



**LiquidHaskell**

Usable Language-Based Verification

Niki Vazou

University of Maryland

# Formal Verification

## Prove Properties of Software

# Formal Verification

## Prove Properties of Real Software

# Formal Verification

Prove Properties of Real Software



“A plane will not crash”

# Formal Verification

Prove Properties of Real Software



“Your passwords are SAFE”

# Formal Verification, in Practice

Prove Properties of ~~Real Software~~  
in Verification Specific Tools

# Verification Specific Tools

```
Lemma plus_Snm_nSm : forall n m, S n + m = n + S m.  
intros.  
simpl in |- *.  
rewrite (plus_comm n m).  
rewrite (plus_comm n (S m)).  
trivial with arith.  
Qed.
```



“Plus is indeed associative!”

# Verification Specific Tools

Difficult to use for Real Programs

Difficult to install

Special Syntax

No Compiler Optimizations

No Parallelism

**Very Few Users!**

My goal:

Verification of Real Programs

# Verification of Real Programs

My approach:

Turn a **Language** into a Verifier

Reuse language's syntax, runtime, and users!

# Verification of Real Programs

My approach:

Turn a **Language** into a Verifier

Target Language: Haskell

Haskell

+

Refinement Types

=



LiquidHaskell

# Haskell

take :: [a] -> Int -> [a]

```
> take [1,2,3] 2  
> [1,2]
```

# Haskell

take :: [a] -> Int -> [a]

```
> take [1,2,3] 500  
> ???
```

# Refinement Types

```
take :: xs:[a] -> {i:Int | i < len xs} -> [a]
```



take :: xs:[a] -> {i:Int | i < len xs} -> [a]

```
> take [1,2,3] 500
> Type Error!
```



Use Haskell's syntax, runtime, and **users**!

Used in **Industry**: to speed up code

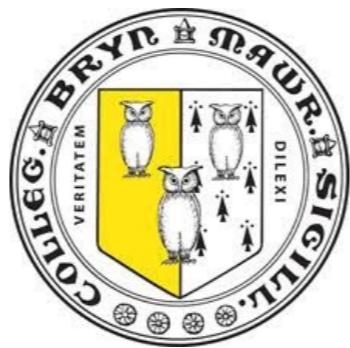


AWAKE



Well-Typed

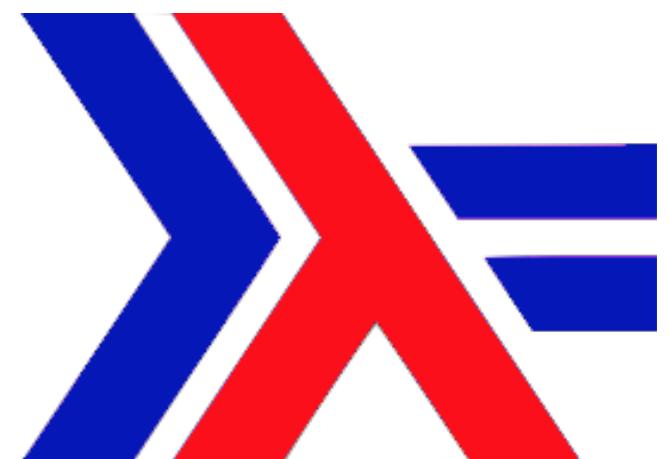
Used in **Education**: in Haskell courses!



# Haskell

## Functional Programming Language

Based on  
Strong Typing +  $\lambda$ -calculus

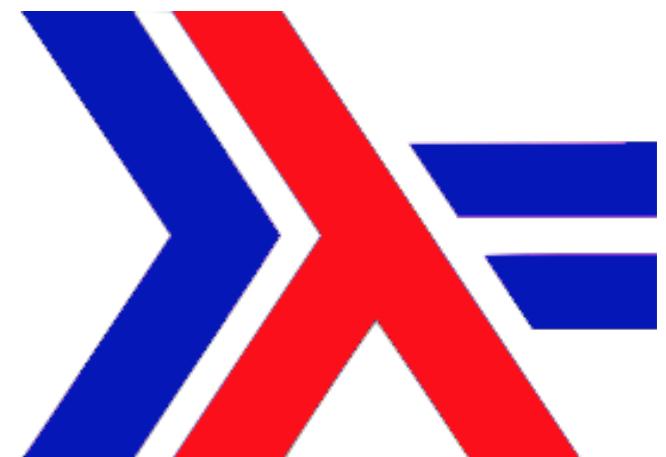


# Haskell

## Practical Programming Language

### Fast Memory Manipulation with C wrappers

#### Allowing overread bugs



# The Heartbleed Bug



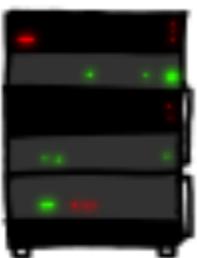
Buffer overread in OpenSSL. 2015

# HOW THE HEARTBLEED BUG WORKS:

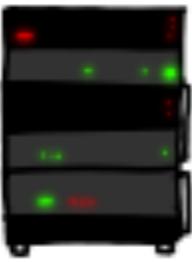
SERVER, ARE YOU STILL THERE?  
IF SO, REPLY "POTATO" (6 LETTERS).



User Eric wants pages about "boats". User Erica requests secure connection using key "4538538374224". User Meg wants these 6 letters: POTATO. User Ada wants pages about "irl games". Unlocking secure records with master key 5130985733435. Macie (chrome user) sends this message: "H



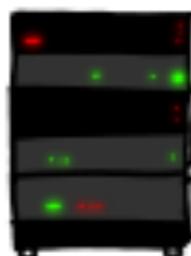
POTATO



SERVER, ARE YOU STILL THERE?  
IF SO, REPLY "BIRD" (4 LETTERS).



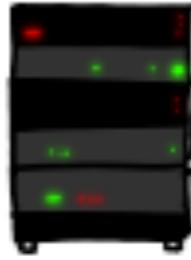
User Olivia from London wants pages about "new bees in car why". Note: Files for IP 375.381. 283.17 are in /tmp/files-3843. User Meg wants these 4 letters: BIRD. There are currently 348 connections open. User Brendan uploaded the file selfie.jpg (contents: 834ba962e2ceb9ff89bd3bfff84)



HMM...



BIRD



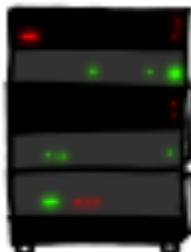
SERVER, ARE YOU STILL THERE?

a connection. Jake requested pictures of deer. User Meg wants these 500 letters: HAT. Lucas

SERVER, ARE YOU STILL THERE?  
IF SO, REPLY "HAT" (500 LETTERS).

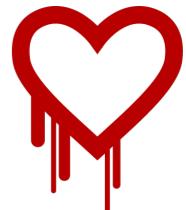
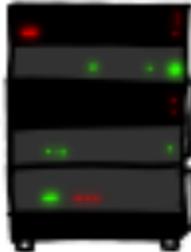


a connection. Jake requested pictures of deer.  
User Meg wants these 500 letters: HAT. Lucas  
requests the "missed connections" page. Eve  
(administrator) wants to set server's master  
key to "14835038534". Isabel wants pages about  
"snakes but not too long". User Karen wants to  
change account password to "CoHoBaSt". User



HAT. Lucas requests the "missed connections" page. Eve (administrator) wants to set server's master key to "14835038534". Isabel wants pages about "snakes but not too long". User Karen wants to change account password to "CoHoBaSt". User

a connection. Jake requested pictures of deer.  
User Meg wants these 500 letters: HAT. Lucas  
requests the "missed connections" page. Eve  
(administrator) wants to set server's master  
key to "14835038534". Isabel wants pages about  
"snakes but not too long". User Karen wants to  
change account password to "CoHoBaSt". User





in



```
module Data.Text where
take :: t:Text -> i:Int -> Text
```

```
> take "hat" 500
> *** Exception: Out Of Bounds!
```

# Runtime Checks

```
take :: t:Text -> i:Int -> Text
take t i | i < len t
  = Unsafe.take t i
take t i
  = error "Out Of Bounds!"
```

**Safe, but slow**

# No Checks

```
take :: t:Text -> i:Int -> Text
take t i | i < len t
          = Unsafe.take t i
take t i
error "Out Of Bounds!"
```

**Fast, but unsafe!**

# No Checks

```
take :: t:Text -> i:Int -> Text
take t i | i < len t
          = Unsafe.take t i
take t i
error "Out Of Bounds!"
```

Overread

```
> take "hat" 500
> "hat\58456\2594\SOH\NUL..."
```

# Static Checks

```
take :: t:Text -> i:Int -> Text
take t i | i < len t
          = Unsafe.take t i
take t i
          = error "Out Of Bounds!"
```

# Static Checks

```
take :: t:Text -> i:{i < len t} -> Text
take t i | i < len t
  = Unsafe.take t i
take t i
  = error "Out Of Bounds!"
```

# Static Checks

```
take :: t:Text -> i:{i < len t} -> Text
take t i | i < len t
= Unsafe.take t i
take t i
= error "Out Of Bounds!"
```

