 5	5.17 ± 0.02	4.89 ± 0.09
B3	4 / 880	0 / 0	5.29 ± 0.09	1.07 ± 0.03	4 / 888	0 / 0	4.99 ± 0.03	1.03 ± 0.01
B4	3.88e+05 / 4.00e+05	100 / 100	5.78 ± 0.03	54.89 ± 0.23	9.22e+12 / 2.81e+13	67200 / 0	5.48 ± 0.08	30.57 ± 0.07
B5	720 / 6.70e+06	67 / 0	6.02 ± 0.07	13.26 ± 0.09	6300 / 6.72e+06	192 / 0	5.96 ± 0.04	15.25 ± 0.03

(b) Powerset of intervals with size 3

\* Mardziel, Magill, Hicks, and Srivatsa. J. Comp. Sec. 2013. Dynamic enforcement of knowledge-based security policies using probabilistic abstract interpretation.

# Evaluation

#	Name	No. of fields	Size of ind. sets
B1	Birthday	2	259 / 13246
B2	Ship	3	1.01e+06 / 2.43e+07
B3	Photo	3	4 / 884
B4	Pizza	4	1.37e+10 / 2.81e+13
B5	Travel	4	2160 / 6.72e+06

#	Under-approximation				Over-approximation			
	Size	% diff.	Verif. time	Synth. time	Size	% diff.	Verif. time	Synth. time
B1	259 / 9620	0 / 27	2.78 ± 0.03	1.11 ± 0.01	259 / 13505	0 / 2	2.64 ± 0.03	1.07 ± 0.01
B2	2.21e+05 / 1.01e+07	78 / 58	3.62 ± 0.02	9.26 ± 0.04	2.02e+06 / 2.54e+07	100 / 5	3.17 ± 0.02	4.00 ± 0.12
B3	4 / 664	0 / 25	3.12 ± 0.06	0.90 ± 0.07	4 / 888	0 / 0	2.83 ± 0.03	0.90 ± 0.01
B4	3.53e+04 / 1.35e+05	100 / 100	3.66 ± 0.04	20.92 ± 0.11	9.22e+12 / 2.81e+13	67200 / 0	3.29 ± 0.08	10.87 ± 0.01
B5	360 / 5.04e+06	83 / 25	3.12 ± 0.04	1.38 ± 0.04	35460 / 6.72e+06	1542 / 0	3.47 ± 0.04	0.89 ± 0.01

Synthesis times are reasonable. Static analysis tools such as Prob\* are faster. But ANOSY synthesises knowledge at compile time.

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Interval abstract domain								
	Over-approximation							
	Synth. time	Size	% diff.	Verif. time	Synth. time			
	1.13 ± 0.02	259 / 13505	0 / 2	4.34 ± 0.03	1.08 ± 0.01			
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Approximation accuracy gets better with increasing the size of the powerset.

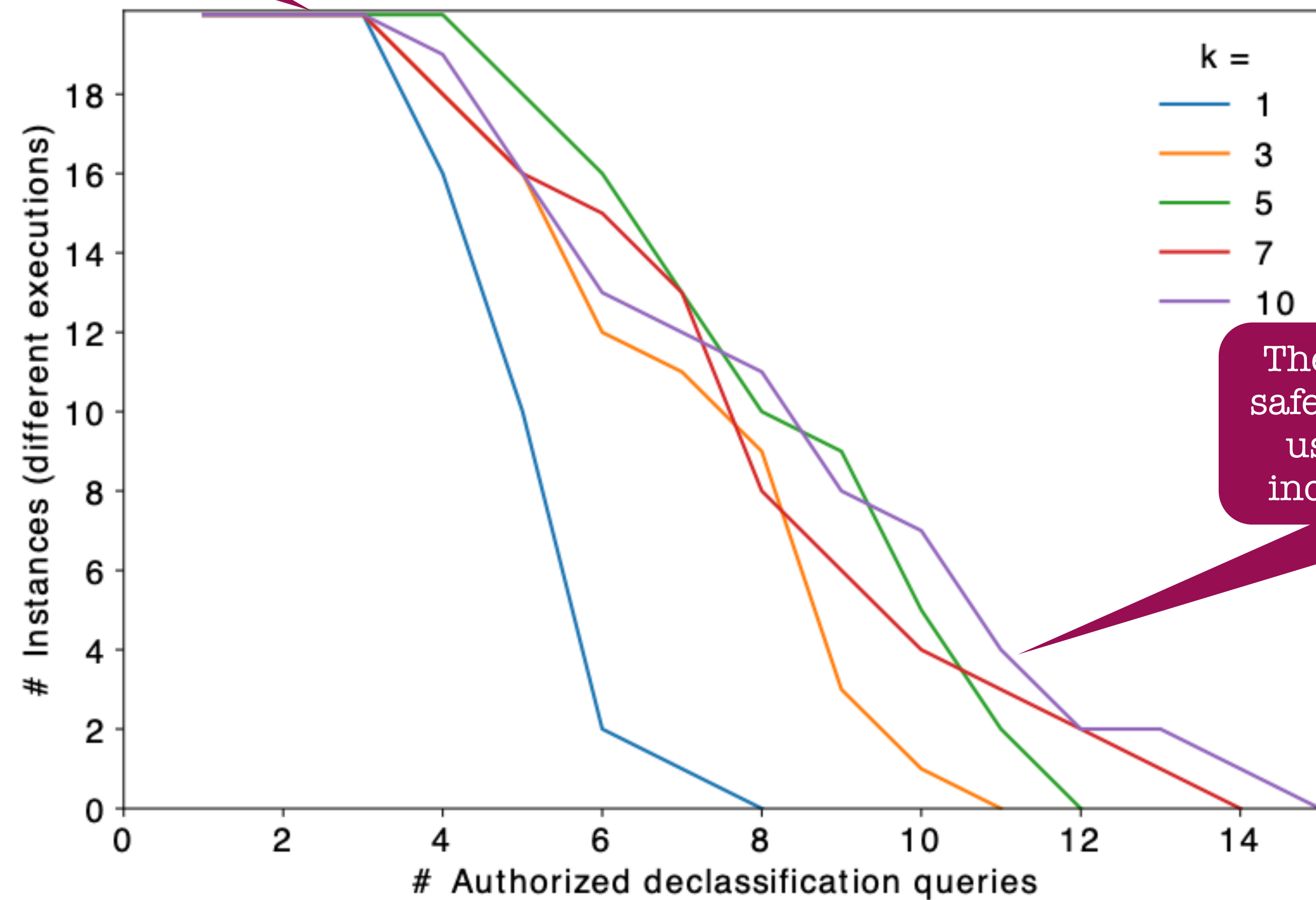
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# Evaluation: Location Example

All these queries are verified safe for the nearby query.



The system handles more safe declassifications of if a user is nearby with the increase in powerset size

## **Summary**

Haskell is Ideal for IFC (e.g., LIO, LWeb, STORM)

Realistic IFC apps downgrade (potentially leaking info)

### **Anosy: Bounded Downgrade**

AnosyT keeps track of prior leaked knowledge

For each query, abstract knowledge is  
synthesised via SMT  
verified via Liquid Haskell

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Anosy @ PLDI



Looking for  
PhDs/interns

Thanks!