

# Fundamental statistical concepts

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ANALYTICS PRIMER

A solid orange horizontal bar at the bottom of the slide.

# 3 Main Pieces of Statistics

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Statistics and analytics in general boils down to three main pieces:

1. Data Collection
2. Data Analysis
3. Inference

Together these pieces summarize the data lifecycle from beginning to end.

# 3 Main Pieces of Statistics

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Statistics and analytics in general boils down to three main pieces:

1. **Data Collection**
2. Data Analysis
3. Inference

One of the most overlooked pieces, but the most important!

- Bad data → Bad Results!

# Populations vs. Samples

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## **Population**

- Set of all objects/individuals of interest
- Usually too large to obtain information from entire population

## **Sample**

- Subset of the population that information is actually obtained

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- **Sampling frame** – actual list from which the sample is taken

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## Sample

- Subset of the population that information is actually obtained
- **Sampling frame** – actual list from which the sample is taken → MAY NOT EQUAL POPULATION

# Parameters vs. Statistics

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## Parameter

- Measures computed from a population.

## Statistic

- Measures computed from a sample.
- Sample statistics is the **point estimate** of the population parameter.

# Parameters vs. Statistics

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Population

Sample

Parameter

Statistic



# Parameters vs. Statistics

---

Population  Sample

Parameter

Statistic

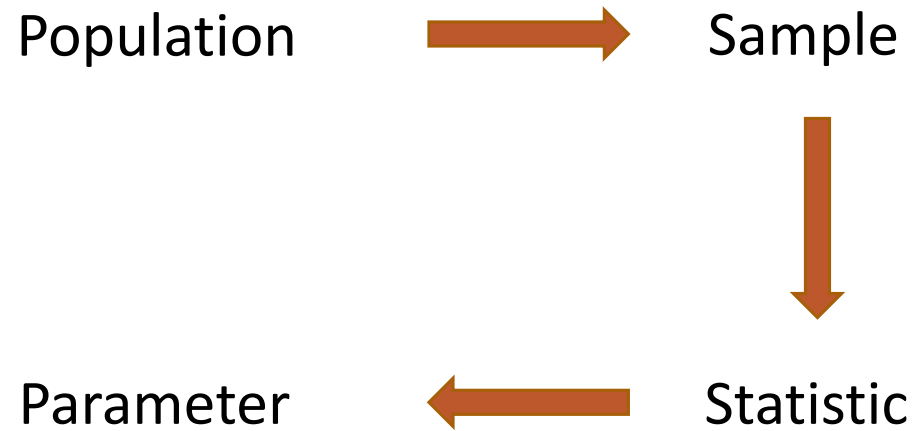
# Parameters vs. Statistics

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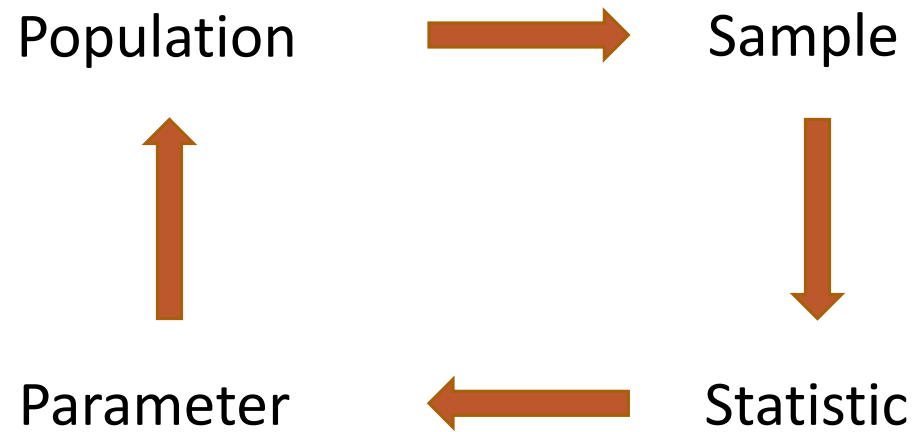
# Parameters vs. Statistics

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# Example

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A retail chain is trying to determine if a new product they introduced is selling well across their stores. The retail chain has 2135 stores nationwide. The analyst in charge of this project is tasked to estimate the average daily sales of this new product across all stores. Older computing technology forces the company to randomly pick 179 stores spread evenly throughout the nation to gather the data. The average daily sales from these 179 stores is \$129.19.

Identify population, sample, parameter, statistic.

Any sampling frame issues?

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Identify population, sample, parameter, **statistic**.

Any sampling frame issues?