# Static Checks

```
take :: t:Text -> i:{i < len t} -> Text
take t i
= Unsafe.take t i
```

# Static Checks

```
take :: t:Text -> i:{i < len t} -> Text
take t i
= Unsafe.take t i
```

```
> take "hat" 500
```

Type Error



LiquidHaskell

# Refinement Types



**Checks valid arguments, under facts.**

# Checks valid arguments, under facts.

```
take :: t:Text -> {v | v < len t} -> Text
heartbleed = let x = "hat"
            in take x 500
```

len x = 3 => v = 500 => v < len x

# Checks valid arguments, under facts.

```
take :: t:Text -> {v | v < len t} -> Text
heartbleed = let x = "hat"
            in take x 500
```

len x = 3 => v = 500 => v < len x

# **Checks valid arguments, under facts.**

```
take :: t:Text -> {v | v < len t} -> Text
```

```
heartbleed = let x = "hat"  
           in take x 500
```

len x = 3 => v = 500 => v < len x

# **Checks valid arguments, under facts.**

```
take :: t:Text -> {v | v < len t} -> Text
```

```
heartbleed = let x = "hat"  
           in take x 500
```

len x = 3 => v = 500 => v < len x

# **Checks valid arguments, under facts.**

```
take :: t:Text -> {v | v < len t} -> Text  
heartbleed = let x = "hat"  
           in take x 500
```

len x = 3 => v = 500 => v < len x

# Checks valid arguments, under facts.

```
take :: t:Text -> {v | v < len t} -> Text
heartbleed = let x = "hat"
             in take x 500
```

```
len x = 3 => v = 500 => v < len x
```

# Checks valid arguments, under facts.

```
take :: t:Text -> {v | v < len t} -> Text  
heartbleed = let x = "hat"  
            in take x 500
```

SMT-  
query

len x = 3 => v = 500 => v < len x

# Checks valid arguments, under facts.

```
take :: t:Text -> {v | v < len t} -> Text
heartbleed = let x = "hat"
            in take x 500
```

SMT-  
invalid

len x = 3 => v = 500 => v < len x

# Checks valid arguments, under facts.

```
take :: t:Text -> {v | v < len t} -> Text
heartbleed = let x = "hat"
            in take x 500
```

Checker reports **Error**

len x = 3 => v = 500 => v < len x

# Checks valid arguments, under facts.

```
take :: t:Text -> {v | v < len t} -> Text
```

```
heartbleed = let x = "hat"
```

```
in take x 500
```

Checker reports **Error**

len x = 3 => v = 500 => v < len x

# Checks valid arguments, under facts.

```
take :: t:Text -> {v | v < len t} -> Text
```

```
heartbleed = let x = "hat"  
           in take x 2
```

Checker reports **OK**

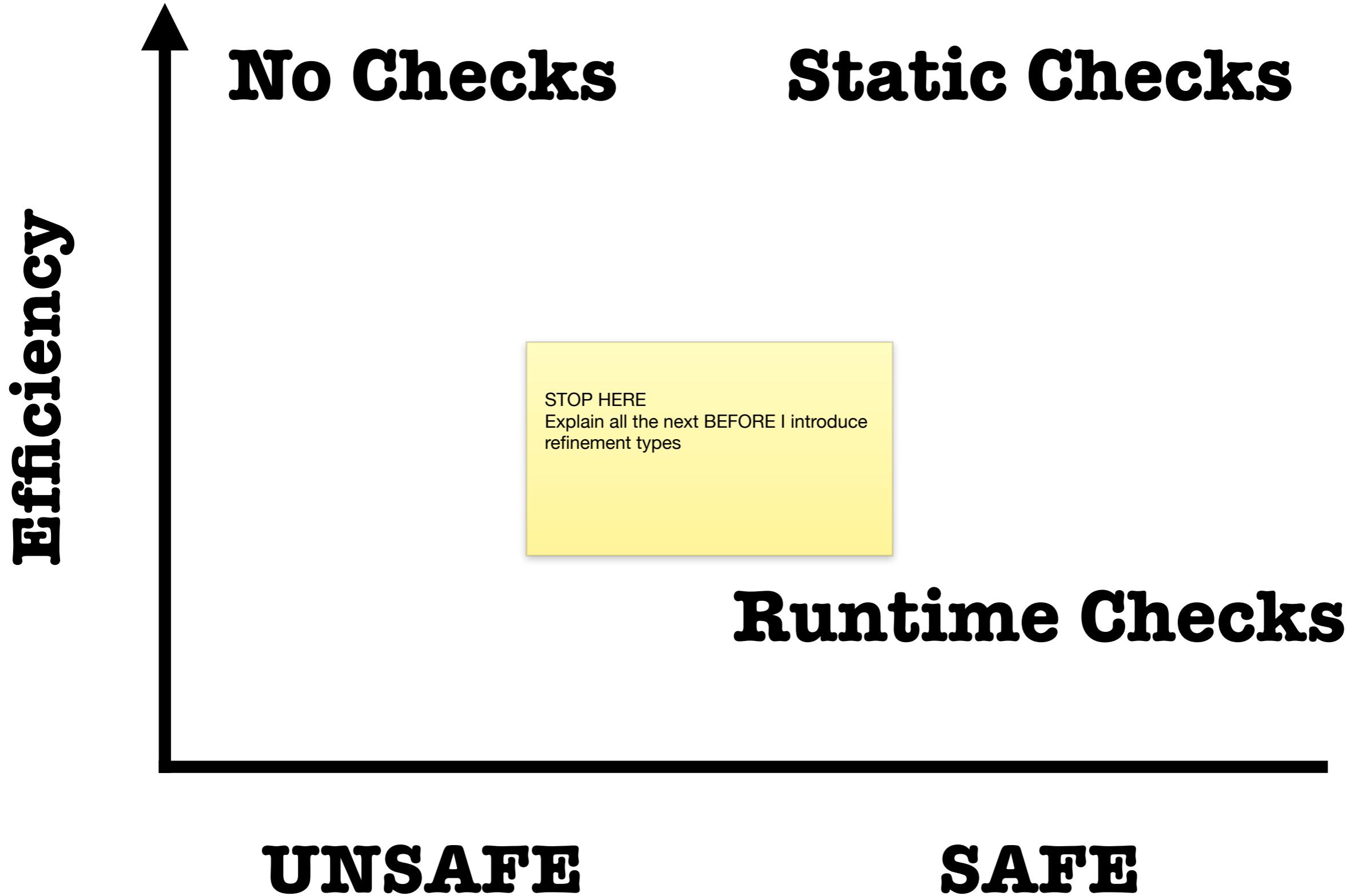
SMT-  
valid

len x = 3 => v = 2 => v < len x



**Checks valid arguments, under facts.**

**Static Checks**





**LiquidHaskell**

**Static Checks**

**Safe & Fast Code!**

**Static Checks**

**Safe & Fast Code!**

**Application: Speed up Parsing**

# **Application: Speed up Parsing**

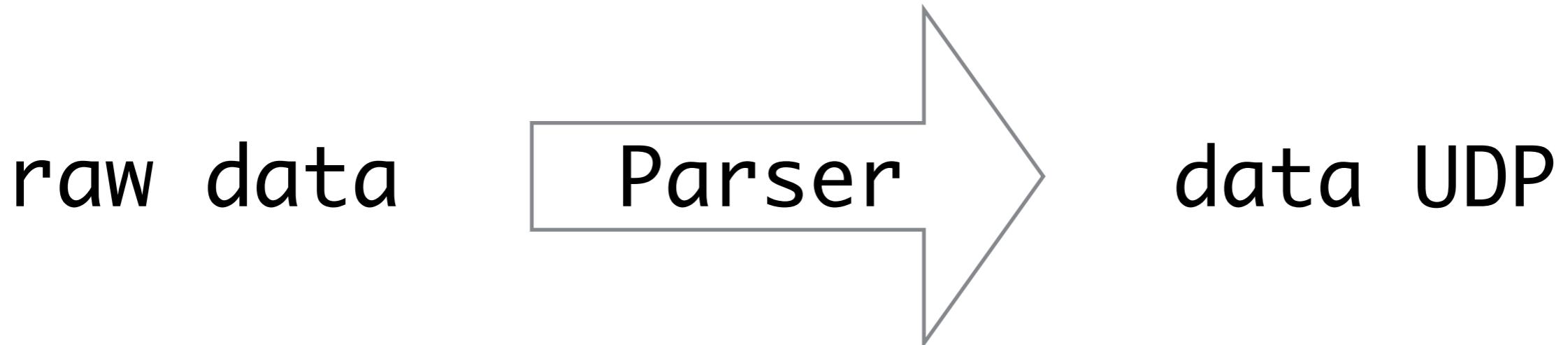
Simplified application of Liquid Haskell

by Gabriel Gonzalez



# **Application: Speed up Parsing**

## **UDP:User Datagram Protocol**



# Application: Speed up Parsing

```
data UDP = UDP
  { udpSrcPort :: Text -- 2 chars
  , udpDestPort :: Text -- 2 chars
  , udpLength :: Text -- 2 chars
  , udpChecksum :: Text -- 2 chars
  }
```

# Application: Speed up Parsing

```
udpP :: Text -> UDP
udpP bs =
  let (udp1, bs1) = splitAt 2 bs
  let (udp2, bs2) = splitAt 2 bs1
  let (udp3, bs3) = splitAt 2 bs2
  let (udp4, bs4) = splitAt 2 bs3
in UDP (udp1 upd2 udp3 upd4)
```

Safe but Slow (4 runtime checks)

Solution: Merge checks

# Application: Speed up Parsing

```
udpP :: Text -> Maybe UDP
udpP bs =
  if length bs >= 8 then
    let (udp1, bs1) = US.splitAt 2 bs
    let (udp2, bs2) = US.splitAt 2 bs1
    let (udp3, bs3) = US.splitAt 2 bs2
    let (udp4, bs4) = US.splitAt 2 bs3
    in Just (UDP udp1 udp2 udp3 udp4)
  else Nothing
```

Safe and Fast (1 runtime check!)

# Application: Speed up Parsing

```
udpP :: Text -> Maybe UDP
udpP bs =
  if length bs >= 8 then
    let (udp1, bs1) = US.splitAt 2 bs
    let (udp2, bs2) = US.splitAt 2 bs1
    let (udp3, bs3) = US.splitAt 4 bs2
    let (udp4, bs4) = US.splitAt 2 bs3
    in Just (UDP udp1 upd2 upd3 upd4)
  else Nothing
```

Safe and Fast, but error prone

# Application: Speed up Parsing

```
udpP :: Text -> Maybe UDP
udpP bs =
  if length bs >= 8 then
    let (udp1, bs1) = US.splitAt 2 bs
      in Just (UDP udp1 upd2 upd3 upd4)
  else Nothing

splitAt :: i:Int -> t:{i < len t} ->
(tl:{i = len tl}, tr:{len tr = len t - i})
```

Enforce Static Checks!

# Application: Speed up Parsing

```
udpP :: Text -> Maybe UDP
```

```
udpP bs =  
  if length bs >= 8 then  
    let (udp1, bs1) = US.splitAt 2 bs0  
    let (udp2, bs2) = US.splitAt 2 bs1  
    let (udp3, bs3) = US.splitAt 4 bs2  
    let (udp4, bs4) = US.splitAt 2 bs3  
    in Just (UDP udp1 upd2 upd3 upd4)  
  else Nothing
```

Error

Enforce Static Checks!

# Application: Speed up Parsing

OK

```
udpP :: Text -> Maybe UDP
udpP bs =
  if length bs >= 8 then
    let (udp1, bs1) = US.splitAt 2 bs
    let (udp2, bs2) = US.splitAt 2 bs
    let (udp3, bs3) = US.splitAt 2 bs
    let (udp4, bs4) = US.splitAt 2 bs
    in Just (UDP udp1 upd2 upd3 upd4)
  else Nothing
```

Haskell code!  
- syntax  
- compiler

No proofs!  
- SMT automated!

Provably Correct & Faster (x6) Code!

# Application: Speed up Parsing

```
udpP :: Text -> Maybe UDP
udpP bs =
  if length bs >= 8 then
    let (udp1, bs1) = US.splitAt 2 bs
    let (udp2, bs2) = US.splitAt 2 bs1
    let (udp3, bs3) = US.splitAt 2 bs2
    let (udp4, bs4) = US.splitAt 2 bs3
    in Just (UDP udp1 upd2 upd3 upd4)
  else Nothing
```

Provably Correct & Faster (x6) Code!  
Haskell Code: Verification with SMT



# LiquidHaskell

Provably Correct & Faster (x6) Code!

Haskell Code: Verification with SMT



AWAKE

# Verification with SMT

If p is safe indexing

```
{t:Text | i < len t }
```

# Verification with SMT

If  $p$  from decidable theories

$$\{t : a \mid p\}$$

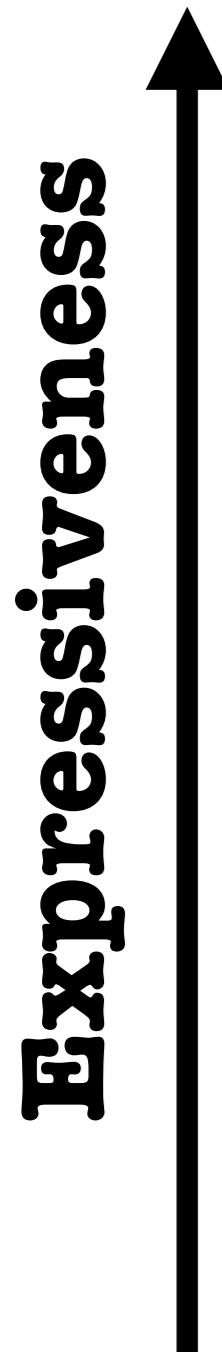
Boolean Logic

(QF) Linear Arithmetic

Uninterpreted Functions ...

What other properties can we express?

# Verification with SMT



**Critical Properties (Goal):**

“The plane will not crash!”

**Math Theorems (POPL’18):**

“If  $f(x) < f(x+1)$ , then  $f$  is monotonic”

**Safe Indexing (Haskell’14):**

“Your passwords are safe!”

# **Verification with SMT**

**Refinement Reflection, POPL'18**

**for Theorem Proving in Haskell!**

“If  $f(x) < f(x+1)$ , then  $f$  is monotonic”

# Fibonacci in Haskell

```
fib :: i:{Int | 0≤i} -> {v:Int | 0<v ∧ i≤v}
fib i
| i≤1          = 1
| otherwise     = fib (i-1) + fib (i-2)
```

# Fibonacci in Haskell

```
fib :: i:{Int | 0≤i} -> {v:Int | 0<v ∧ i≤v}
fib i
| i≤1          = 1
| otherwise     = fib (i-1) + fib (i-2)
```

How to express **theorems** about functions?

\forall i.  $0 \leq i \Rightarrow \text{fib } i \leq \text{fib } (i+1)$

# How to express **theorems** about functions?

## **Step 1:** Definition

In SMT **fib** is “Uninterpreted Function”

\forall i j. i = j => fib i = fib j

How to connect logic **fib** with target **fib**?

# How to connect logic fib with target fib?

```
fib :: i:{Int | 0≤i} -> {v:Int | 0<v∧i≤v}
fib i
| i≤1          = 1
| otherwise    = fib (i-1) + fib (i-2)
```

Not Decidable!

SMT Axiom

\forall i.

if  $i \leq 1$  then  $\text{fib } i = 1$   
else  $\text{fib } i = \text{fib } (i-1) + \text{fib } (i-2)$

# How to connect logic fib with target fib?

```
fib :: i:{Int | 0≤i} -> {v:Int | 0<v∧i≤v}
fib i
| i≤1          = 1
| otherwise = fib (i-1) + fib (i-2)
```

## Refinement Reflection

```
fib :: i:{Int | 0≤i} -> {v:Int | v=fib i ∧
  if i≤1 then fib i = 1
  else fib i = fib (i-1) + fib (i-2)
}
```

# Refinement Reflection

**Step 1:** Definition

**Step 2:** Reflection

```
fib :: i:{Int | 0≤i} -> {v:Int | v=fib i ∧
  if i≤1 then fib i = 1
  else fib i = fib (i-1) + fib (i-2)
}
```

# Refinement Reflection

## Step 1: Definition

## Step 2: Reflection

```
fib :: i:{Int | 0≤i} -> {v:Int | v=fib i ∧  
    if i≤1 then fib i = 1  
    else fib i = fib (i-1) + fib (i-2)  
}
```

## Step 3: Application

```
fib 0 :: {v:Int | v=fib 0 ∧ fib 0 = 1}
```

# Application is Type Level Computation

fib 0

fib 0 = 1

# Application      Type Level Computation

fib 0

fib 0 = 1

fib 1

fib 1 = 1

fib 2

fib 2 = fib 1 + fib 0

fib i

?

- ? if  $i \leq 1$  then fib i = 1
- ? else fib i = fib (i-1) + fib (i-2)

# Application      Type Level Computation

fib 0

fib 0 = 1

fib 1

fib 1 = 1

fib 2

fib 2 = fib 1 + fib 0

if 1 < i then

fib i

fib i = fib (i-1) + fib (i-2)

if  $i \leq 1$  then fib i = 1

else fib i = fib (i-1) + fib (i-2)

# Application      Type Level Computation

**fib 0**

**fib 0 = 1**

**fib 1**

**fib 1 = 1**

**fib 2**

**fib 2 = fib 1 + fib 0**

**if 1 < i then**

**fib i**

**fib i = fib (i-1) + fib (i-2)**

**fib (i+1)**

**fib (i+1) = fib i + fib (i-1)**

# Theorem Proving

```
fibUp :: i:Nat -> {fib i ≤ fib (i+1)}
fibUp i
| i == 0
= fib 0 <. fib 1
*** QED
| i == 1
= fib 1 <=. fib 1 + fib 0 <= fib 2
*** QED
| otherwise
= fib i
<=. fib i + fib (i-1)
<=. fib (i+1)
*** QED
```

# Reflection for Theorem Proving

**Theorems** are refinement types.

**Proofs** are functions.

**Check** that functions prove theorems.

**Proofs** are functions.

`fibUp :: i:Nat -> {fib i ≤ fib (i+1)}`

# Proofs are functions.

```
fibUp :: i:Nat -> {fib i ≤ fib (i+1)}
```

Let's call them!

```
fibUp 4 :: {fib 4 ≤ fib 5}
```

```
fibUp i :: {fib i ≤ fib (i+1)}
```

```
fibUp (j-1) :: {fib (j-1) ≤ fib j}
```

# Proofs are functions. Let's call them!

```
fibMono :: i:Nat -> j:{Nat | i < j}  
         -> {fib i ≤ fib j}
```

```
fibMono i j  
| i + 1 == j  
= fib i  
<=. fib (i+1) ? fibUp i  
==. fib j  
*** QED  
| otherwise  
= fib i  
<=. fib (j-1) ? fibMono i (j-1)  
<=. fib j      ? fibUp (j-1)  
*** QED
```

# Proofs are functions. Let's call them!

```
fibMono :: i:Nat -> j:{Nat | i < j}  
         -> {fib i ≤ fib j}
```

```
fibMono i j  
| i + 1 == j  
= fib i  
<=. fib (i+1) ? fibUp i  
==. fib j  
*** QED  
| otherwise  
= fib i  
<=. fib (j-1) ? fibMono i (j-1)  
<=. fib j      ? fibUp (j-1)  
*** QED
```

# Proofs are functions. Let's abstract them!

```
fibMono :: i:Nat -> j:{Nat | i < j}
          -> fib:(Nat -> Int)
          -> (k:Nat -> {fib k ≤ fib (k+1)})
          -> {fib i ≤ fib j}
```

```
fibMono i j fib fibUp
| i + 1 == j
= fib i
<=. fib (i+1) ? fibUp i
==. fib j
*** QED
| otherwise
= fib i
<=. fib (j-1) ? fibMono i (j-1)
<=. fib j      ? fibUp (j-1)
*** QED
```



LiquidHaskell

# Refinement Reflection for **Expressiveness**

 Liquid Haskell

# Refinement Reflection for **Expressiveness**

Application (Haskell'17):  
String Matching Parallelization

# Refinement Reflection for **Expressiveness**

Idea:

Encode HO specs in FO SMT decidable logic

Metatheory:

THEOREM 4.1. [Soundness of  $\lambda^R$  ]

- **Denotations** If  $\Gamma; R \vdash p : \tau$  then  $\forall \theta \in [\![\Gamma]\!]. \theta \cdot p \in [\![\theta \cdot \tau]\!]$ .
- **Preservation** If  $\emptyset; \emptyset \vdash p : \tau$  and  $p \hookrightarrow^* w$ , then  $\emptyset; \emptyset \vdash w : \tau$ .