# Example

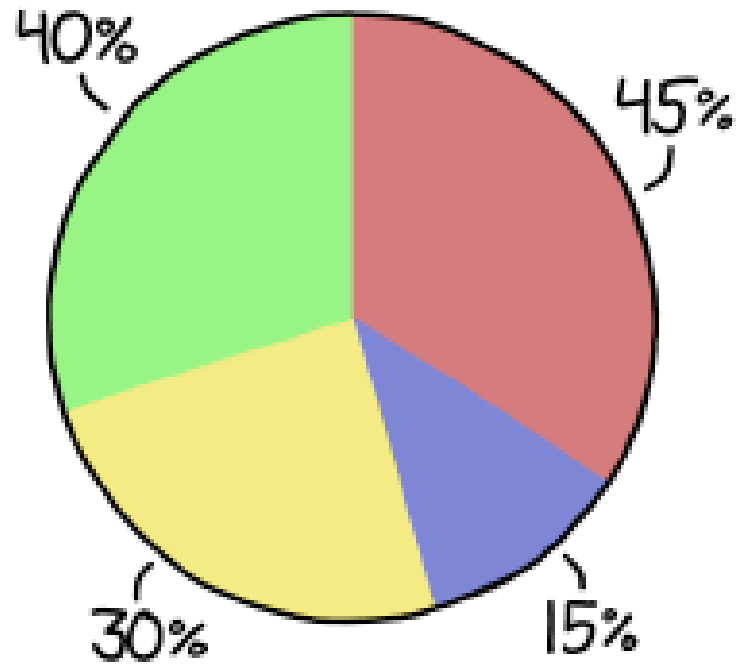
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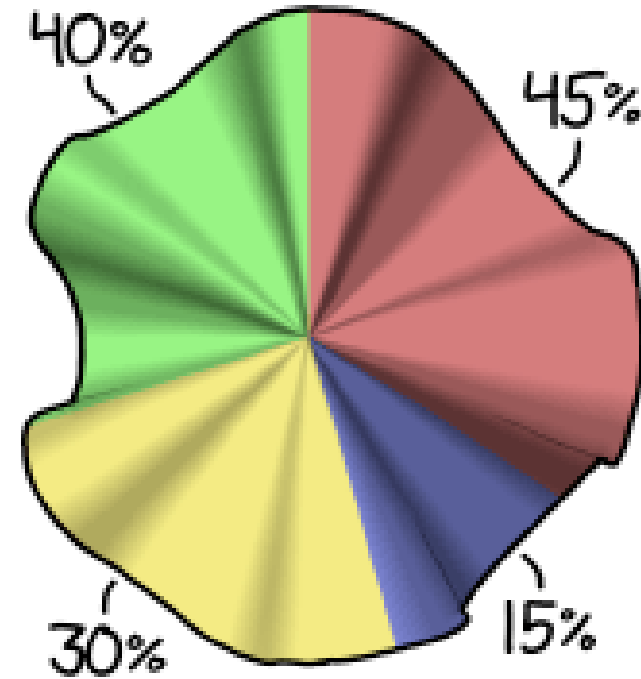
Identify population, sample, parameter, statistic.

Any sampling frame issues? **NO**

WRONG:



RIGHT:



HOW TO MAKE A PIE CHART IF YOUR  
PERCENTAGES DON'T ADD UP TO 100

Source: xkcd.com

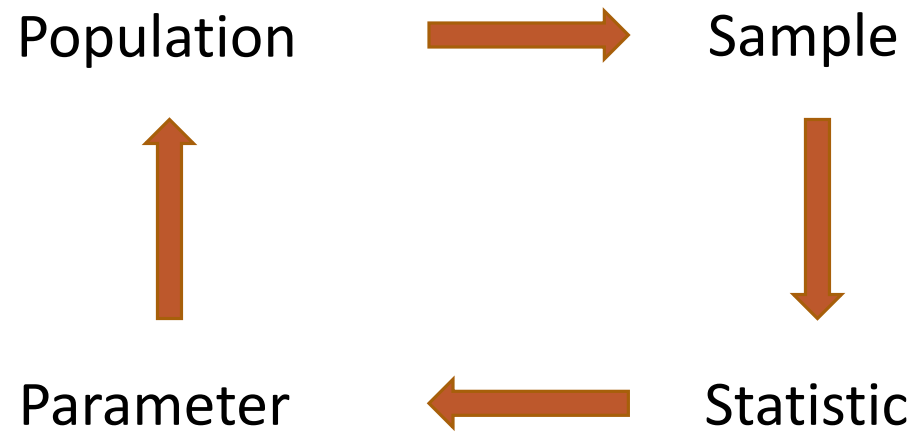
# Sampling Techniques

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FUNDAMENTAL STATISTICAL CONCEPTS (2 OF 3)