## E PROOF OF SOUNDNESS

We prove Theorem 4.1 of § D by reduction to Soundness of  $\lambda^U$  [Vazou et al. 2014a].

**THEOREM E.1.** [Denotations] If  $\Gamma \vdash p : \tau$  then  $\forall \theta \in [\Gamma]. \theta \cdot p \in [\theta \cdot \tau]$ .

**PROOF.** We use the proof from [Vazou et al. 2014b] and specifically Lemma 4 that is identical to the statement we need to prove. Since the proof proceeds by induction in the type derivation, we need to ensure that all the modified rules satisfy the statement.

- T-EXACT Assume  $\Gamma \vdash e : \{v : B \mid \{r\} \wedge v = e\}$ . By inversion  $\Gamma \vdash e : \{v : B \mid \{r\}\}$ (1). By (1) and IH we get  $\forall \theta \in [\Gamma]. \theta \cdot e \in [\theta \cdot \{v : B \mid \{r\}\}]$ . We fix a  $\theta \in [\Gamma]$ . We get that if  $\theta \cdot e \hookrightarrow^* w$ , then  $\theta \cdot \{r\} \hookrightarrow^* \text{True}$ . By the Definition of  $=$  we get that  $w = w \hookrightarrow^* \text{True}$ . Since  $\theta \cdot (v = e) \vdash v = e$ , we have  $\theta \cdot e \in [\theta \cdot \{v : B \mid \{r\} \wedge v = e\}]$ .
- T-LET Assume  $\Gamma \vdash \text{let } rec \tau \text{ in } e \text{ end} : \tau$  (2), and  $\Gamma \vdash \tau$  (3). By IH we get  $\forall \theta \in [\Gamma]. \theta \cdot \tau \in [\theta \cdot \tau]$  (2'). By (1') and by the type derivation rule T-LET we get  $\forall \theta \in [\Gamma]. \theta \cdot p \in [\theta \cdot \{v : B \mid \{r\} \wedge v = e\}]$  (3').
- T-REFL Assume  $\Gamma \vdash \text{refl } e : \tau$ . By IH,  $\forall \theta \in [\Gamma]. \theta \cdot e \in [\theta \cdot \tau]$ . Since type derivations are closed under evaluation, we get  $\forall \theta \in [\Gamma]. \theta \cdot p \in [\theta \cdot \tau]$ .
- T-FIX In Theorem 8.3 from [Wadler and Paolini 2004]) we prove that  $\forall \theta \in [\Gamma]. \theta \cdot p \in [\theta \cdot \tau]$ .

$\Gamma \vdash e \rightsquigarrow p$

sort Fun  $s_x s$ ,  
action of sort

# Refinement Reflection, POPL'18

by **Vazou**, Tondwalkar, Choudhury, Scott, Newton, Wadler, and Jhala

**THEOREM E.2.** [Preservation] If  $\emptyset \vdash p : \tau$  and  $p \hookrightarrow^* w$  then  $\emptyset \vdash w : \tau$ .

**PROOF.** In [Vazou et al. 2014b] proof proceeds by iterative application of Type Preservation Lemma 7. Thus, it suffices to ensure Type Preservation in  $\lambda^R$ , which is true by the following Lemma.  $\square$

**LEMMA E.3.** If  $\emptyset \vdash p : \tau$  and  $p \hookrightarrow^* p'$  then  $\emptyset \vdash p' : \tau$ .

**PROOF.** Since Type Preservation in  $\lambda^U$  is proved by induction on the type derivation tree, we need to ensure that all the modified rules satisfy the statement.

- T-EXACT Assume  $\emptyset \vdash p : \{v : B \mid \{r\} \wedge v = p\}$ . By inversion  $\emptyset \vdash p : \{v : B \mid \{r\}\}$ . By IH we get  $\emptyset \vdash p' : \{v : B \mid \{r\}\}$ . By rule T-EXACT we get  $\emptyset \vdash p' : \{v : B \mid \{r\} \wedge v = p'\}$ . Since subtyping is closed under evaluation, we get  $\emptyset \vdash \{v : B \mid \{r\} \wedge v = p'\} \leq \{v : B \mid \{r\} \wedge v = p\}$ . By rule T-SUB we get  $\emptyset \vdash p' : \{v : B \mid \{r\} \wedge v = p\}$ .

By 25, the above set is not empty, and hence  $\tau$  is valid under  $d$ .  $\square$

**Example: Fibonacci is increasing** In § 2 we verified that under a definition  $d$  that includes fib, the term fibUp proves

$$n : \text{Nat} \rightarrow \{\text{fib } n \leq \text{fib } (n + 1)\}$$

Thus, by Theorem D.3 we get

$$\forall n. 0 \leq n \hookrightarrow^* \text{True} \Rightarrow \text{fib } n \leq \text{fib } (n + 1) \hookrightarrow^* \text{True}$$

for all assignments  $\sigma \models p$ .

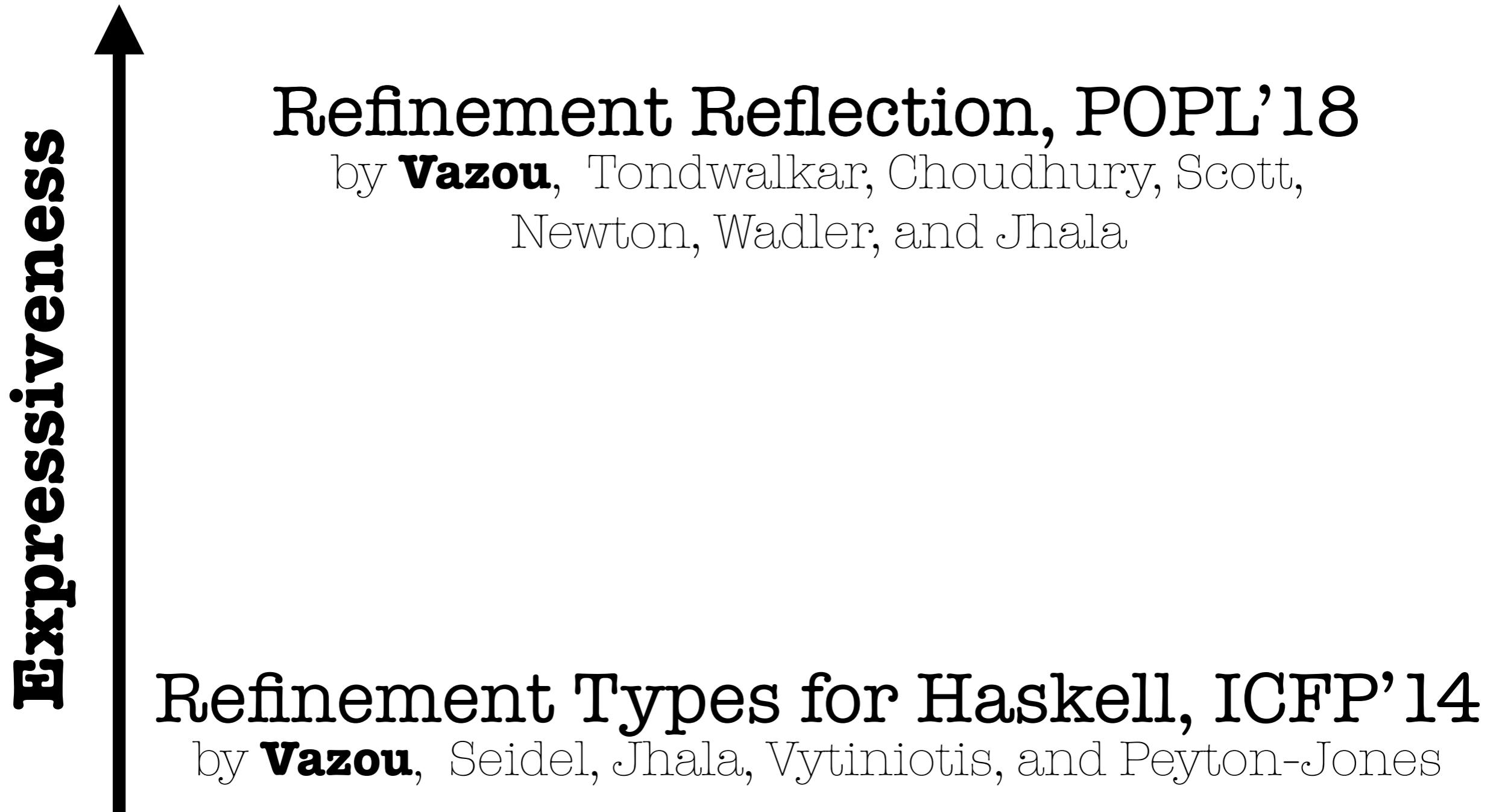
**Embedding Functions** As  $\lambda^o$  is a first-order logic, we embed  $\lambda$ -abstraction and application using the uninterpreted functions lam and app. We embed  $\lambda$ -abstractions using lam as shown in

**COROLLARY E.3.** If  $\Gamma \vdash e : \text{Bool}$ ,  $e$  reduces to a value and  $\Gamma \vdash e \rightsquigarrow p$ , then for every  $\theta \in [\Gamma]$  and every  $\sigma \in \theta^\perp$ ,  $\theta^\perp \cdot e \hookrightarrow^* \text{True}$  iff  $\sigma^\beta \models p$ .

referring to the proofs in [Vazou et al. 2014b].

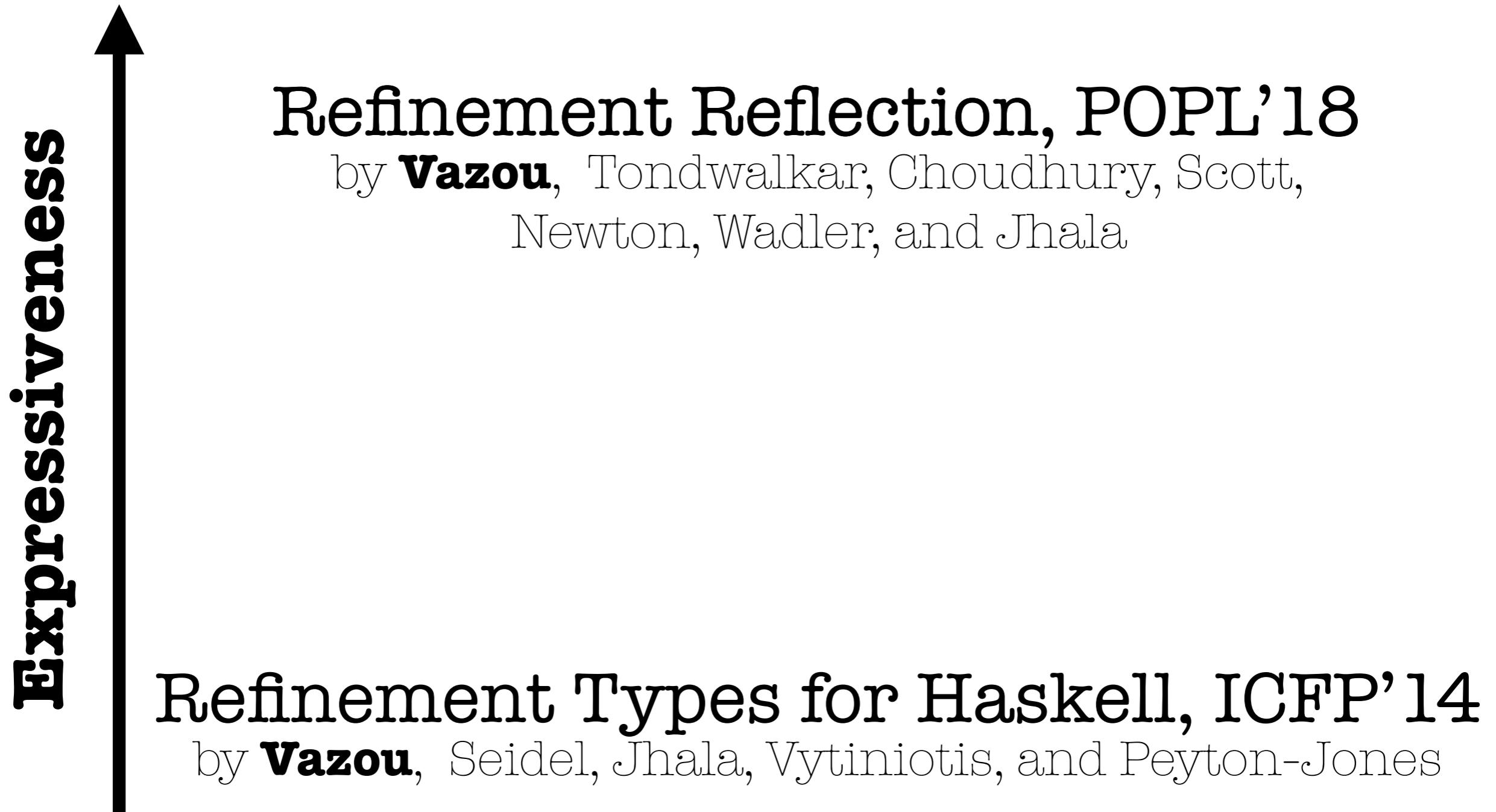


# Liquid Haskell on papers



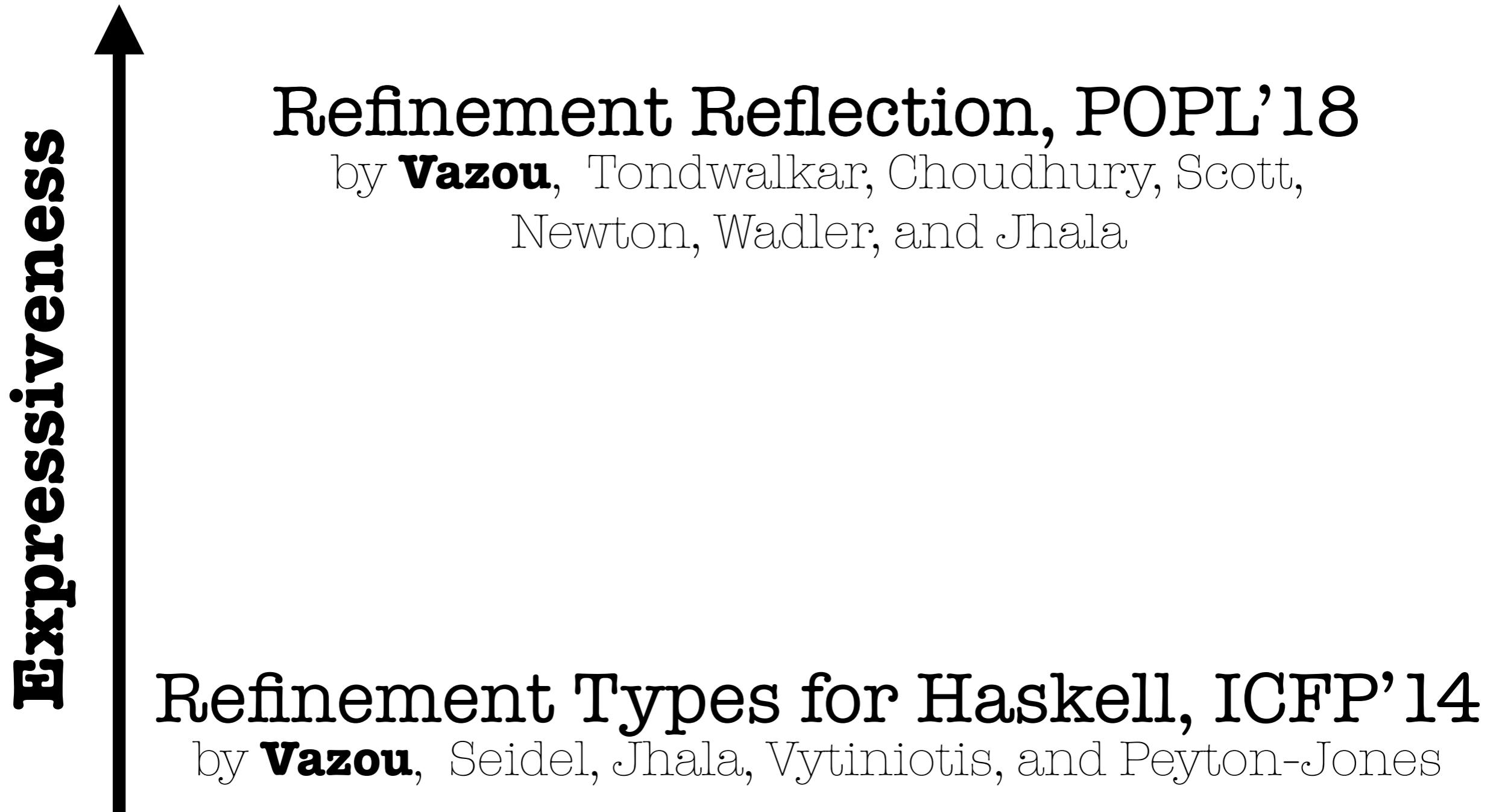


# Liquid Haskell on papers



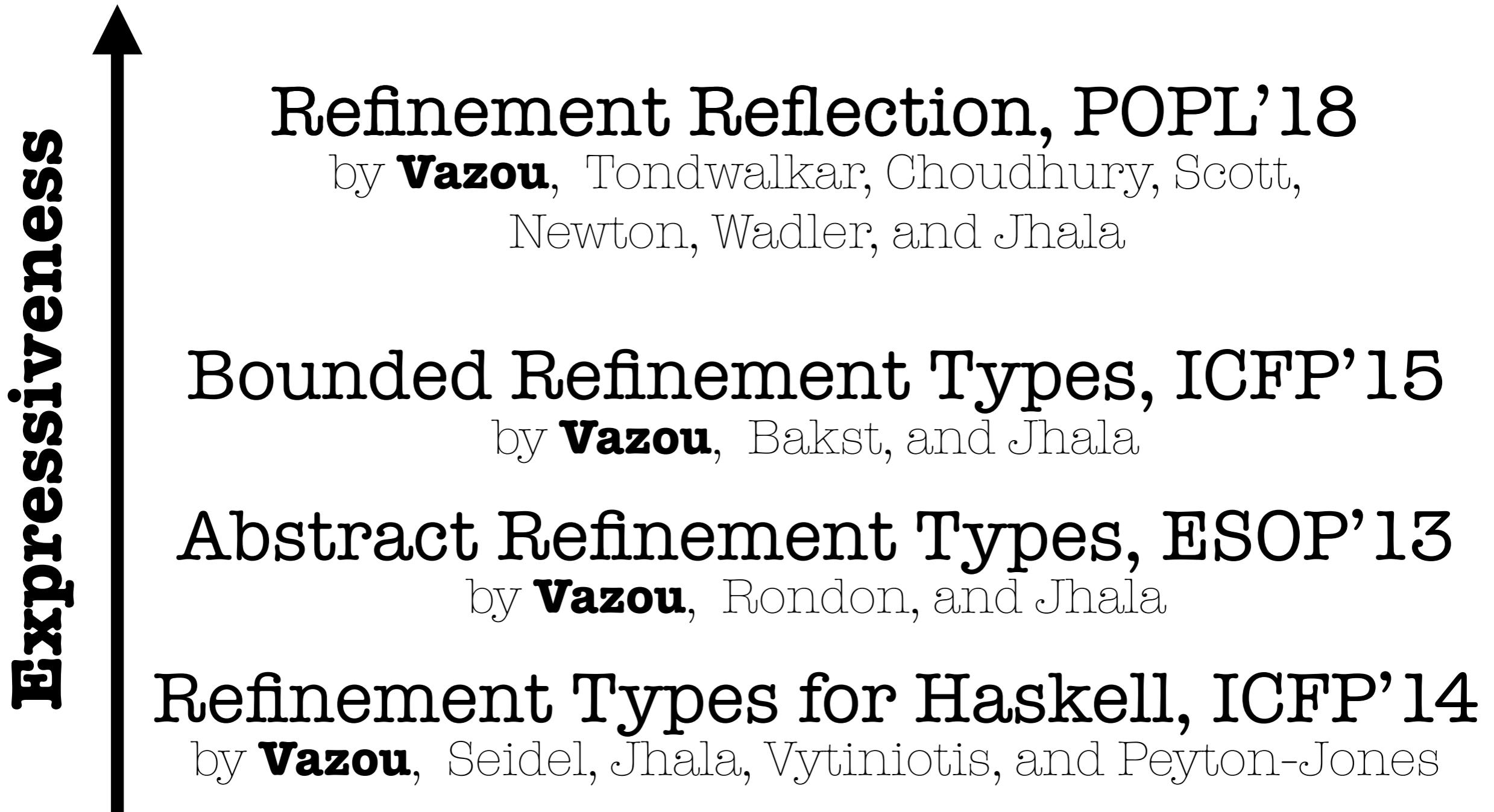


# Liquid Haskell on papers





# Liquid Haskell on papers



# Liquid Haskell on github

ucsd-progsys / liquidhaskell

Unwatch 22 Star 473 Fork 75

Code Issues 201 Pull requests 5 Projects 0 Wiki Insights Settings

Liquid Types For Haskell Edit

Add topics

8,382 commits 94 branches 19 releases 38 contributors

Branch: develop New pull request Create new file Upload files Find file Clone or download

nikivazou Merge pull request #1223 from ucsd-progsys/HaskellFunInRefs ... Latest commit 82f5baa 5 days ago

benchmarks move tests into pos a month ago

devel Fix travis error 6 days ago

# Liquid Haskell on github

Jan 15, 2012 – Jan 25, 2018

Contributions: Commits ▾



[ranjitjhala](#)

3,093 commits 474,271 ++ 304,536 --