# Parameters vs. Statistics

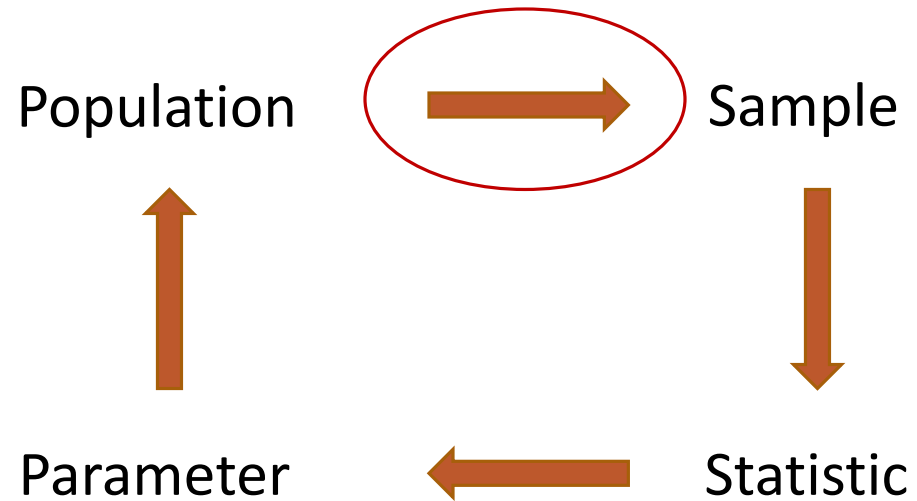
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# Parameters vs. Statistics

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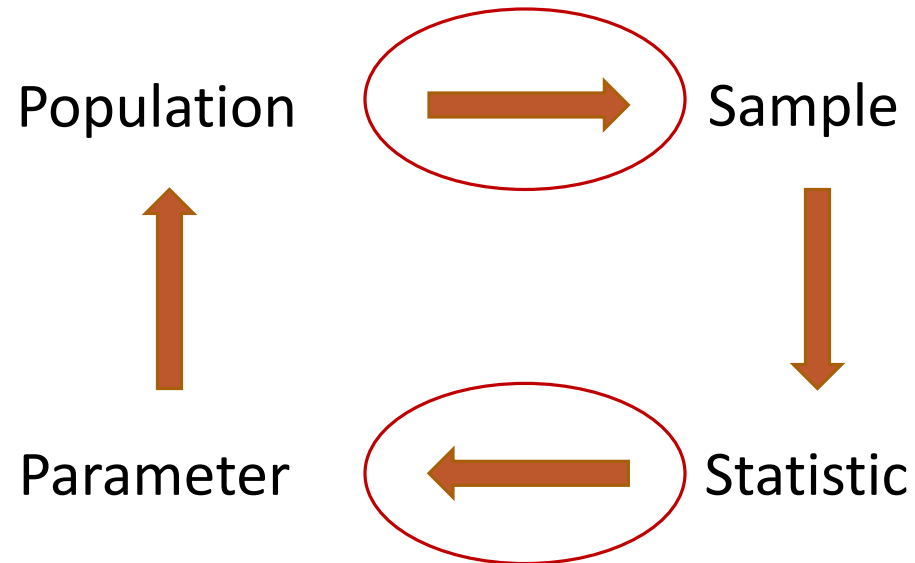
Need good sampling to...



# Parameters vs. Statistics

---

Need good sampling to...



...have good estimates.

# Sampling

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There are many different ways to sample data from population.

Mistakes in sampling can lead to bias in the sample.

**Bias** – certain outcomes are favored over other outcomes in samples.



# Types of Bias

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2 Common Types of Bias:

1. Sampling Bias
2. Selection Bias

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2 Common Types of Bias:

1. Sampling Bias

- a) **Convenience sampling** – technique that selects subjects from population based on accessibility and ease.
- b) **Voluntary sampling** – technique where subjects volunteer themselves to sample.

2. Selection Bias

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2 Common Types of Bias:

1. Sampling Bias
2. Selection Bias
  - a) **Undercoverage** – frame and population are not equal (ex. Phone book)
  - b) **Nonresponse** – subject in sample cannot / will not respond or be measured (ex. Telemarketer)

# Statistical Techniques

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Statistical sampling techniques use selection methods based on chance selection instead of convenience or judgement.

4 Common Techniques:

1. Simple Random Sampling (SRS)
2. Stratified Random Sampling
3. Cluster Sampling
4. Systematic Sampling

# Simple Random Sampling (SRS)

A method of sampling items from a population such that every possible sample of a specified size has an equal chance of being selected.

Sampling Frame



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# Simple Random Sampling (SRS)

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A method of sampling items from a population such that every possible sample of a specified size has an equal chance of being selected.

## Advantages:

- No statistical bias, no previous information about sample needed ahead of time

## Disadvantages:

- Expensive, time consuming, hard to implement (need list of population)

# Stratified Random Sampling (STS)

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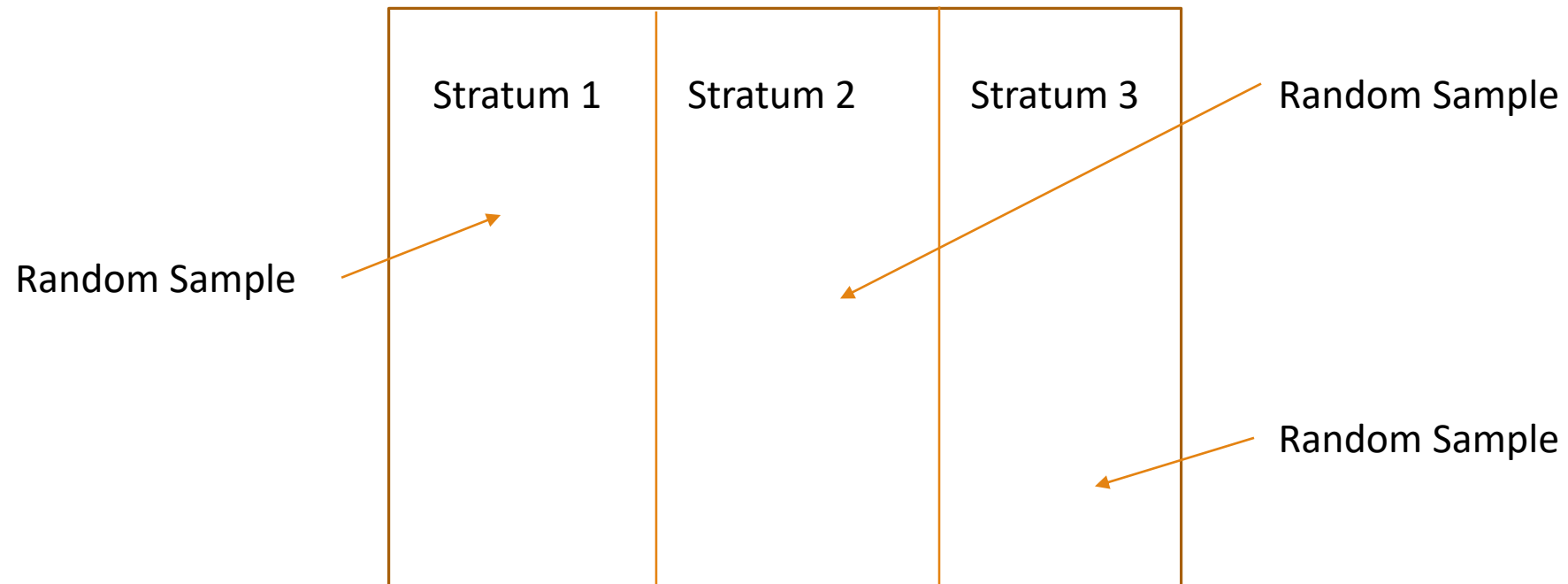
A method of sampling items where the population is divided *a priori* into subgroups, called **strata**, so that each member in the population belongs to only one stratum. Sample items from **every** stratum (with SRS for example).

Stratum 1	Stratum 2	Stratum 3

# Stratified Random Sampling (STS)

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# Stratified Random Sampling (STS)

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## Advantages:

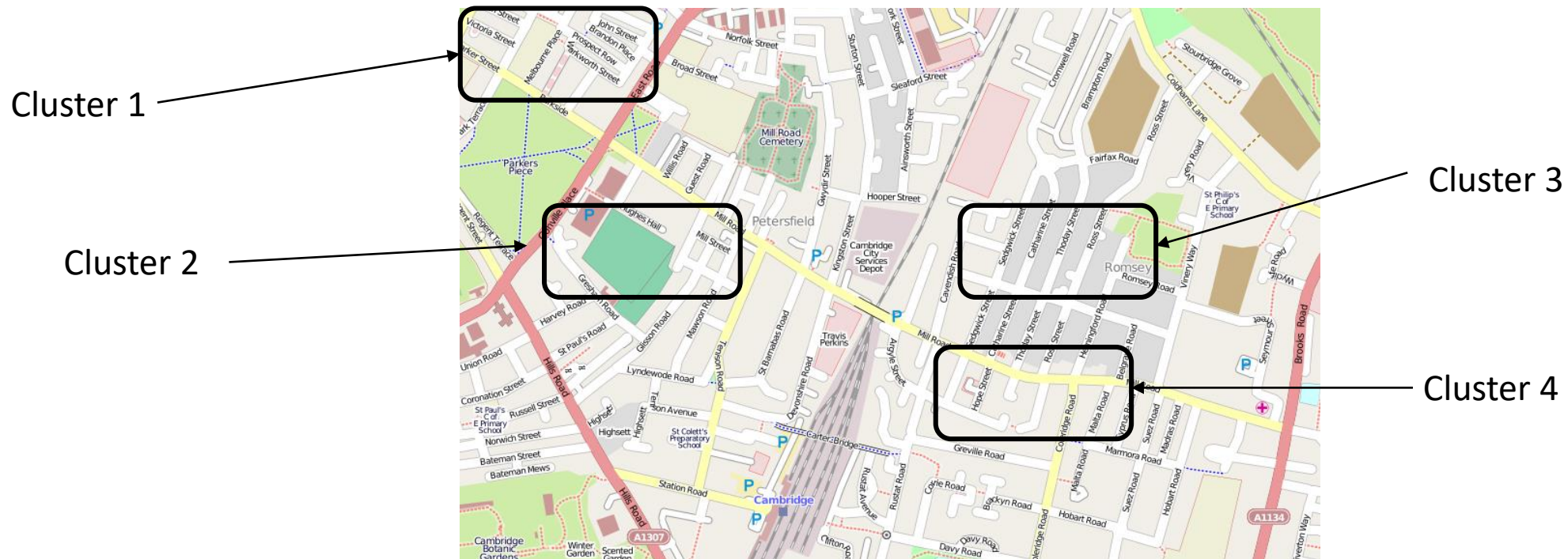
- Smaller sample sizes can achieve same accuracy as SRS, more information about parts of population

## Disadvantages:

- Need information about population ahead of time to split on!

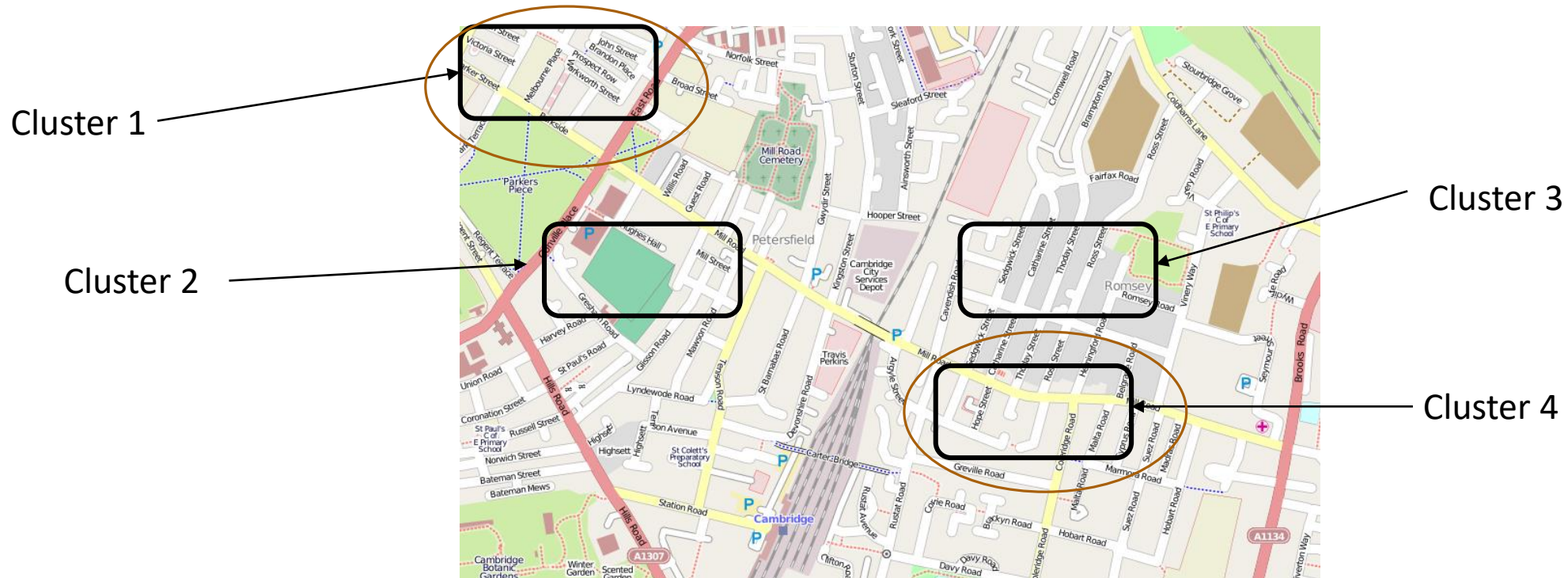
# Cluster Sampling

A method of sampling items where the population is divided *a priori* into subgroups, called **clusters**, so that each member in the population belongs to only one cluster. Sample items from **a sample** of  $m$  clusters selected randomly.