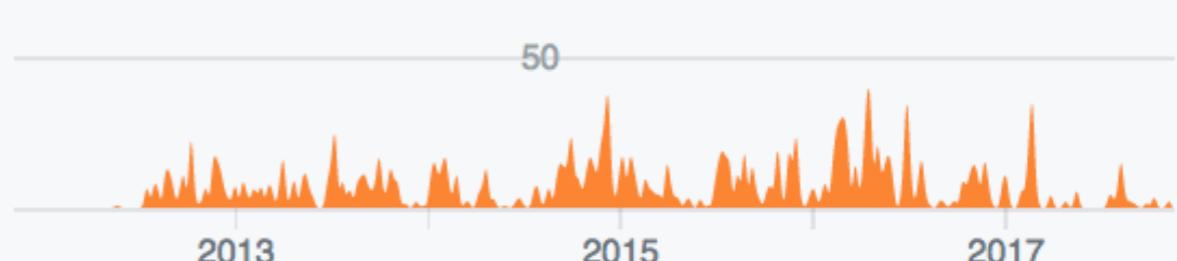
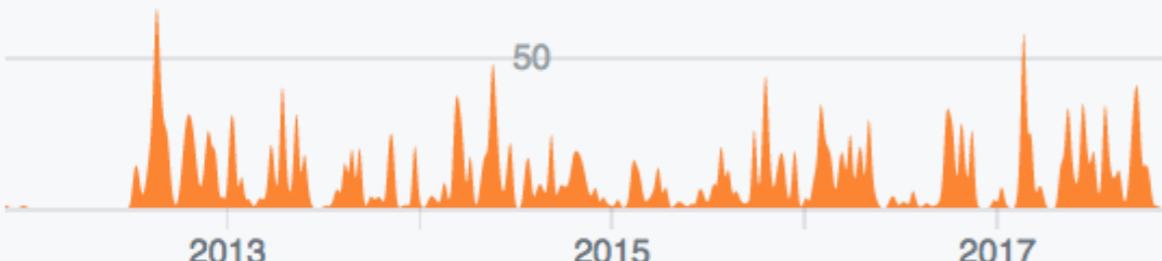
#1



[nikivazou](#)

2,113 commits 358,364 ++ 294,962 --

#2



[gridaphobe](#)

814 commits 114,731 ++ 79,008 --

#3



[spinda](#)

155 commits 7,430 ++ 5,350 --

#4

# Liquid Haskell dev team



Niki Vazou & Ranjt Jhala,  
Liquid Haskell dev team

# Liquid Haskell in the real world

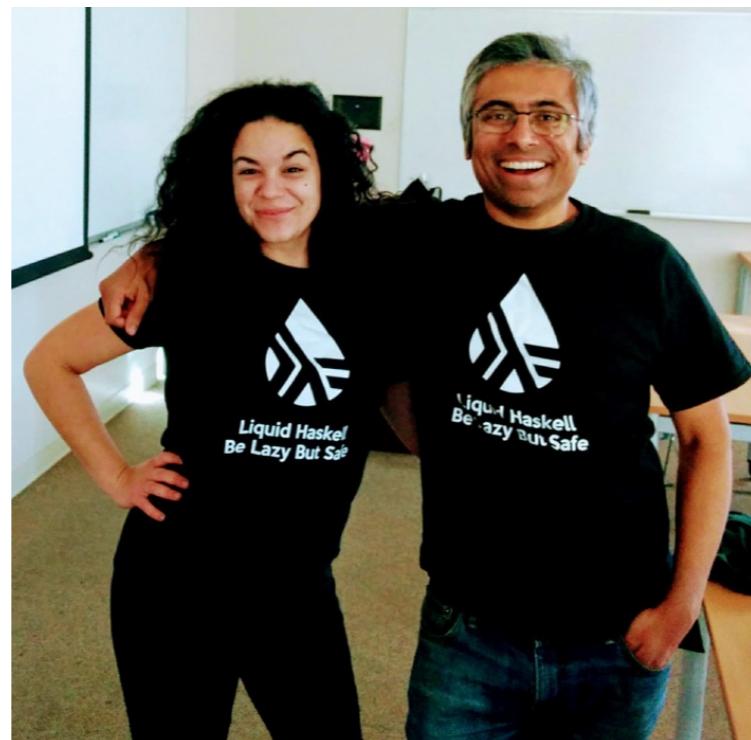
## Education



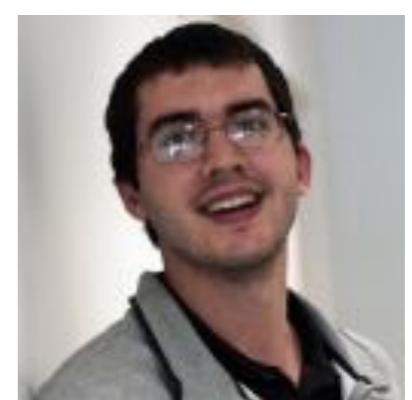
Will Kunkel,  
undergrad @UMD



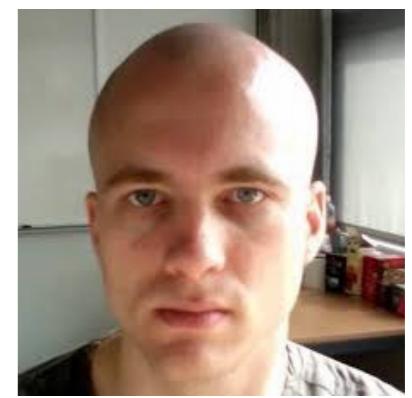
Rachel Xu & Xinyue Zhang,  
undergrads @Bryn Mawr College



Niki Vazou & Ranjt Jhala,  
Liquid Haskell dev team



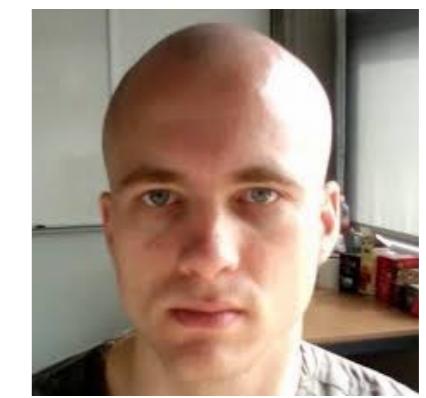
Gabriel Gonzalez  
Awake Security



Edsko de Vries  
Well-Typed



Gabriel Gonzalez  
Awake Security



Edsko de Vries  
Well-Typed

# Liquid Haskell in Education

This is Will Kunkel.