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## Advantages:

- Overcome issues with travel, time, and expense; Easier to implement than SRS or STS

## Disadvantages:

- May have slight bias if random clusters aren't representative; actual sample size depends on number of units within each cluster sampled



# Systematic Sampling

A method of sampling items that involves selecting every  $k^{th}$  item in the population after randomly selecting a starting point between 1 and  $k$ . The value  $k$  is determined as the ratio of the population size over the desired sample size.

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Random Starting point

Say  $k=5$

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9. Awa Abge	54. Lydia Habila	99. Awagana Musa	144. Fatima Tabji
10. Deborah Abge	55. Liyatu Habitu	100. Hanatu Musa	145. Hauwa Takai
11. Kummai Aboku	56. Febi Haruna	101. Hauwa Musa	146. Hauwa Tella
12. Hamsatu Abubakar	57. Tabitha Hyelampa	102. Helen Musa	147. Solomi Titus
13. Mairama Abubakar	58. Ladi Ibrahim	103. Maryamu Musa	148. Esther Usman
14. Hasana Adamu	59. Rahap Ibrahim	104. Palmata Musa	149. Maimuna Usman
15. Naomi Adamu	60. Hanatu Ishaku	105. Rejoice Musa	150. Mary Usman
16. Amina Ali	61. Ruth Ishaku	106. Saraya Musa	151. Ladi Wadai
17. Asabe Ali	62. Zara Ishaku	107. Hauwa Mubah	152. Muli Waligam
18. Mary Ali	63. Hauwa Ishaya	108. Kume Mubah	153. Margret Watsai
19. Comfort Amos	64. Hauwa Isuwa	109. Lugwa Mubah	154. Maryamu Wavi
20. Deborah Amos	65. Awa James	110. Ruth Ngladar	155. Hauwa Wule
21. Mary Amos*	66. Deborah Jafaru	111. Hauwa Nkeki	156. Glory Yaga
22. Rifkatu Amos	67. Ladi Joel	112. Racheal Nkeki	157. Mairama Yahaya
23. Ruth Amos	68. Esther John	113. Hanatu Nuhu	158. Christy Yahi
24. Saraya Amos	69. Jummai John	114. Pindar Nuhu	159. Anthonia Yahnna
25. Esther Ayuba	70. Laraba John	115. Grace Paul	160. Debora Yahnna
26. Saratu Ayuba	71. Rhoda John	116. Jummai Paul	161. Laraba Yahnna
27. Hauwa Balti	72. Eli Joseph	117. Laraba Paul	162. Mary Yahnna*
28. Awa Bitrus	73. Esther Joshua	118. Ladi Paul	163. Na'omi Yahnna
29. Christiana Bitrus	74. Hauwa Joseph	119. Mary Paul	164. Rahila Yahnna
30. Godiya Bitrus	75. Rebeca Joseph	120. Saraya Paul	165. Dorcas* Yakubu
31. Na'omi Bitrus	76. Ruth Joshua	121. Deborah Peter	166. Hadiza Yakubu
32. Rahila Bitrus	77. Yana Joshua	122. Hauwa Peter	167. Juliana Yakubu
33. Ruth Bitrus	78. Rebeca Kabu	123. Rhoda Peter	168. Mary Yakubu
34. Nguba Buba	79. Ruth Kollo	124. Naomi Philimon	169. Maryamu Yakubu
35. Maryamu Bulama	80. Hauwa Kwakwi	125. Mwa Malam Pogu	170. Rifkatu Yakubu
36. Abigail Bukar	81. Rakiya Kwamtah	126. Salomi Pogu	171. Suzana Yakubu
37. Yana Bukar	82. Kauna Lalai	127. Tabitha Pogu	172. Jinkai Yama
38. Gloria Dama	83. Aisha Lawan	128. Yana Pogu	173. Margret Yama
39. Maifa Dama	84. Falta Lawan	129. Luggwa Samuel	174. Saraya Yanga
40. Muwa Daniel	85. Maryamu Samuel	130. Saraya Samuel	175. Yana Yidau
41. Talata Daniel	86. Ruth Lawan	131. Serah Samuel	176. Hauwa Yirma
42. Filo Dauda	87. Kauna Luka	132. Luggwa Sanda	177. Naomi Zakaria
43. Mary Dauda	88. Na'omi Luka	133. Rejoice Sanki	
44. Saratu Dauda	89. Rebecca Luka	134. Margret Shettima	
45. Patient Dzakwa	90. Gloria Mainta	135. Yanke Shittima	

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15 April, 2014: At least 276 girls aged 15-18 yo were kidnapped from their boarding school in Chibok, Nigeria.  
4 May, 2014: Christian Association of Nigeria released this list of 177 names reportedly confirmed still missing.