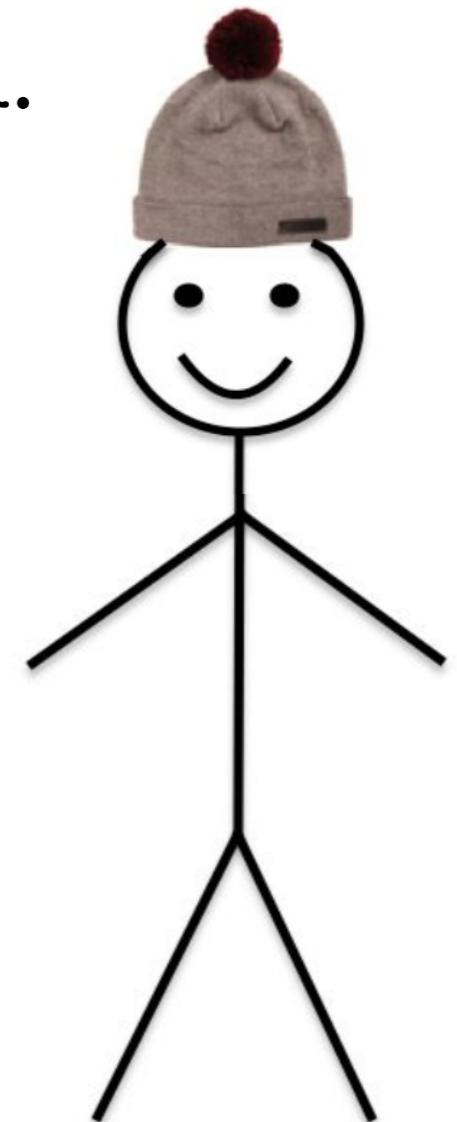
Will took my undergrad course on Haskell.

Will learnt Liquid Haskell in 2 weeks.

Will was **3rd** in POPL'18 **Student Research Competition** with his project “Comparing Liquid Haskell and Coq”

Will is smart.

Be like Will.



# Liquid Haskell in Education

Two winners in POPL'18 Student Research Competition



“Comparing Liquid Haskell and Coq”



Will Kunkel,  
undergrad @UMD



“Comparing Dependent Haskell,  
Liquid Haskell and F\*”



Rachel Xu & Xinyue Zhang,  
undergrads @Bryn Mawr College

# Liquid Haskell in Education

Two winners in POPL'18 Student Research Competition



“Comparing Liquid Haskell and Coq”



Will Kunkel,  
undergrad @UMD



“Comparing Dependent Haskell,  
Liquid Haskell and F\*”



Rachel Xu & Xinyue Zhang,  
undergrads @Bryn Mawr College



# Liquid Haskell in the real world

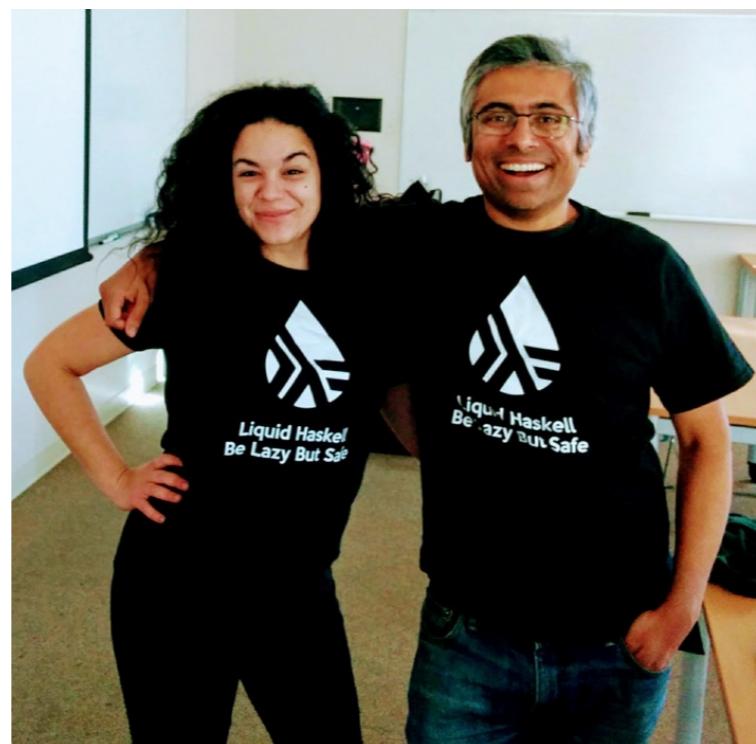
## Education



Will Kunkel,  
undergrad @UMD



Rachel Xu & Xinyue Zhang,  
undergrads @Bryn Mawr College



Niki Vazou & Ranjt Jhala,  
Liquid Haskell dev team



Gabriel Gonzalez  
Awake Security



Edsko de Vries  
Well-Typed



# Liquid Haskell in Industry

Gabriel Gonzalez



Static checks during parsing.

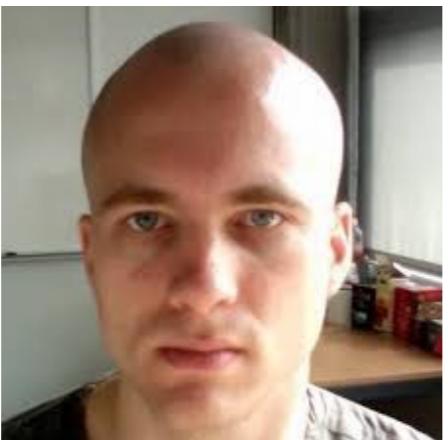
Provably Correct & Faster (x6) Code!

Huge speedup for internet traffic parsing.



# Liquid Haskell in Industry

Gabriel Gonzalez



Edsko de Vries





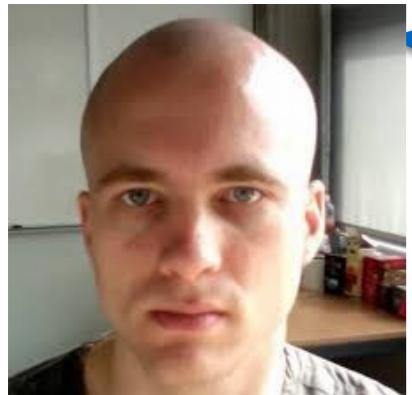
I am a Haskell consultant at a  
**cryptocurrency/blockchain** company.  
We have a blockchain algorithm written  
**in paper & a Haskell implementation.**  
We want Liquid Haskell to connect them.



I am a Haskell consultant at a  
**cryptocurrency/blockchain** company.  
We have a blockchain algorithm written  
**in paper** & a **Haskell implementation**.  
We want Liquid Haskell to connect them.

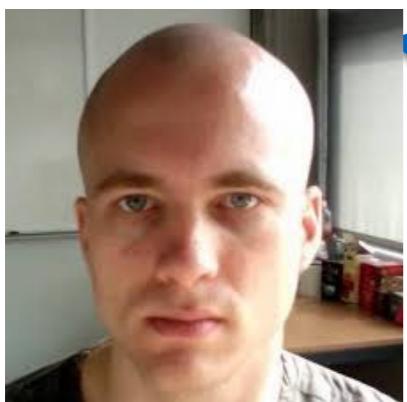
Awesome! Lmk if you need anything!





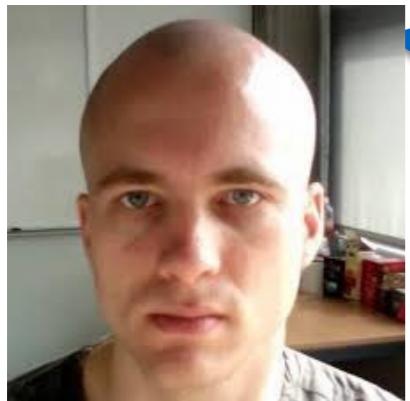
I am a Haskell consultant at a  
**cryptocurrency/blockchain** company.  
We have a blockchain algorithm written  
**in paper** & a **Haskell implementation**.  
We want Liquid Haskell to connect them.

Awesome! Lmk if you need anything!



I want **interactive proof generation**!

# More user suggestions



Edsko de Vries  
industrial rep.

I want **interactive proof generation!**



Richard Eisenberg  
ghc devs rep.

Can we use Liquid Haskell proofs for  
**compiler optimizations?**



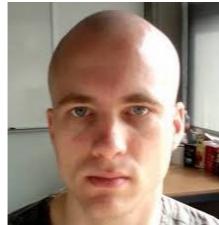
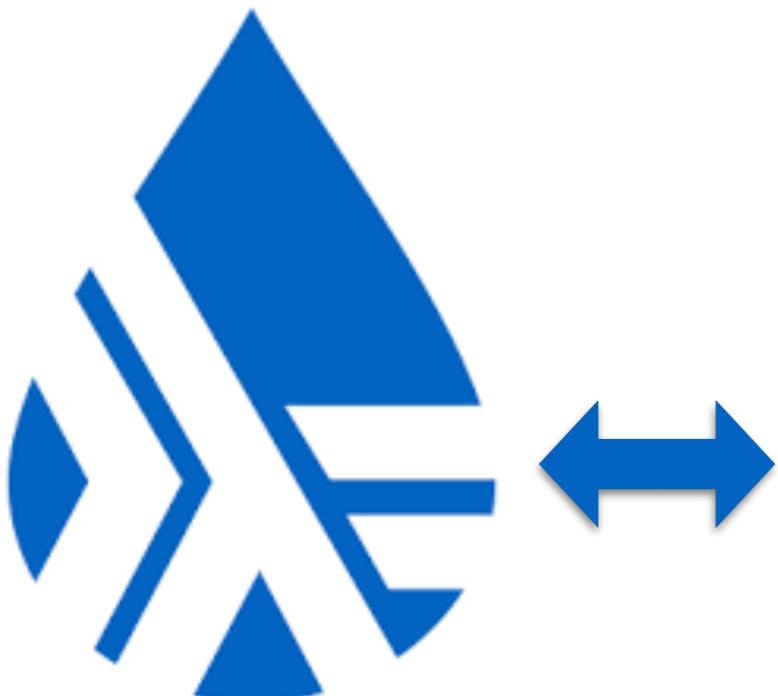
Leo Lambropoulos  
Coq rep.