# Systematic Sampling

A method of sampling items that involves selecting every  $k^{th}$  item in the population after randomly selecting a starting point between 1 and  $k$ . The value  $k$  is determined as the ratio of the population size over the desired sample size.

Random Starting point

And so on....til you reach desired sample

#BRINGBACKOURGIRLS	#BRINGBACKOURGIRLS	#BRINGBACKOURGIRLS	#BRINGBACKOURGIRLS
1. Blessing Abana	46. Saratu Emmanuel	91. Kabu Malla	136. Tabitha Silas
2. Yayi Abana	47. Lydia Emmar	92. Rebecca Mallum	137. Kwanta Simon
3. Deborah Abari	48. Monica Enoch	93. Laraba Maman	138. Lydia Simon
4. Deborah Abbas	49. Aisha Ezekial	94. Asabe Manu	139. Deborah Solomon
5. Hauwa Abdu	50. Rifkatu Galang	95. Kwadugu Manu	140. Rifkatu Solomon
6. Ihayi Abdu	51. Halima Gamba	96. Esther Markus	141. Hana Stephen
7. Safiya Abdu	52. Aishatu Grema	97. Saratu Markus	142. Mary Sule
8. Sieker* Abdul	53. Comfort* Habila	98. Aishatu Musa	143. Saraya Mai Stover
9. Awa Abge	54. Lydia Habila	99. Awagana Musa	144. Fatima Tabji
10. Deborah Abge	55. Liyatu Habitu	100. Hanatu Musa	145. Hauwa Takai
11. Kummai Aboku	56. Febi Haruna	101. Hauwa Musa	146. Hauwa Tella
12. Hamsatu Abubakar	57. Tabitha Hyelampa	102. Helen Musa	147. Solomi Titus
13. Mairama Abubakar	58. Ladi Ibrahim	103. Maryamu Musa	148. Esther Usman
14. Hasana Adamu	59. Rahap Ibrahim	104. Palmata Musa	149. Maimuna Usman
15. Naomi Adamu	60. Hanatu Ishaku	105. Rejoice Musa	150. Mary Usman
16. Amina Ali	61. Ruth Ishaku	106. Saraya Musa	151. Ladi Wadai
17. Asabe Ali	62. Zara Ishaku	107. Hauwa Mubah	152. Muli Waligam
18. Mary Ali	63. Hauwa Ishaya	108. Kume Mubah	153. Margret Watsai
19. Comfort Amos	64. Hauwa Isuwa	109. Lugwa Mubah	154. Maryamu Wavi
20. Deborah Amos	65. Awa James	110. Ruth Ngladar	155. Hauwa Wule
21. Mary Amos*	66. Deborah Jafaru	111. Hauwa Nkeki	156. Glory Yaga
22. Rifkatu Amos	67. Ladi Joel	112. Racheal Nkeki	157. Mairama Yahaya
23. Ruth Amos	68. Esther John	113. Hanatu Nuhu	158. Christy Yahi
24. Saraya Amos	69. Jummai John	114. Pindar Nuhu	159. Anthonia Yehonna
25. Esther Ayuba	70. Laraba John	115. Grace Paul	160. Debora Yehonna
26. Saratu Ayuba	71. Rhoda John	116. Jummai Paul	161. Laraba Yehonna
27. Hauwa Balti	72. Eli Joseph	117. Laraba Paul	162. Mary Yehonna*
28. Awa Bitrus	73. Esther Joshua	118. Ladi Paul	163. Na'omi Yehonna
29. Christiana Bitrus	74. Hauwa Joseph	119. Mary Paul	164. Rahila Yehanna
30. Godiya Bitrus	75. Rebeca Joseph	120. Saraya Paul	165. Dorcas* Yakubu
31. Na'omi Bitrus	76. Ruth Joshua	121. Deborah Peter	166. Hadiza Yakubu
32. Rahila Bitrus	77. Yana Joshua	122. Hauwa Peter	167. Juliana Yakubu
33. Ruth Bitrus	78. Rebeca Kabu	123. Rhoda Peter	168. Mary Yakubu
34. Nguba Buba	79. Ruth Kollo	124. Naomi Philimon	169. Maryamu Yakubu
35. Maryamu Bulama	80. Hauwa Kwakwi	125. Mwa Malam Pogu	170. Rifkatu Yakubu
36. Abigail Bukar	81. Rakiya Kwamtah	126. Salomi Pogu	171. Suzana Yakubu
37. Yana Bukar	82. Kauna Lalai	127. Tabitha Pogu	172. Jinkai Yama
38. Gloria Dama	83. Aisha Lawan	128. Yana Pogu	173. Margret Yama
39. Maifa Dama	84. Falta Lawan	129. Luggwa Samuel	174. Saraya Yanga
40. Muwa Daniel	85. Maryamu Lawan	130. Saraya Samuel	175. Yana Yidau
41. Talata Daniel	86. Ruth Lawan	131. Serah Samuel	176. Hauwa Yirma
42. Filo Dauda	87. Kauna Luka	132. Luggwa Sanda	177. Naomi Zakaria
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# Systematic Sampling

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A method of sampling items that involves selecting every  $k^{th}$  item in the population after randomly selecting a starting point between 1 and  $k$ . The value  $k$  is determined as the ratio of the population size over the desired sample size.

## Advantages:

- Very easy to get sample

## Disadvantages:

- May be biased, especially if order of list of population matters.

# Example

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A large worldwide financial company wants to develop a new retirement plan for the company. They want to survey different managers of branches around the world to find out the most important strategies the new retirement plan should contain. They have 5000 branches worldwide and want to personally interview these branch managers. They have information about the branch size (small, medium, large), and the state/province location of the branch. They want to talk to 50 branch managers.

Develop four separate strategies to sample these branch managers based on the four different statistical sampling techniques discussed previously.

# Example

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Develop four separate strategies to sample these branch managers based on the four different statistical sampling techniques discussed previously.

1. SRS – Randomly sample 50 branches to interview their managers
2. STS – Stratify by size and select SRS from each
3. Cluster – Randomly select sample of states/provinces, then interview branches from those states/provinces
4. Systematic – Select every 100<sup>th</sup> branch in list of branches





# Types of Data

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# 4 Types of Data

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There are four main types of data people typically deal with in data analysis.

These four types are split into two groups

1. Qualitative vs. Quantitative
2. Time Series vs. Cross-sectional



# Quantitative vs. Qualitative

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## Quantitative:

- Data that are numeric that define value or quantity.
- Easy check → Must be able to do basic arithmetic and have it make sense.

## Qualitative:

- Data whose measurement scale is inherently categorical.
- **Nominal** – categories with no logical ordering
- **Ordinal** – categories with a logical order / only two ways to order the categories (binary IS ordinal)

# Time Series vs. Cross-sectional

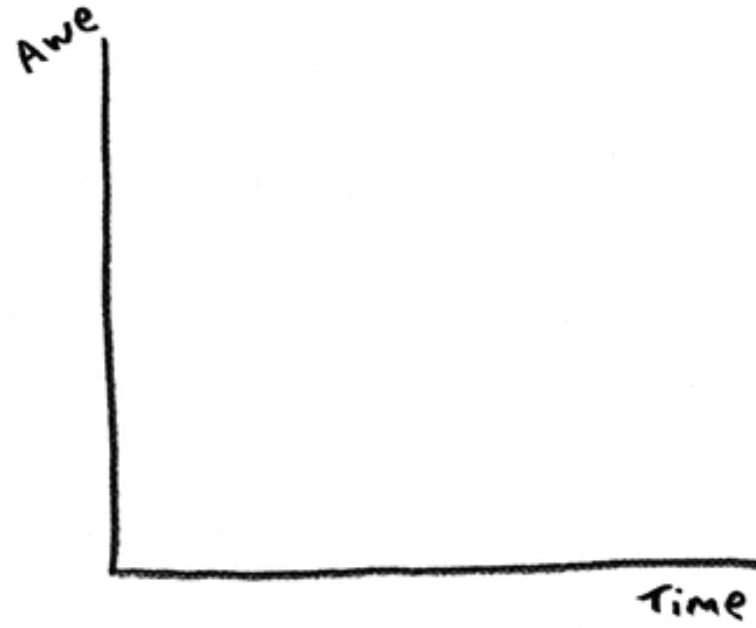
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## **Time Series:**

- Set of ordered data values observed at successive points in time.

## **Cross-sectional:**

- Set of data values observed at a fixed point in time, or where time is of no significance.



How I feel about mountains