I do not trust it! Liquid Haskell should  
generate **proof certificates!**

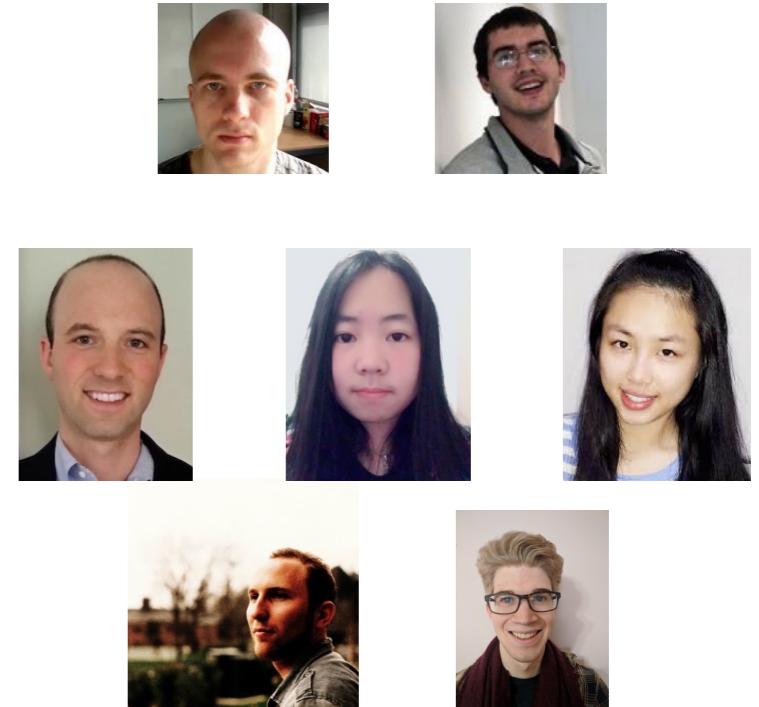


# Liquid Haskell has many users

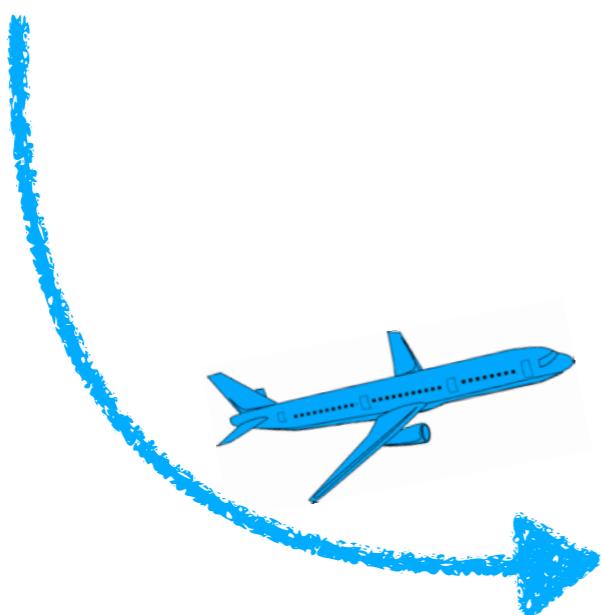
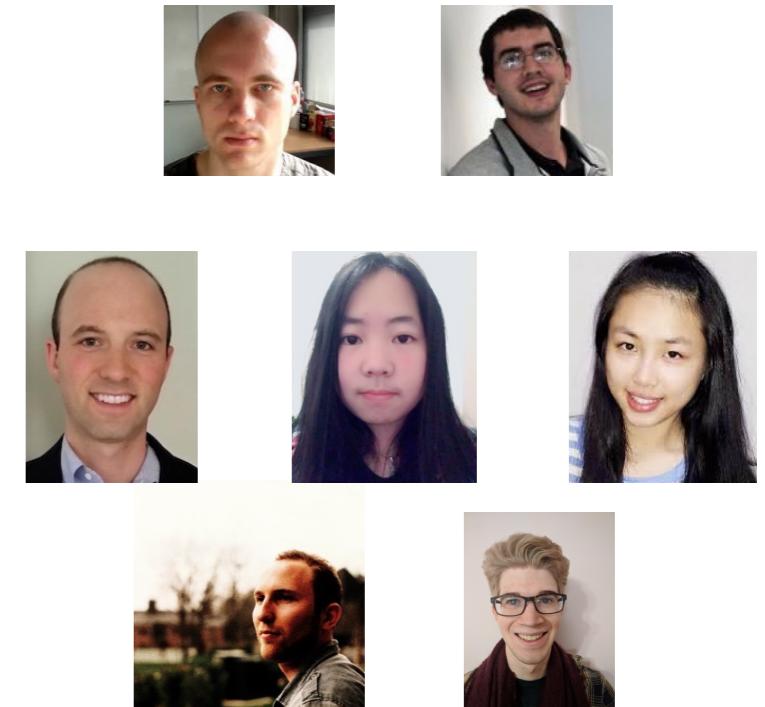
7,765 downloads



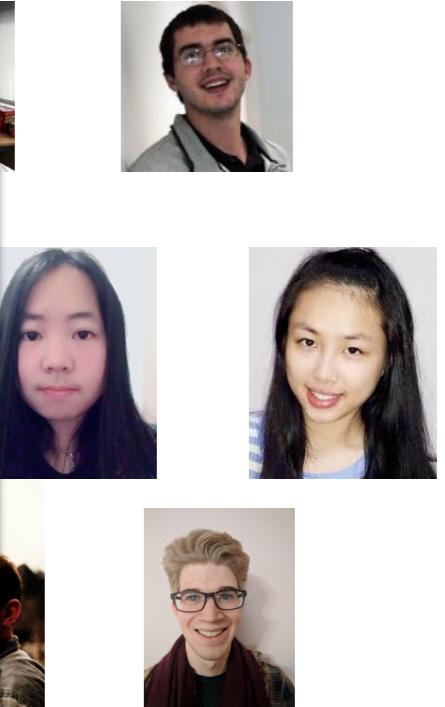
# many users, but two main devs



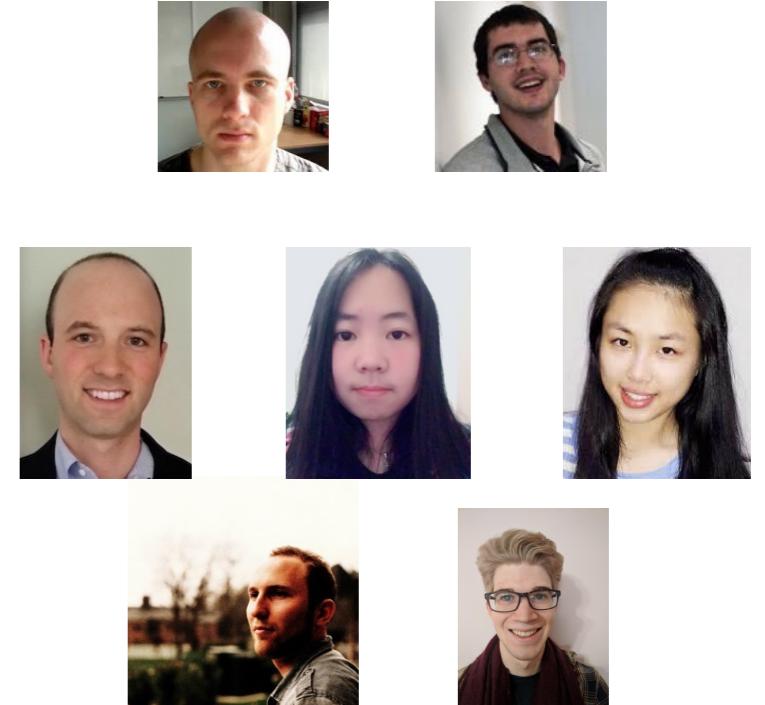
# many users, but two main devs



# many users, but two main devs



# many users, but two main devs



## Goal: Expand the Liquid Haskell Team

# **Future work in Liquid Haskell**

I. Proof Assistance

II. Compiler Interaction

III. Real-world applications

# I. Proof Assistance

**Goal:** Coq-like IDE

for case splitting, sub-goal detection

# I. Proof Assistance

**Idea:** Proofs are Haskell programs

Program Synthesis for Proof Generation

Error Reporting for Failure Diagnosis

# I. Proof Assistance

**Idea:** Proofs are Haskell programs

Program Synthesis for Proof Generation

Error Reporting for Failure Diagnosis

# II. Compiler Interaction

## **Goals:**

more precise error messages  
compiler optimizations

## II. Compiler Interaction

**Idea:**

Translate Refinement to Dependent Types

**Challenge:**

Dependent Types require explicit proofs

# **Future work in Liquid Haskell**

I. Proof Assistance

II. Compiler Interaction

III. Real-world applications

**Vision:**

**Embed verification in Haskell programming**

# Vision: **Embed verification in Haskell programming**

Specs are just comments **inside** the languages, ...  
thus, learning effort is small.

Semi-**automatically** machine checked, via SMTs.  
For runtime **optimizations**, by the user or the **compiler**.

# Vision: Embed verification in ~~Haskell~~-programming mainstream

Ruby, JavaScript, Scala, ...

Refinement Types for Ruby

Refinement Types for TypeScript

SMT-Based Checking of Predicate-Qualified Types for Scala

Georg Stefan Schmid    Viktor Kuncak

EPFL, Switzerland

{firstname.lastname}@epfl.ch

Univ



# LiquidHaskell

## Embed verification in Haskell programming

**Fast & Safe Code**  
Static Checks

**Theorem Proving**  
Refinement Reflection

**Applications**  
Education & Industry

Thanks!



LiquidHaskell

**Embed verification in Haskell programming**